

Exploring QCD at high energy in DIS off nucleons and nuclei

Anna Staśto
Penn State & RIKEN BNL

EIC Meeting at Stony Brook, January 11, 2010

Outline

- What have we learned from HERA.
- High gluon densities and parton saturation.
- Hints of saturation at HERA and RHIC.
- Why next ep/eA collider? New directions and possibilities.

Quantum Chromodynamics

QCD Lagrangian:

$$\mathcal{L}_{\text{QCD}} = -\frac{1}{4}F_{\mu\nu}^a F_a^{\mu\nu} + \sum_{\text{flavours}} \bar{q}_a (iD^\mu \gamma_\mu - m_f)_{ab} q_b$$

Field strength:

$$F_{\mu\nu}^a = \partial_\mu A_\nu^a - \partial_\nu A_\mu^a - g f^{abc} A_\mu^b A_\nu^c$$

Quantum Chromodynamics

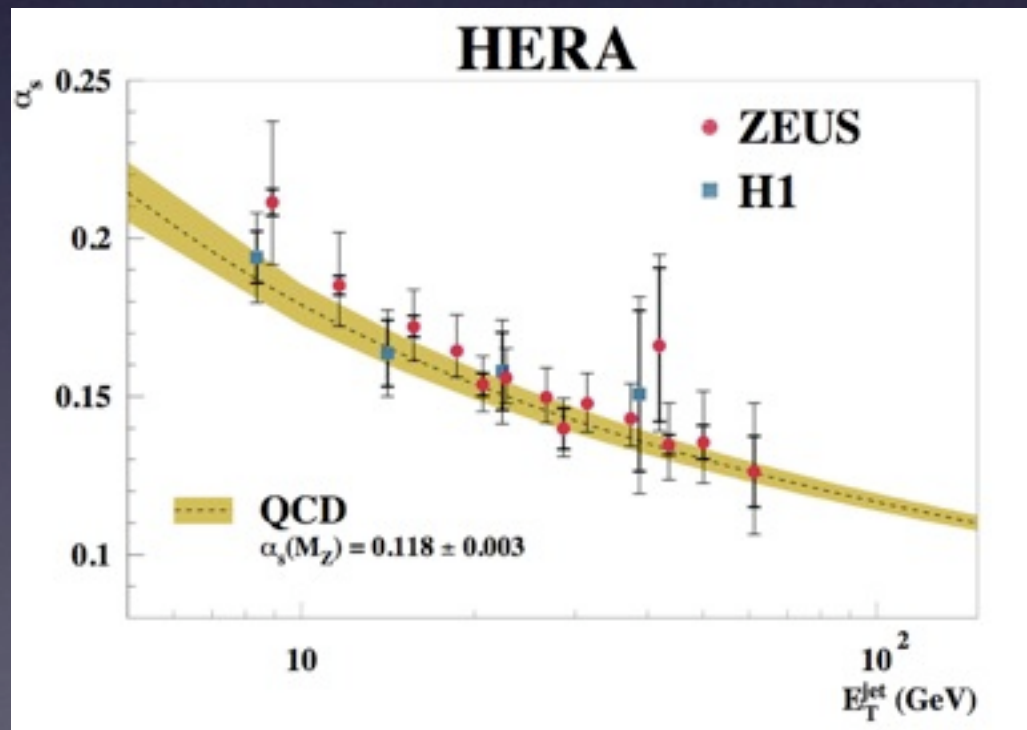
QCD Lagrangian:

$$\mathcal{L}_{\text{QCD}} = -\frac{1}{4}F_{\mu\nu}^a F_a^{\mu\nu} + \sum_{\text{flavours}} \bar{q}_a (iD^\mu \gamma_\mu - m_f)_{ab} q_b$$

Field strength:

$$F_{\mu\nu}^a = \partial_\mu A_\nu^a - \partial_\nu A_\mu^a - g f^{abc} A_\mu^b A_\nu^c$$

Asymptotic freedom



Small
scales

Large
scales

Quantum Chromodynamics

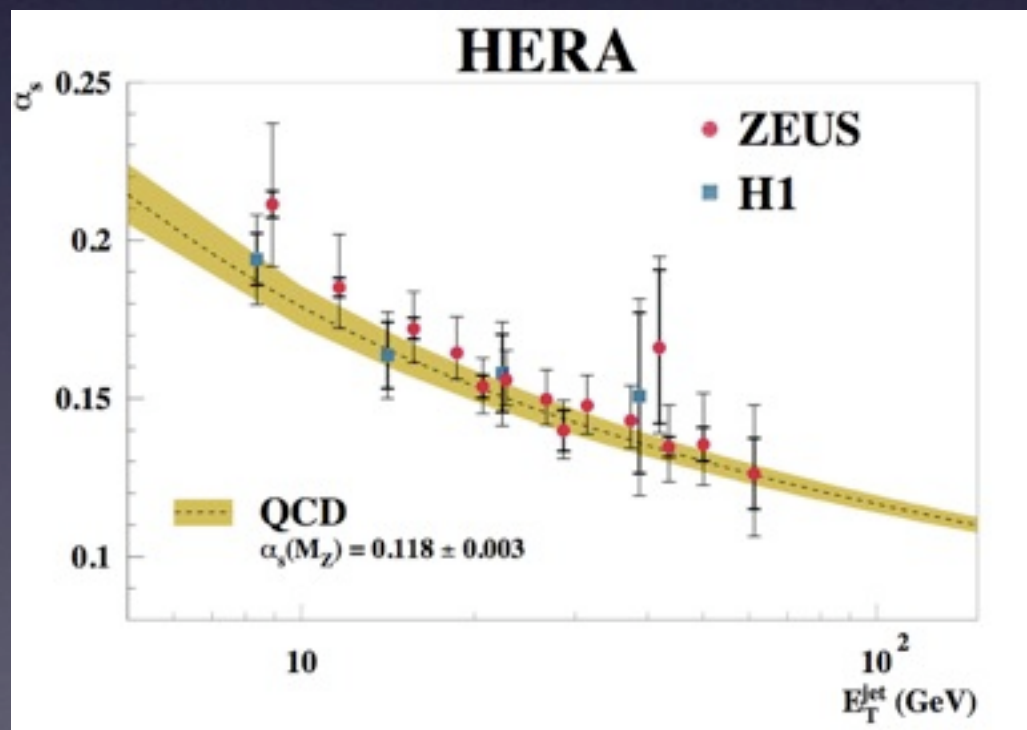
QCD Lagrangian:

$$\mathcal{L}_{\text{QCD}} = -\frac{1}{4}F_{\mu\nu}^a F_a^{\mu\nu} + \sum_{\text{flavours}} \bar{q}_a (iD^\mu \gamma_\mu - m_f)_{ab} q_b$$

Field strength:

$$F_{\mu\nu}^a = \partial_\mu A_\nu^a - \partial_\nu A_\mu^a - g f^{abc} A_\mu^b A_\nu^c$$

Asymptotic freedom



Small
scales

Large
scales

- Rich and very complicated structure due to non-linear interactions of gluons.
- Emergent phenomena: confinement, Regge trajectories, hadron spectrum.
- Extremely complex dynamics at high energies or at small Bjorken x .

Quantum Chromodynamics

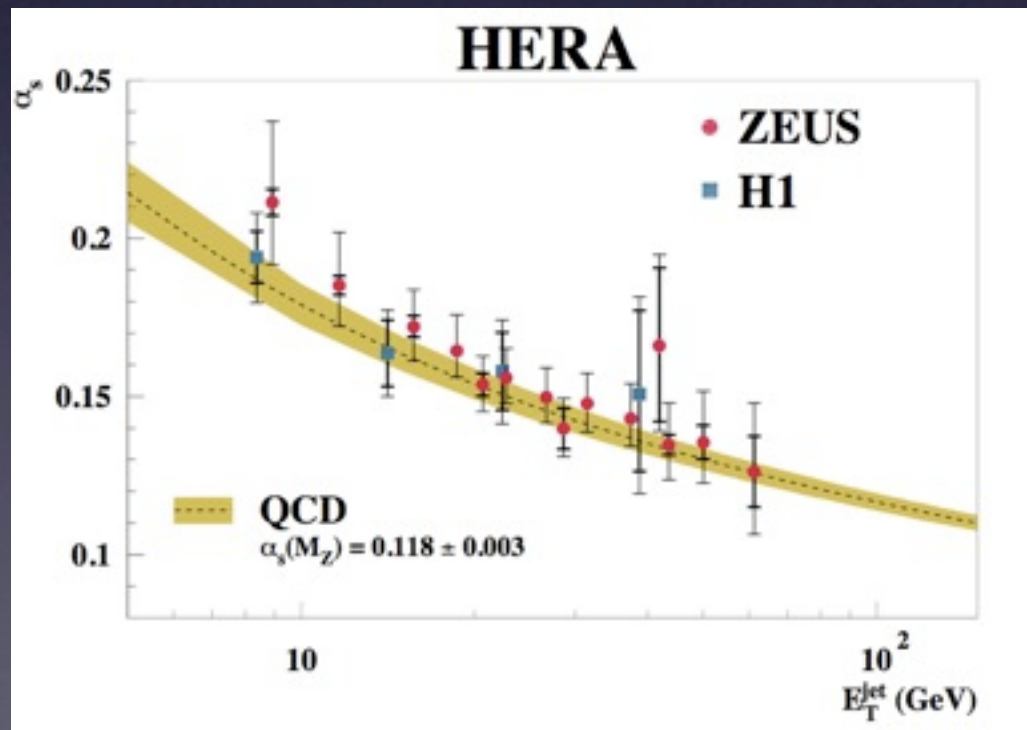
QCD Lagrangian:

$$\mathcal{L}_{\text{QCD}} = -\frac{1}{4}F_{\mu\nu}^a F_a^{\mu\nu} + \sum_{\text{flavours}} \bar{q}_a (iD^\mu \gamma_\mu - m_f)_{ab} q_b$$

Field strength:

$$F_{\mu\nu}^a = \partial_\mu A_\nu^a - \partial_\nu A_\mu^a - g f^{abc} A_\mu^b A_\nu^c$$

Asymptotic freedom



Small
scales

Large
scales

- Rich and very complicated structure due to non-linear interactions of gluons.
- Emergent phenomena: confinement, Regge trajectories, hadron spectrum.
- Extremely complex dynamics at high energies or at small Bjorken x .

Understanding of the dynamics of the gluon fields is of fundamental importance.

How do we know that gluons play such an important role at high energies?

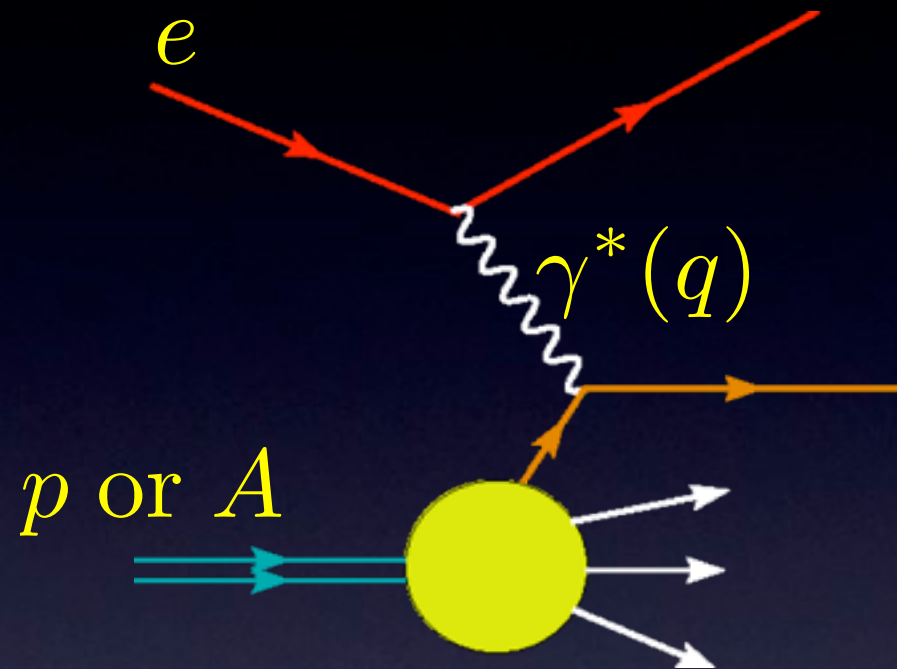
Deep Inelastic Scattering

Deep Inelastic Scattering

Scattering of electron off a hadron(proton):

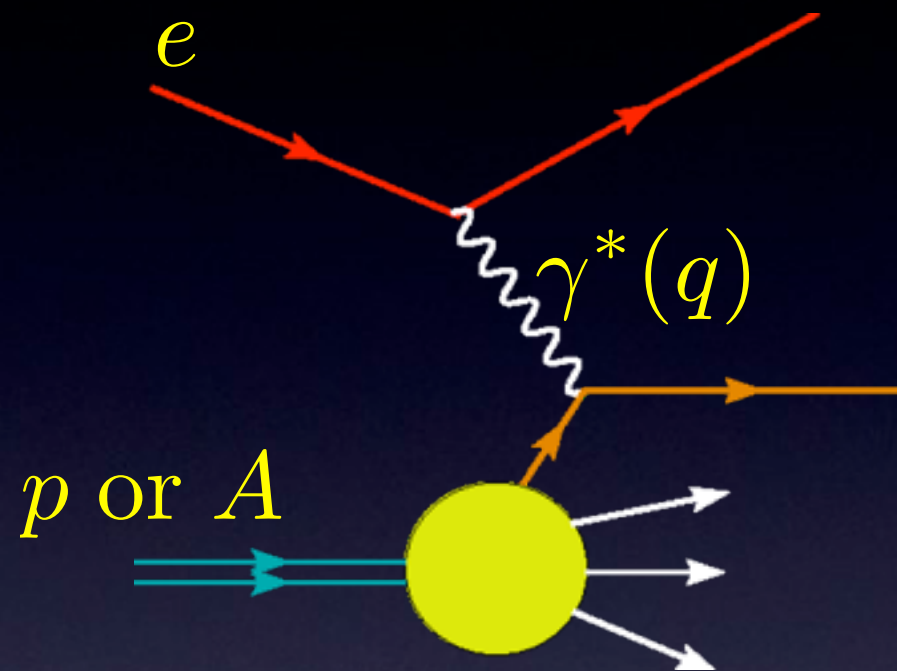
Deep Inelastic Scattering

Scattering of electron off a hadron(proton):



Deep Inelastic Scattering

Scattering of electron off a hadron(proton):

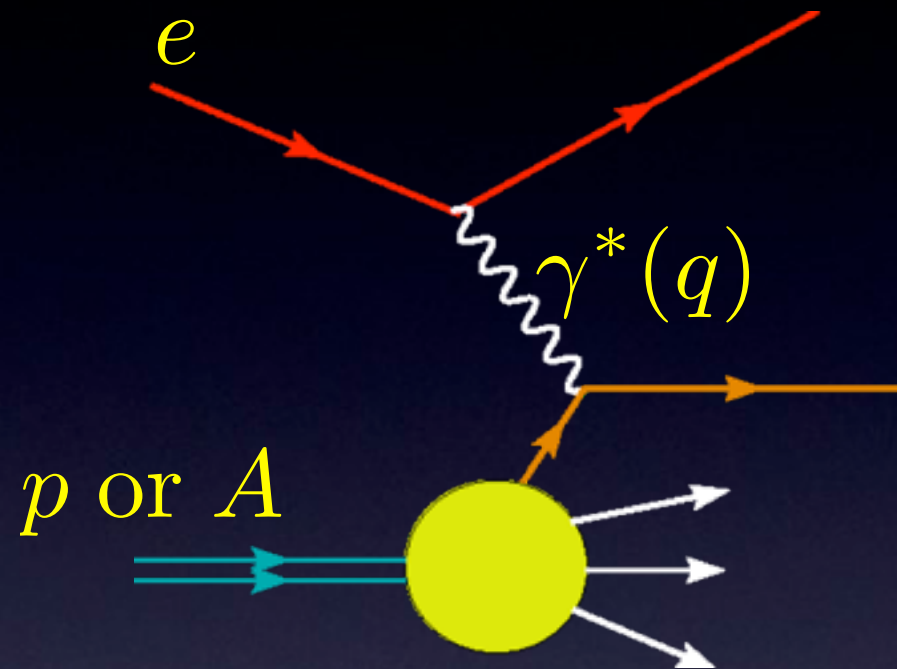


Photon virtuality:

$$Q^2 = -q^2 > 0$$

Deep Inelastic Scattering

Scattering of electron off a hadron(proton):



Photon virtuality:

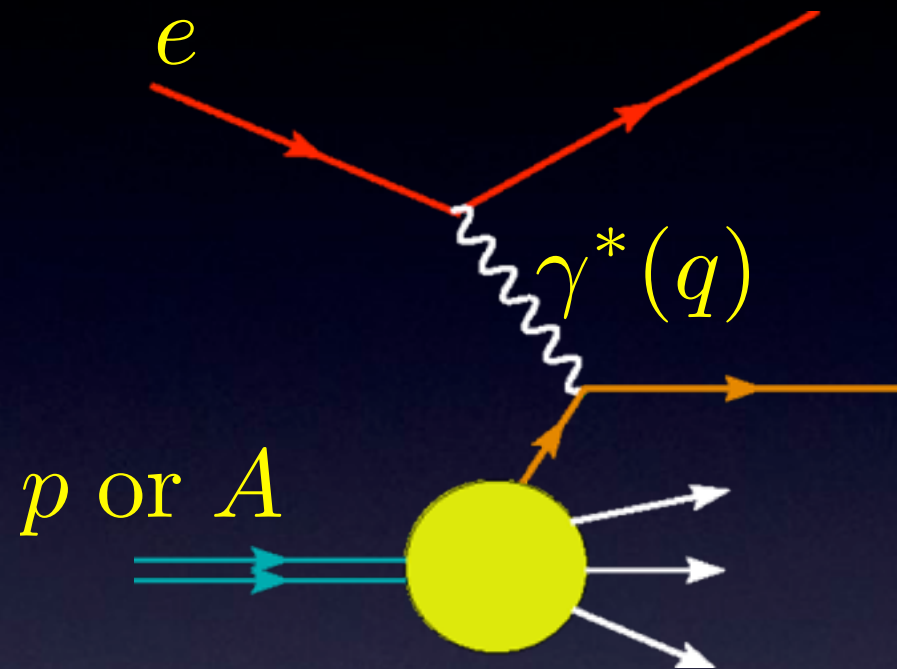
$$Q^2 = -q^2 > 0$$

Total energy of the photon-proton system

$$s = (p + q)^2$$

Deep Inelastic Scattering

Scattering of electron off a hadron(proton):



Photon virtuality:

$$Q^2 = -q^2 > 0$$

Total energy of the photon-proton system

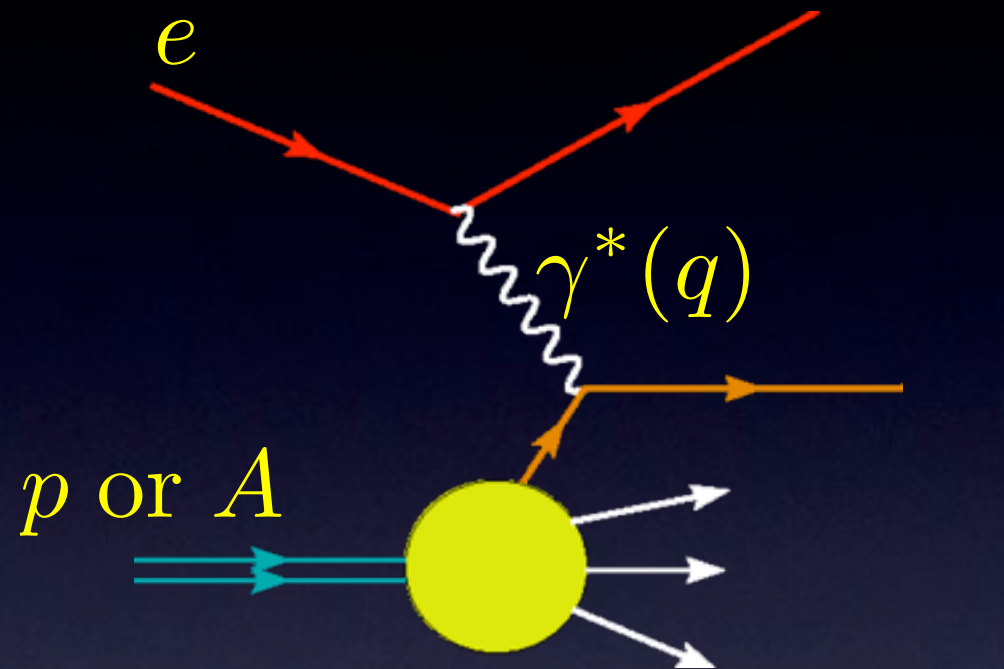
$$s = (p + q)^2$$

Bjorken x

$$x = \frac{Q^2}{s + Q^2} \simeq \frac{Q^2}{s}$$

Deep Inelastic Scattering

Scattering of electron off a hadron(proton):



cross section

parton density

$$\sigma^{\gamma^* p} \sim \frac{1}{Q^2} x f(x, Q^2)$$

Photon virtuality:

$$Q^2 = -q^2 > 0$$

Total energy of the photon-proton system

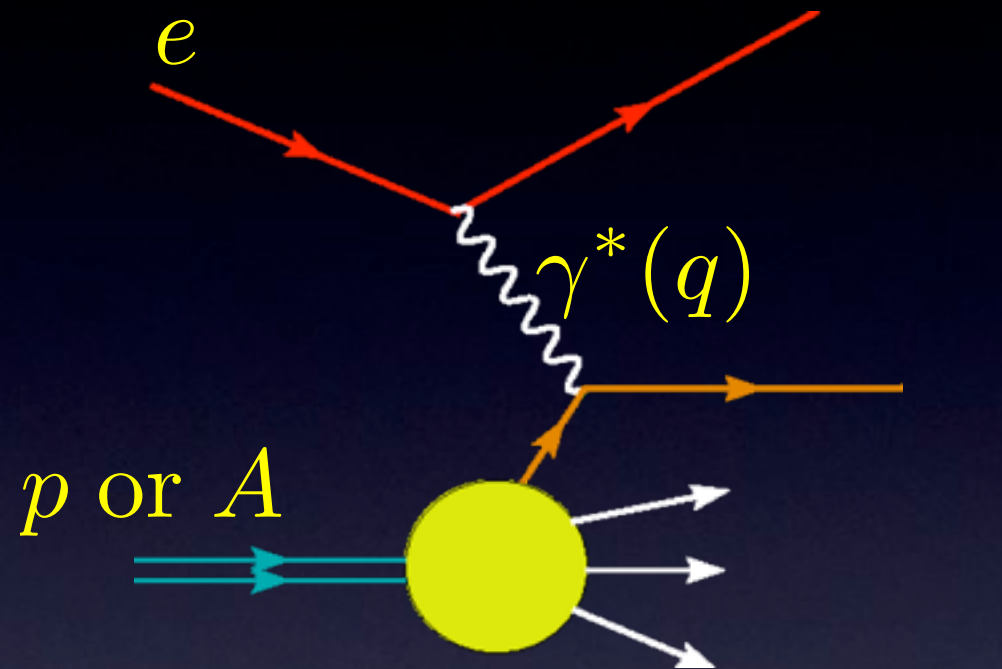
$$s = (p + q)^2$$

Bjorken x

$$x = \frac{Q^2}{s + Q^2} \simeq \frac{Q^2}{s}$$

Deep Inelastic Scattering

Scattering of electron off a hadron(proton):



Photon virtuality:

$$Q^2 = -q^2 > 0$$

Total energy of the photon-proton system

$$s = (p + q)^2$$

Bjorken x

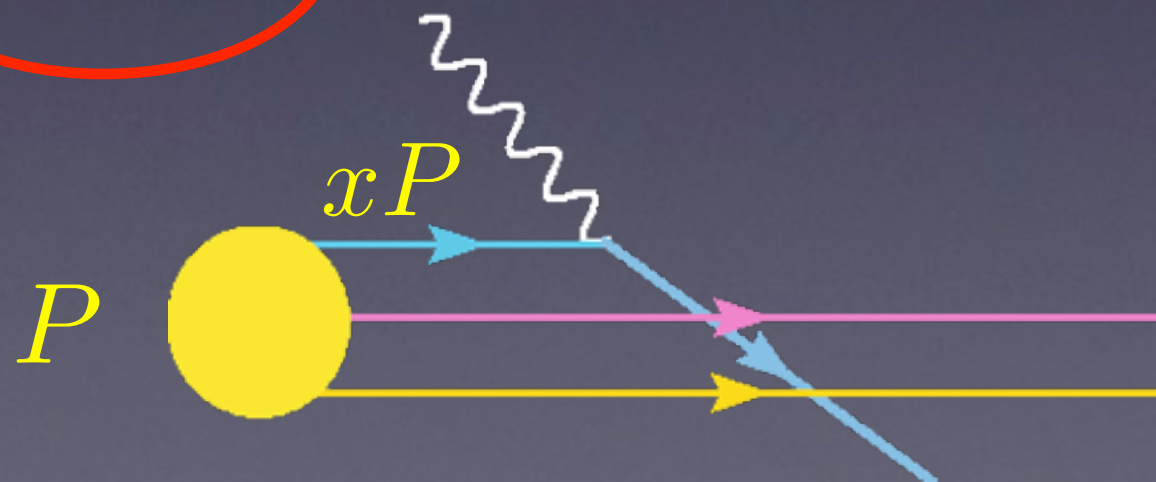
$$x = \frac{Q^2}{s + Q^2} \simeq \frac{Q^2}{s}$$

cross section

parton density

$$\sigma^{\gamma^* p} \sim \frac{1}{Q^2} x f(x, Q^2)$$

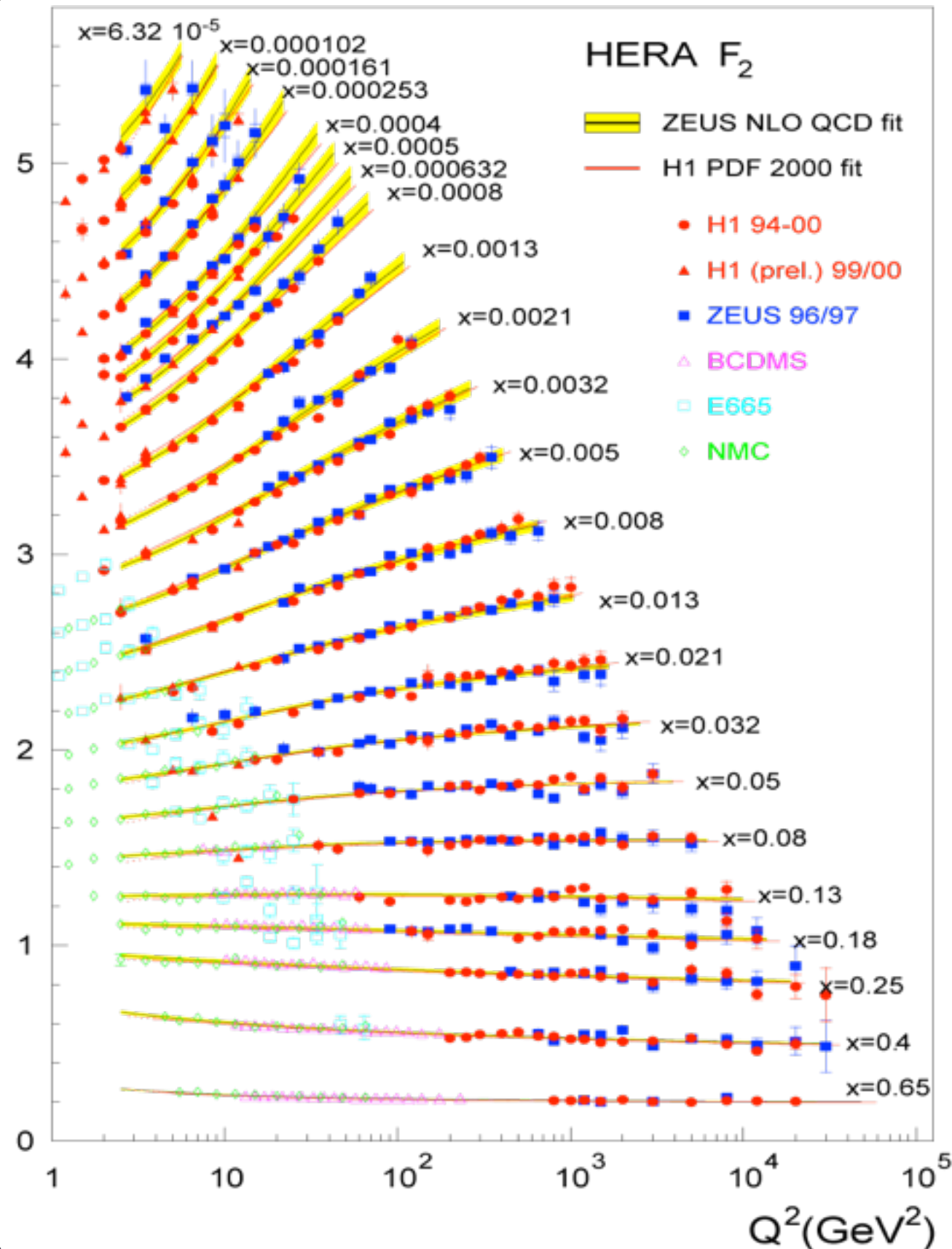
$$0 \leq x \leq 1$$



x fraction of the longitudinal momentum of the proton carried by the quark

DIS

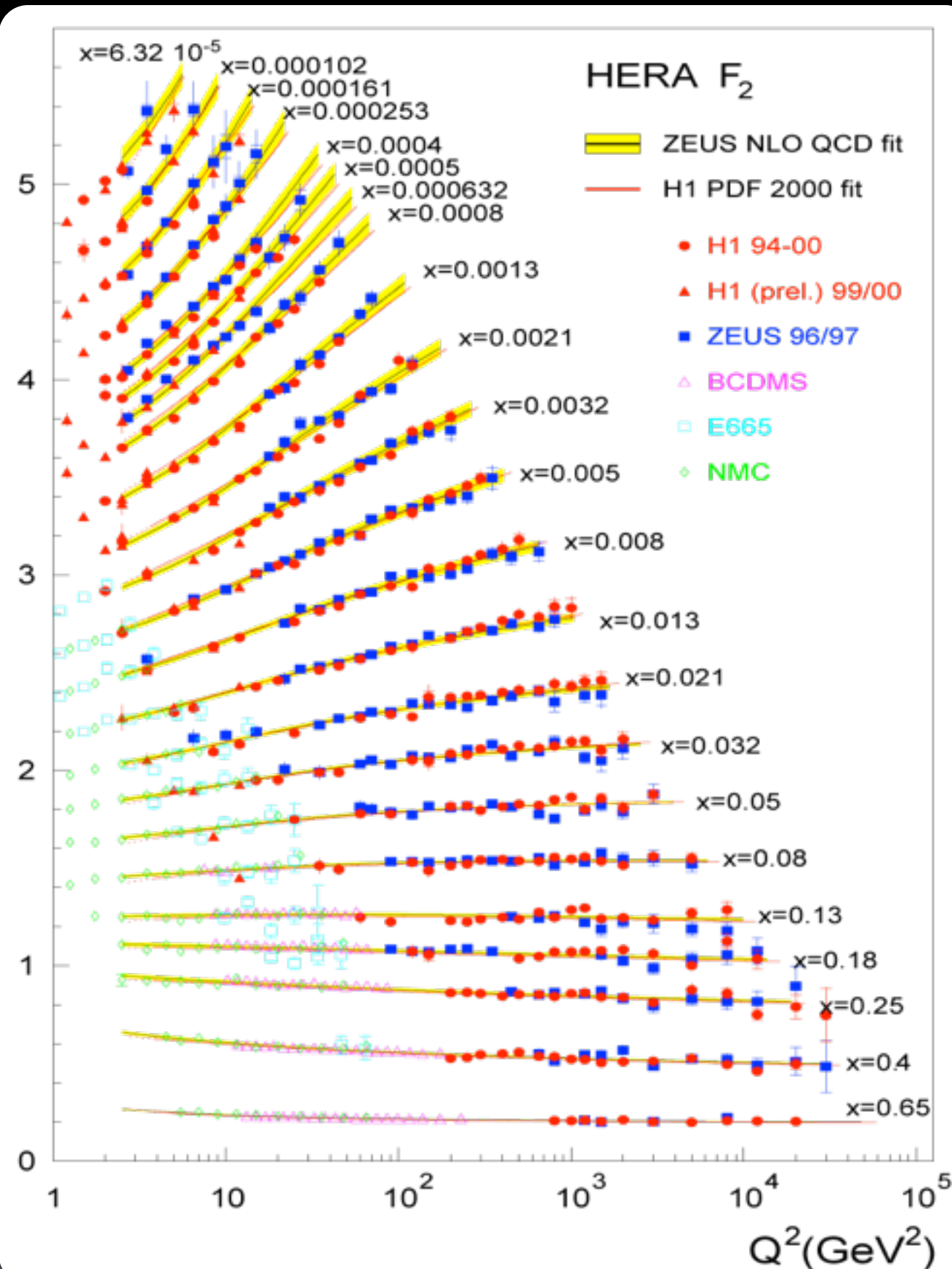
$$\frac{d^2\sigma^{ep\rightarrow eX}}{dx dQ^2} = \frac{4\pi\alpha_{\text{em}}^2}{xQ^4} \left[\left(1 - y + \frac{y^2}{2}\right) F_2(x, Q^2) - \frac{y^2}{2} F_L(x, Q^2) \right]$$



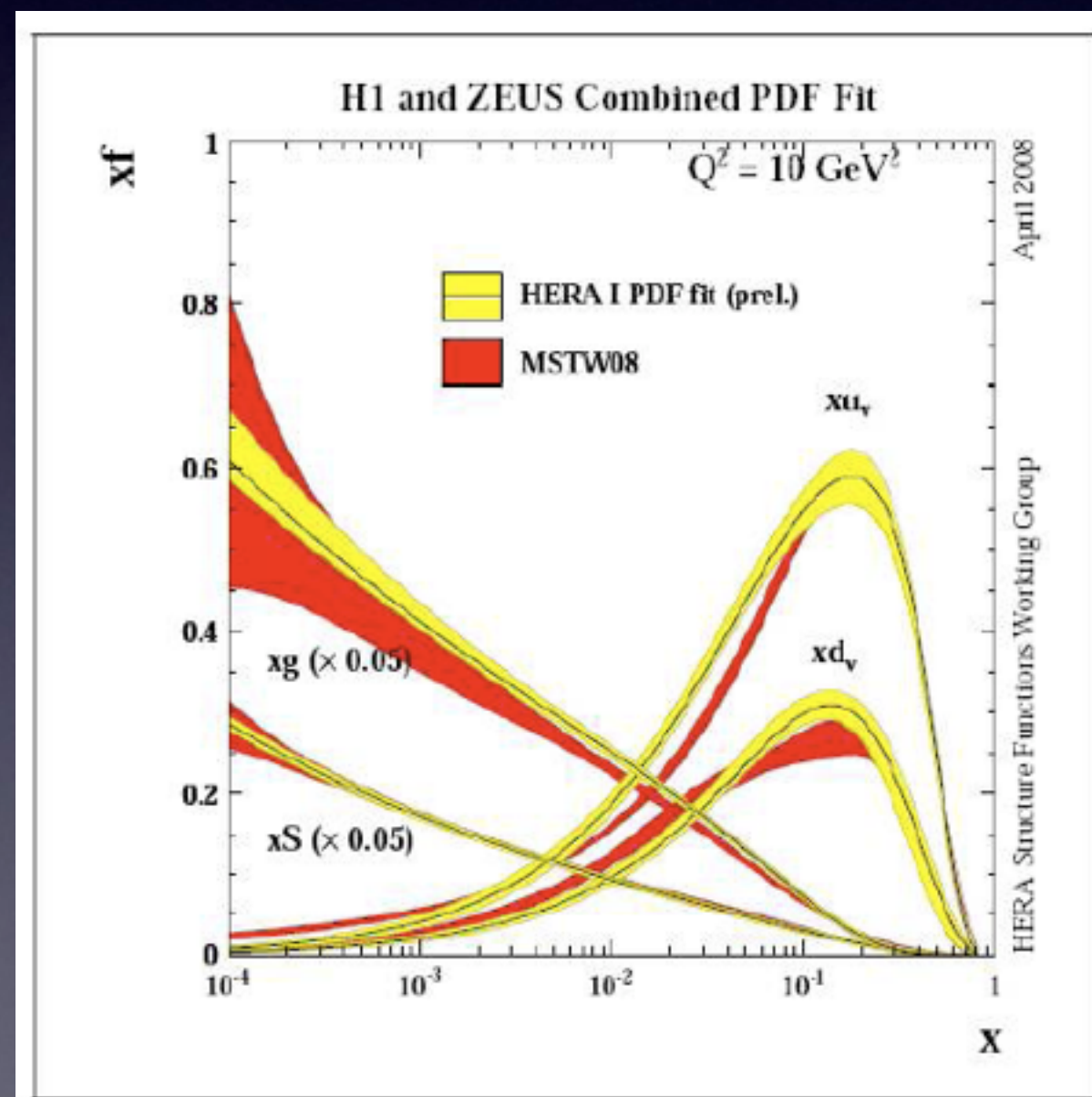
Observation of large scaling violations.

DIS

$$\frac{d^2\sigma^{ep\rightarrow eX}}{dx dQ^2} = \frac{4\pi\alpha_{\text{em}}^2}{xQ^4} \left[\left(1 - y + \frac{y^2}{2}\right) F_2(x, Q^2) - \frac{y^2}{2} F_L(x, Q^2) \right]$$

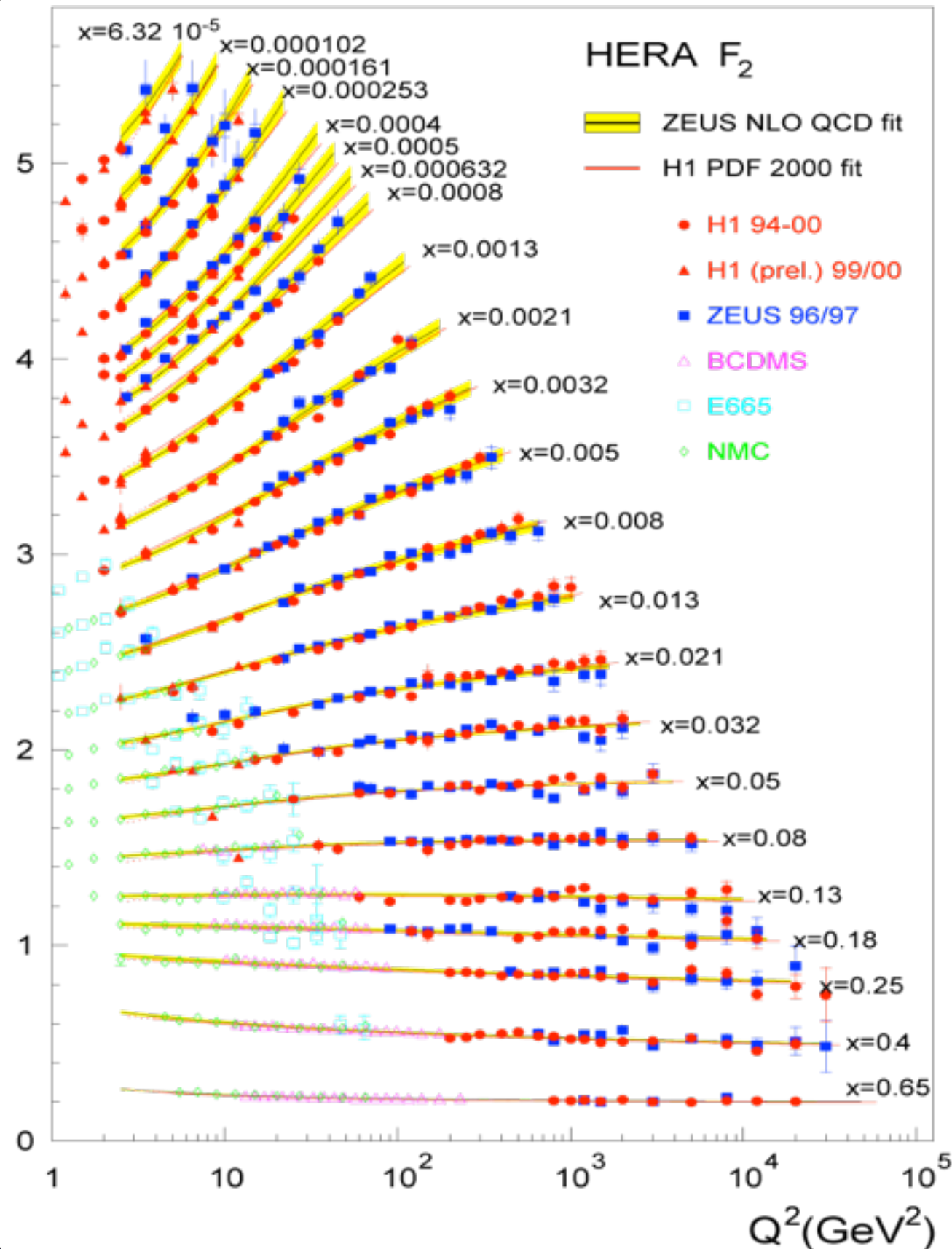


Observation of large scaling violations.



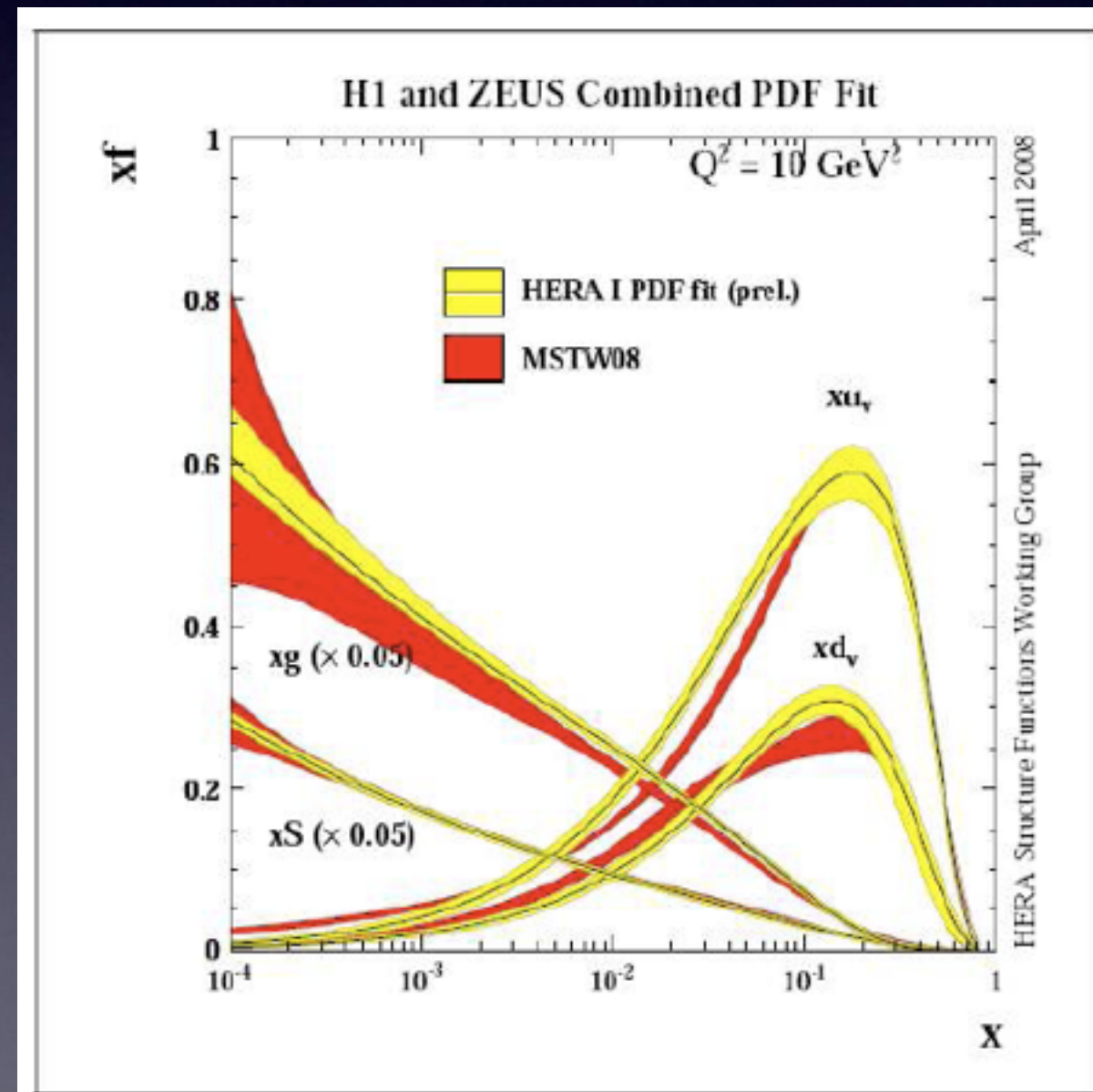
DIS

$$\frac{d^2\sigma^{ep\rightarrow eX}}{dx dQ^2} = \frac{4\pi\alpha_{\text{em}}^2}{xQ^4} \left[\left(1 - y + \frac{y^2}{2}\right) F_2(x, Q^2) - \frac{y^2}{2} F_L(x, Q^2) \right]$$

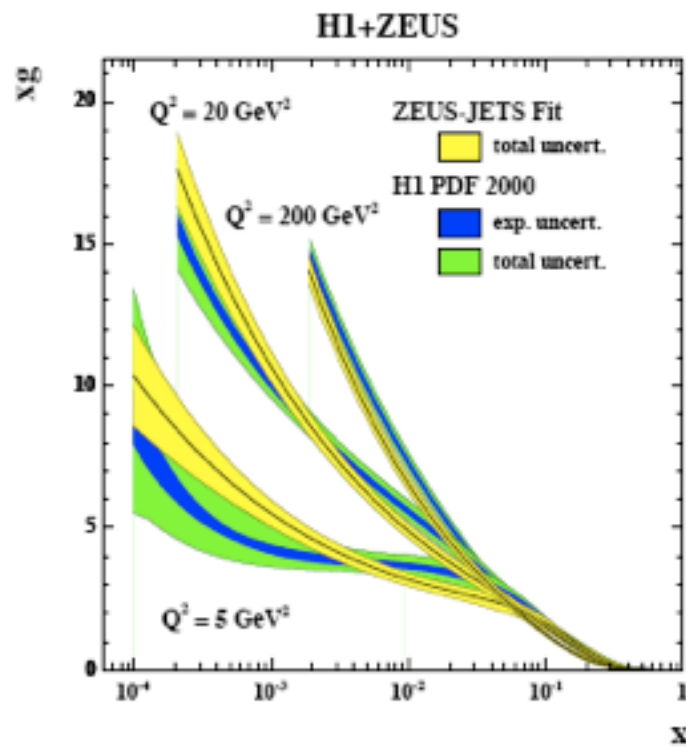


Observation of large scaling violations.

Gluon density dominates at small x !

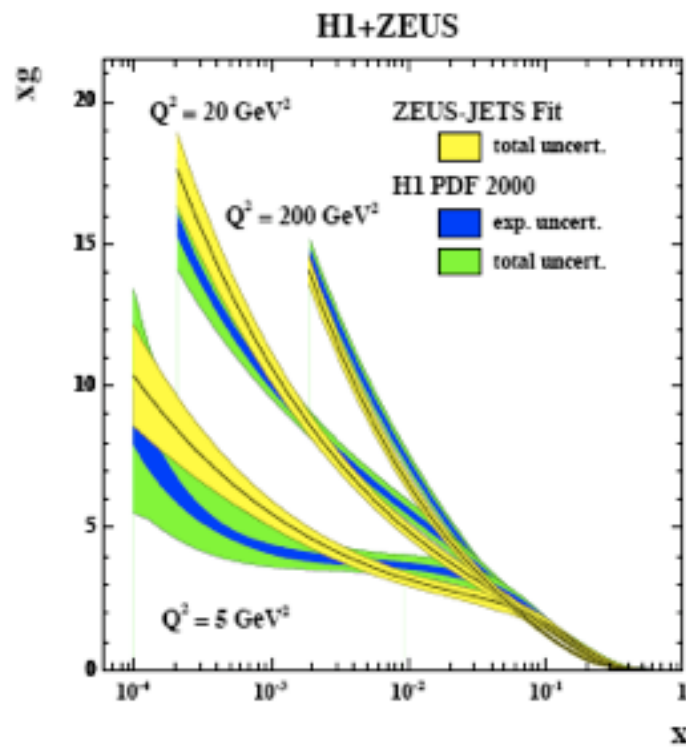


Estimates of gluon density



Estimates of gluon density

Extrapolation of gluon density to various energies



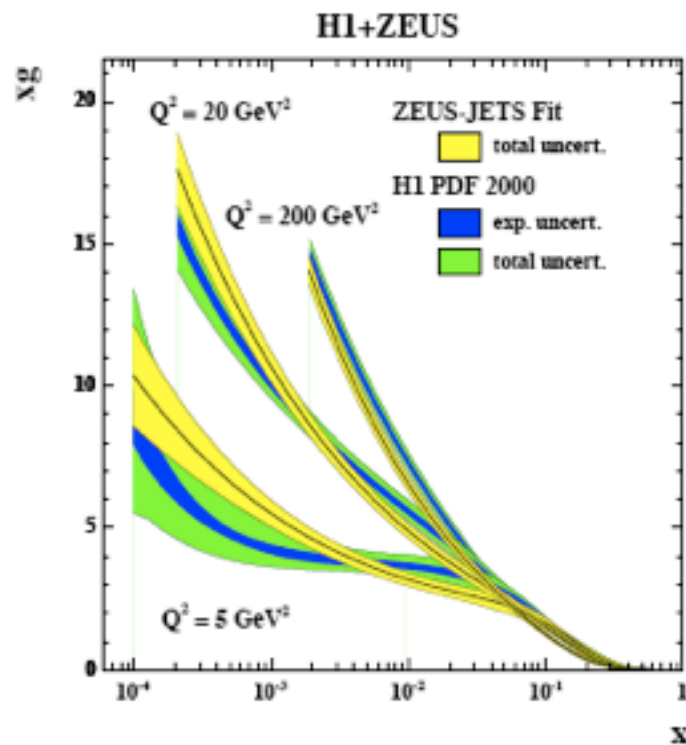
Estimates of gluon density

Extrapolation of gluon density
to various energies

Scale

$$Q^2 = 5 \text{ GeV}^2$$

$$x \sim \frac{Q^2}{s}$$



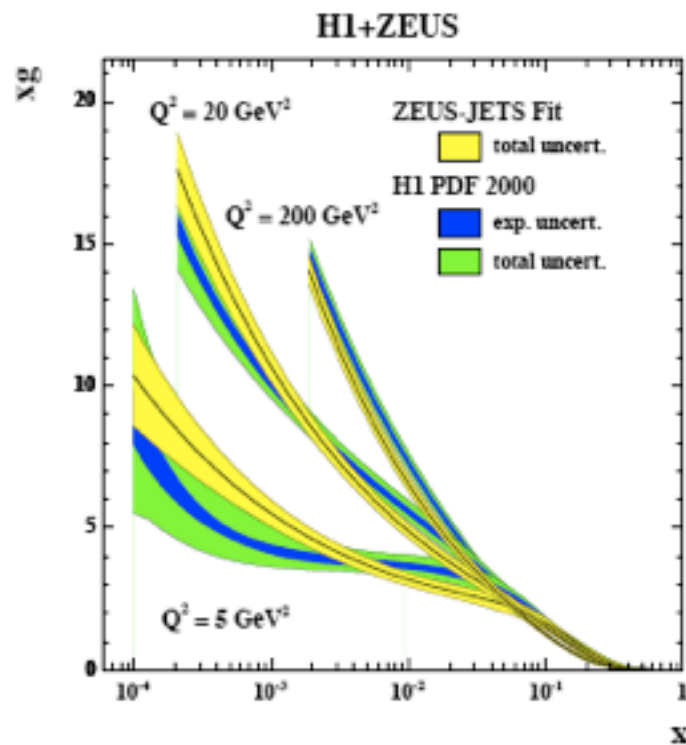
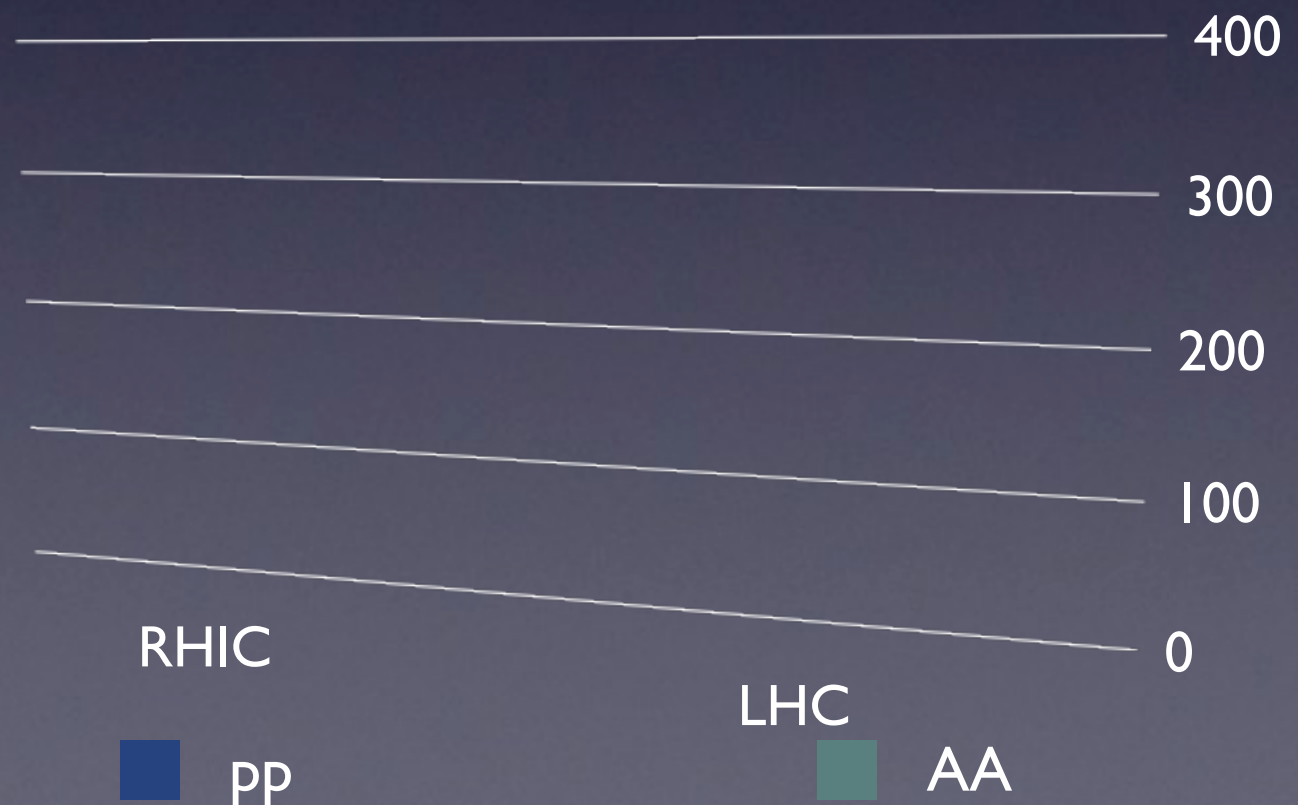
Estimates of gluon density

Extrapolation of gluon density
to various energies

Scale $Q^2 = 5 \text{ GeV}^2$

$$x \sim \frac{Q^2}{s}$$

gluon density



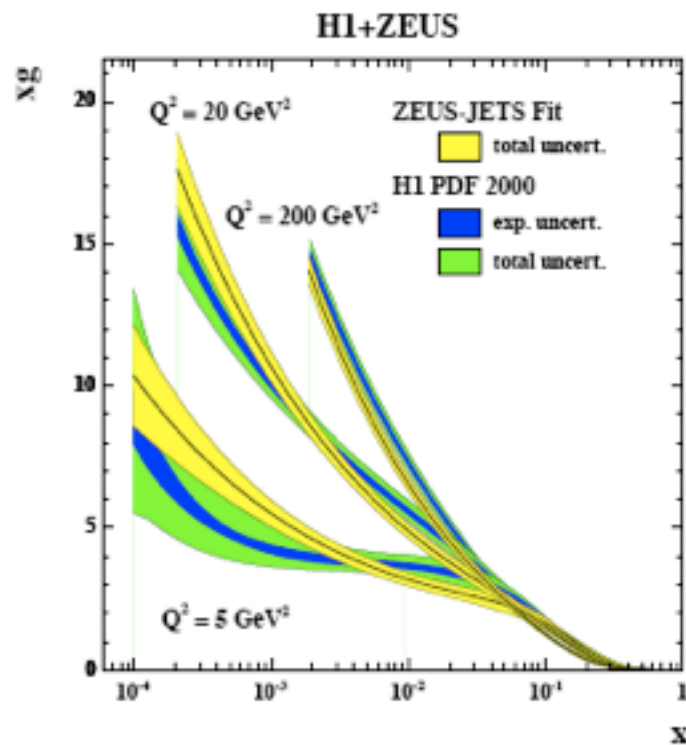
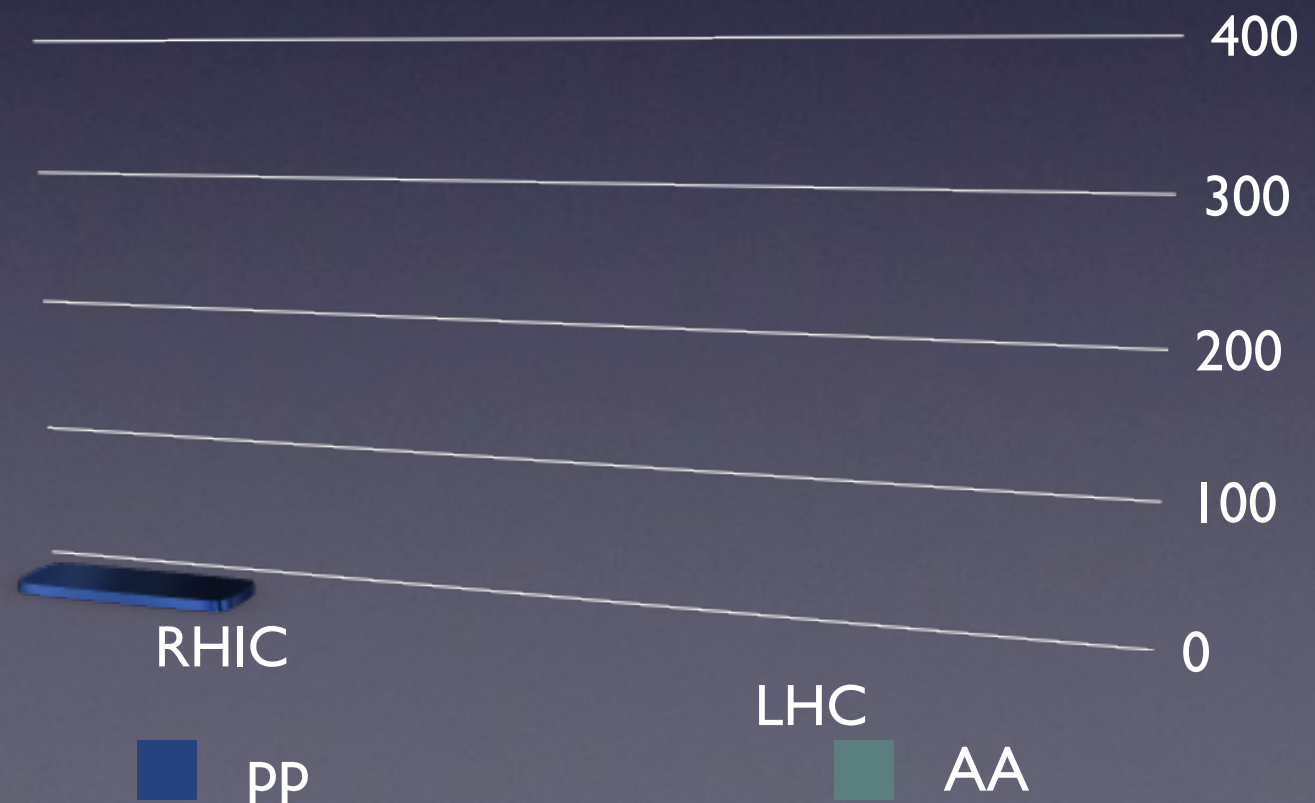
Estimates of gluon density

Extrapolation of gluon density
to various energies

Scale $Q^2 = 5 \text{ GeV}^2$

$$x \sim \frac{Q^2}{s}$$

gluon density



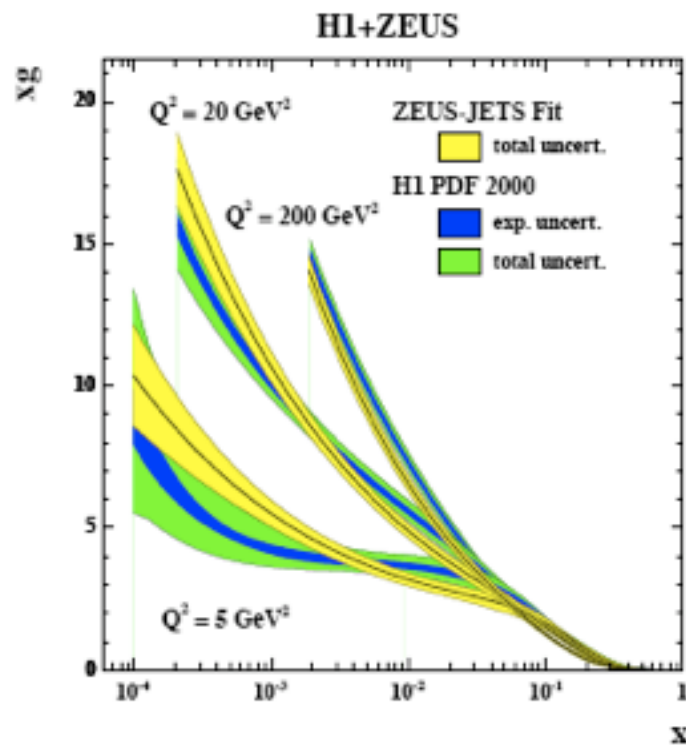
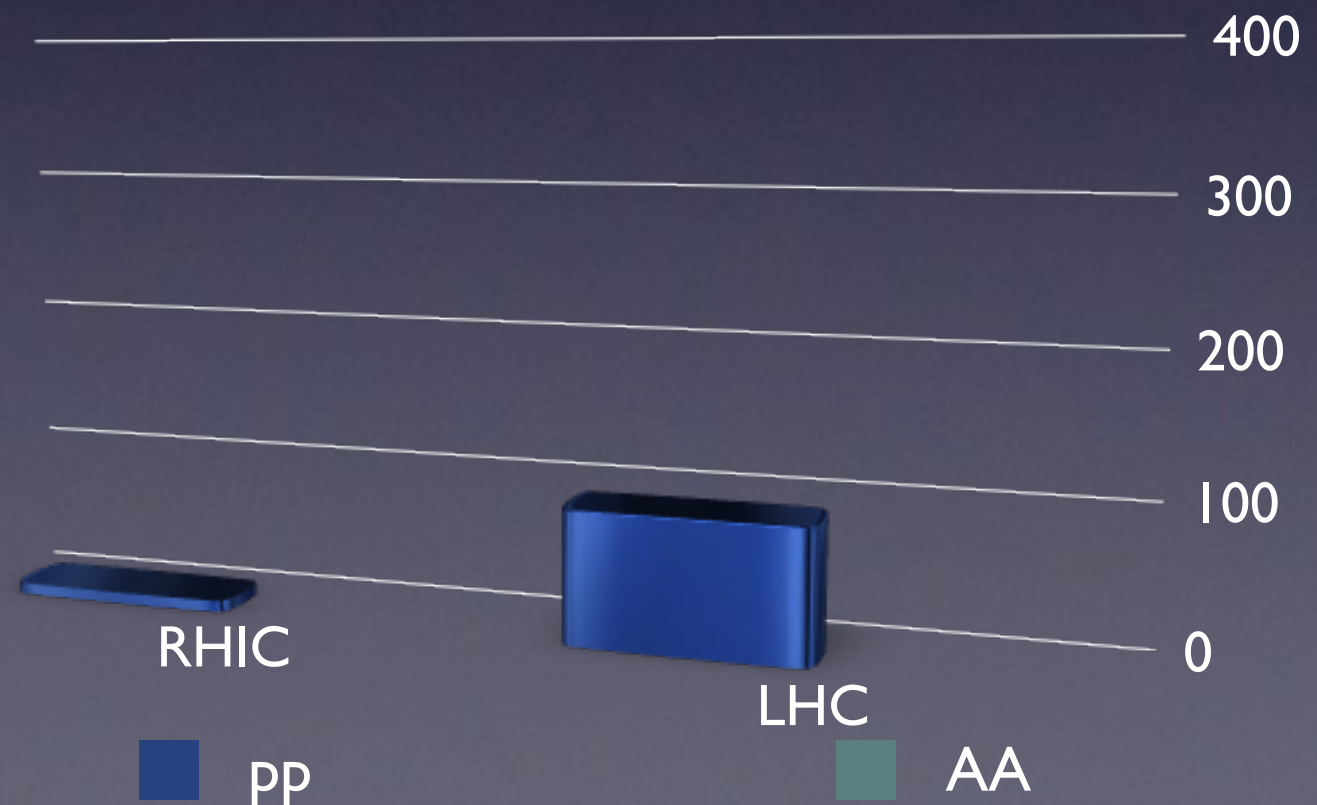
Estimates of gluon density

Extrapolation of gluon density
to various energies

Scale $Q^2 = 5 \text{ GeV}^2$

$$x \sim \frac{Q^2}{s}$$

gluon density



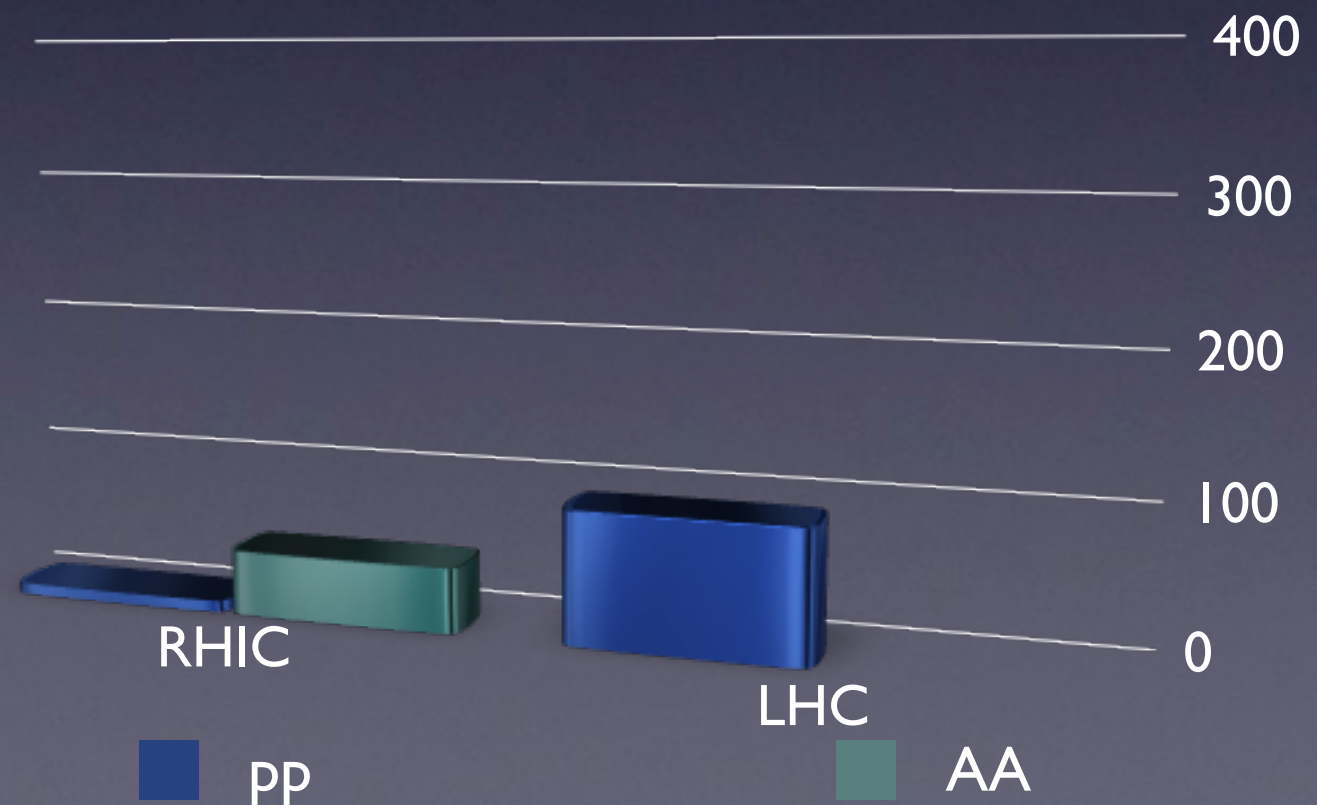
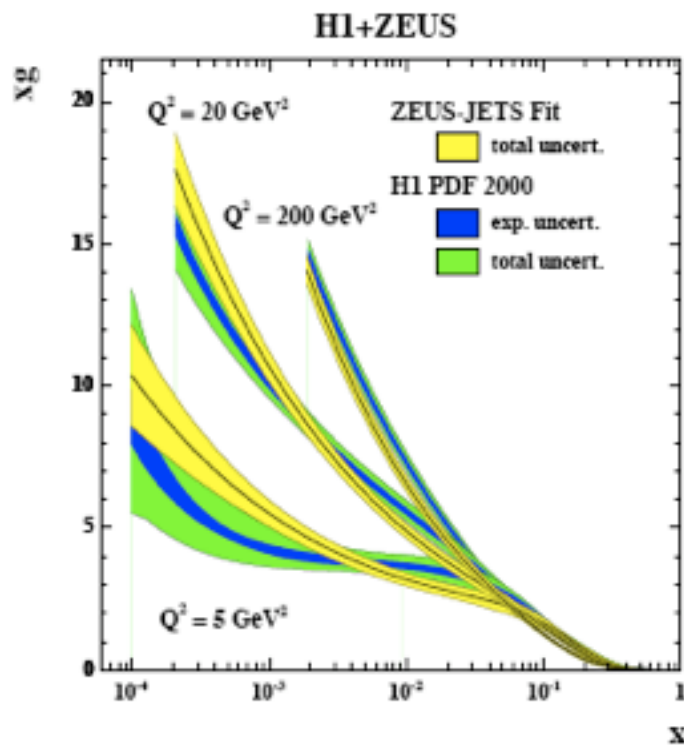
Estimates of gluon density

Extrapolation of gluon density
to various energies

Scale $Q^2 = 5 \text{ GeV}^2$

$$x \sim \frac{Q^2}{s}$$

gluon density



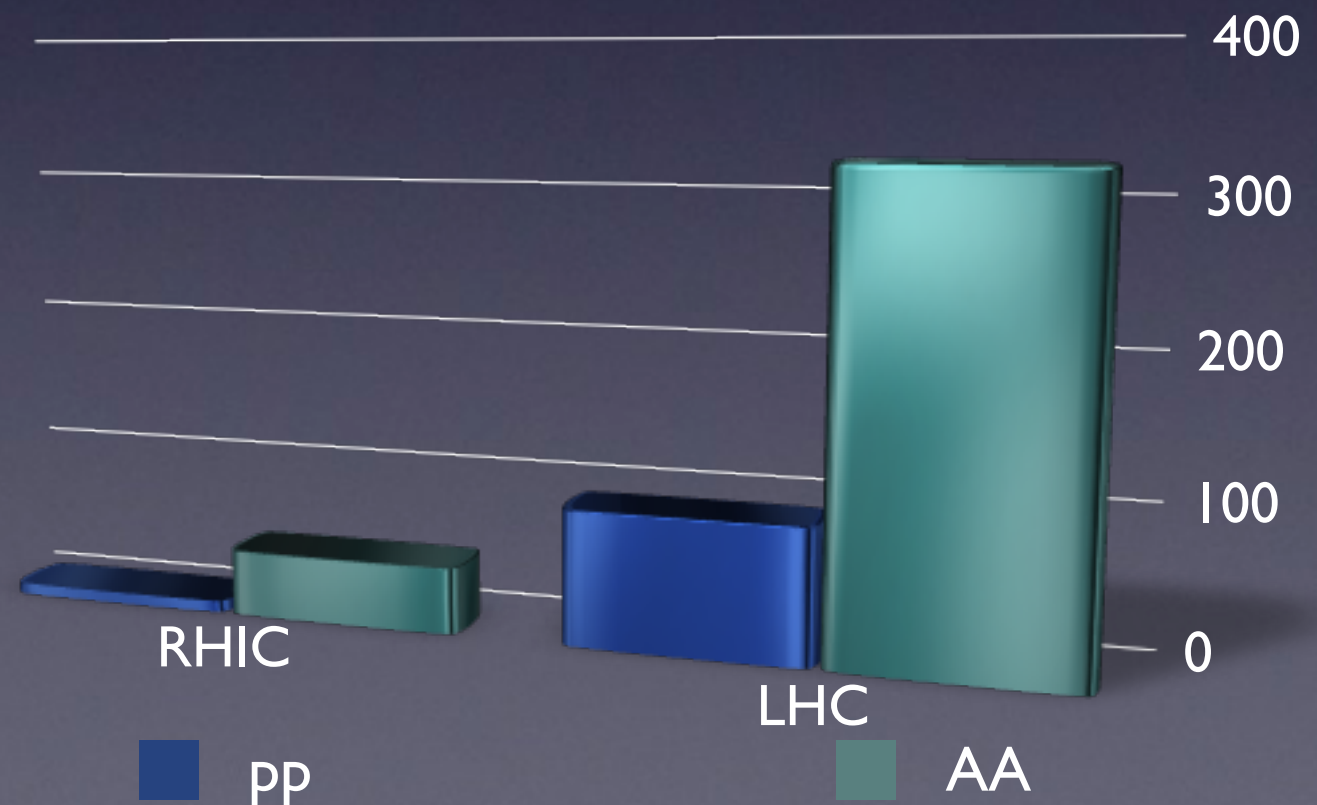
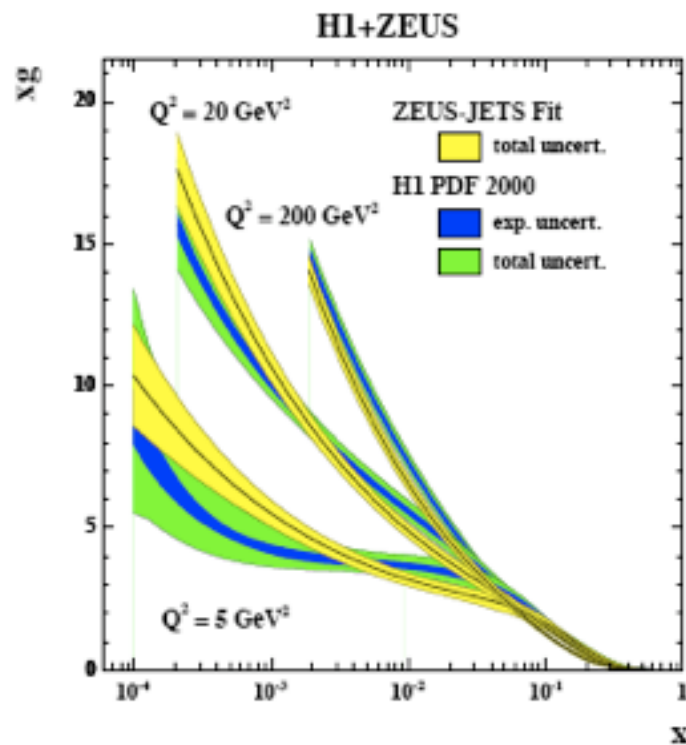
Estimates of gluon density

Extrapolation of gluon density
to various energies

Scale $Q^2 = 5 \text{ GeV}^2$

$$x \sim \frac{Q^2}{s}$$

gluon density



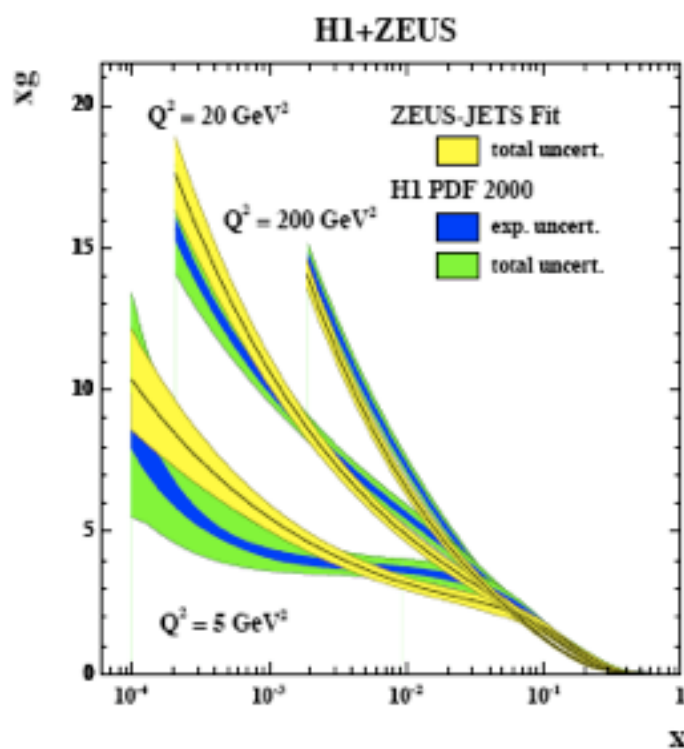
Estimates of gluon density

Extrapolation of gluon density to various energies

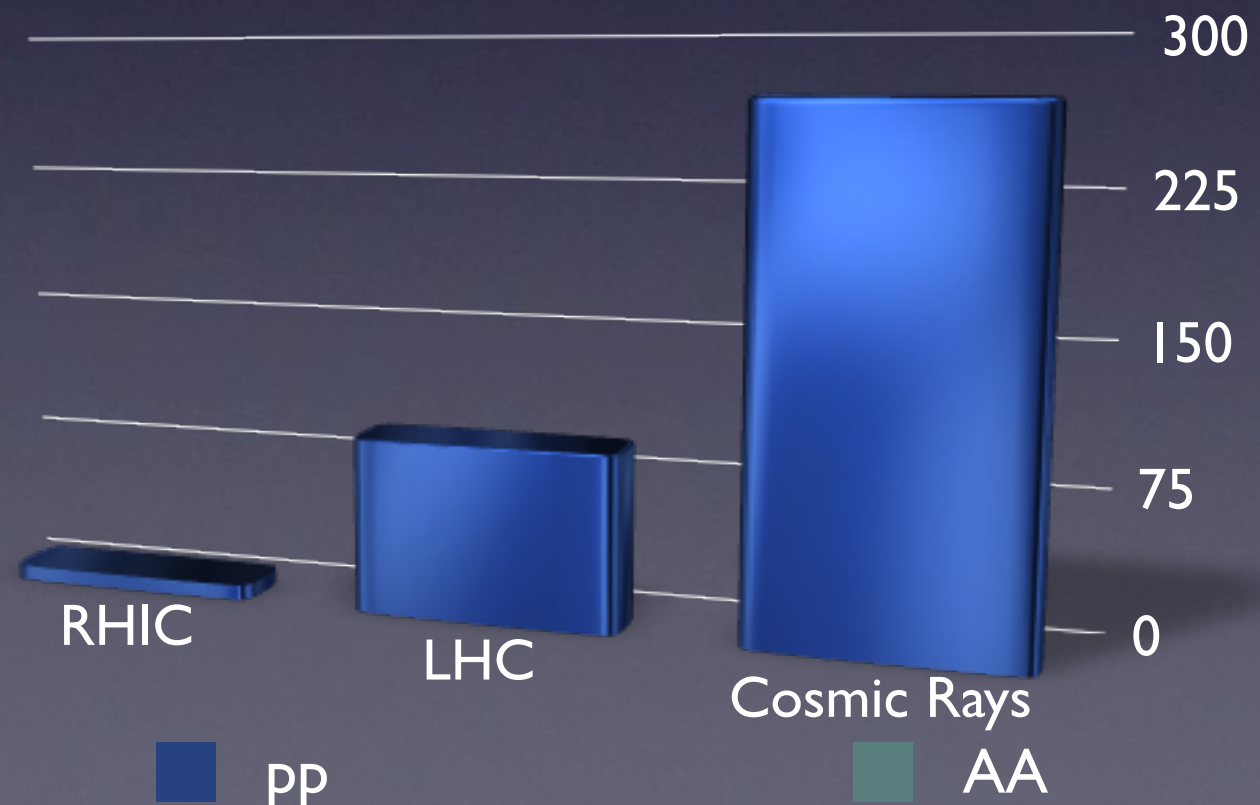
Scale $Q^2 = 5 \text{ GeV}^2$

$$x \sim \frac{Q^2}{s}$$

gluon density



- Increase of the gluon density either via increasing energy or increasing size of the projectile (AA)
- Very small x probed at LHC and Cosmic Ray energies.
- Large gluon densities.



Why the gluon density grows?

Grows with:

- increasing Q (resolution)
- decreasing x (increasing energy)

DGLAP evolution: in Q^2

Increasing photon virtuality, means increasing resolution.
More parton fluctuations resolved.

$$\frac{\partial}{\partial \ln Q^2 / \Lambda^2} f_a(x, Q^2) = P_{ab} \otimes f(x, Q^2)$$

splitting
function

P_{ab}

describes splitting of parton b into a

BFKL evolution: in x

Decreasing x or increasing total energy s . Resolution is fixed.
Opening the kinematic phase space for more parton emissions.

Again linear evolution in density, differential equation in x

$$\frac{df_g(x, k_T^2)}{d \ln 1/x} = \frac{\alpha_s N_c}{\pi} \int d^2 k'_T \mathcal{K}(k_T, k'_T) f_g(x, k'_T)$$

$\mathcal{K}(k, k')$ branching kernel for gluons

Solution:

$$f_g(x, k_T) \sim x^{-\omega_P}$$

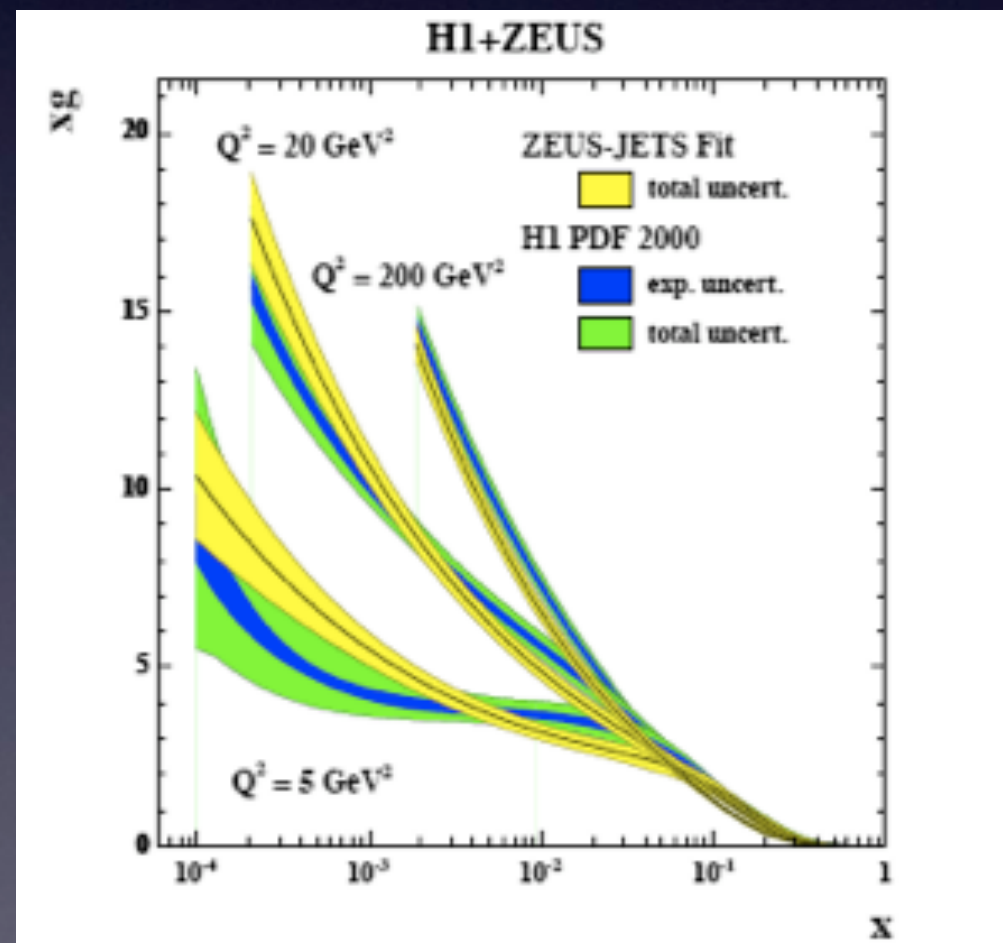
Leading exponent(spin)

$$\omega_P = j - 1 = \frac{\alpha_s N_c}{\pi} 4 \ln 2$$

Very fast increase of the density with small x !

Parton Saturation

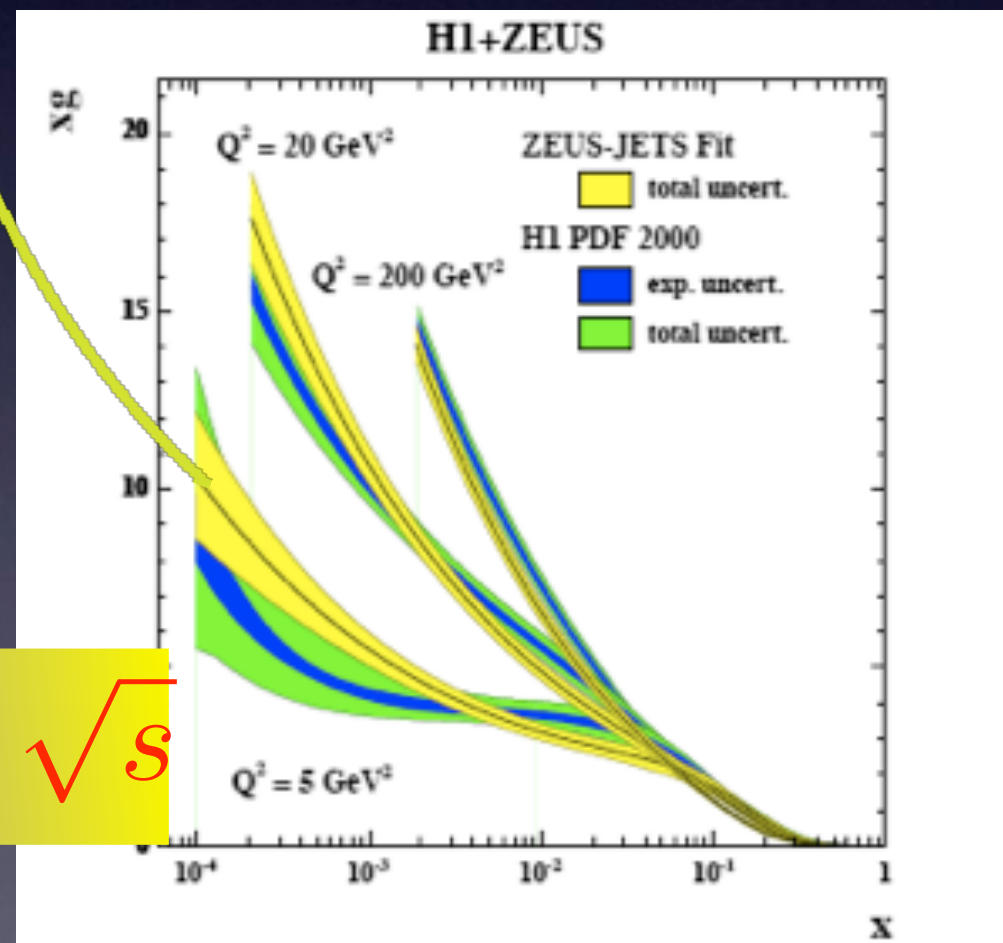
Can the gluon density rise
forever?
How fast?



Can the gluon density rise forever?

How fast?

very large density of gluons



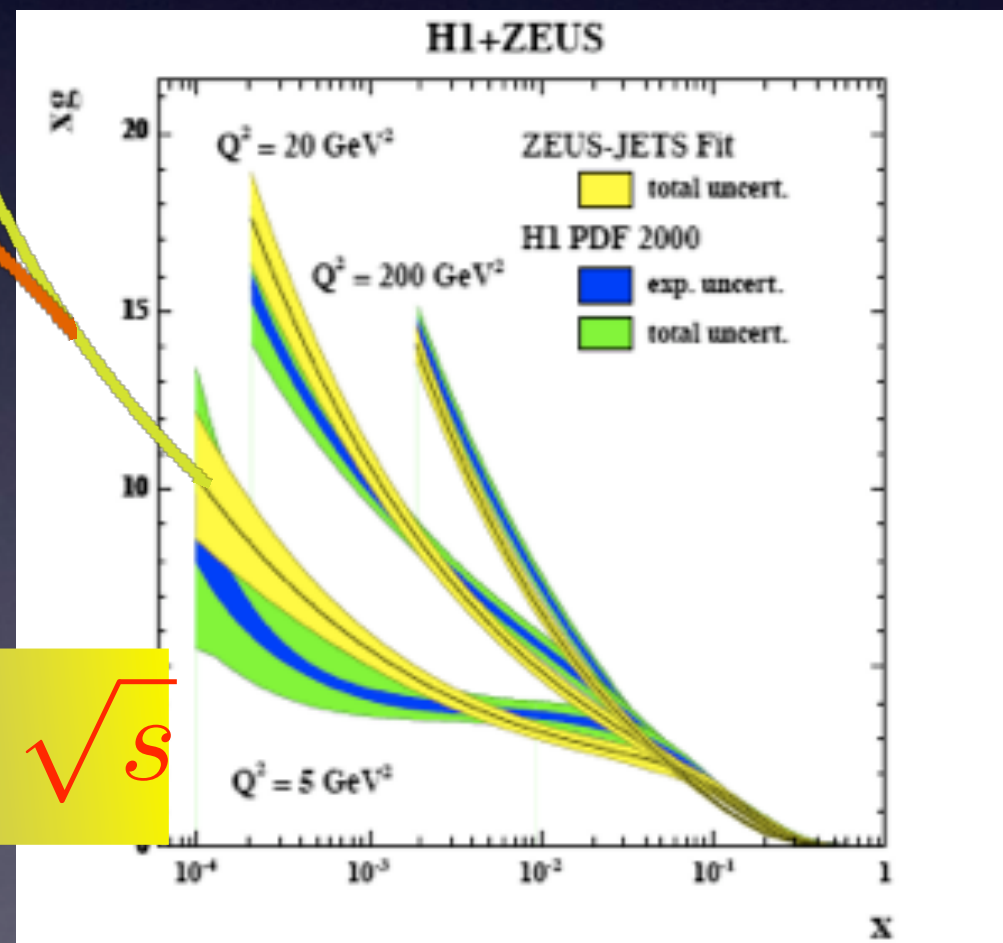
Increase energy $\sqrt{s}$

Can the gluon density rise forever?

How fast?

very large density of gluons

Increase energy $\sqrt{s}$



Can the gluon density rise forever?

Froissart bound is a limit on energy behavior of the total cross section:

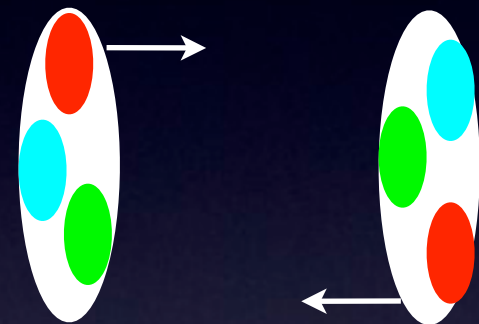
$$\sigma_{hh}^{\text{TOT}} \leq \frac{\pi}{m_{\pi}^2} (\ln s)^2$$

Can the gluon density rise forever?

Froissart bound is a limit on energy behavior of the total cross section:

$$\sigma_{hh}^{\text{TOT}} \leq \frac{\pi}{m_{\pi}^2} (\ln s)^2$$

Origin of growth of the cross section:



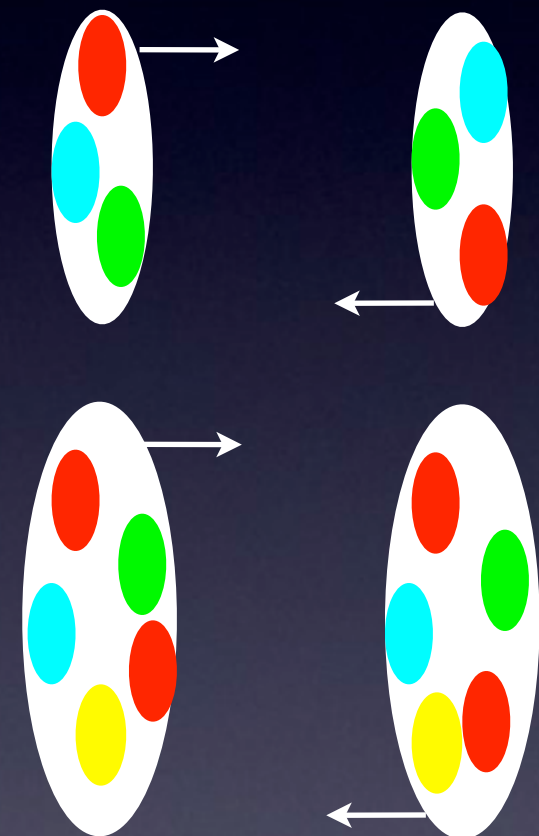
Can the gluon density rise forever?

Froissart bound is a limit on energy behavior of the total cross section:

$$\sigma_{hh}^{\text{TOT}} \leq \frac{\pi}{m_\pi^2} (\ln s)^2$$

Origin of growth of the cross section:

- Growth in the interaction area.
- Limited by the confinement.
- Strong force is short range: $R \rightarrow 1/m_\pi$



Can the gluon density rise forever?

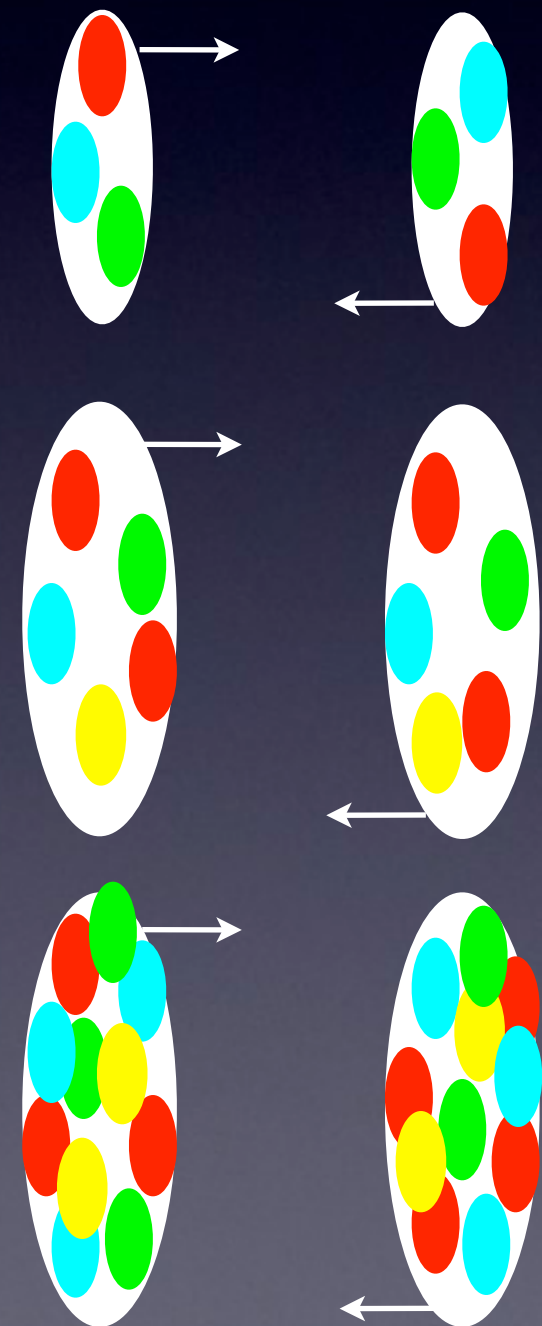
Froissart bound is a limit on energy behavior of the total cross section:

$$\sigma_{hh}^{\text{TOT}} \leq \frac{\pi}{m_\pi^2} (\ln s)^2$$

Origin of growth of the cross section:

- Growth in the interaction area.
- Limited by the confinement.
- Strong force is short range: $R \rightarrow 1/m_\pi$
- Increase in the density of the projectile.
- It is limited by the **unitarity** at fixed impact parameter. Probability of the interaction:

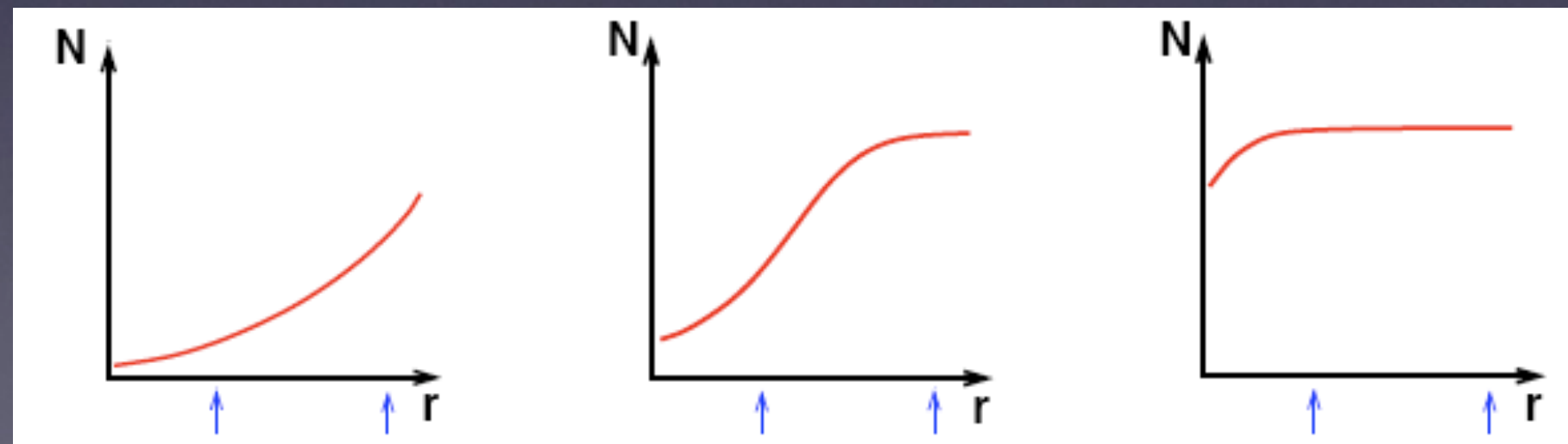
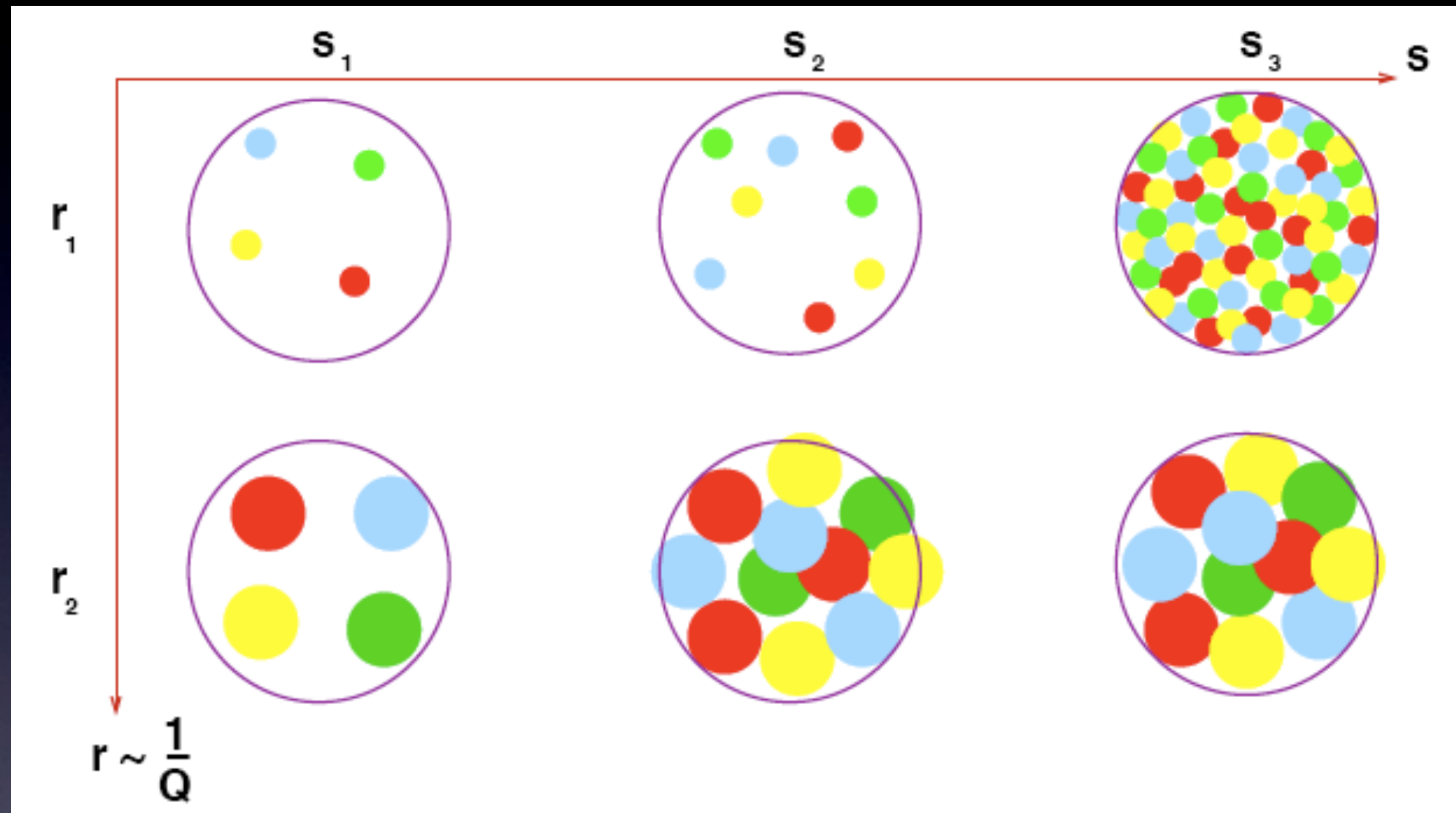
$$N(b) \leq 1$$



Parton saturation

energy of the interaction

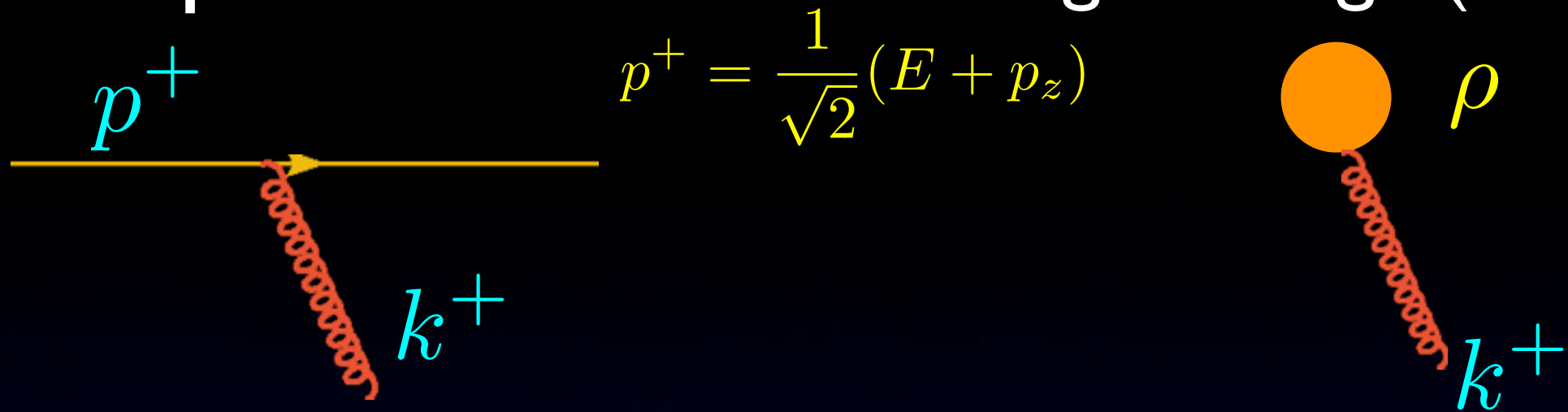
size of
the
probe



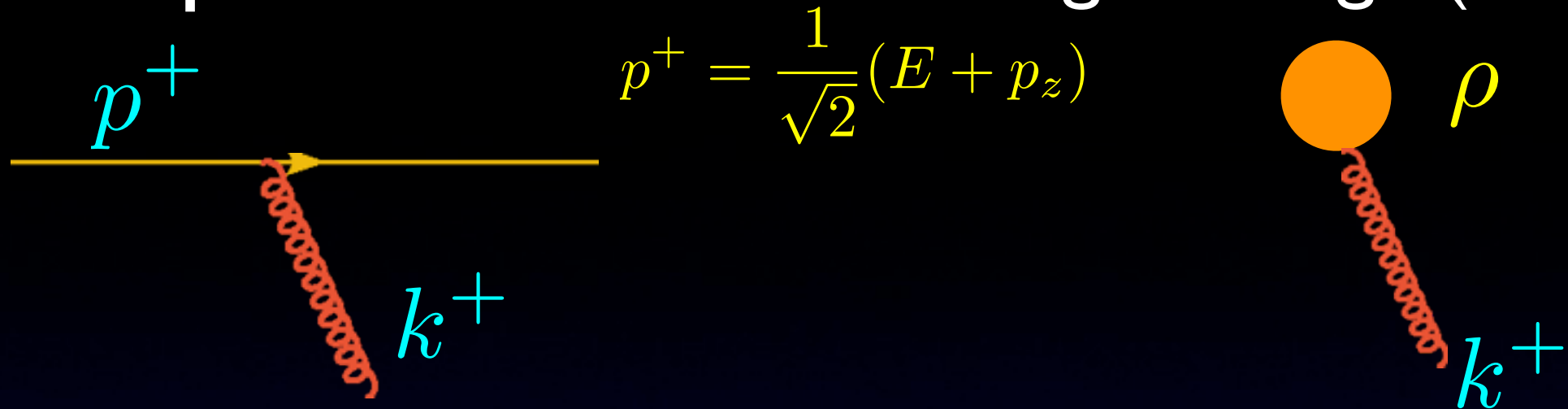
Microscopic mechanism:


$$p^+ = \frac{1}{\sqrt{2}}(E + p_z)$$

Microscopic mechanism: Single charge (source)

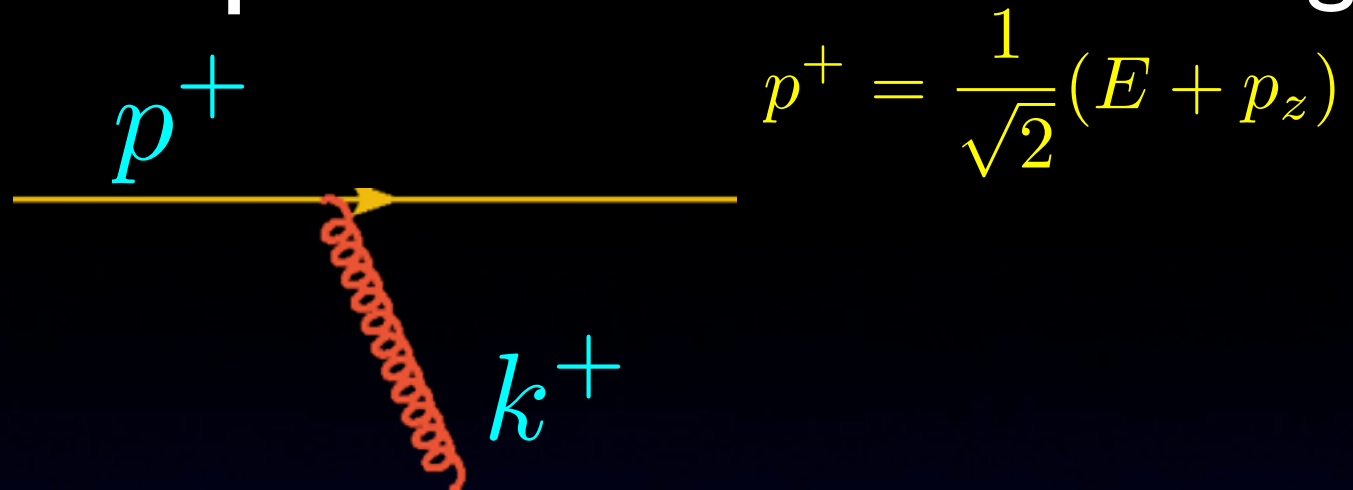


Microscopic mechanism: Single charge (source)

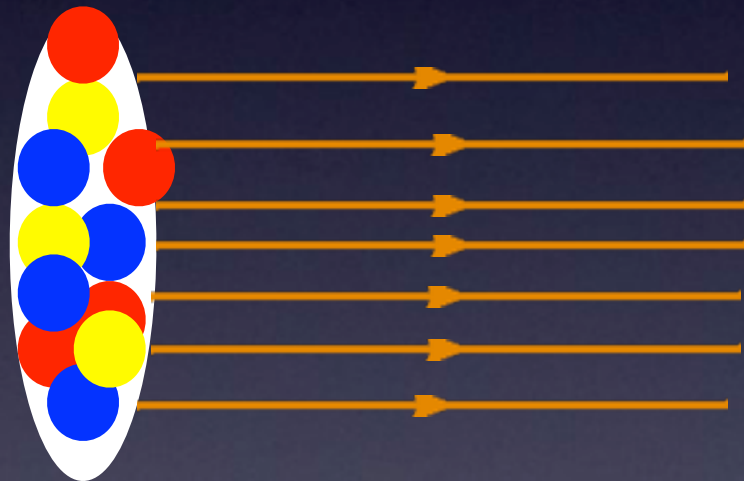


Fast hadron or a nucleus

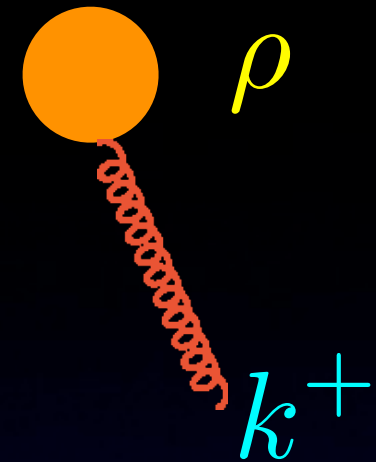
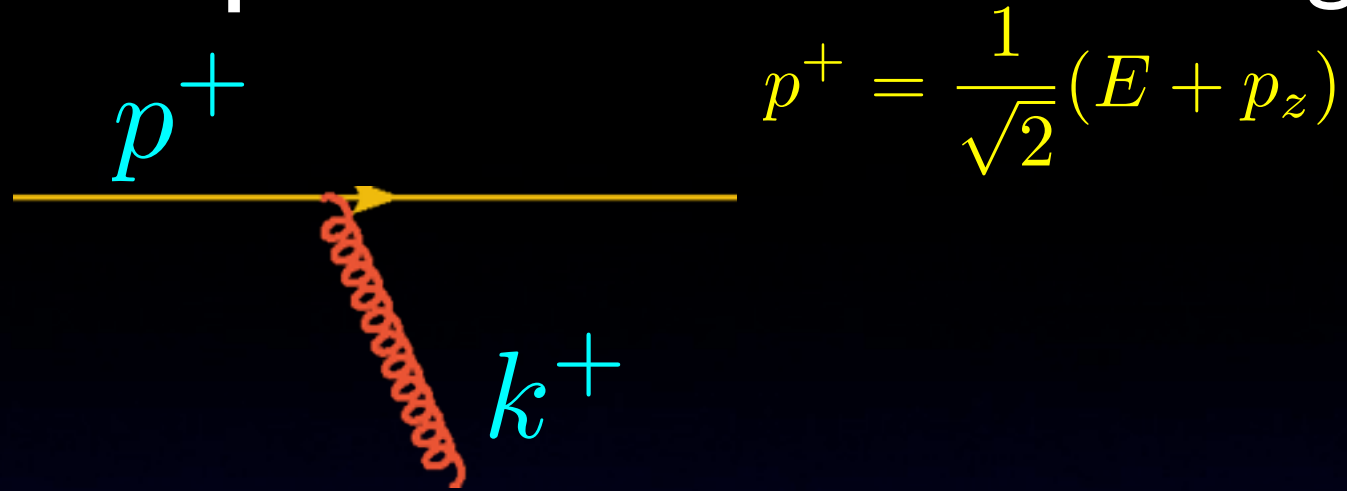
Microscopic mechanism: Single charge (source)



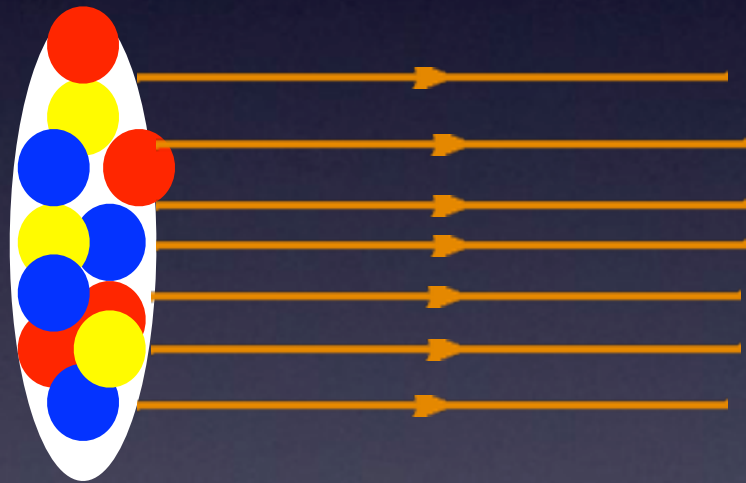
Fast hadron or a nucleus



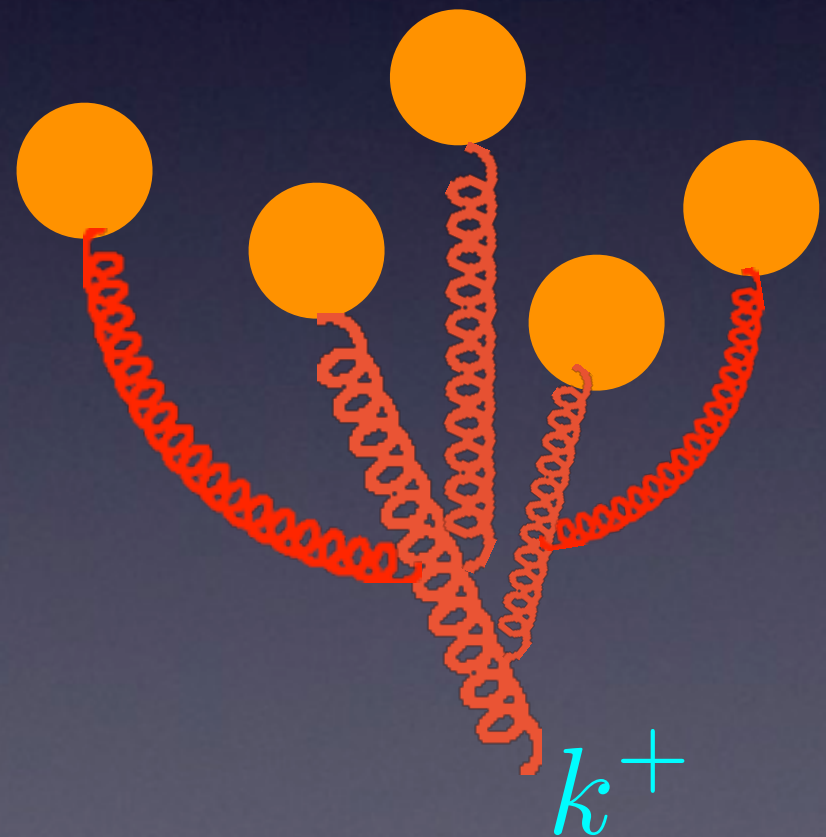
Microscopic mechanism: Single charge (source)



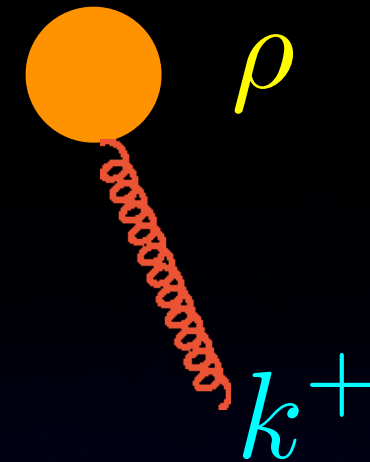
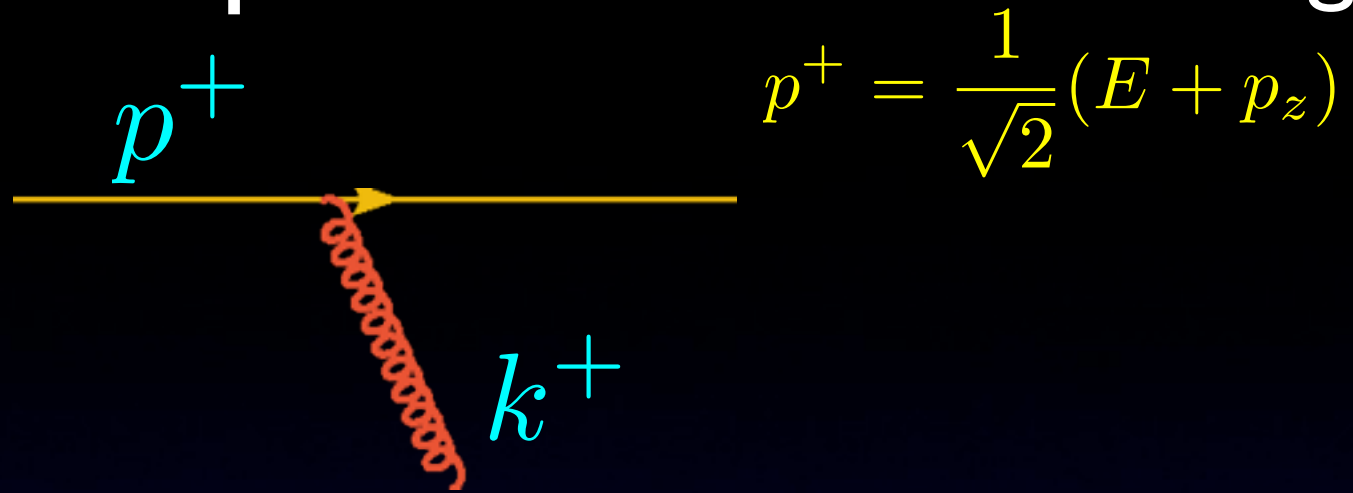
Fast hadron or a nucleus



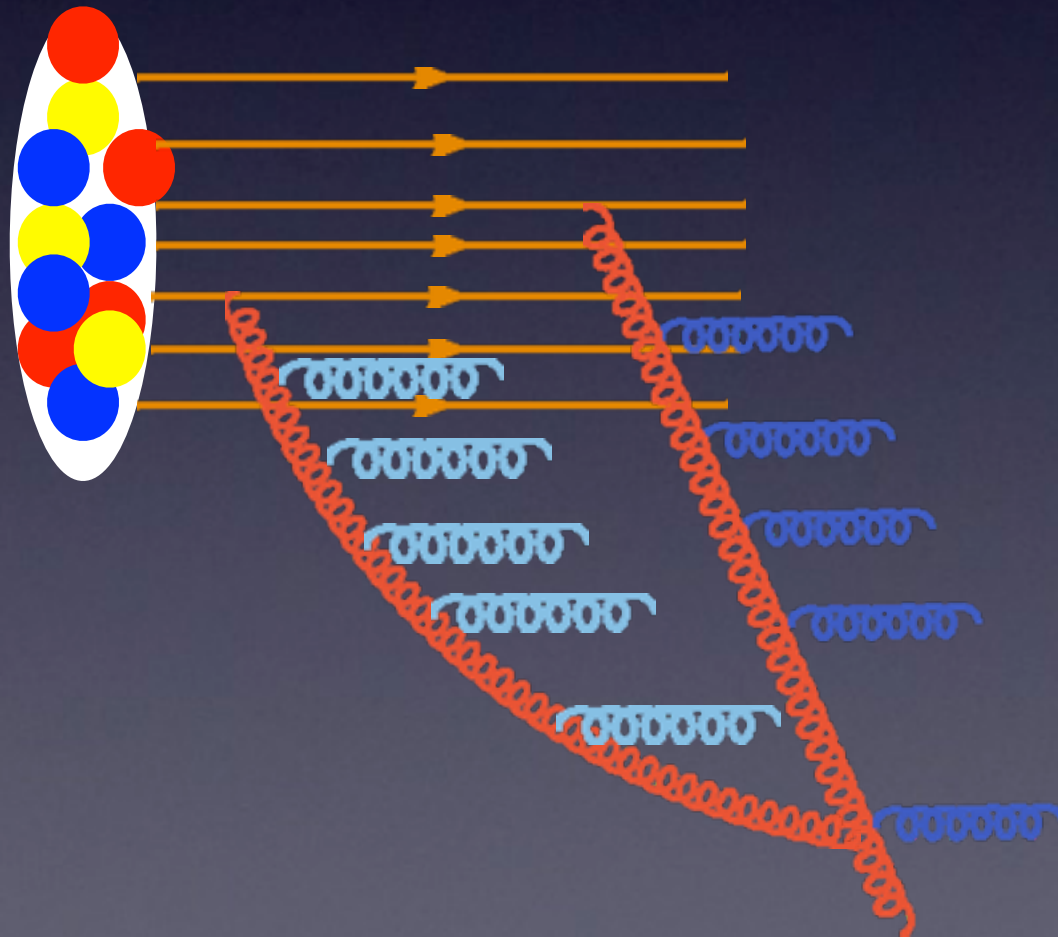
Many charges (sources)



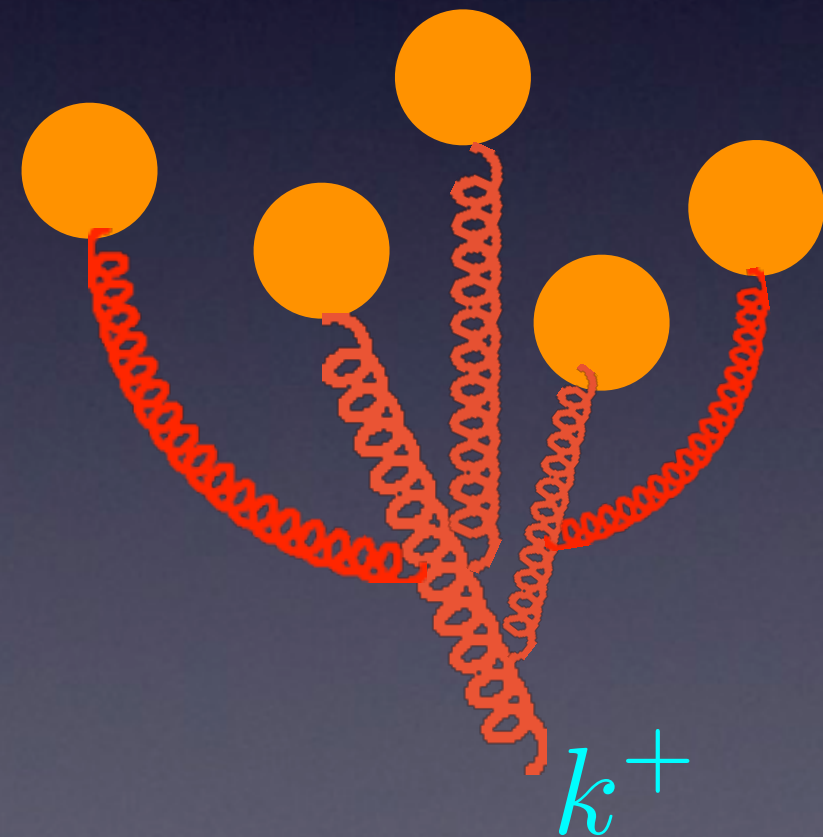
Microscopic mechanism: Single charge (source)



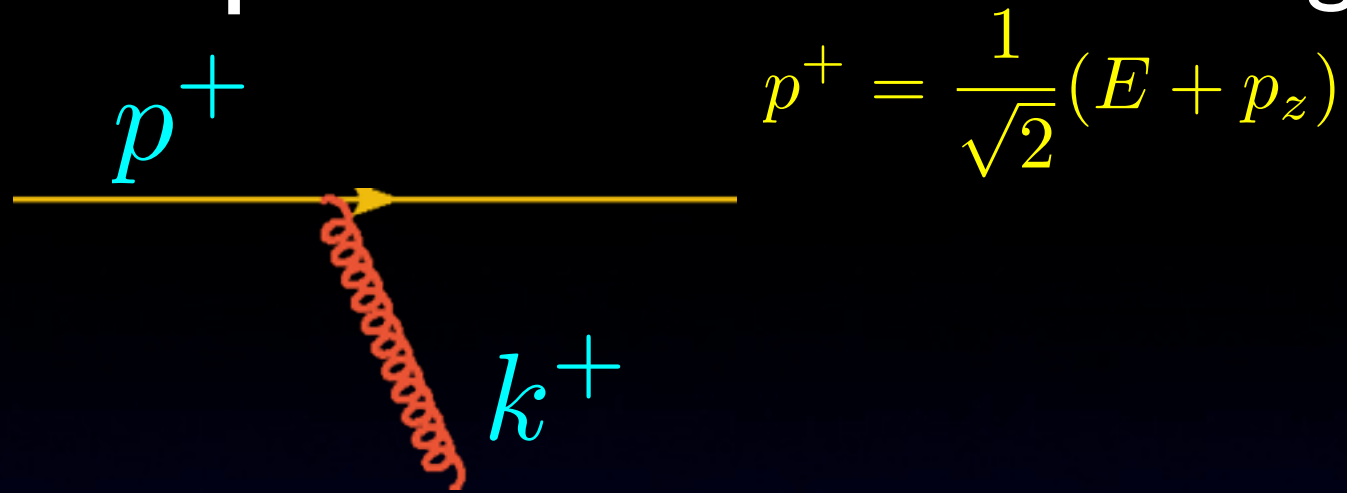
Fast hadron or a nucleus



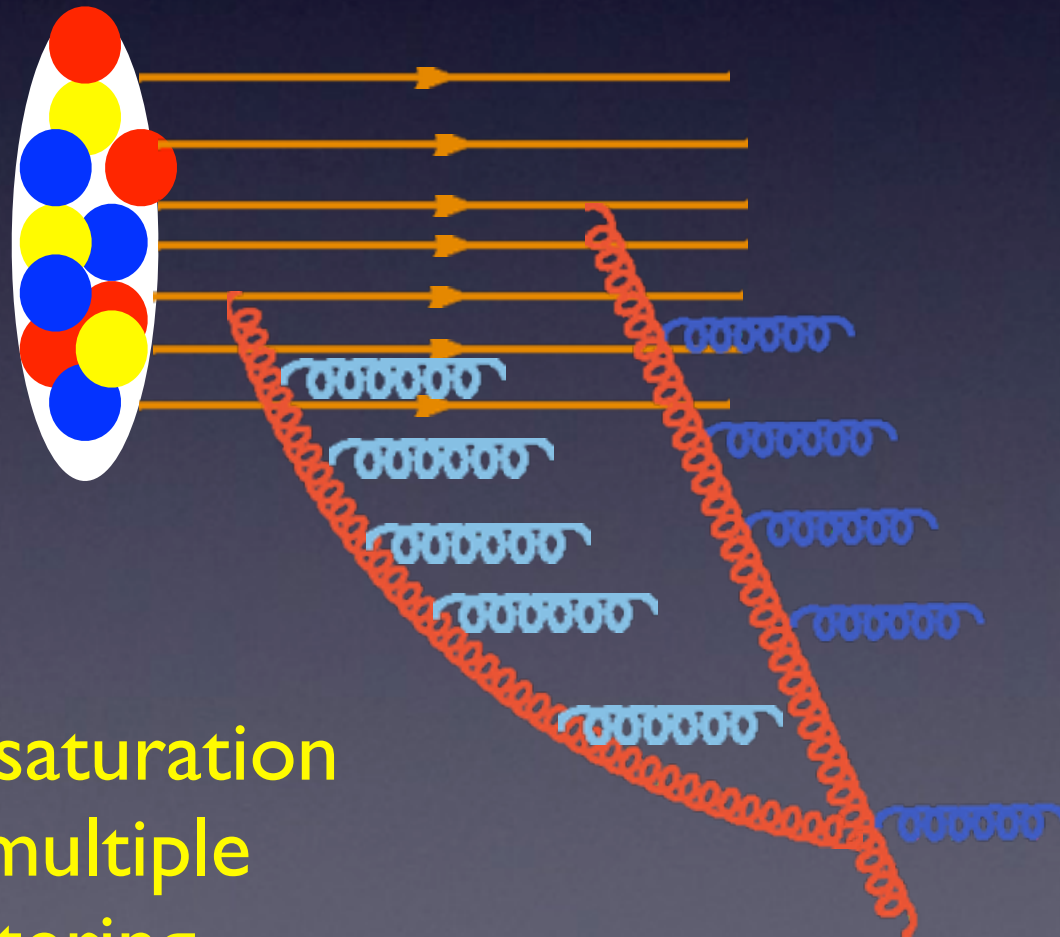
Many charges (sources)



Microscopic mechanism: Single charge (source)

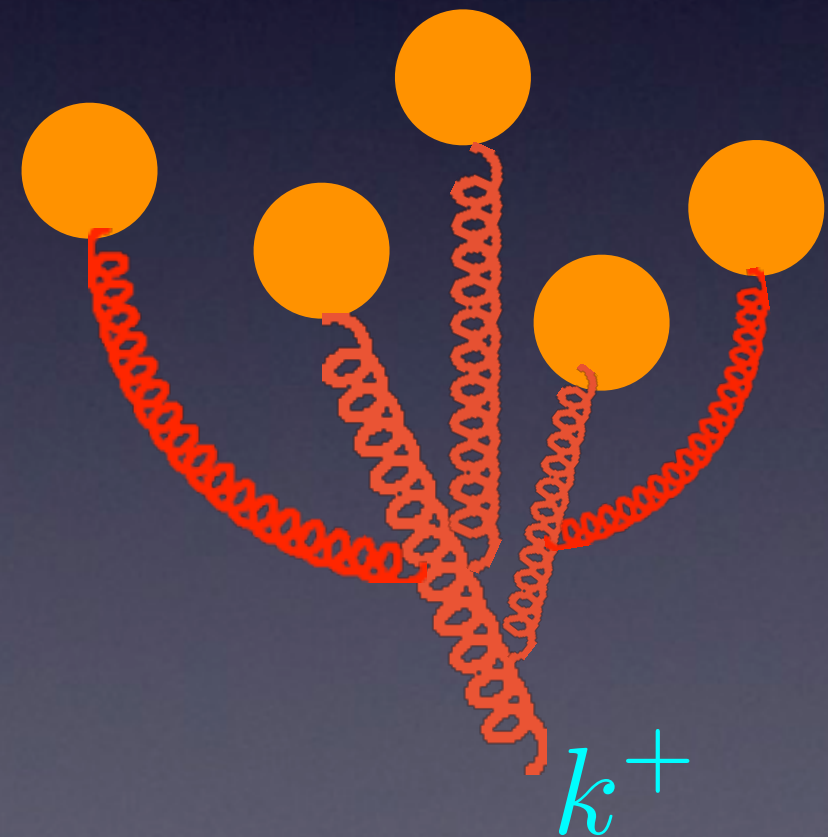


Fast hadron or a nucleus



Parton saturation
as a multiple
scattering.

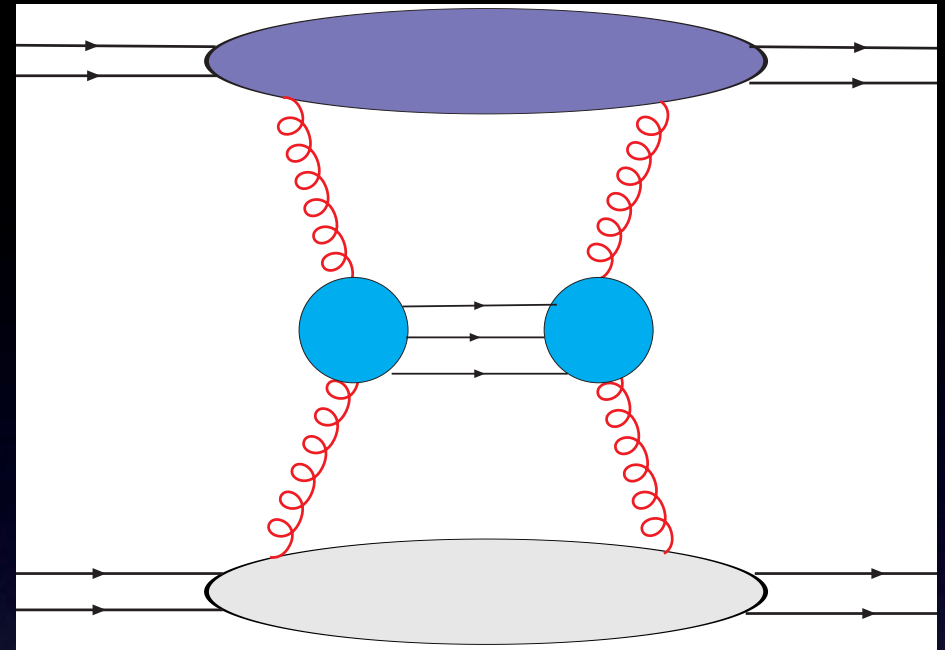
Many charges (sources)



Multiple scatterings

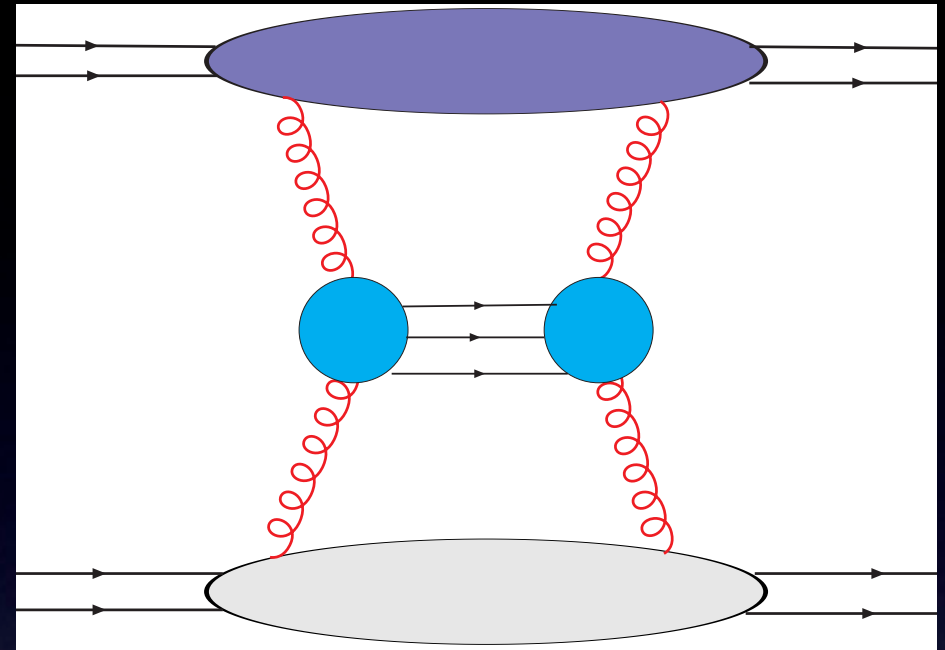
Multiple scatterings

Single scattering: 2-point function, measures gluon density(number).

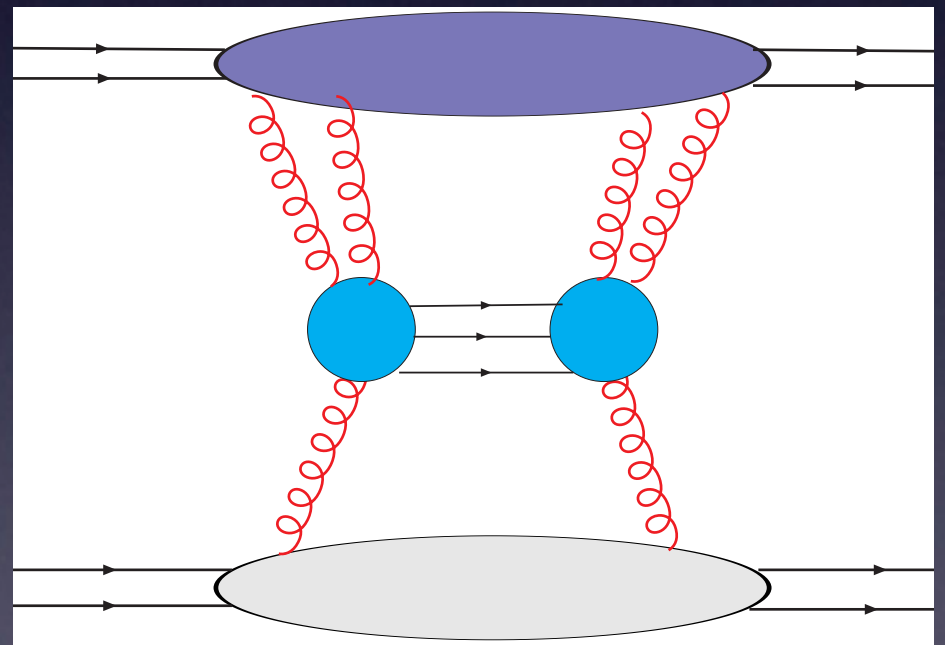


Multiple scatterings

Single scattering: 2-point function, measures gluon density(number).

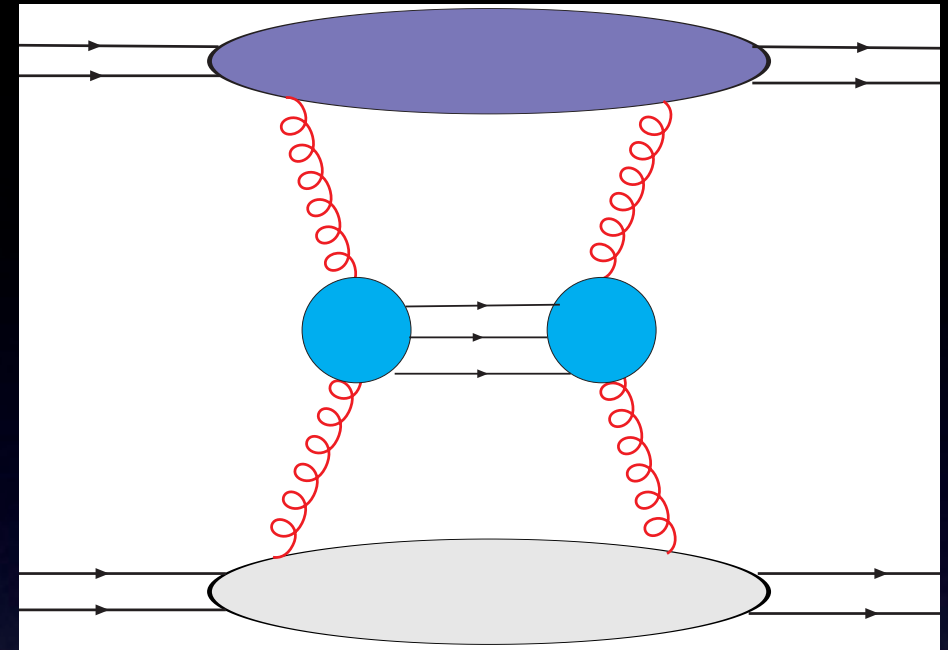


Double scattering: 4-point function, measures correlation.

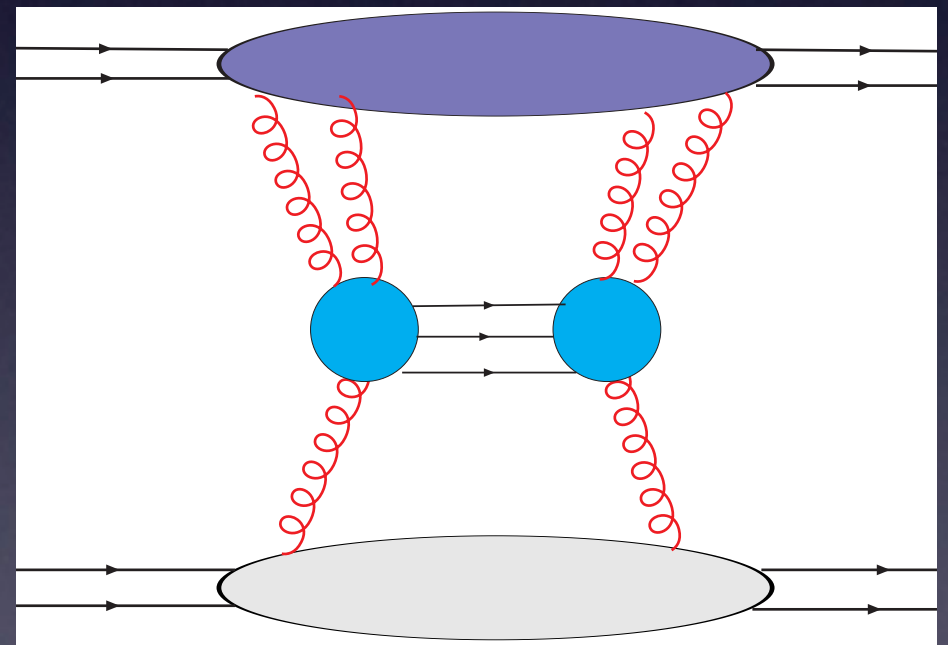


Multiple scatterings

Single scattering: 2-point function, measures gluon density(number).



Double scattering: 4-point function, measures correlation.



Color Glass Condensate: an effective theory derived from QCD in the limit of high energies and high densities which systematically incorporates higher correlators.

Color Glass Condensate

Can compute the evolution of the distribution of the color sources in the projectile with rapidity.

Color Glass Condensate

Can compute the evolution of the distribution of the color sources in the projectile with rapidity.

$$\frac{\partial W_Y}{\partial Y} = \mathcal{H}W_Y$$

W_Y

distribution functional describes the color sources in the projectile at given rapidity

Color Glass Condensate

Can compute the evolution of the distribution of the color sources in the projectile with rapidity.

$$\frac{\partial W_Y}{\partial Y} = \mathcal{H} W_Y$$

W_Y

distribution functional describes the color sources in the projectile at given rapidity

$$\mathcal{H} = \frac{1}{2} \int_{x_\perp, y_\perp} \frac{\delta}{\delta A^+(y_\perp)} \eta(x_\perp, y_\perp) \frac{\delta}{\delta A^+(x_\perp)}$$

JIMWLK Hamiltonian

Color Glass Condensate

Can compute the evolution of the distribution of the color sources in the projectile with rapidity.

$$\frac{\partial W_Y}{\partial Y} = \mathcal{H} W_Y$$

W_Y

distribution functional describes the color sources in the projectile at given rapidity

$$\mathcal{H} = \frac{1}{2} \int_{x_\perp, y_\perp} \frac{\delta}{\delta A^+(y_\perp)} \eta(x_\perp, y_\perp) \frac{\delta}{\delta A^+(x_\perp)}$$

JIMWLK Hamiltonian

$$-\nabla_\perp^2 A^+(x_\perp) = \rho(x_\perp)$$

Color charge(source)

Color Glass Condensate

Can compute the evolution of the distribution of the color sources in the projectile with rapidity.

$$\frac{\partial W_Y}{\partial Y} = \mathcal{H} W_Y$$

W_Y

distribution functional describes the color sources in the projectile at given rapidity

$$\mathcal{H} = \frac{1}{2} \int_{x_\perp, y_\perp} \frac{\delta}{\delta A^+(y_\perp)} \eta(x_\perp, y_\perp) \frac{\delta}{\delta A^+(x_\perp)}$$

JIMWLK Hamiltonian

$$-\nabla_\perp^2 A^+(x_\perp) = \rho(x_\perp)$$

Color charge(source)

Higher point correlators are included in the evolution.

Color Glass Condensate

Can compute the evolution of the distribution of the color sources in the projectile with rapidity.

$$\frac{\partial W_Y}{\partial Y} = \mathcal{H} W_Y$$

W_Y

distribution functional describes the color sources in the projectile at given rapidity

$$\mathcal{H} = \frac{1}{2} \int_{x_\perp, y_\perp} \frac{\delta}{\delta A^+(y_\perp)} \eta(x_\perp, y_\perp) \frac{\delta}{\delta A^+(x_\perp)}$$

JIMWLK Hamiltonian

$$-\nabla_\perp^2 A^+(x_\perp) = \rho(x_\perp)$$

Color charge(source)

Higher point correlators are included in the evolution.

Evolution resums leading powers of $\ln 1/x$.

Color Glass Condensate

Can compute the evolution of the distribution of the color sources in the projectile with rapidity.

$$\frac{\partial W_Y}{\partial Y} = \mathcal{H} W_Y$$

W_Y

distribution functional describes the color sources in the projectile at given rapidity

$$\mathcal{H} = \frac{1}{2} \int_{x_\perp, y_\perp} \frac{\delta}{\delta A^+(y_\perp)} \eta(x_\perp, y_\perp) \frac{\delta}{\delta A^+(x_\perp)}$$

JIMWLK Hamiltonian

$$-\nabla_\perp^2 A^+(x_\perp) = \rho(x_\perp)$$

Color charge(source)

Higher point correlators are included in the evolution.

Evolution resums leading powers of $\ln 1/x$.

For small densities in the projectile the evolution equation reduces to the BFKL evolution equation for the gluon density.

The evolution equation becomes nonlinear in density

$$\frac{df_g(x, k_T^2)}{d \ln 1/x} = \frac{\alpha_s N_c}{\pi} \int d^2 k'_T \mathcal{K}(k_T, k'_T) f_g(x, k'_T)$$

The evolution equation becomes nonlinear in density

$$\frac{df_g(x, k_T^2)}{d \ln 1/x} = \frac{\alpha_s N_c}{\pi} \int d^2 k'_T \mathcal{K}(k_T, k'_T) f_g(x, k'_T) - \frac{\alpha_s N_c}{\pi} (f_g(x, k_T^2))^2$$

*L.V.Gribov, E. Levin, M. Ryskin;
Mueller, Qiu; I. Balitsky, Y. Kovchegov; J. Jalilian-
Marian, E. Iancu, L. McLerran, H. Weigert,
Leonidov*

The evolution equation becomes nonlinear in density

$$\frac{df_g(x, k_T^2)}{d \ln 1/x} = \frac{\alpha_s N_c}{\pi} \int d^2 k'_T \mathcal{K}(k_T, k'_T) f_g(x, k'_T) - \frac{\alpha_s N_c}{\pi} (f_g(x, k_T^2))^2$$

*L.V.Gribov, E. Levin, M. Ryskin;
Mueller, Qiu; I. Balitsky, Y. Kovchegov; J. Jalilian-
Marian, E. Iancu, L. McLerran, H. Weigert,
Leonidov*

Note: Compare with Verhulst logistic equation for the population dynamics.

The evolution equation becomes nonlinear in density

$$\frac{df_g(x, k_T^2)}{d \ln 1/x} = \frac{\alpha_s N_c}{\pi} \int d^2 k'_T \mathcal{K}(k_T, k'_T) f_g(x, k'_T) - \frac{\alpha_s N_c}{\pi} (f_g(x, k_T^2))^2$$

L.V.Gribov, E. Levin, M. Ryskin;
Mueller, Qiu; I. Balitsky, Y. Kovchegov; J. Jalilian-
Marian, E. Iancu, L. McLerran, H. Weigert,
Leonidov

Note: Compare with Verhulst logistic equation for the population dynamics.

Linear term: gluon splitting, increase of the density.

The evolution equation becomes nonlinear in density

$$\frac{df_g(x, k_T^2)}{d \ln 1/x} = \frac{\alpha_s N_c}{\pi} \int d^2 k'_T \mathcal{K}(k_T, k'_T) f_g(x, k'_T) - \frac{\alpha_s N_c}{\pi} (f_g(x, k_T^2))^2$$

L.V.Gribov, E. Levin, M. Ryskin;
Mueller, Qiu; I. Balitsky, Y. Kovchegov; J. Jalilian-
Marian, E. Iancu, L. McLerran, H. Weigert,
Leonidov

Note: Compare with Verhulst logistic equation for the population dynamics.

Linear term: gluon splitting, increase of the density.

Nonlinear term: gluon merging, slow down the growth of the density with the energy.

The evolution equation becomes nonlinear in density

$$\frac{df_g(x, k_T^2)}{d \ln 1/x} = \frac{\alpha_s N_c}{\pi} \int d^2 k'_T \mathcal{K}(k_T, k'_T) f_g(x, k'_T) - \frac{\alpha_s N_c}{\pi} (f_g(x, k_T^2))^2$$

L.V.Gribov, E. Levin, M. Ryskin;
Mueller, Qiu; I. Balitsky, Y. Kovchegov; J. Jalilian-
Marian, E. Iancu, L. McLerran, H. Weigert,
Leonidov

Note: Compare with Verhulst logistic equation for the population dynamics.

Linear term: gluon splitting, increase of the density.

Nonlinear term: gluon merging, slow down the growth of the density with the energy.

Equilibrium: nonlinear compensates the linear term.

The evolution equation becomes nonlinear in density

$$\frac{df_g(x, k_T^2)}{d \ln 1/x} = \frac{\alpha_s N_c}{\pi} \int d^2 k'_T \mathcal{K}(k_T, k'_T) f_g(x, k'_T) - \frac{\alpha_s N_c}{\pi} (f_g(x, k_T^2))^2$$

L.V.Gribov, E. Levin, M. Ryskin;
Mueller, Qiu; I. Balitsky, Y. Kovchegov; J. Jalilian-
Marian, E. Iancu, L. McLerran, H. Weigert,
Leonidov

Note: Compare with Verhulst logistic equation for the population dynamics.

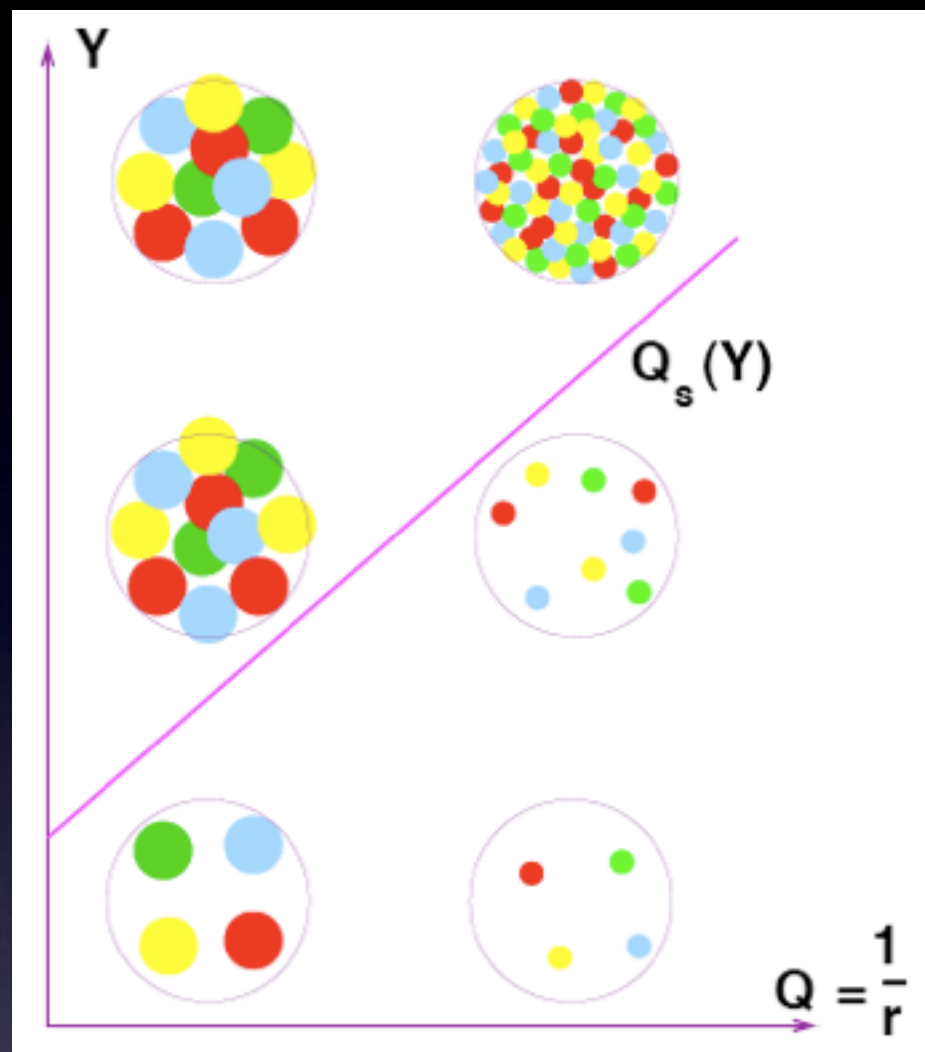
Linear term: gluon splitting, increase of the density.

Nonlinear term: gluon merging, slow down the growth of the density with the energy.

Equilibrium: nonlinear compensates the linear term.

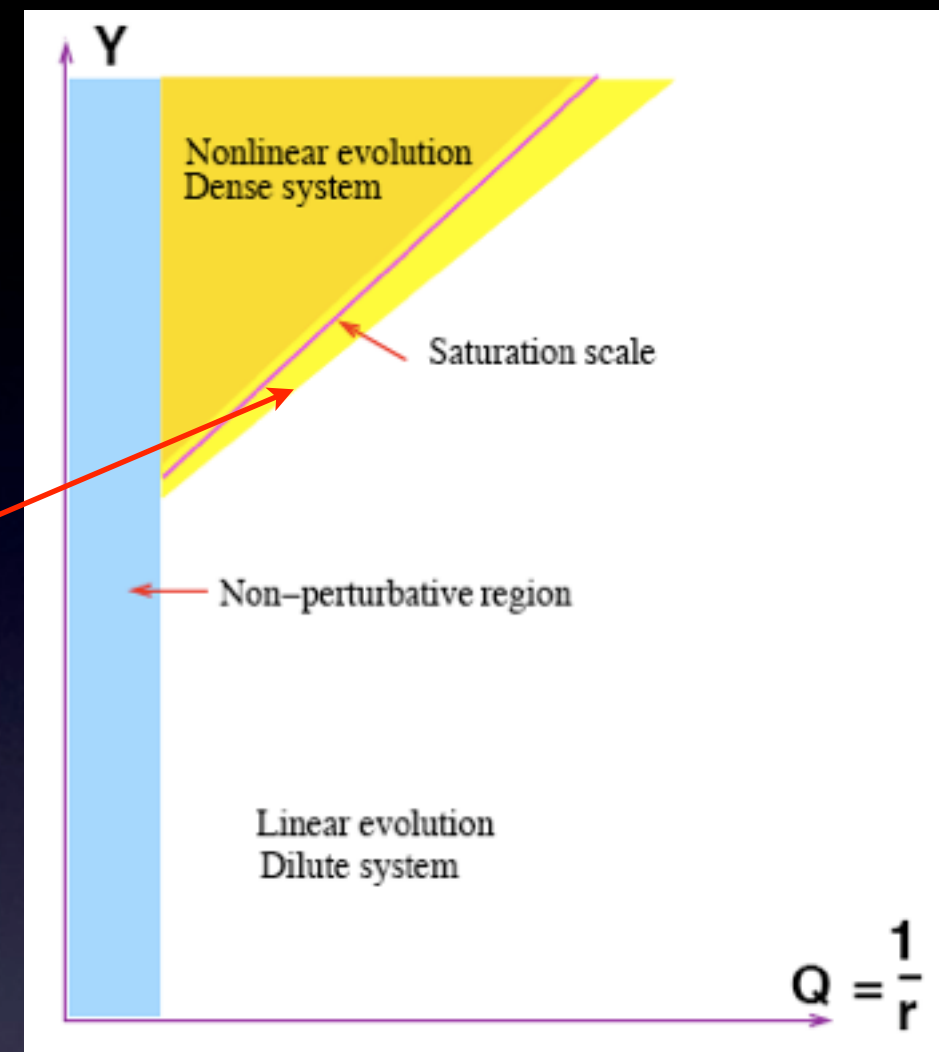
parton saturation

Saturation scale



transition between
dilute and dense is
rather smooth

extended region of
transition



saturation scale

$$Q_s(x) \sim x^{-\lambda}$$

Dynamically generated

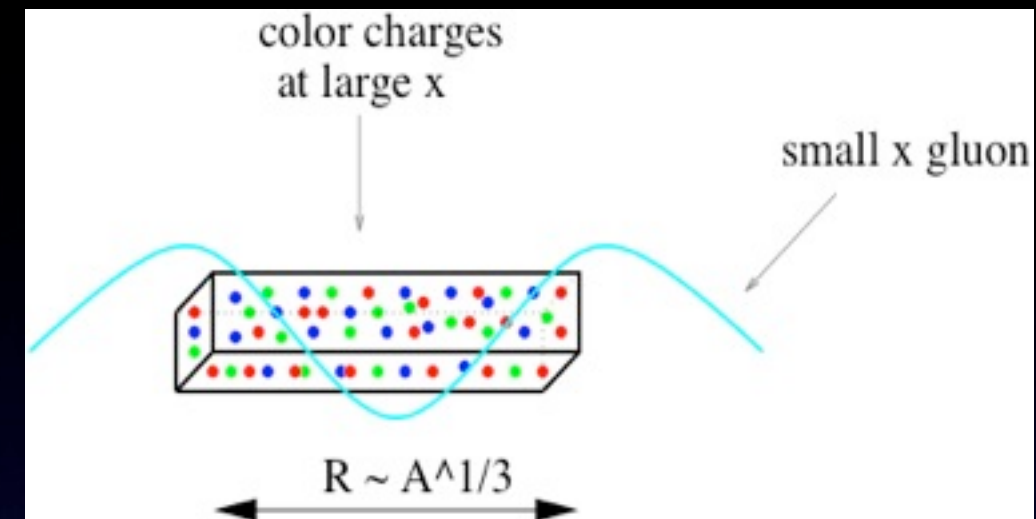
At small x this scale can become large:

$$Q_s(x) \gg \Lambda_{QCD}$$

Note: when running coupling is included, the saturation scale provides a natural regularization of the strong coupling.

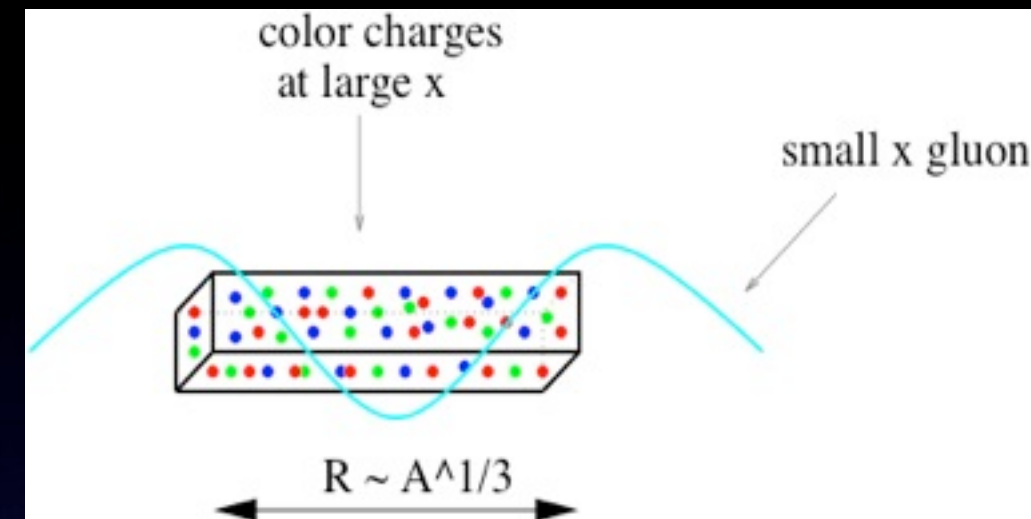
Saturation scale grows with A

- Probes interact over distances $L \sim \frac{1}{2m_N x}$
- For $L > 2R_A \sim A^{1/3}$ high-energy probes interact coherently across nuclear size.
Very large field strengths.



Saturation scale grows with A

- Probes interact over distances $L \sim \frac{1}{2m_N x}$
- For $L > 2R_A \sim A^{1/3}$ high-energy probes interact coherently across nuclear size.
Very large field strengths.

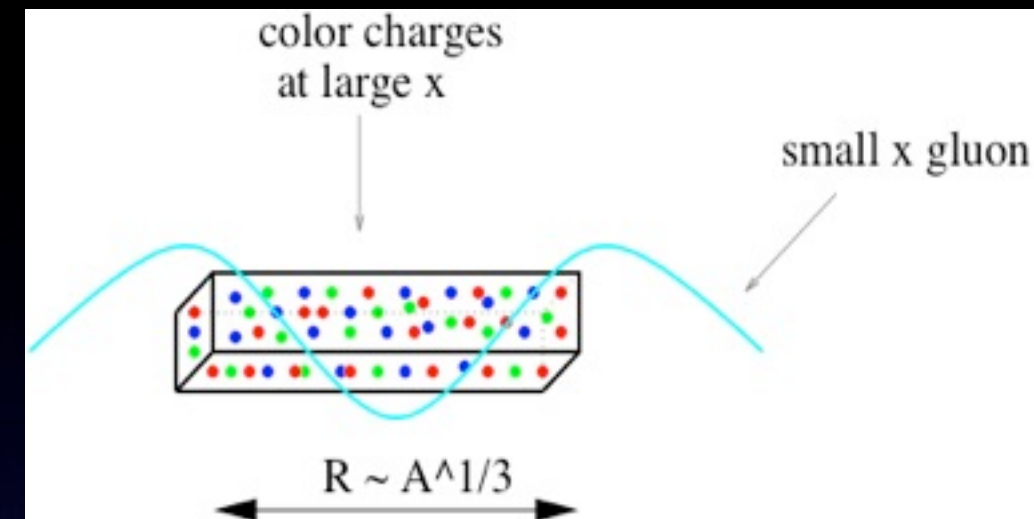


Pocket formula:

$$Q_s^2(x, A) \sim Q_0^2 \left(\frac{A}{x} \right)^{1/3}$$

Saturation scale grows with A

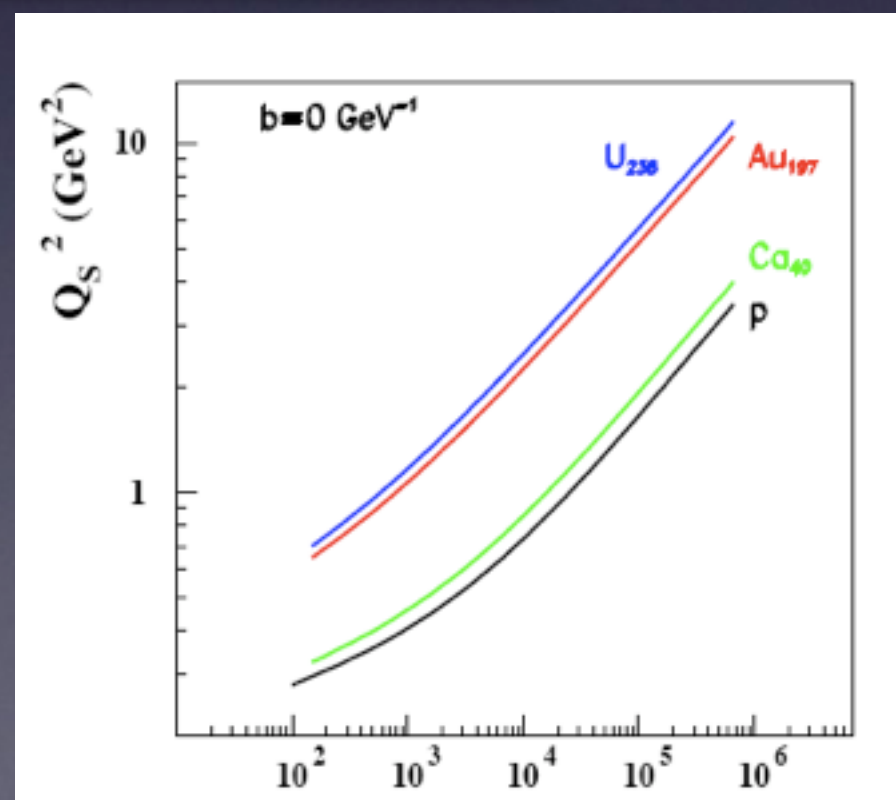
- Probes interact over distances $L \sim \frac{1}{2m_N x}$
- For $L > 2R_A \sim A^{1/3}$ high-energy probes interact coherently across nuclear size.
Very large field strengths.



Pocket formula:

$$Q_s^2(x, A) \sim Q_0^2 \left(\frac{A}{x} \right)^{1/3}$$

Scattering off nuclei: Saturation is reached for smaller energies due to the enhancement from A.

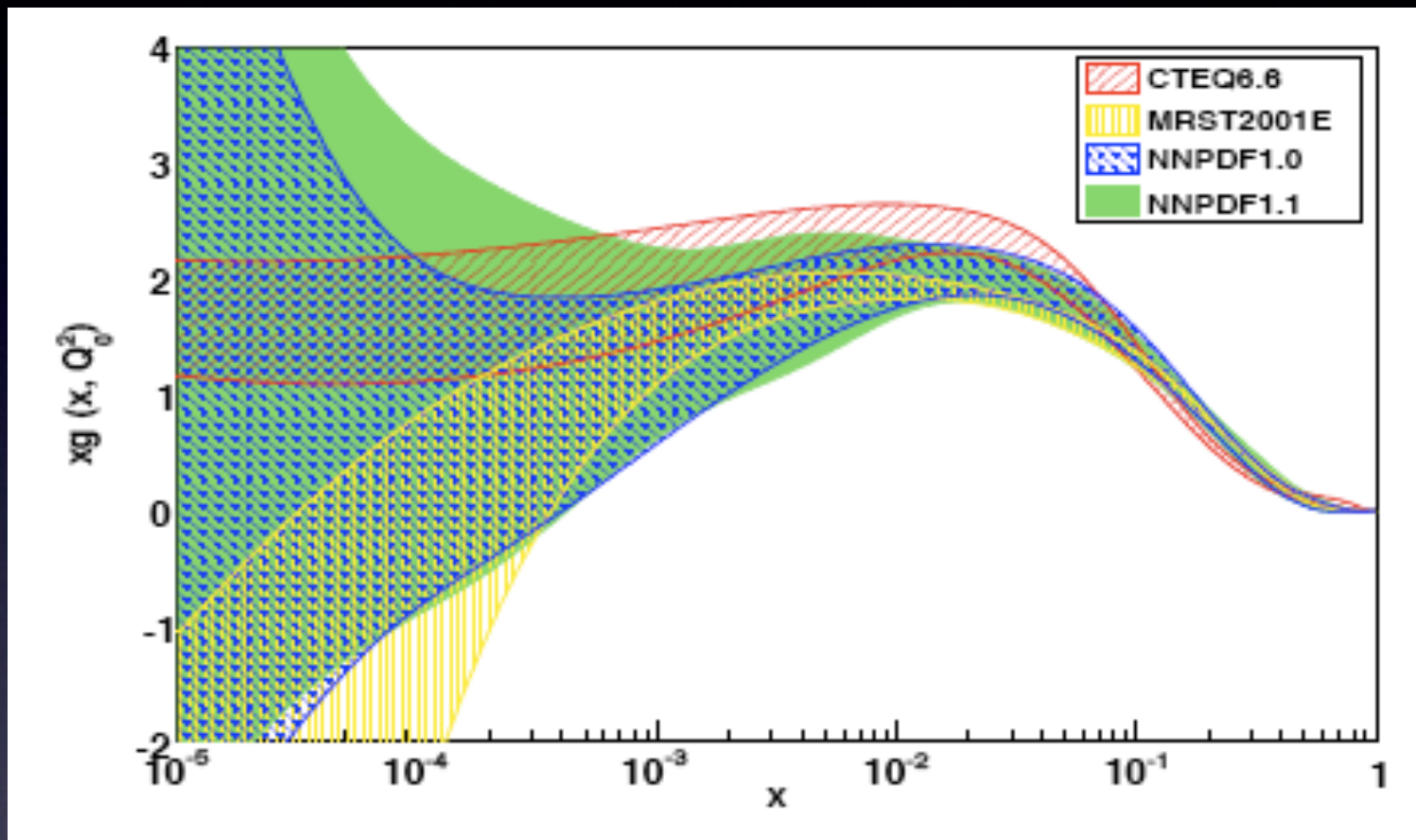


Kowalski, Teaney

Hints of saturation at HERA and RHIC

Hints of saturation at HERA

Failure of standard description at low Q and x



Gluon density at
small Q and small x .

$$Q^2 = 2 \text{ GeV}^2$$

- Strange behavior of the gluon density for small x and small Q . Gluon density largely unconstrained. Implications for longitudinal structure function.
- Signal of the breakdown of linear DGLAP evolution?
- Higher twist/saturation, or resummation (of higher orders in $\ln 1/x$) effects needed?

Geometrical scaling vs data

K.Golec-Biernat, M.Wusthoff

Saturation model: a few
parameter model with a
saturation scale and scaling
property built in:

$$N(r, x) = N(r^2 Q_s(x)^2)$$



DIS ep

$$\sigma^{\gamma^* p}(Q^2 / Q_s^2(x))$$

At small x.

Geometrical scaling vs data

K.Golec-Biernat, J.Kwiecinski, A.Stasto

K.Golec-Biernat, M.Wusthoff

Saturation model: a few
parameter model with a
saturation scale and scaling
property built in:

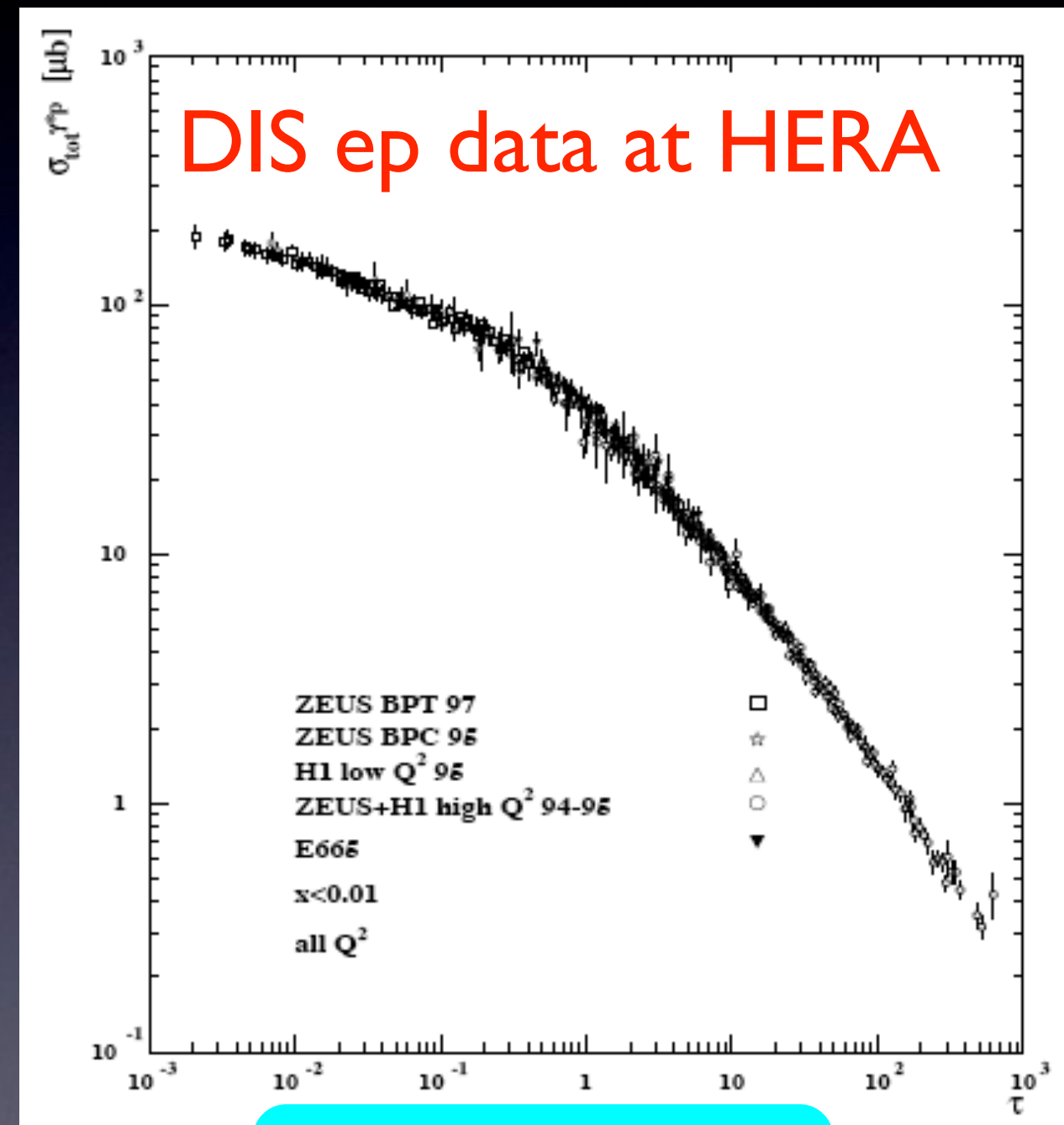
$$N(r, x) = N(r^2 Q_s(x)^2)$$



DIS ep

$$\sigma^{\gamma^* p}(Q^2 / Q_s^2(x))$$

At small x .



$$\tau = Q^2 / Q_s^2(x)$$

Geometrical scaling vs data

K.Golec-Biernat, J.Kwiecinski, A.Stasto

K.Golec-Biernat, M.Wusthoff

Saturation model: a few
parameter model with a
saturation scale and scaling
property built in:

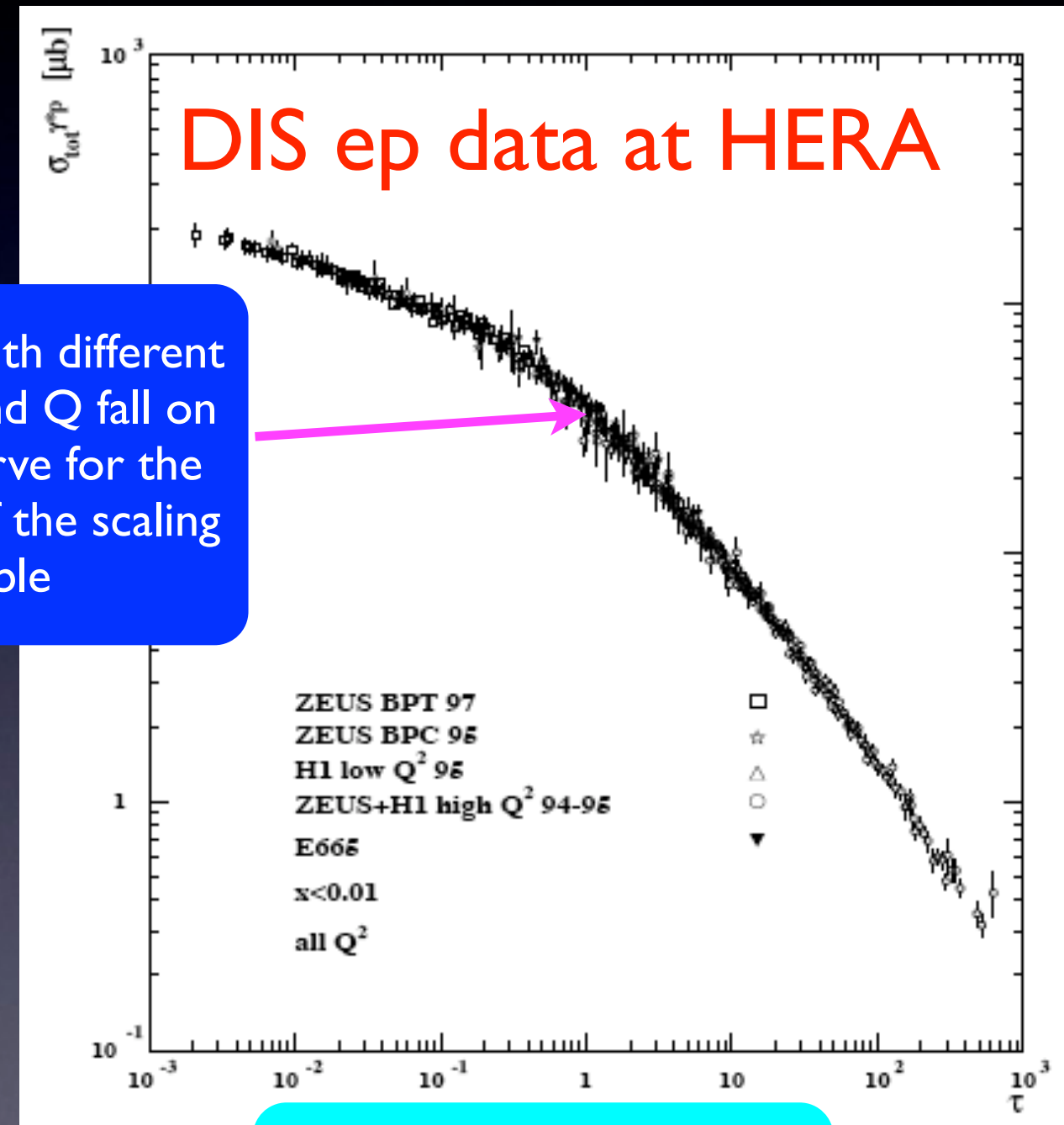
$$N(r, x) = N(r^2 Q_s(x), x)$$

DIS ep

$$\sigma^{\gamma^* p}(Q^2 / Q_s^2(x))$$

At small x.

Datapoints with different
values of x and Q fall on
the same curve for the
same value of the scaling
variable



$$\tau = Q^2 / Q_s^2(x)$$

Geometrical scaling vs data

K.Golec-Biernat, J.Kwiecinski, A.Stasto

K.Golec-Biernat, M.Wusthoff

Saturation model: a few
parameter model with a
saturation scale and scaling
property built in:

$$N(r, x) = N(r^2 Q_s(x), x)$$

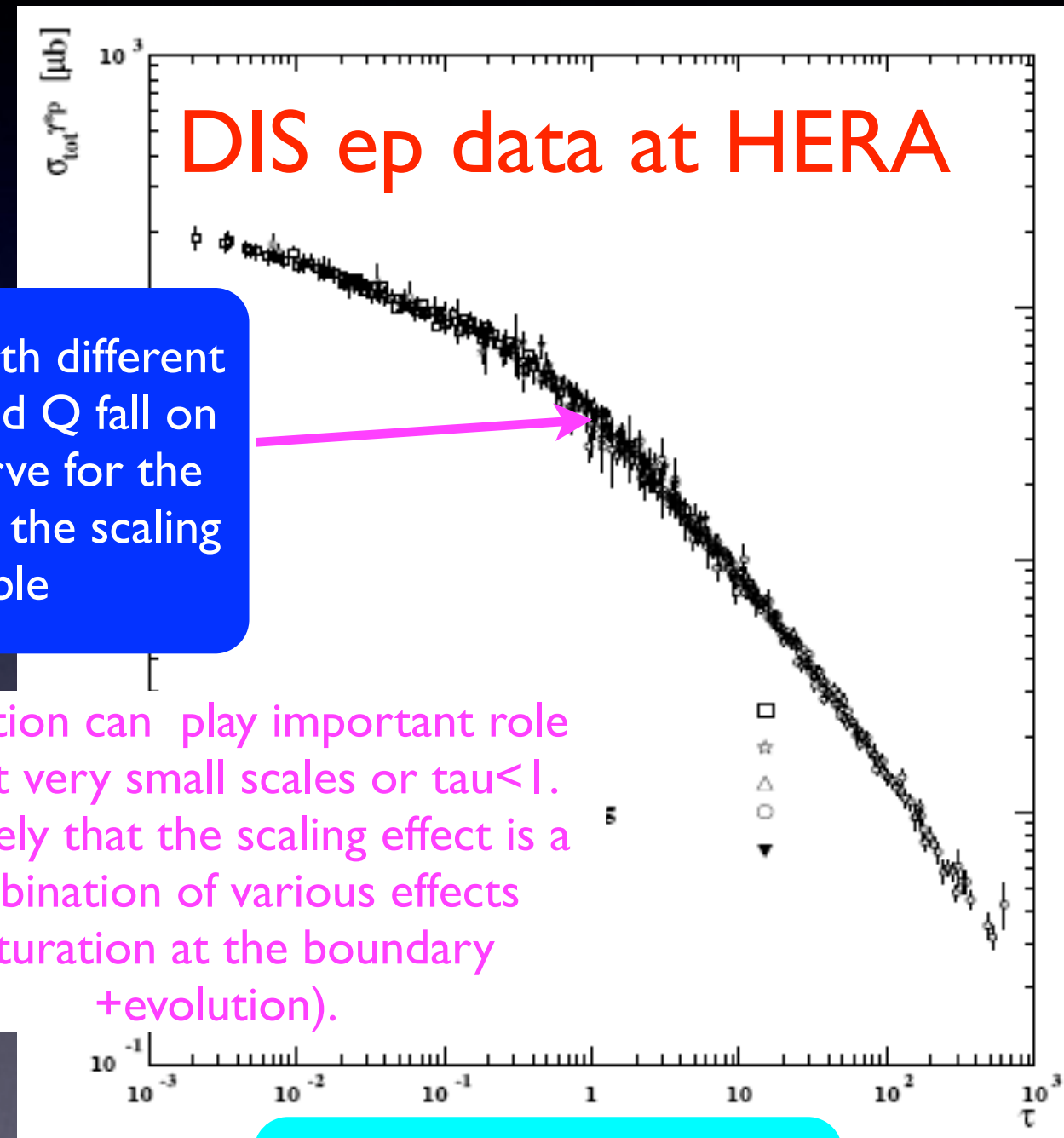
DIS ep

$$\sigma^{\gamma^* p}(Q^2 / Q_s^2(x))$$

At small x.

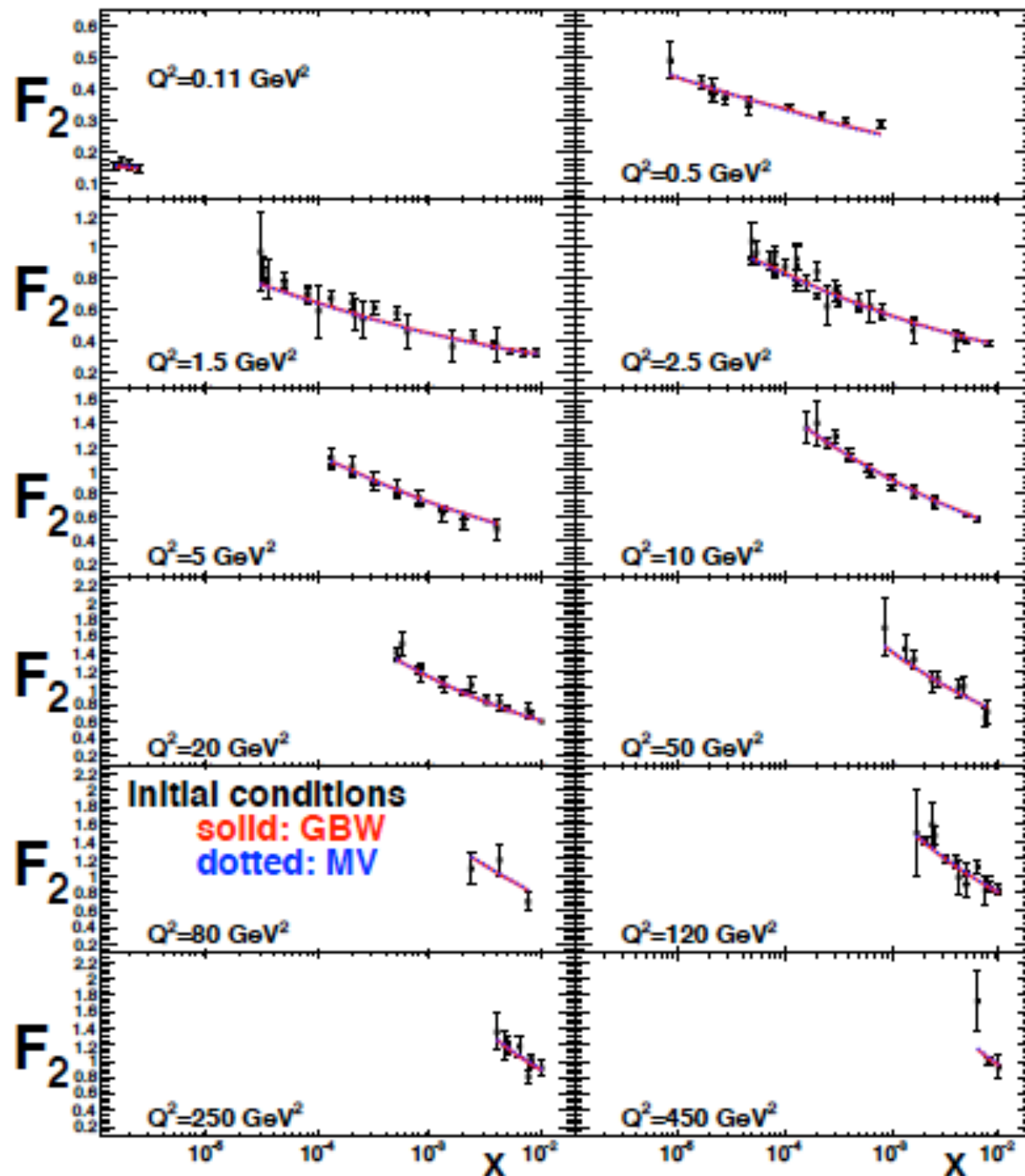
Datapoints with different
values of x and Q fall on
the same curve for the
same value of the scaling
variable

Saturation can play important role
only at very small scales or $\tau < 1$.
It is likely that the scaling effect is a
combination of various effects
(saturation at the boundary
+ evolution).



$$\tau = Q^2 / Q_s^2(x)$$

Description of structure function F_2 down to low photon virtualities



- Dipole models which are supplemented by the saturation describe the experimental data very well.
- Down to very low scales.
- Transition from large to low Q is correctly reproduced by the models which include saturation.

Diffractive to inclusive ratio in ep

Naively:

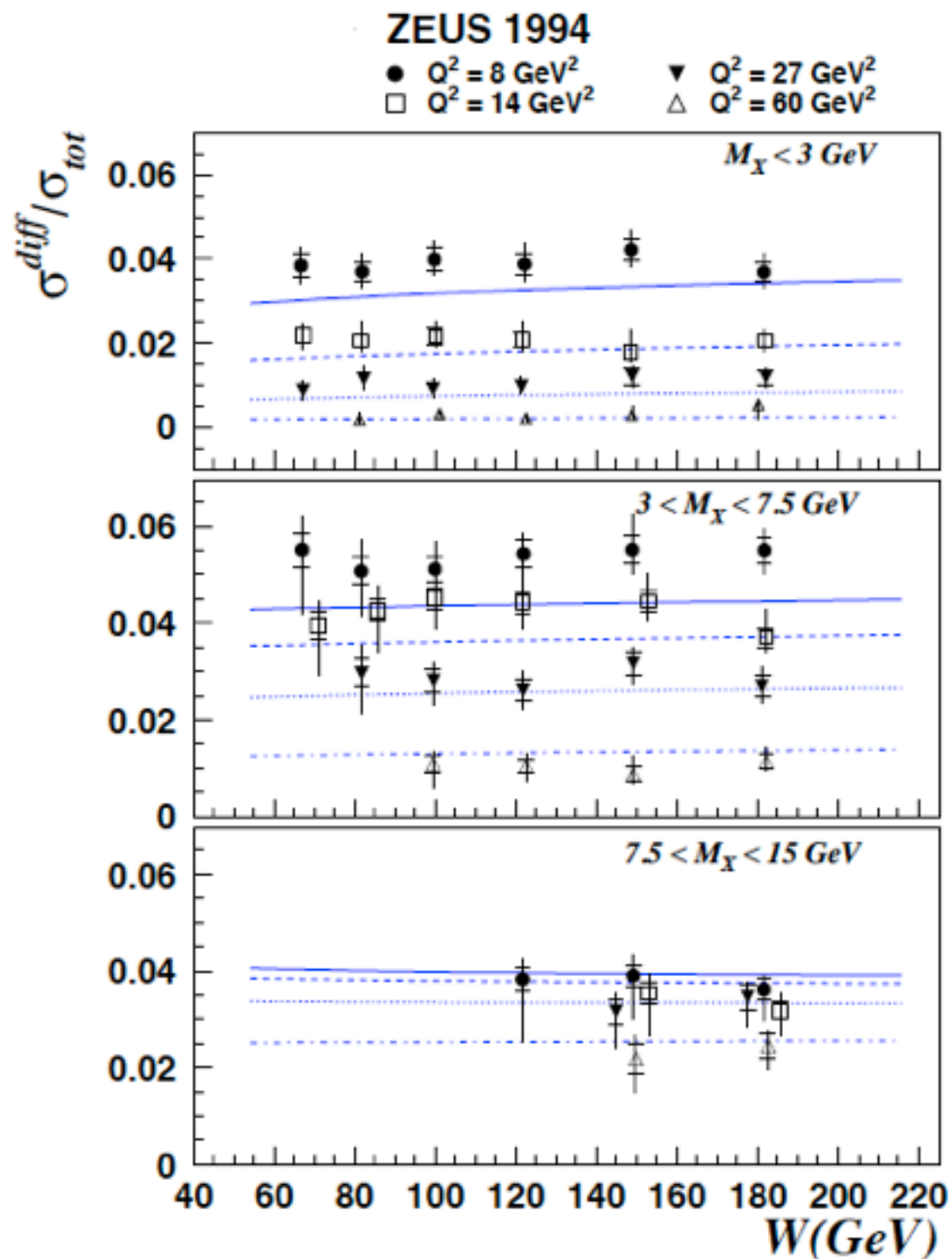
$$\sigma^{incl} \sim xg(x, Q^2)$$

$$\sigma^{diff} \sim xg(x, Q^2)^2$$

Therefore ratio should have non-trivial energy dependence.

Constant ratio naturally explained in the saturation model.

Is it the same ratio and still constant at higher energy?



Hints from RHIC

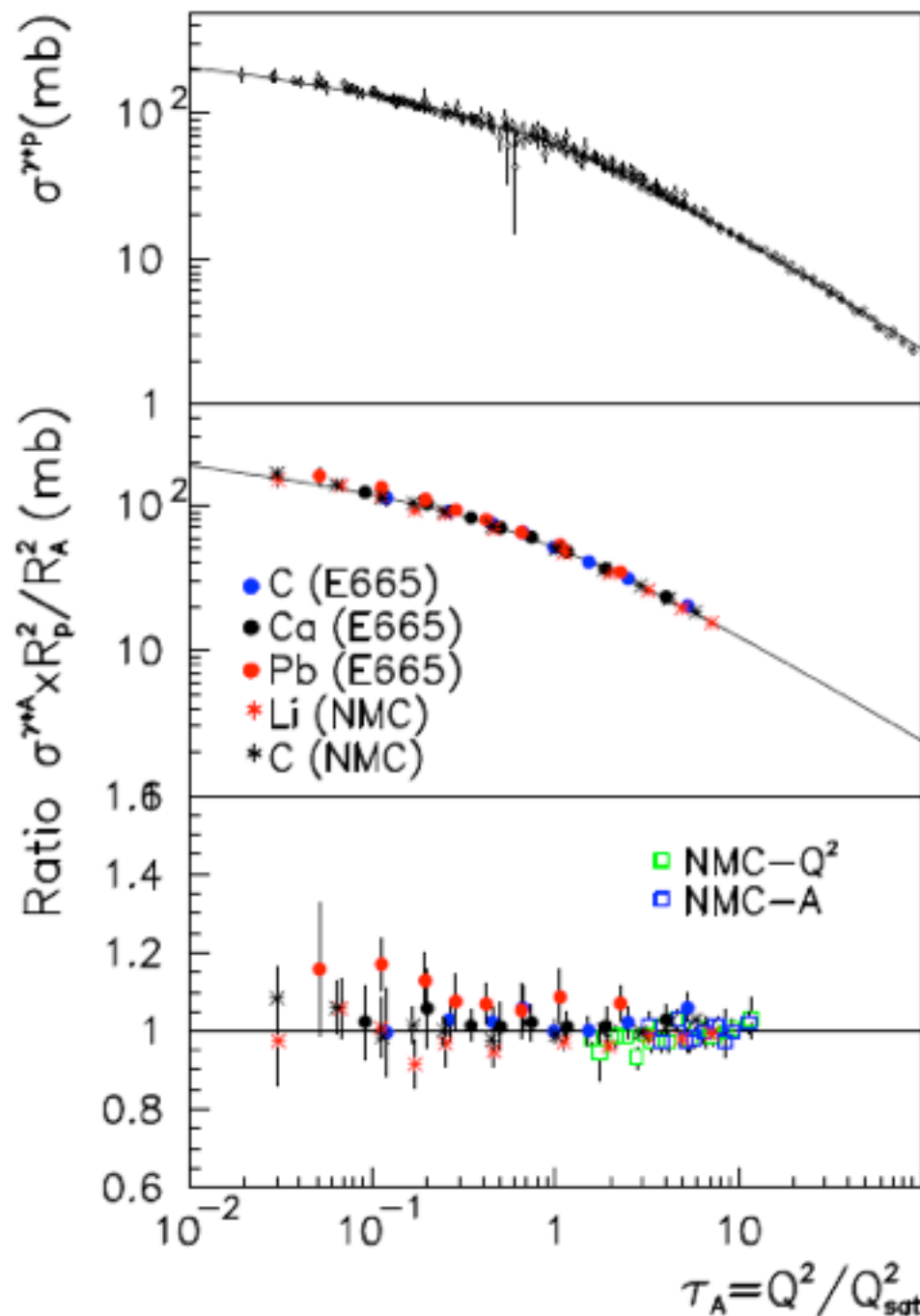
Multiplicities in AA:

Saturation scale in nuclei

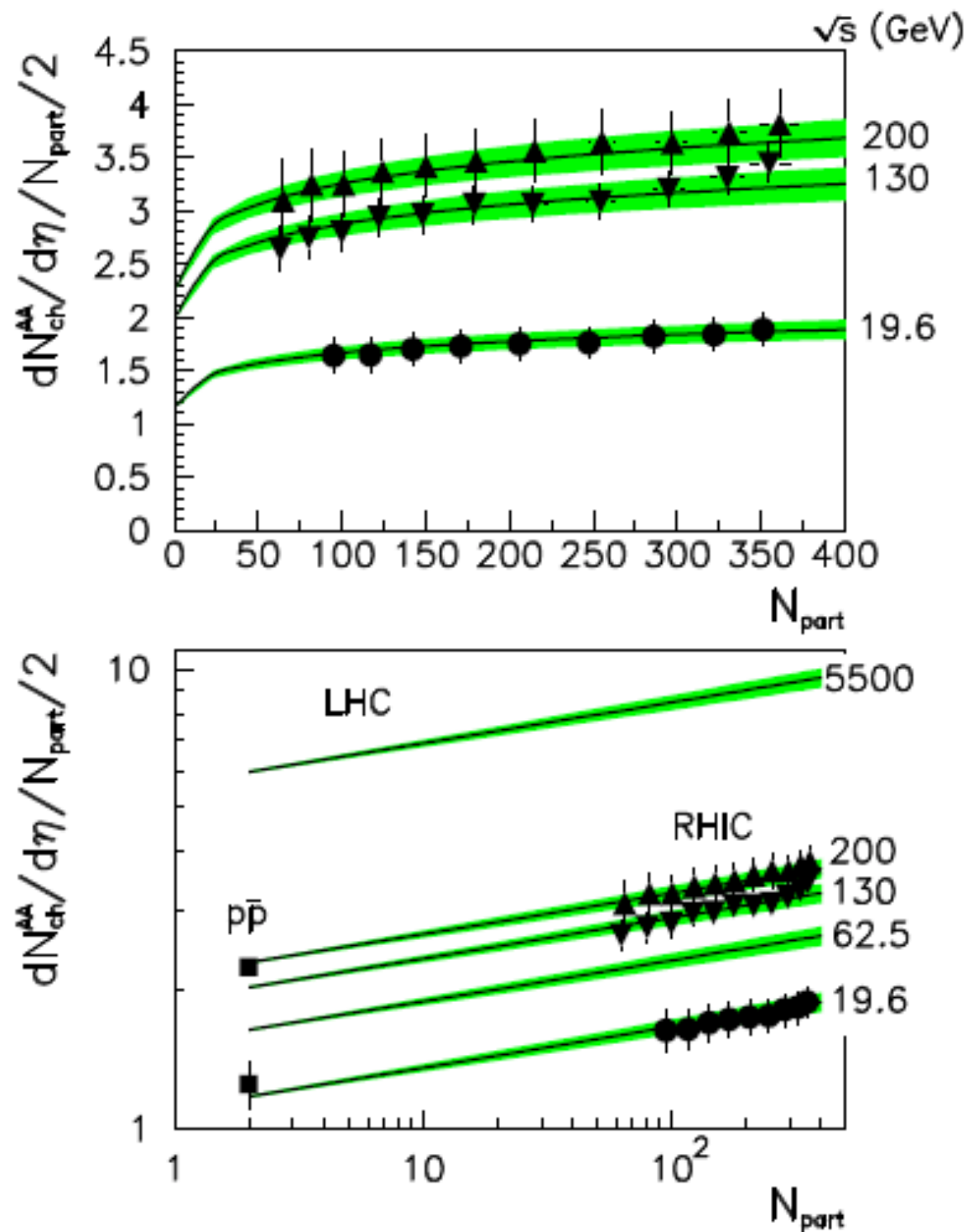
$$Q_{s,A}^2(x) = Q_{s,p}^2(x) \left(A \frac{R_p^2}{R_A^2} \right)^\delta$$

Extension of geometric scaling and saturation picture to nuclei.

Very good description of different kinds of nuclei (though limited statistics).



Multiplicities in AA



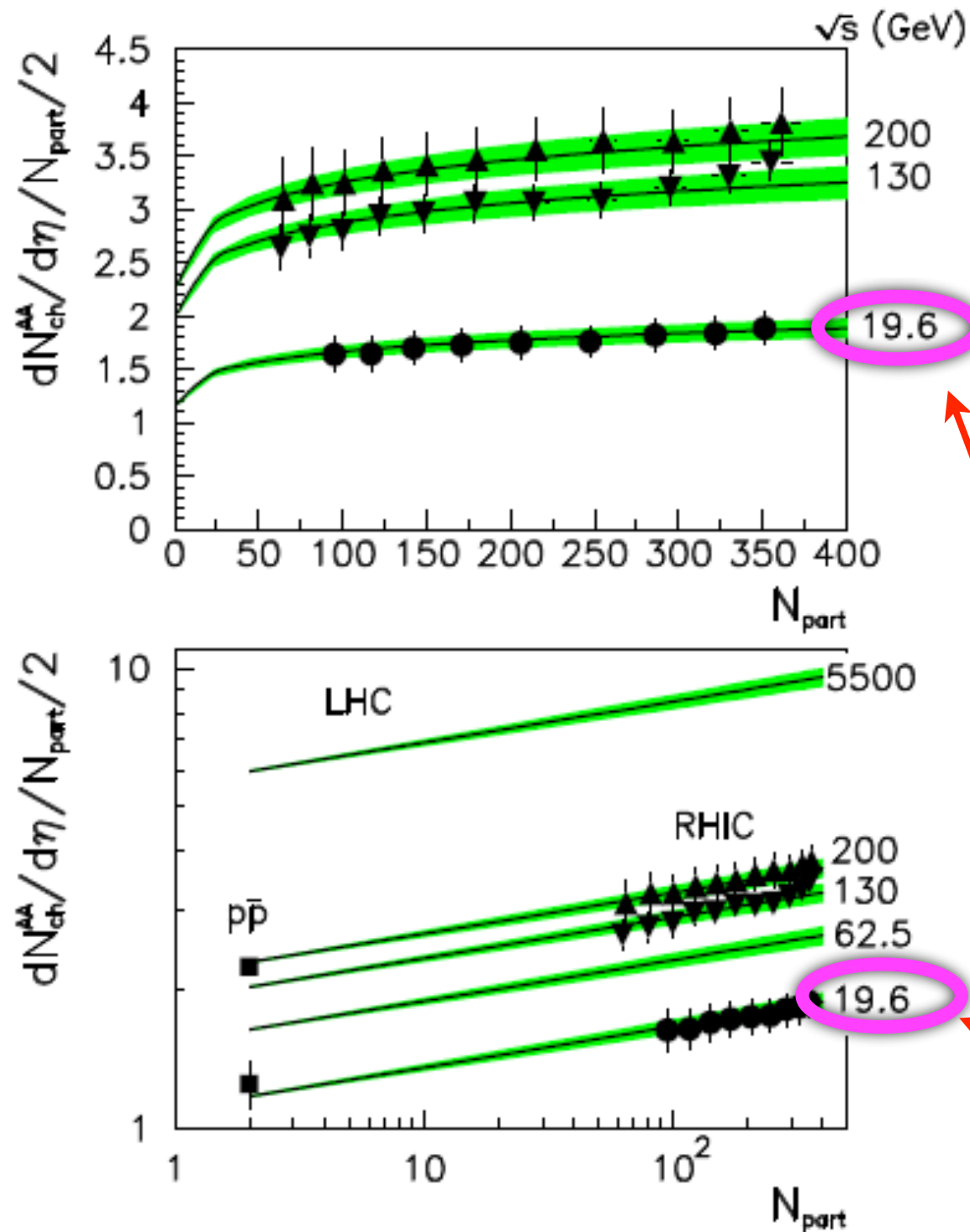
$$\frac{dN^{AA}}{d\eta}(N_{part}, \sqrt{s})$$

Using CGC type of picture, kt factorization, supplemented by the centrality dependence.

Very good description for range of energies and centralities.

Questions remain: why the description is so good at low energies?

Multiplicities in AA



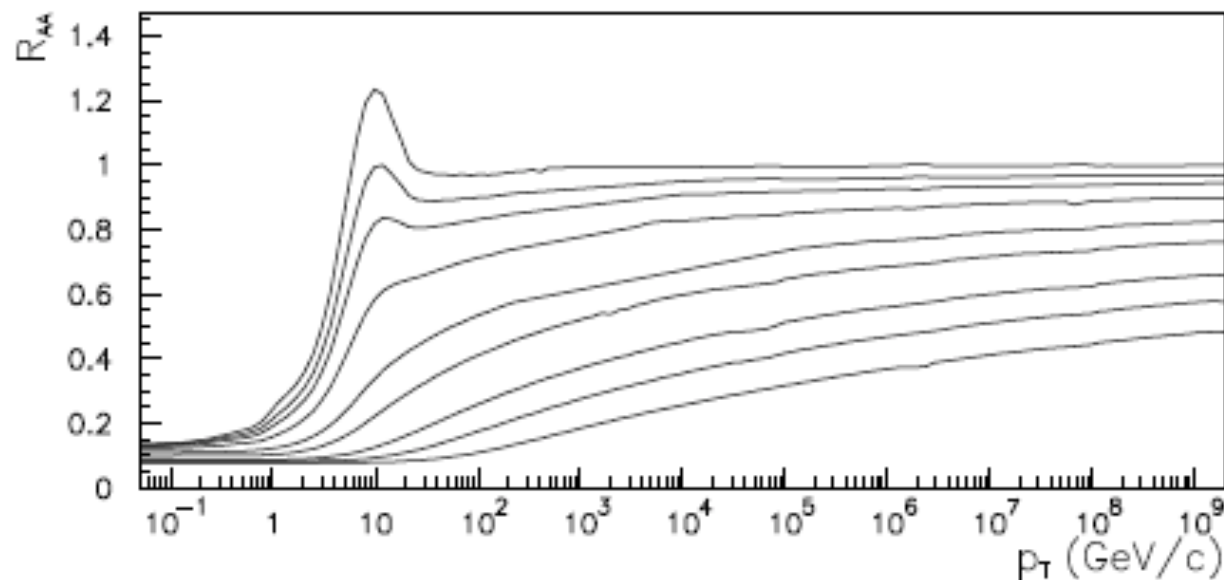
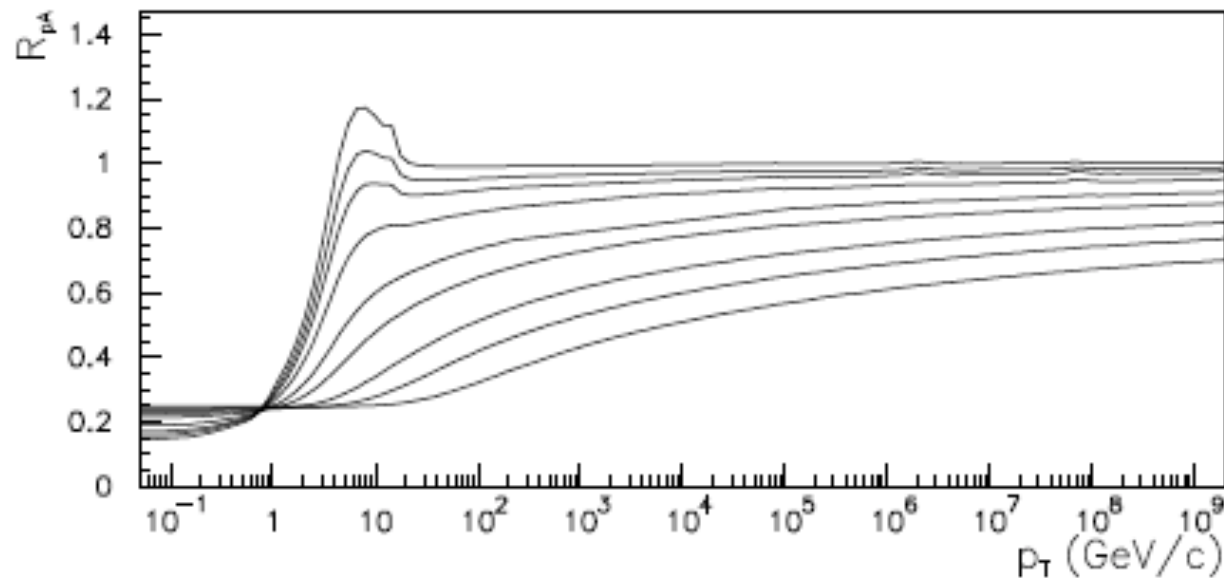
$$\frac{dN^{AA}}{d\eta}(N_{part}, \sqrt{s})$$

Using CGC type of picture, kt factorization, supplemented by the centrality dependence.

Very good description for range of energies and centralities.

Questions remain: why the description is so good at low energies?

Disappearance of Cronin enhancement



Ratios of pA and AA for particle yields as a function of transverse momenta normalized to pp spectra.

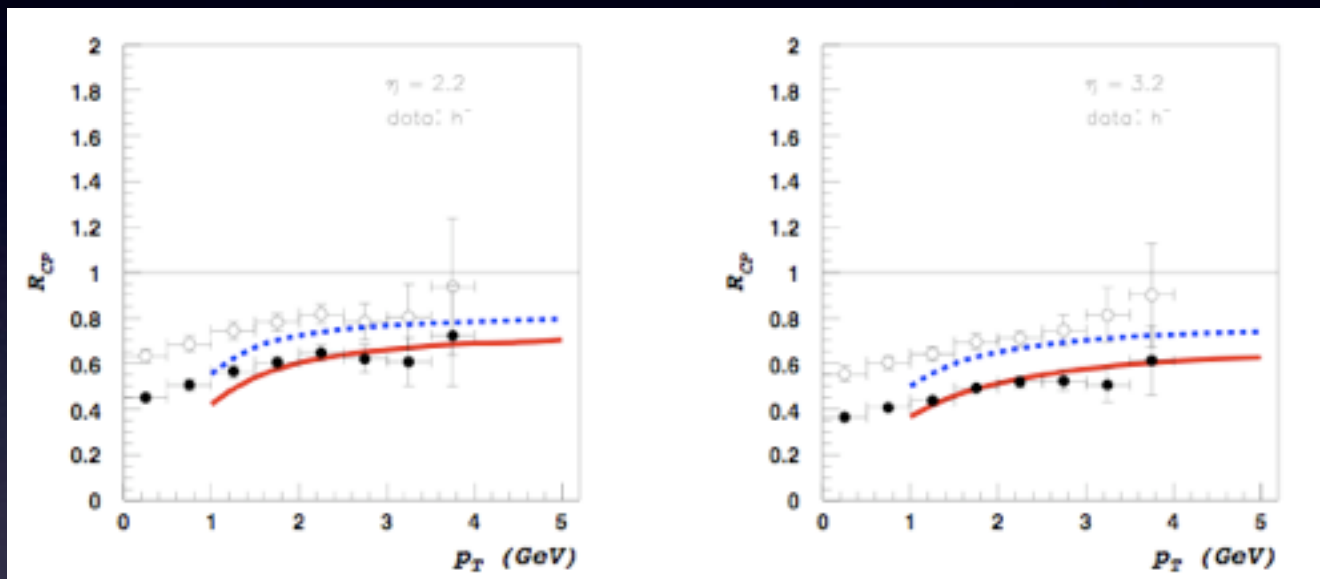
Small x evolution completely washes out the Cronin enhancement at forward rapidities.

Javier L. Albacete, Nestor Armesto,
Alex Kovner, Carlos A. Salgado, Urs
Achim Wiedemann

Saturation: phenomenology at RHIC

$$\eta = 2.2$$

$$\eta = 3.2$$

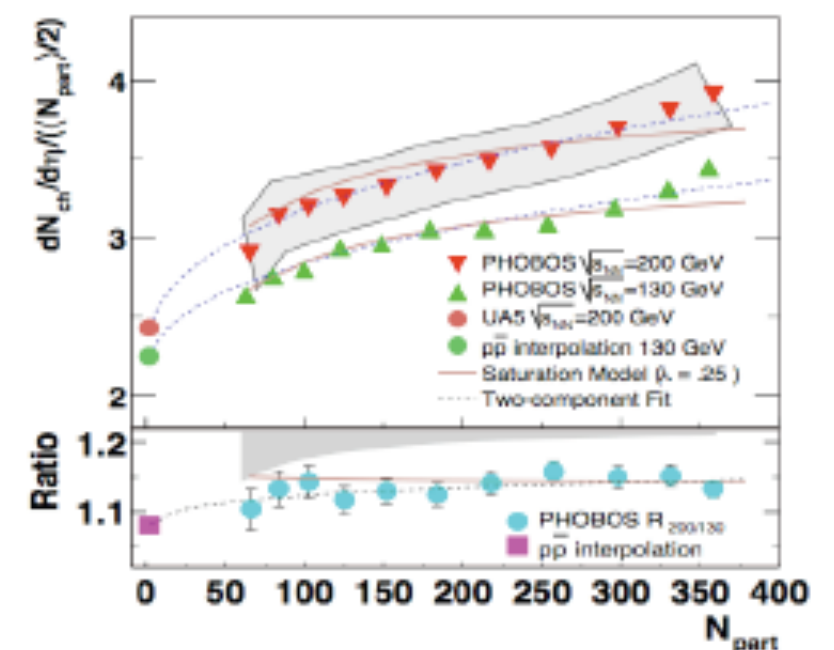
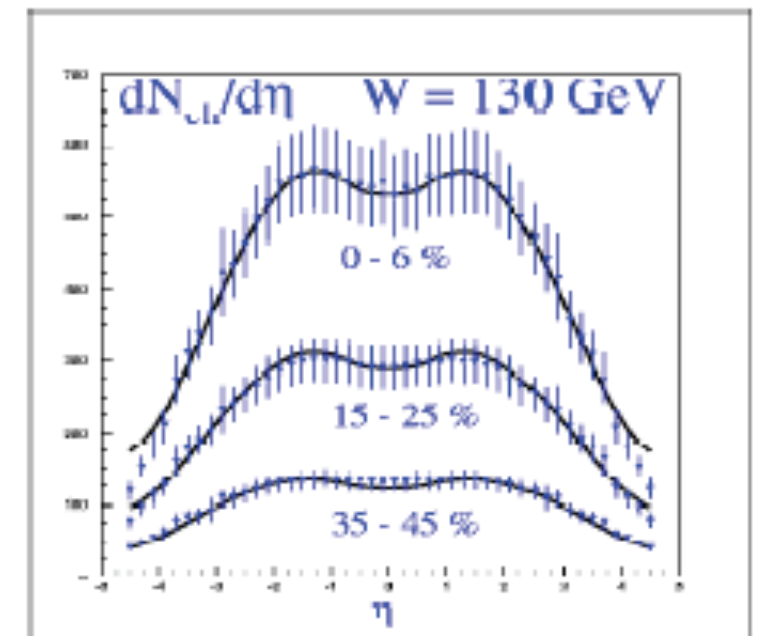


Kharzeev, Kovchegov, Tuchin

dAu : suppression of the transverse momentum distribution at forward rapidities

Very good agreement with the data!

Rapidity distributions

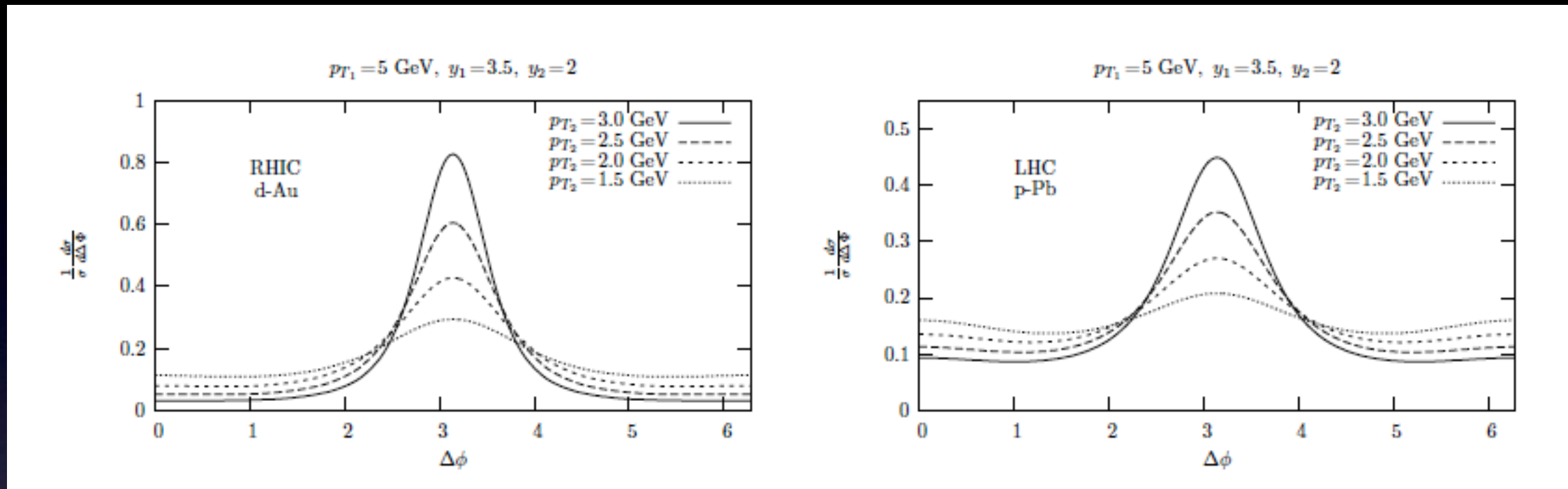


Kharzeev, Levin, Nardi

Two particle correlations in pA/dA

Predictions from CGC

$$pA \rightarrow h_1 h_2 X$$



Cyrille Marquet

Decreasing p_t at fixed rapidity reduces the correlation in azimuthal angle. At LHC smaller values of x can be reached and so the decorrelation is bigger.

Consistent with the signals from RHIC

Is it really a signal of saturation? Dependence on centrality is crucial. x dependence should come out also from the linear type evolution: enhanced phase space, more emissions, more decorrelation.

Why ep/eA collider?

- Electron as a clean probe of the proton/nucleus.
- Initial state measurement: direct extraction of the parton densities.
- If the energy of electron is changed, longitudinal structure function can be measured: direct constraint on the gluon density.
- Polarized structure functions.

Why ep/eA collider?

- Electron as a clean probe of the proton/nucleus.
- Initial state measurement: direct extraction of the parton densities.
- If the energy of electron is changed, longitudinal structure function can be measured: direct constraint on the gluon density.
- Polarized structure functions.

EIC and LHeC are complementary proposals

Why ep/eA collider?

- Electron as a clean probe of the proton/nucleus.
- Initial state measurement: direct extraction of the parton densities.
- If the energy of electron is changed, longitudinal structure function can be measured: direct constraint on the gluon density.
- Polarized structure functions.

EIC and LHeC are complementary proposals

**EIC: Focus on nuclei. Measurement of the nuclear pdfs.
Polarized option.**

Why ep/eA collider?

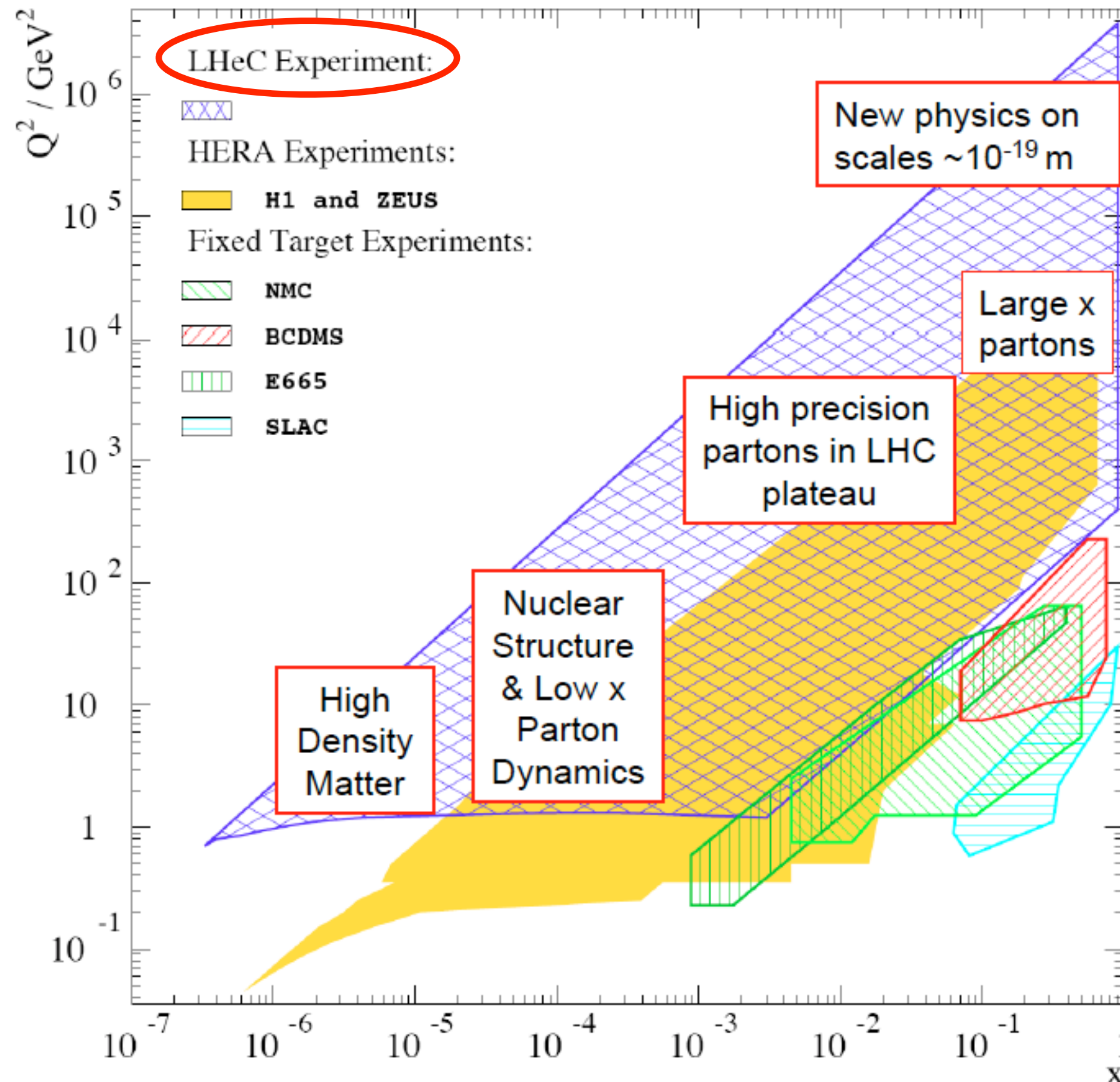
- Electron as a clean probe of the proton/nucleus.
- Initial state measurement: direct extraction of the parton densities.
- If the energy of electron is changed, longitudinal structure function can be measured: direct constraint on the gluon density.
- Polarized structure functions.

EIC and LHeC are complementary proposals

**EIC: Focus on nuclei. Measurement of the nuclear pdfs.
Polarized option.**

**LHeC: High energy. Extended kinematics. Nuclear
option also possible.**

Kinematics & Motivation (140 GeV x 7 TeV)



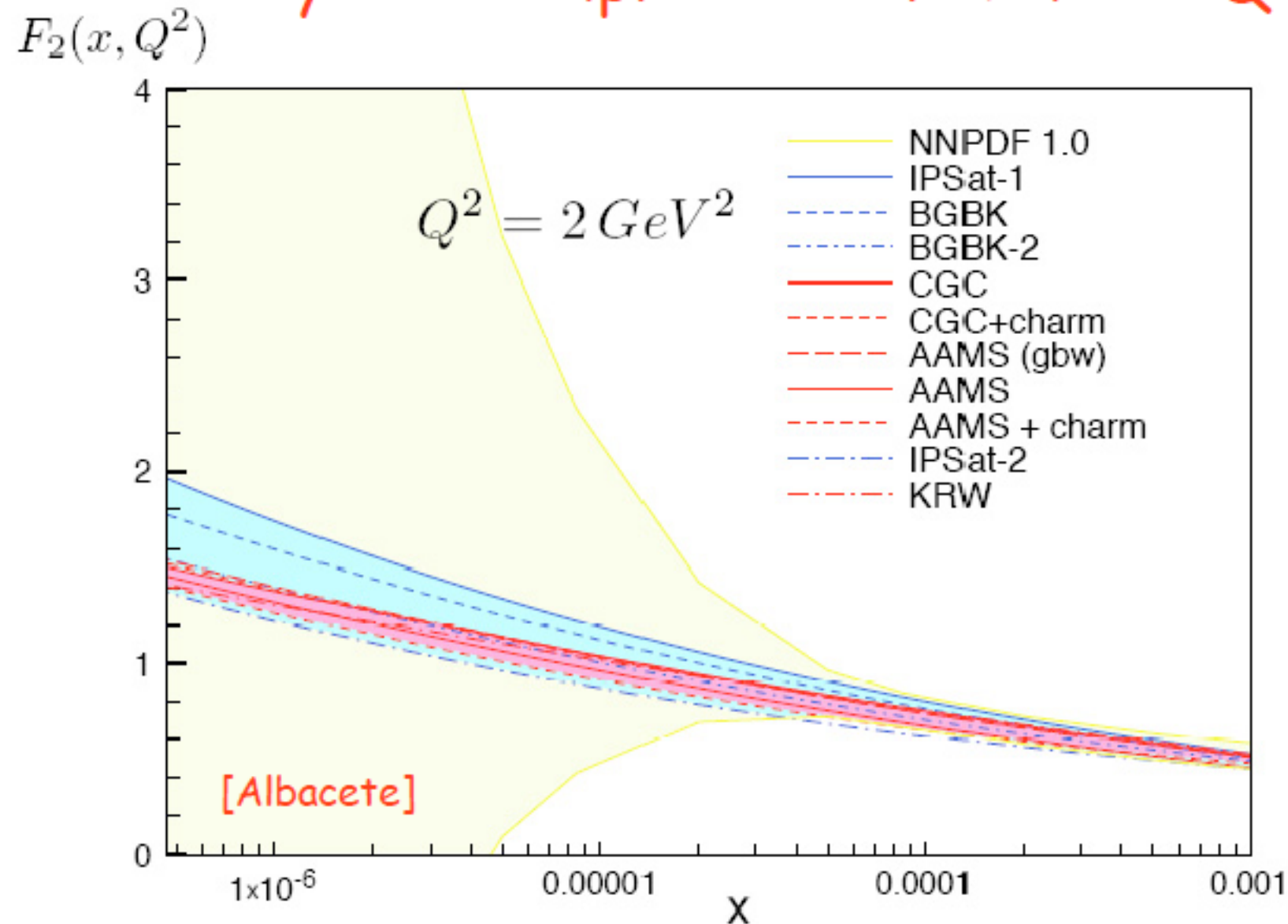
$$\sqrt{s} = 2 \text{ TeV}$$

- High mass (M_{eq} , Q^2) frontier
- EW & Higgs
- Q^2 lever-arm at moderate & high $x \rightarrow$ PDFs
- Low x and eA Frontier $\rightarrow$ novel QCD ...

$$x \geq 5 \cdot 10^{-7} \text{ at } Q^2 \leq 1 \text{ GeV}^2$$

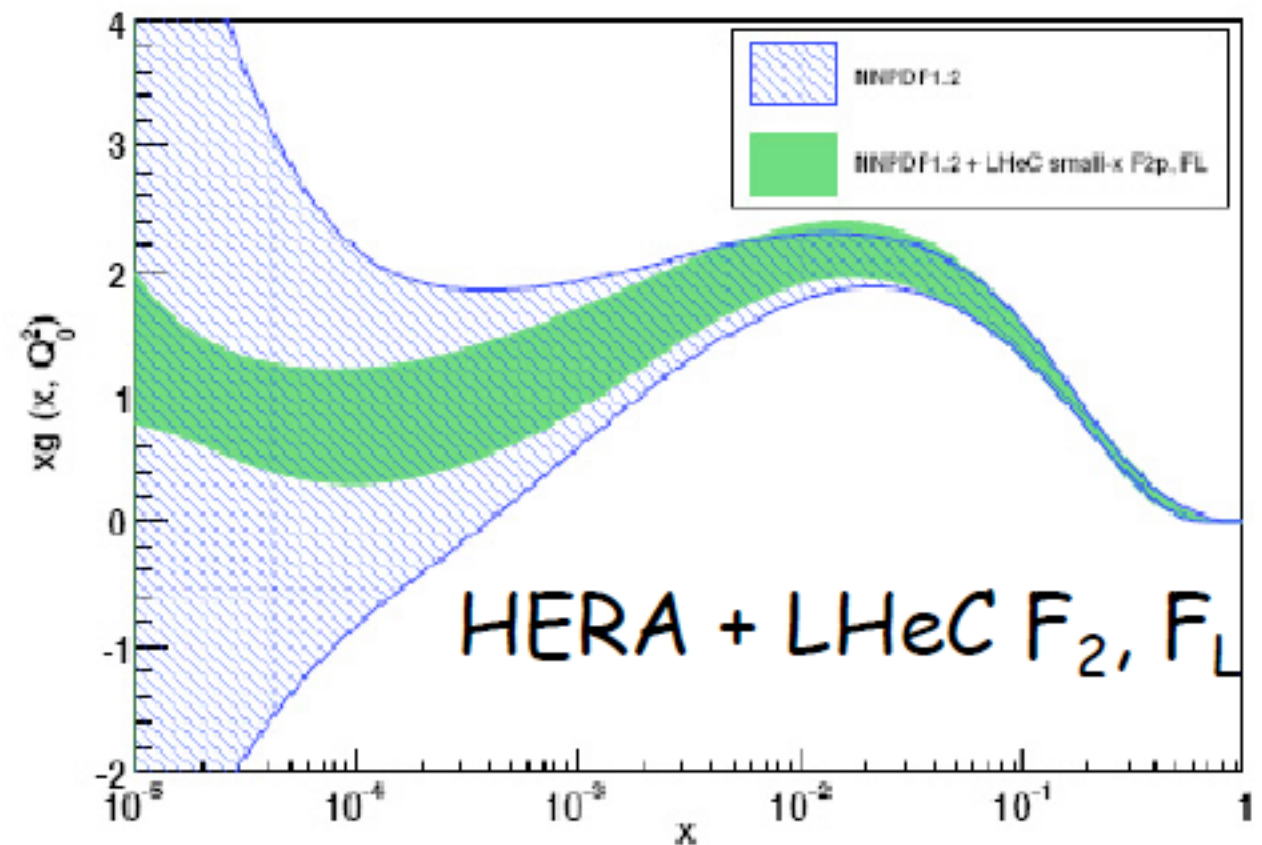
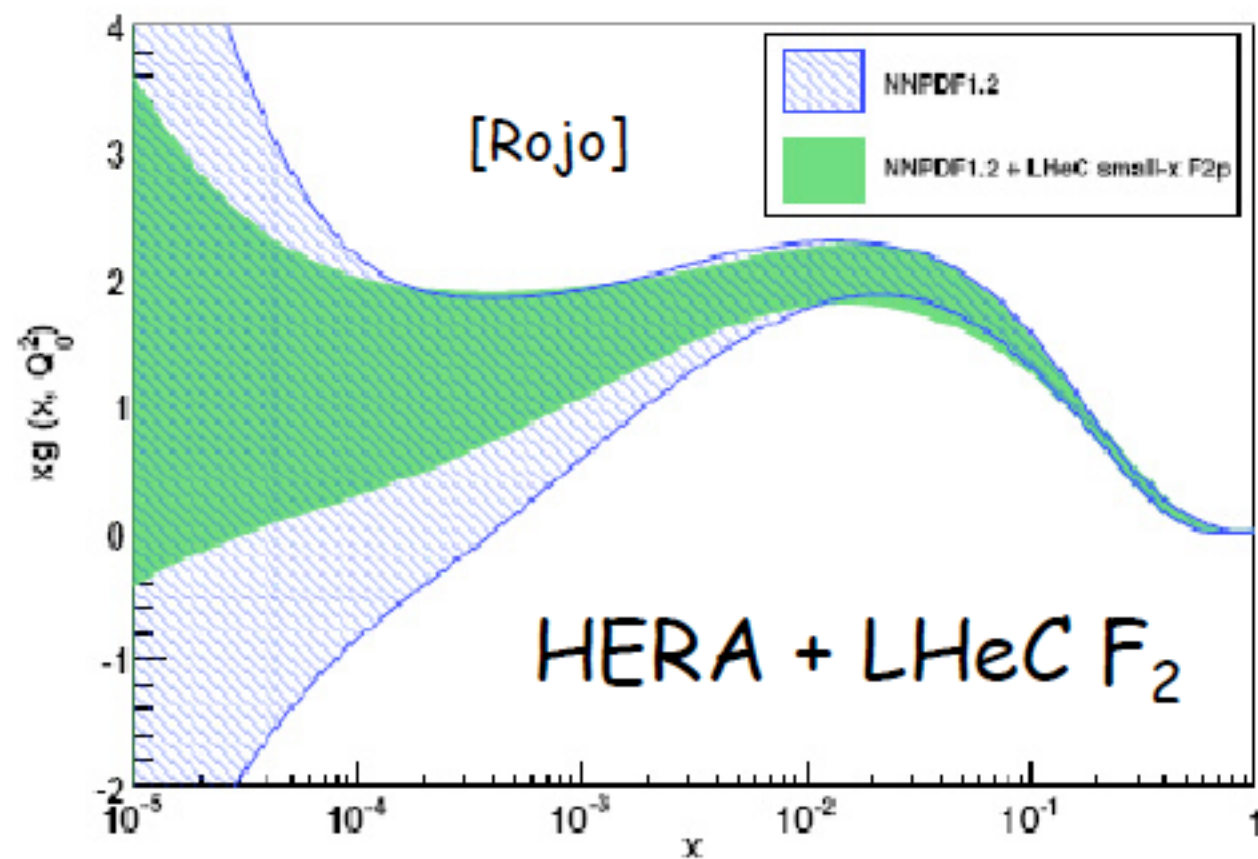
Another look at Extrapolations of F_2

NNPDF parameter-free NLO DGLAP QCD fit ...
uncertainty band explodes at low x and Q^2



Very wide range of possibilities allowed by pQCD ...
... whilst retaining a good fit to to HERA data

Constraining the Gluon with LHeC F_2 and F_L



($Q^2 = 2 \text{ GeV}^2$)

Including LHeC data in NNPDF DGLAP fit approach ...

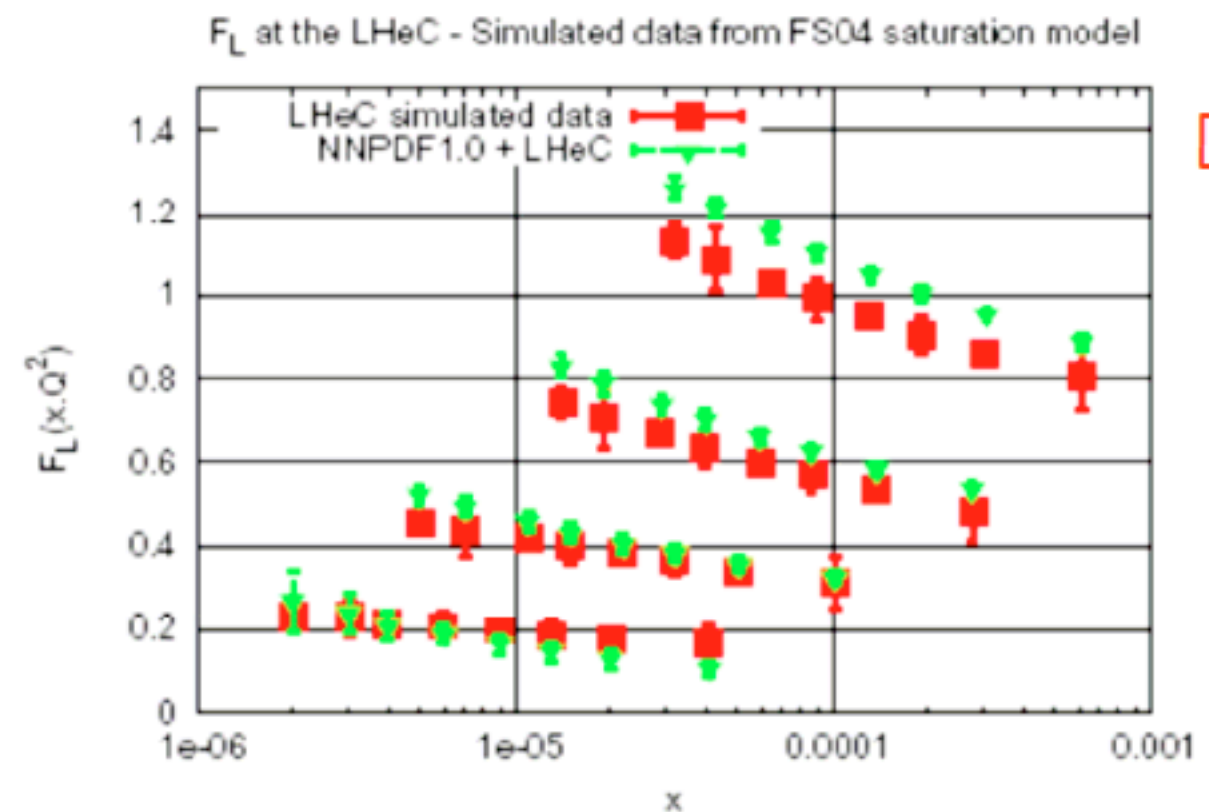
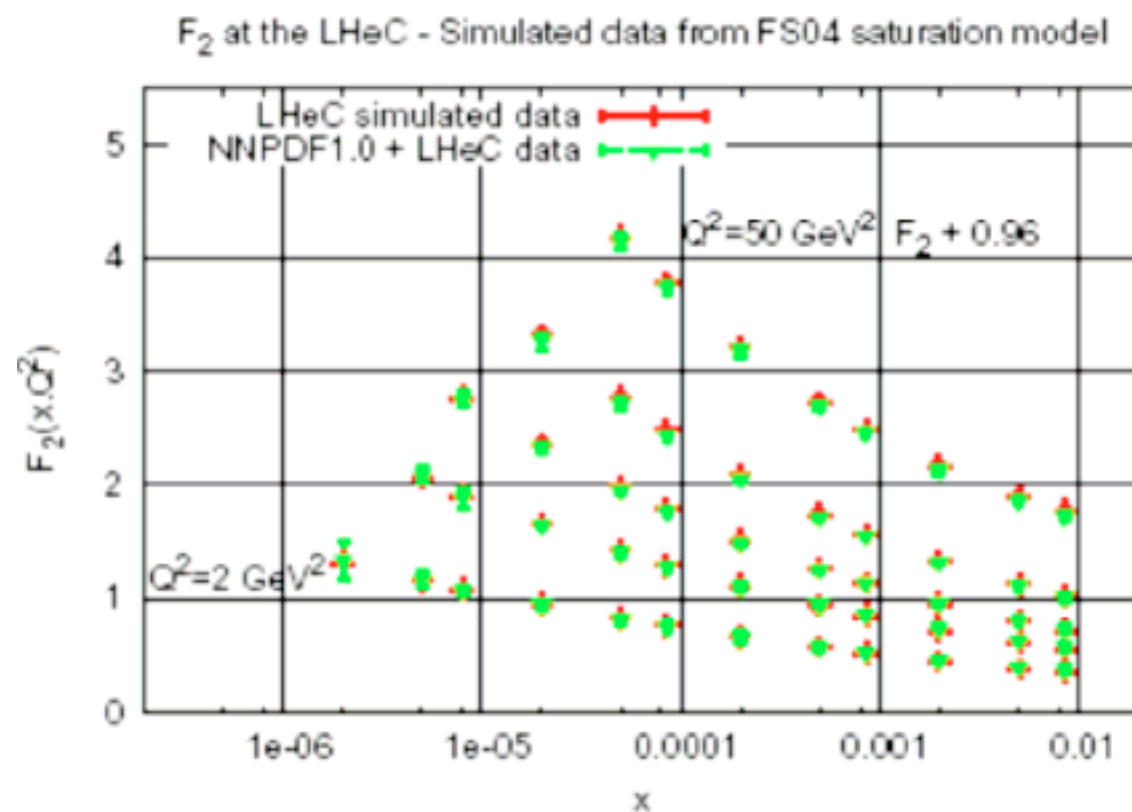
... sizeable improvement in error on low x gluon when both LHeC F_2 & F_L data are included.

... but would DGLAP fits fail if non-linear effects present?

Can Parton Saturation be Established @ LHeC?

Simulated LHeC F_2 and F_L data based on a dipole model containing low x saturation (FS04-sat)...

... NNPDF (also HERA framework) DGLAP QCD fits cannot accommodate saturation effects if F_2 and F_L both fitted



[Rojo]

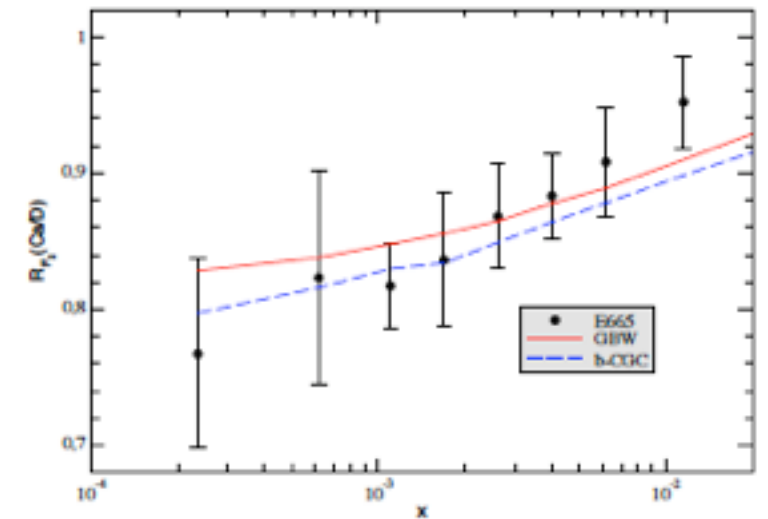
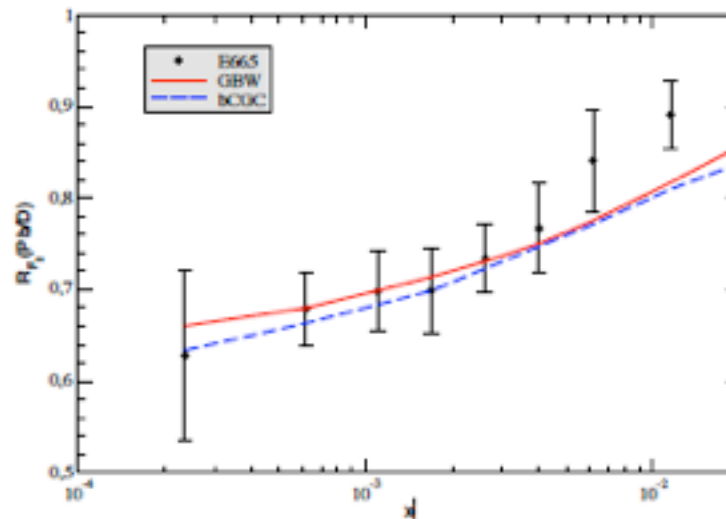
... even with LHeC low x region, multiple ep (& eA) observables will be required for a clear picture of non-linear dynamics.

Inclusive ratios: ep/eA

Ratio $R_{F_2} \equiv 2F_2^A / AF_2^D$ for $A = Pb$ and $A = Ca$

Data from E665 collaboration

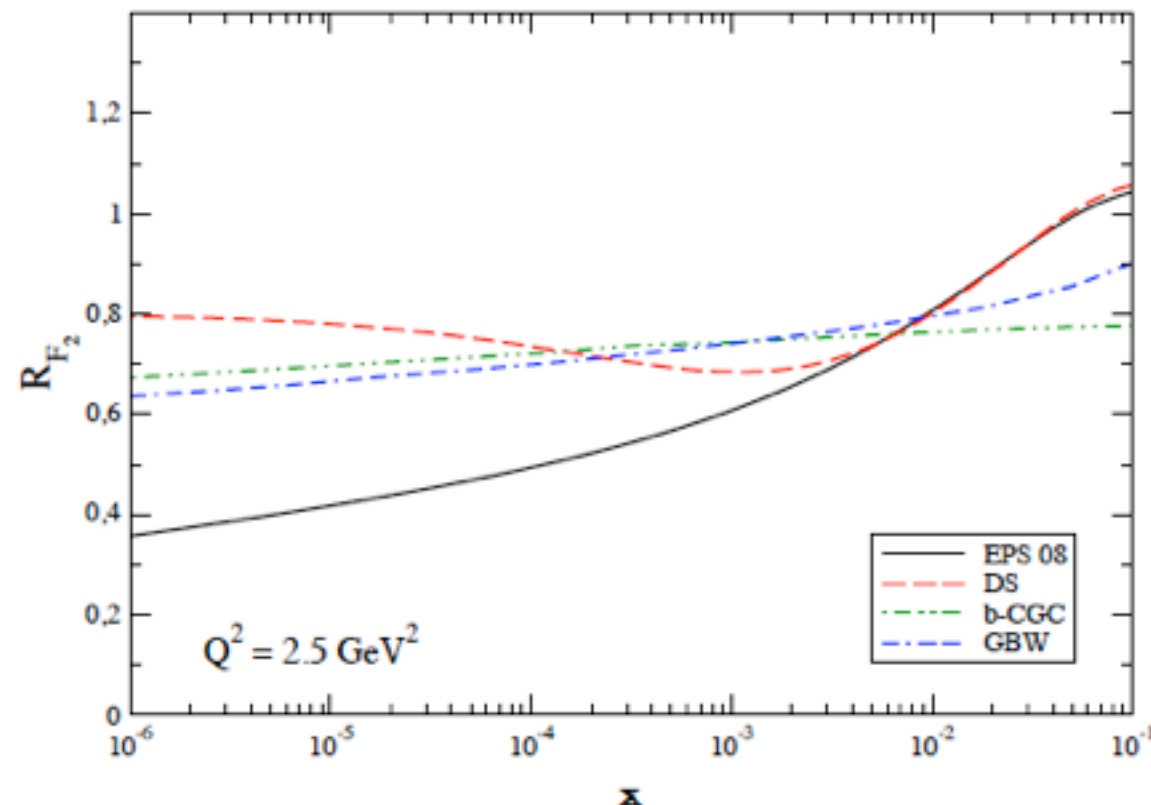
What we know now



Cazaroto, Carvalho, Goncalves, Navarra

Extrapolation to lower x

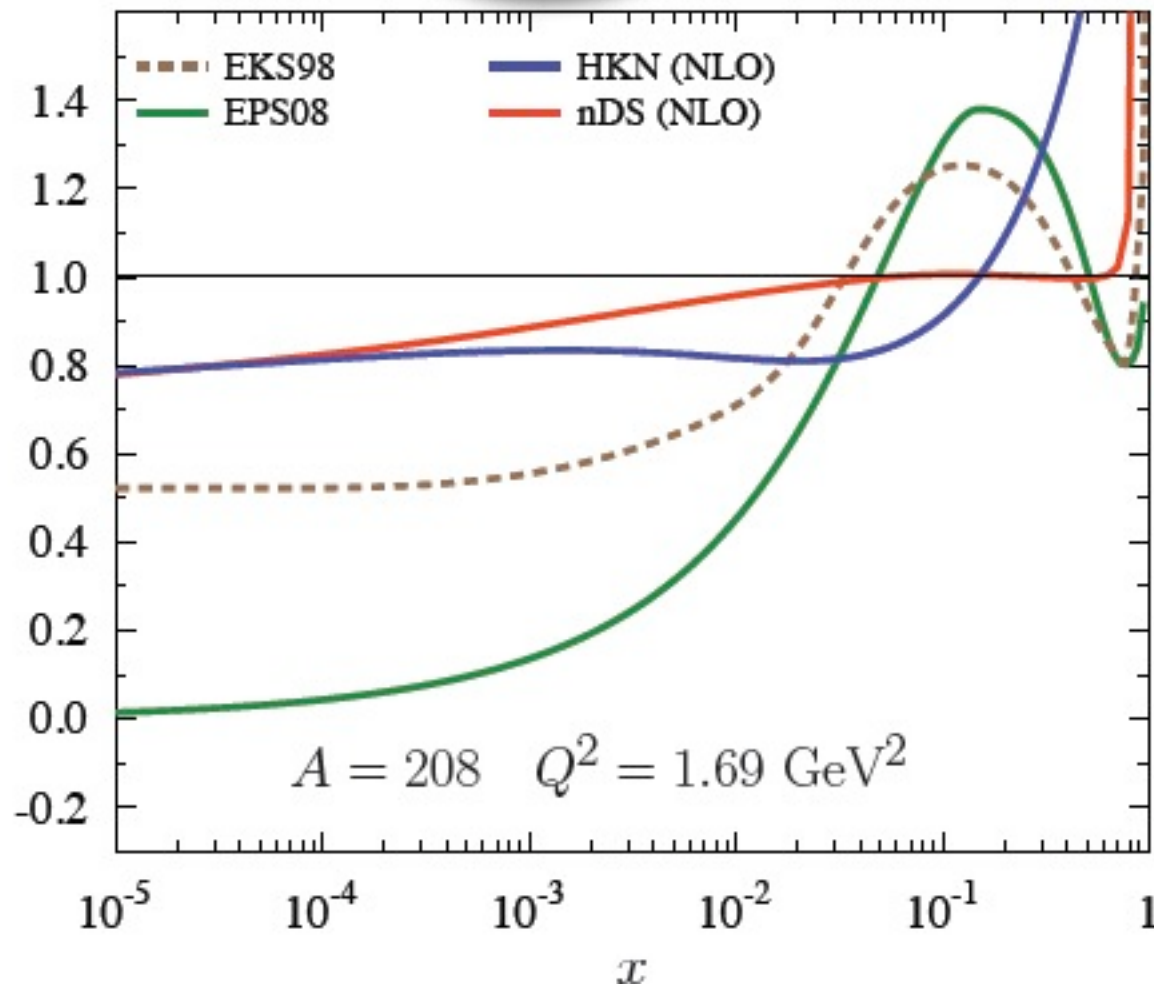
A=Pb



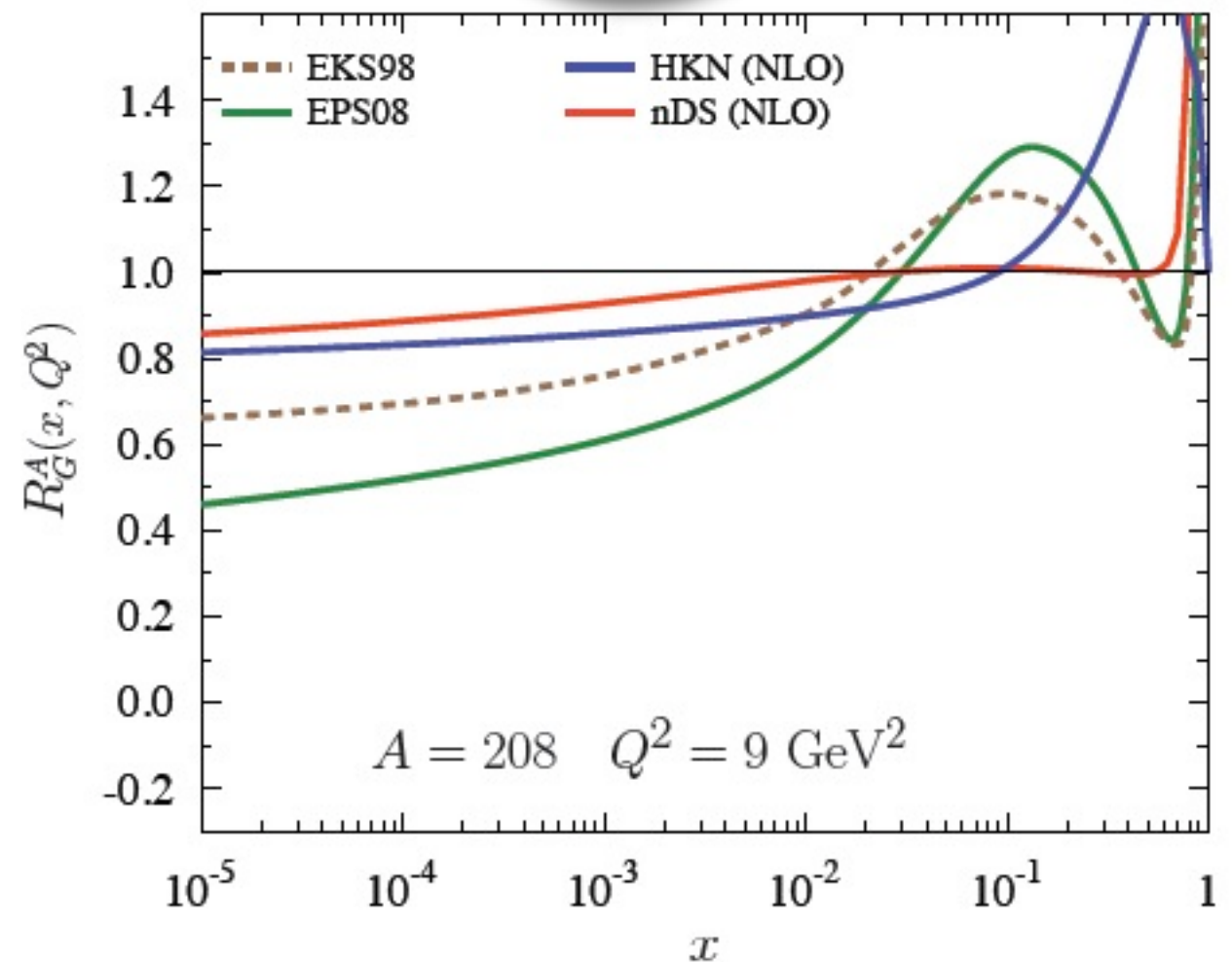
Inclusive ratios: ep/eA

Preliminary calculations of the ratios of gluon densities from N.Armeo et al. Huge difference between models at low x

Ratios for gluons and Pb nuclei



Ratios for gluons and Pb nuclei

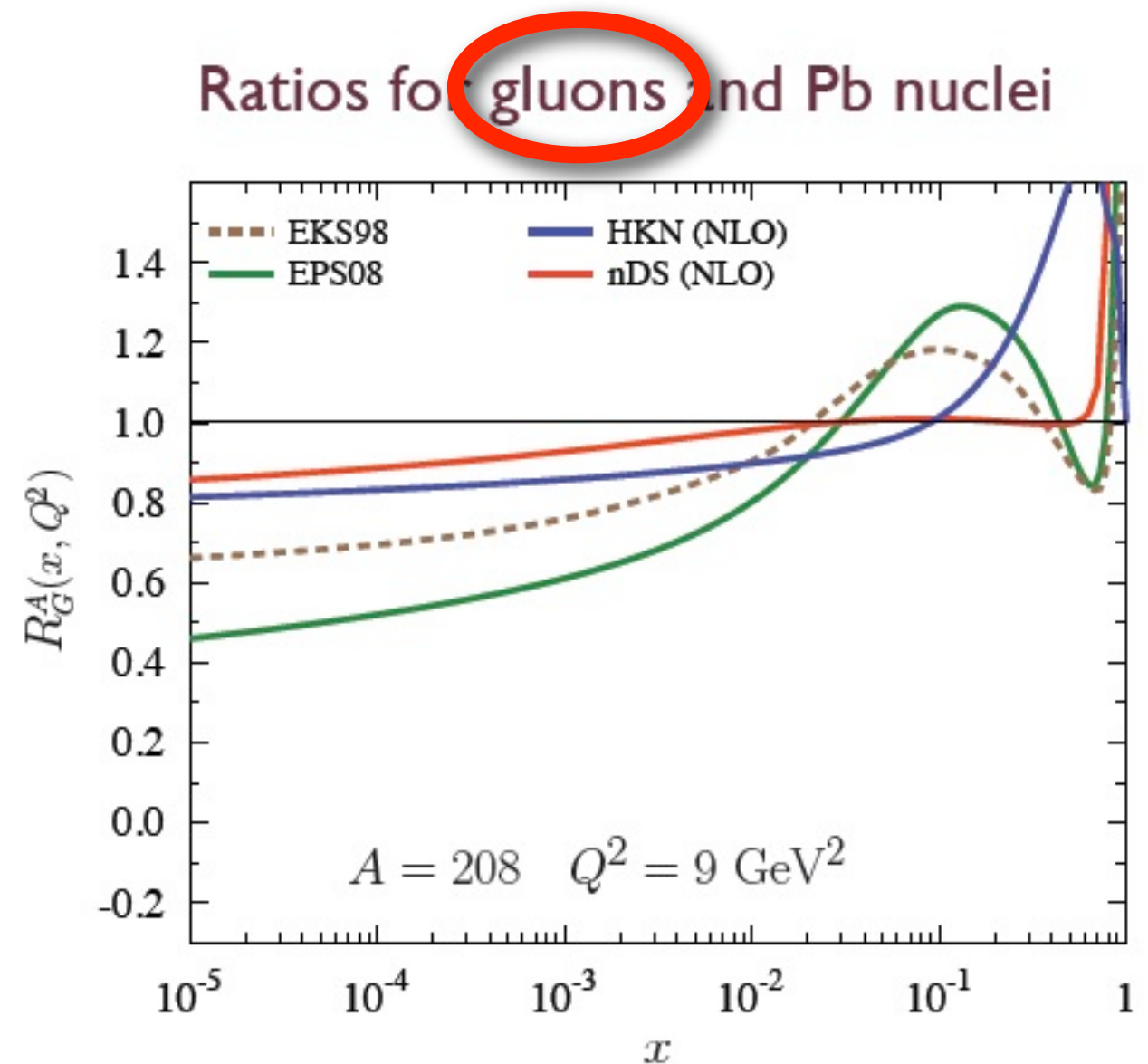


Models tell us that the ratio is not larger than 1 for small x
but can be anywhere between 0 and 1...

Completely new information could be gathered both from EIC and LHeC with nuclei

Inclusive ratios: ep/eA

Preliminary calculations of the ratios of gluon densities from N.Armeo et al. Huge difference between models at low x

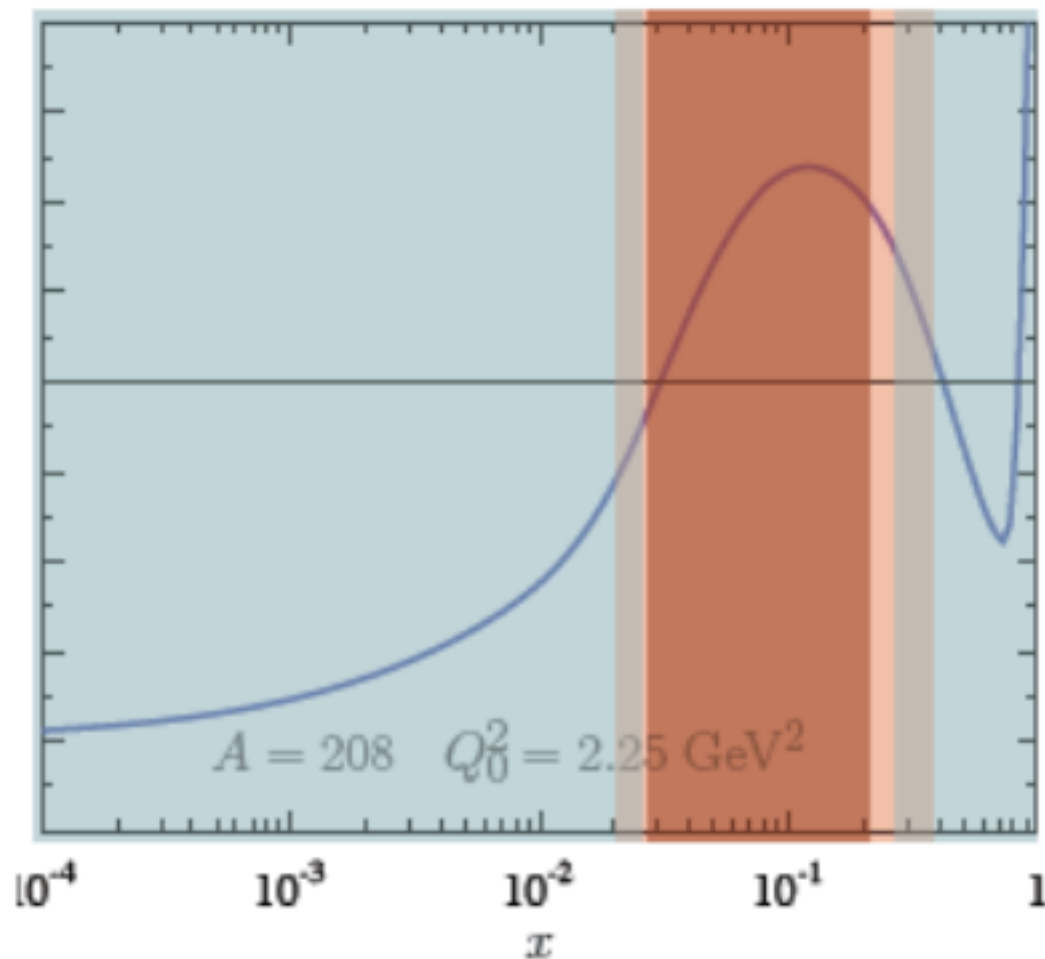


Models tell us that the ratio is not larger than 1 for small x
but can be anywhere between 0 and 1...

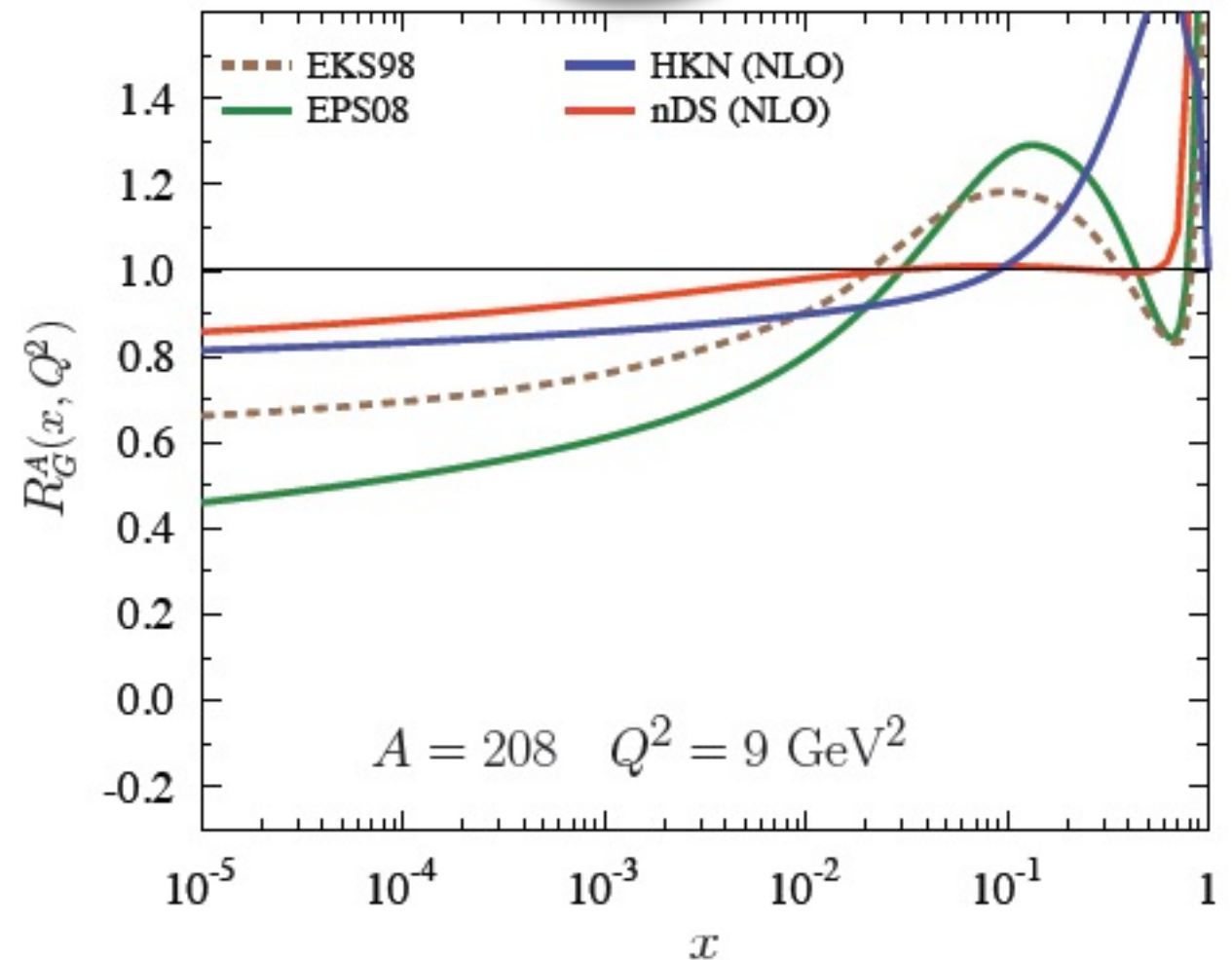
Completely new information could be gathered both from EIC and LHeC with nuclei

Inclusive ratios: ep/eA

Preliminary calculations of the ratios of gluon densities from N.Armeo et al. Huge difference between models at low x



Ratios for **gluons** and Pb nuclei



Models tell us that the ratio is not larger than 1 for small x
but can be anywhere between 0 and 1...

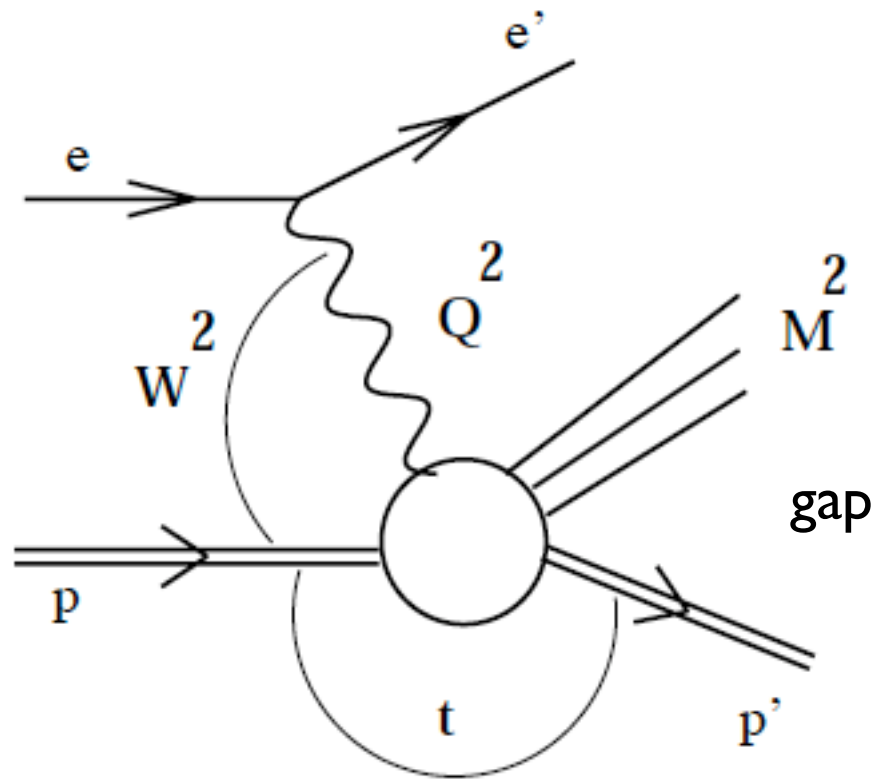
Completely new information could be gathered both from EIC and LHeC with nuclei

Diffraction in ep and eA

Diffraction

$$e + p \rightarrow e' + p' + X$$

Proton stays intact and separated by a rapidity gap



M^2 diffractive mass

$t = (p - p')^2$ momentum transfer

$\Delta\eta = \ln 1/x_P$ Rapidity gap

$$x_P = \frac{Q^2 + M^2 - t}{Q^2 + W^2}$$

momentum fraction of the Pomeron with respect to the hadron

$$\beta = \frac{Q^2}{Q^2 + M^2 - t}$$

momentum fraction of the struck parton with respect to the Pomeron

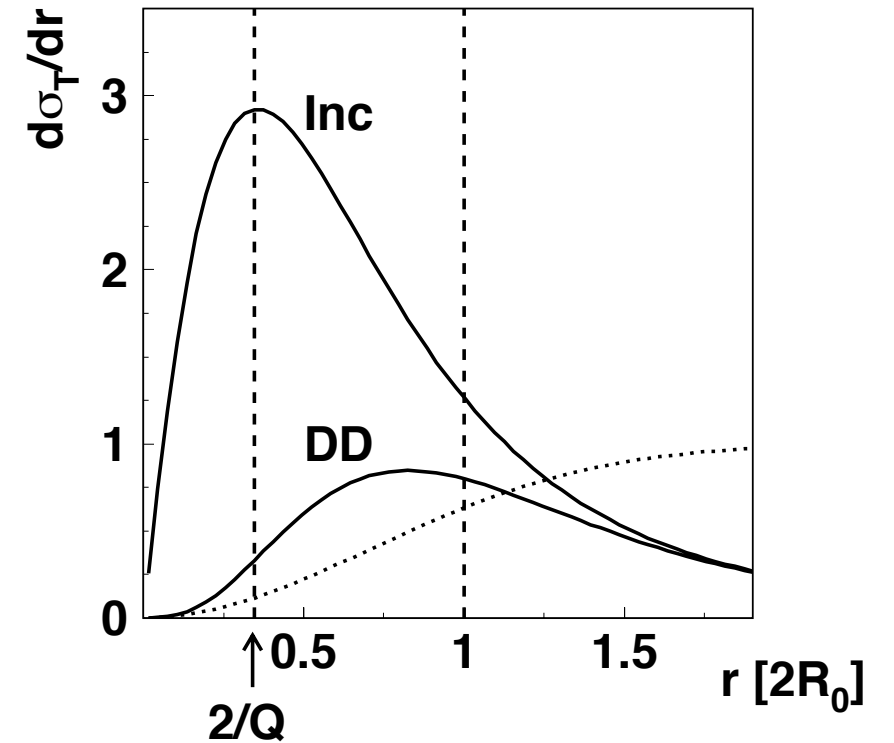
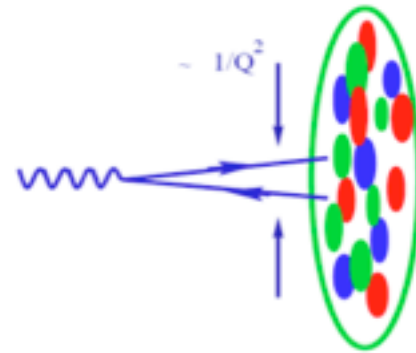
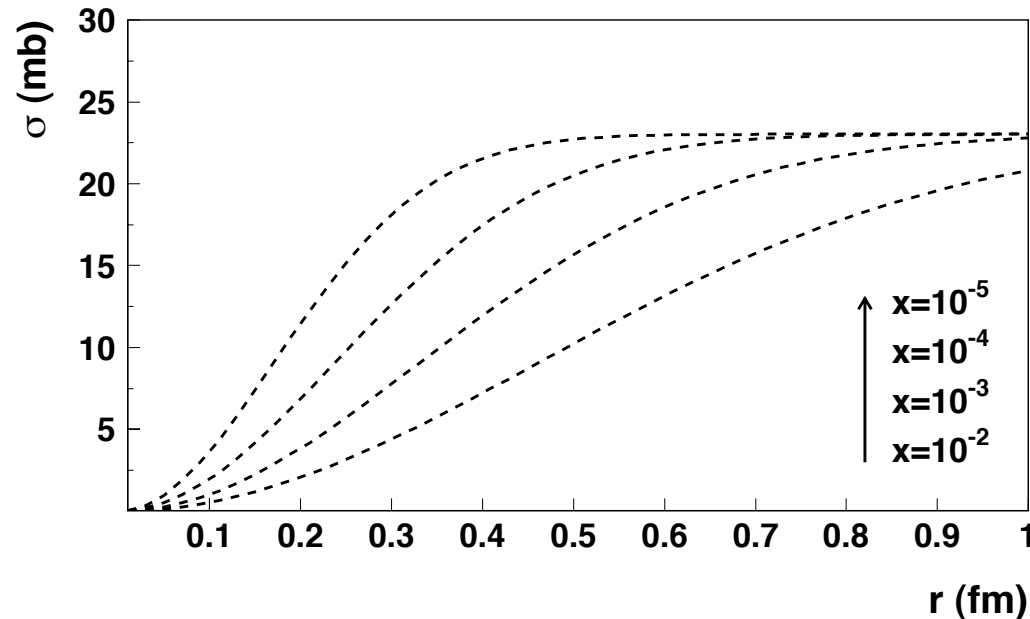
$$x = x_P \beta$$

Bjorken x

Diffraction and saturation

Golec-Biernat, Wuesthoff

overlap function in the dipole model



dipole cross section

$$\sigma_T \sim \underbrace{\frac{\sigma_0}{Q^2 R_0^2}}_{r < 2/Q} + \underbrace{\frac{\sigma_0}{Q^2 R_0^2} \log(Q^2 R_0^2)}_{2/Q < r < 2R_0} + \underbrace{\frac{\sigma_0}{Q^2 R_0^2}}_{r > 2R_0}$$

$$\sigma_T^D \sim \underbrace{\frac{\sigma_0^2}{Q^4 R_0^4}}_{r < 2/Q} + \underbrace{\frac{\sigma_0^2}{Q^2 R_0^2}}_{2/Q < r < 2R_0} + \underbrace{\frac{\sigma_0^2}{Q^2 R_0^2}}_{r > 2R_0} \quad R_0 = \frac{1}{Q_s}$$

$$\sigma_L^D \sim \underbrace{\frac{\sigma_0^2}{Q^4 R_0^4}}_{r < 2/Q} + \underbrace{\frac{\sigma_0^2}{Q^4 R_0^4} \log(Q^2 R_0^2)}_{2/Q < r < 2R_0} + \underbrace{\frac{\sigma_0^2}{Q^4 R_0^4}}_{r > 2r_0}$$

contribution of different dipole sizes

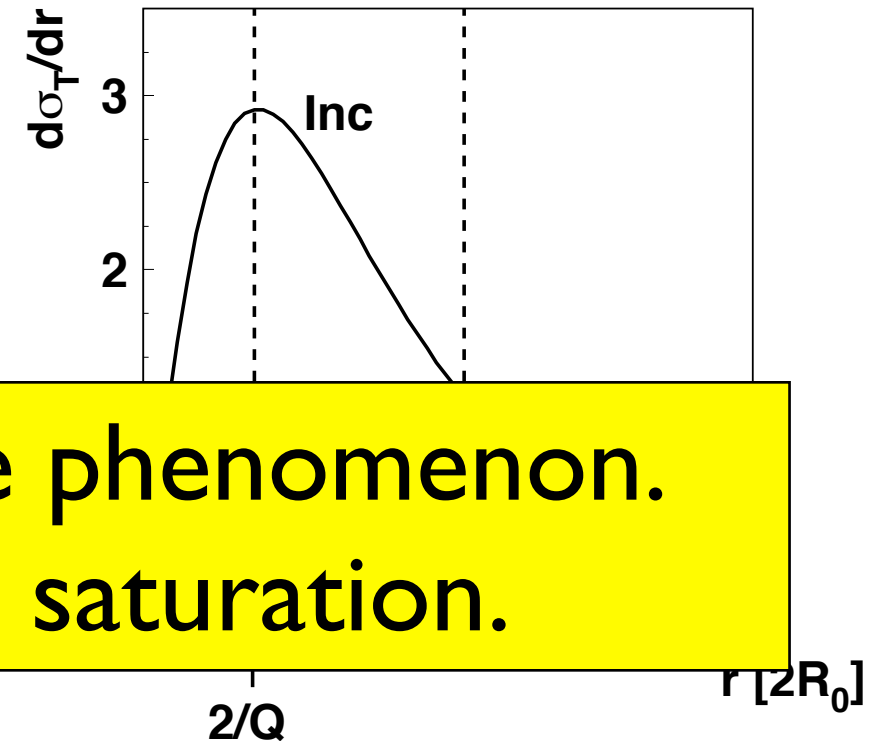
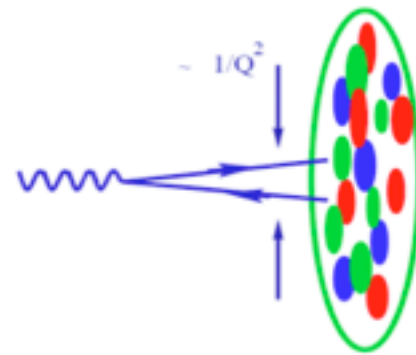
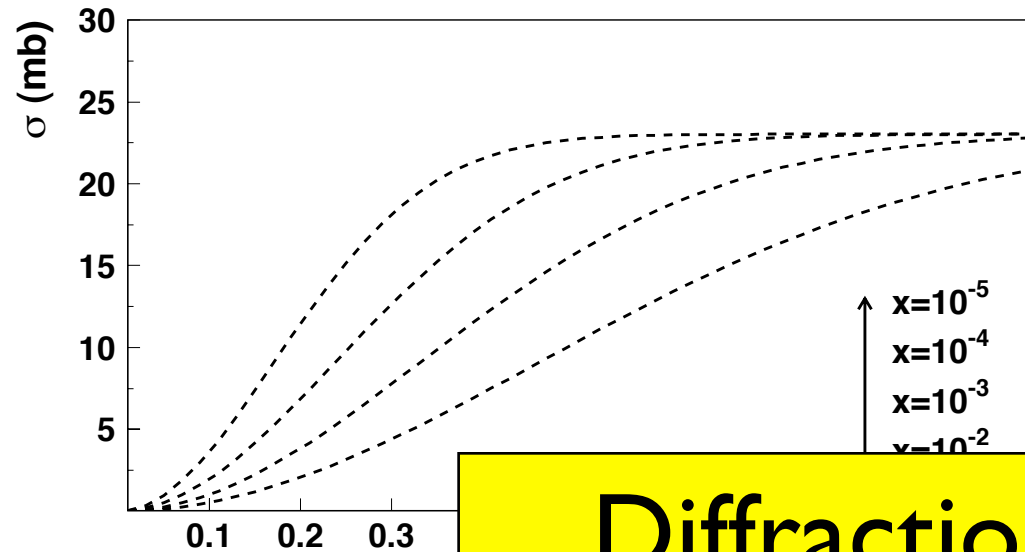
Inclusive: dominated by relatively hard component

Diffractive: dominated by the semi-hard momenta

Diffraction and saturation

Golec-Biernat, Wuesthoff

overlap function in the dipole model



dipole cross

**Diffraction is a collective phenomenon.
Explore relation with saturation.**

$$\sigma_T \sim \underbrace{\frac{\sigma_0}{Q^2 R_0^2}}_{r < 2/Q} + \underbrace{\frac{\sigma_0}{Q^2 R_0^2} \log(Q^2 R_0^2)}_{2/Q < r < 2R_0} + \underbrace{\frac{\sigma_0}{Q^2 R_0^2}}_{r > 2R_0}$$

$$\sigma_T^D \sim \underbrace{\frac{\sigma_0^2}{Q^4 R_0^4}}_{r < 2/Q} + \underbrace{\frac{\sigma_0^2}{Q^2 R_0^2}}_{2/Q < r < 2R_0} + \underbrace{\frac{\sigma_0^2}{Q^2 R_0^2}}_{r > 2R_0} \quad R_0 = \frac{1}{Q_s}$$

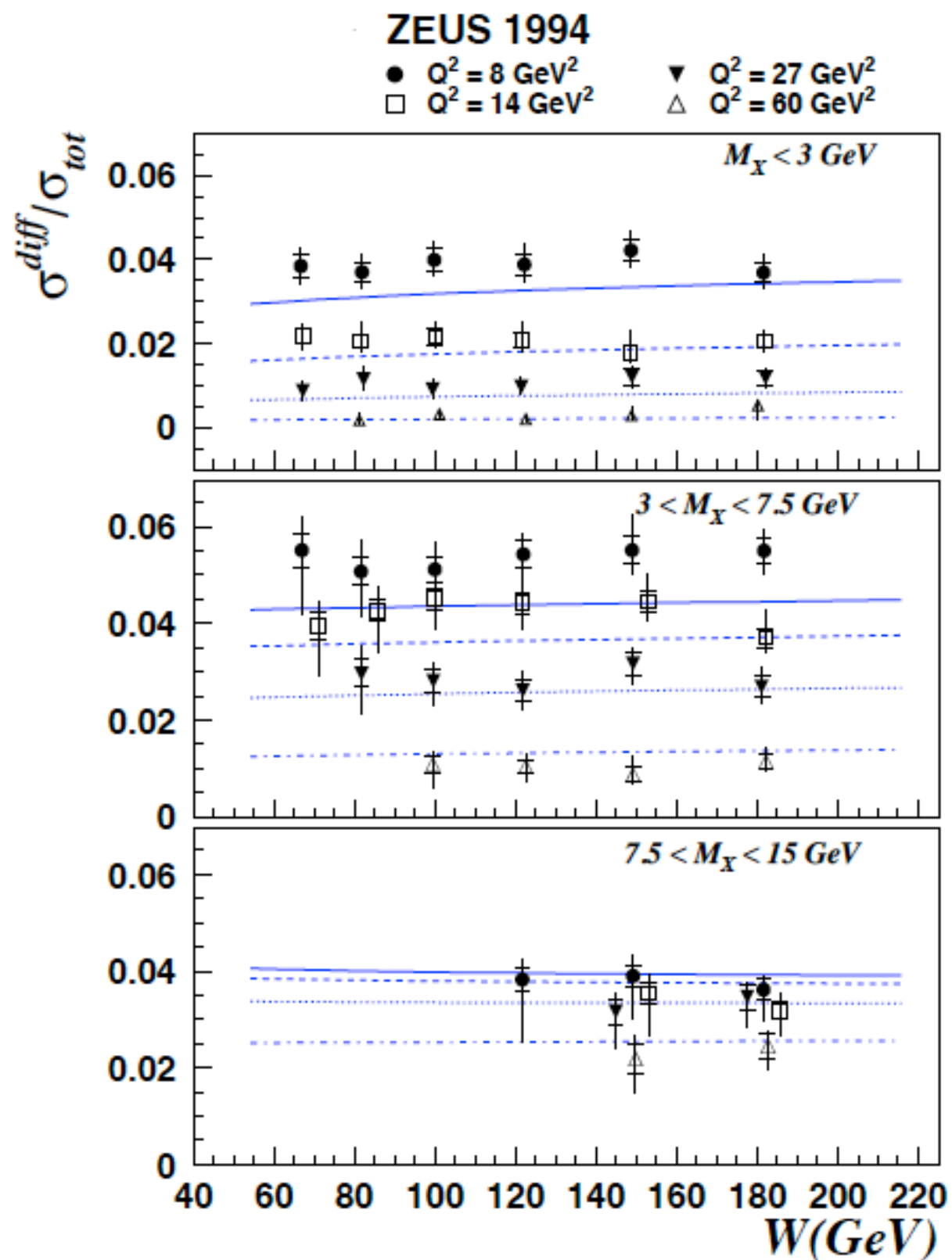
$$\sigma_L^D \sim \underbrace{\frac{\sigma_0^2}{Q^4 R_0^4}}_{r < 2/Q} + \underbrace{\frac{\sigma_0^2}{Q^4 R_0^4} \log(Q^2 R_0^2)}_{2/Q < r < 2R_0} + \underbrace{\frac{\sigma_0^2}{Q^4 R_0^4}}_{r > 2R_0}$$

contribution of different dipole sizes

**Inclusive: dominated by
relatively hard component**

**Diffraction: dominated by
the semi-hard momenta**

Diffractive to inclusive ratio in ep

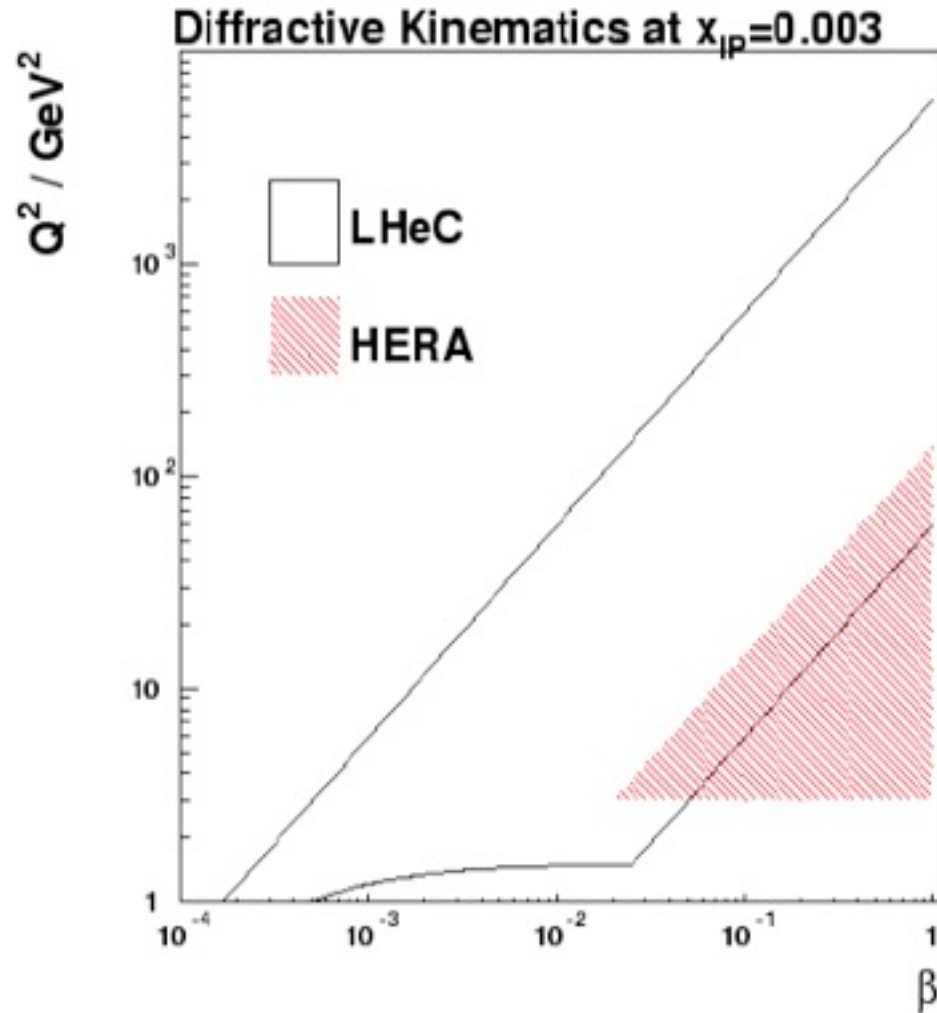


Constant ratio naturally explained
in the saturation model.

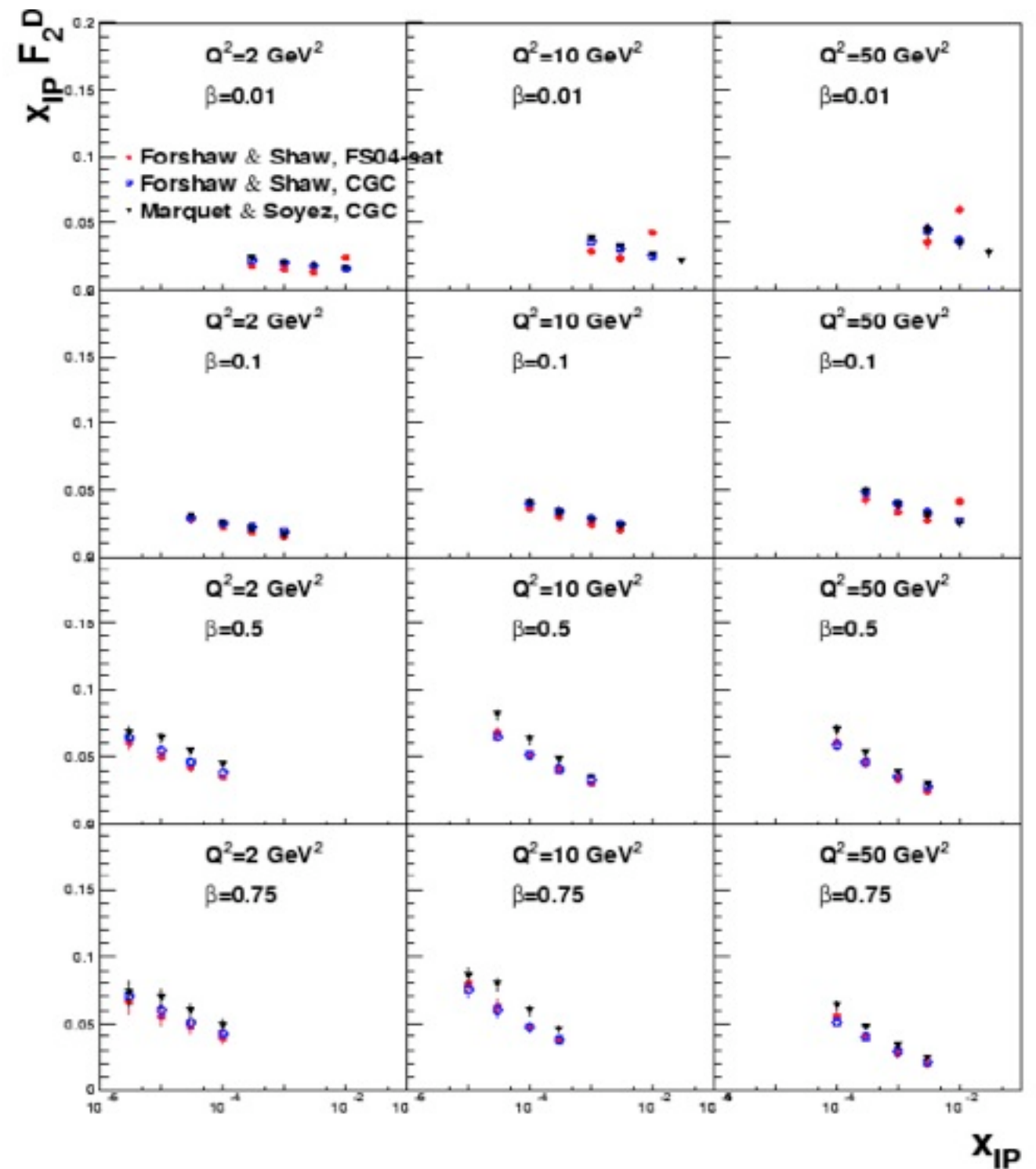
Is it the same ratio and still
constant at higher energy?

What happens in nuclei?

Diffraction at LHeC: new possibilities



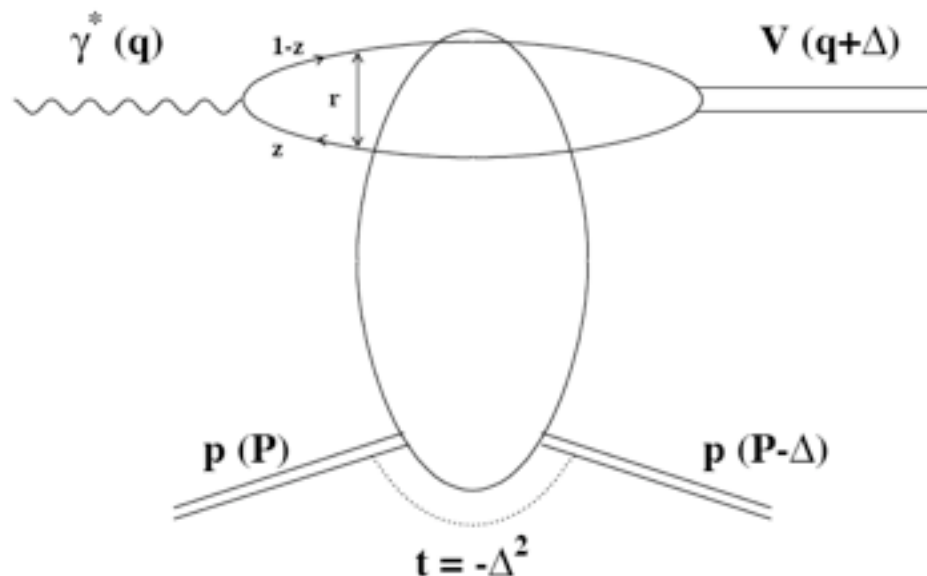
- Studies with 1 degree acceptance,
- Diffractive-PDFs
- Factorization in much bigger range
- Diffractive masses $M_X \sim 100\text{GeV}$ with $x_{IP} = 0.01$
- X can include W,Z,b



Forshaw, Marquet, Newman

Exclusive diffraction of VM

- Exclusive diffractive production of VM is an excellent process for extracting the dipole amplitude
- Suitable process for estimating the 'blackness' of the interaction.
- t-dependence provides an information about the impact parameter profile of the amplitude.



Differential cross section for exclusive VM production

$$\frac{d\sigma}{dt} = \frac{1}{16\pi} |\mathcal{A}_{\text{el}}(x, \Delta, Q)|^2$$

Amplitude for elastic scattering

$$\mathcal{A}_{\text{el}}(x, \Delta, Q) = \sum_{h, \bar{h}} \int d^2\mathbf{r} dz \psi_{\gamma^*}^{h, \bar{h}*}(z, \mathbf{r}; Q) A_{\text{el}}^{q\bar{q}-p}(x, \mathbf{r}, \Delta) \psi_V^{h, \bar{h}}(z, \mathbf{r})$$

Elementary amplitude for elastic scattering

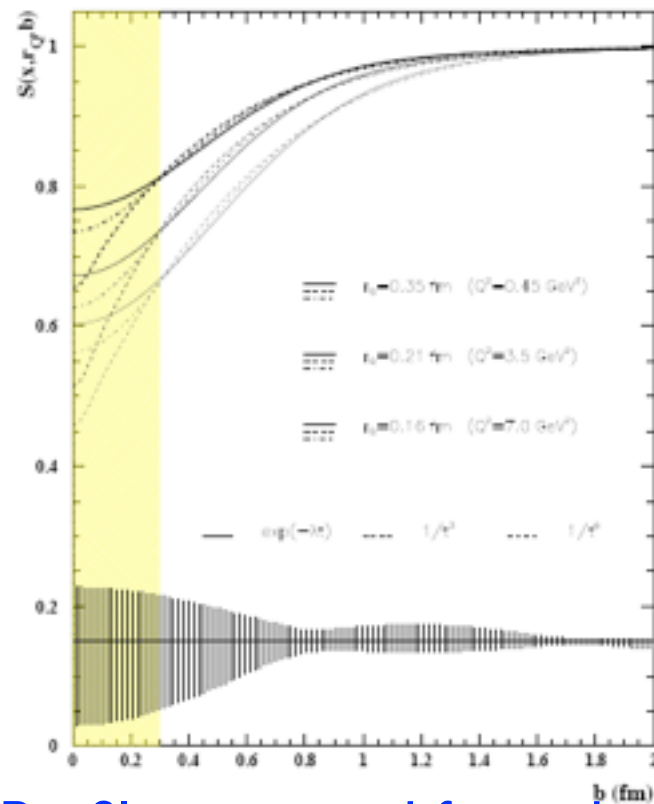
$$A_{\text{el}}^{q\bar{q}-p}(x, \mathbf{r}, \Delta) = \int d^2\mathbf{b} \tilde{A}_{\text{el}}^{q\bar{q}-p}(x, \mathbf{r}, \mathbf{b}) e^{i\mathbf{b}\Delta} = 2 \int d^2\mathbf{b} [1 - S(x, \mathbf{r}, \mathbf{b})] e^{i\mathbf{b}\Delta}$$

Optical theorem

$$\sigma_{\text{tot}}^{q\bar{q}-p}(x, \mathbf{r}) = \mathcal{I}m i A_{\text{el}}^{q\bar{q}-p}(x, \mathbf{r}, \Delta=0).$$

Impact parameter profile

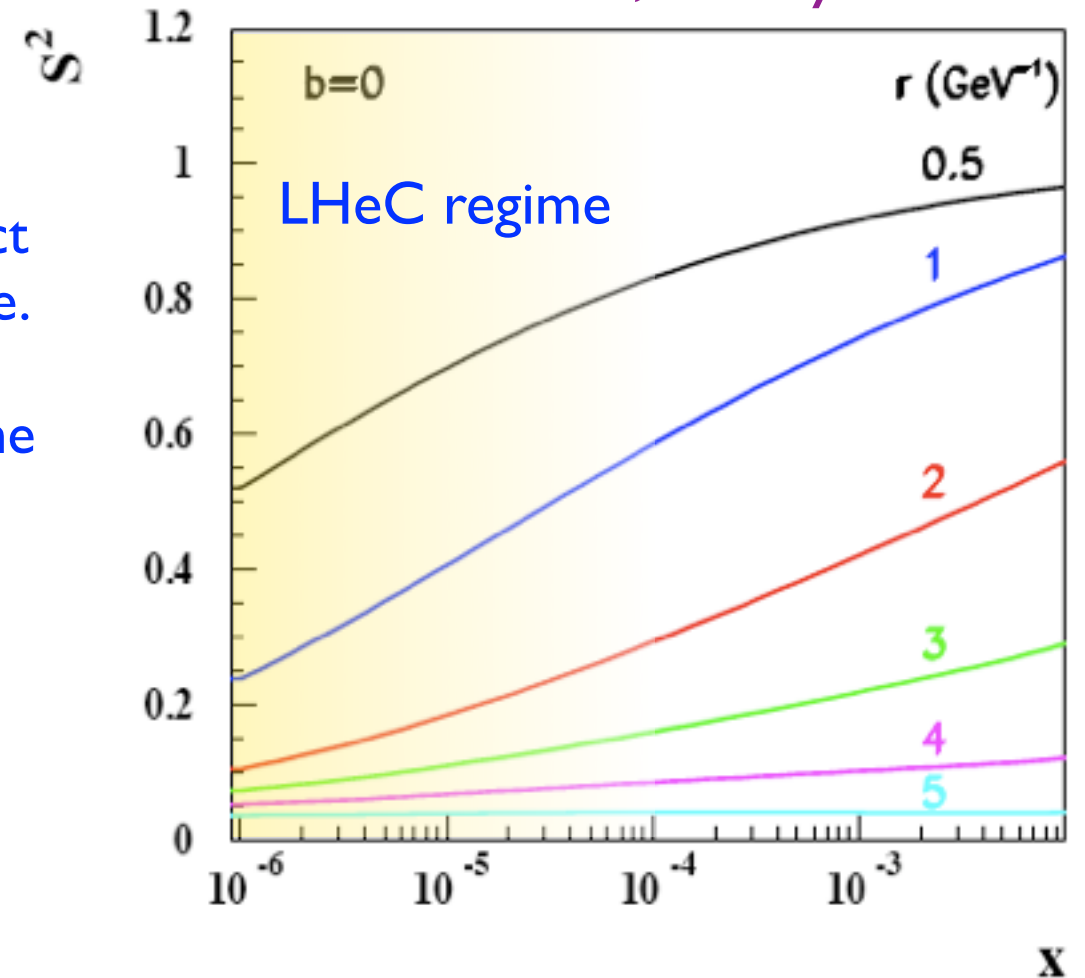
Munier, Stasto, Mueller



Profile extracted from the HERA data

t-dependence vs impact parameter dependence.
What is the characteristic size of the proton in strong interactions?

Kowalski, Teaney



Extrapolations of the S matrix towards lower values of x

$$1 - S^2$$

probability that a dipole passing the proton will induce an inelastic reaction at the given impact parameter

Models indicate significant 'blackness' for central impact parameter

$$Q^2 \sim 5 \text{ GeV}^2$$

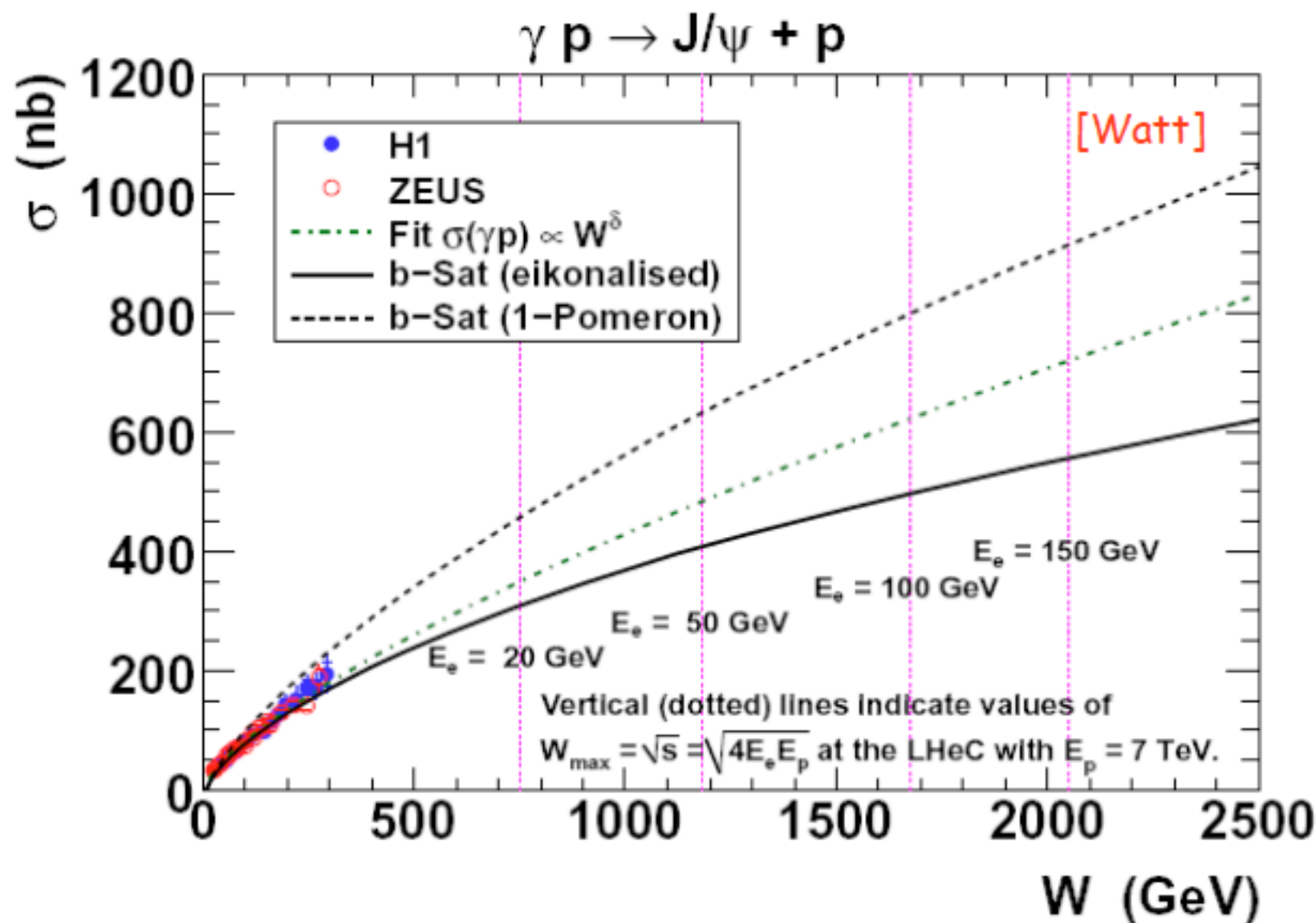
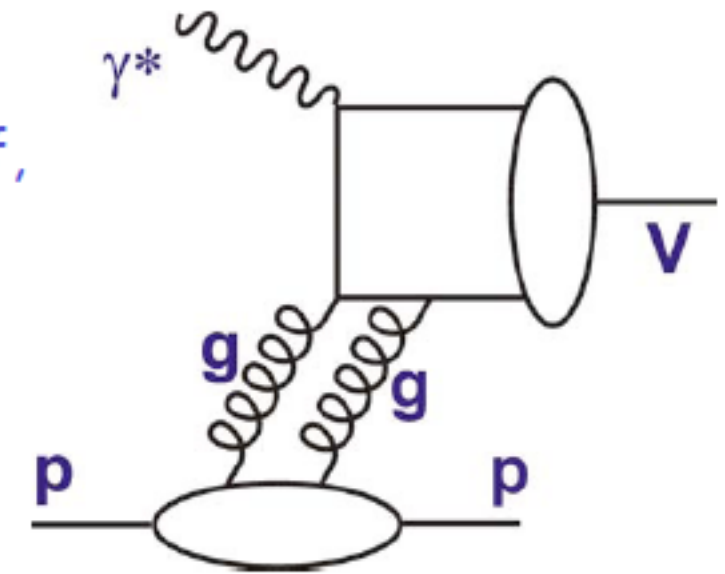
$$x = 10^{-5} - 10^{-6}$$

e.g. J/ψ Photoproduction

e.g. "b-Sat" Dipole model [Golec-Biernat, Wuesthoff, Bartels, Teaney, Kowalski, Motyka, Watt] ...

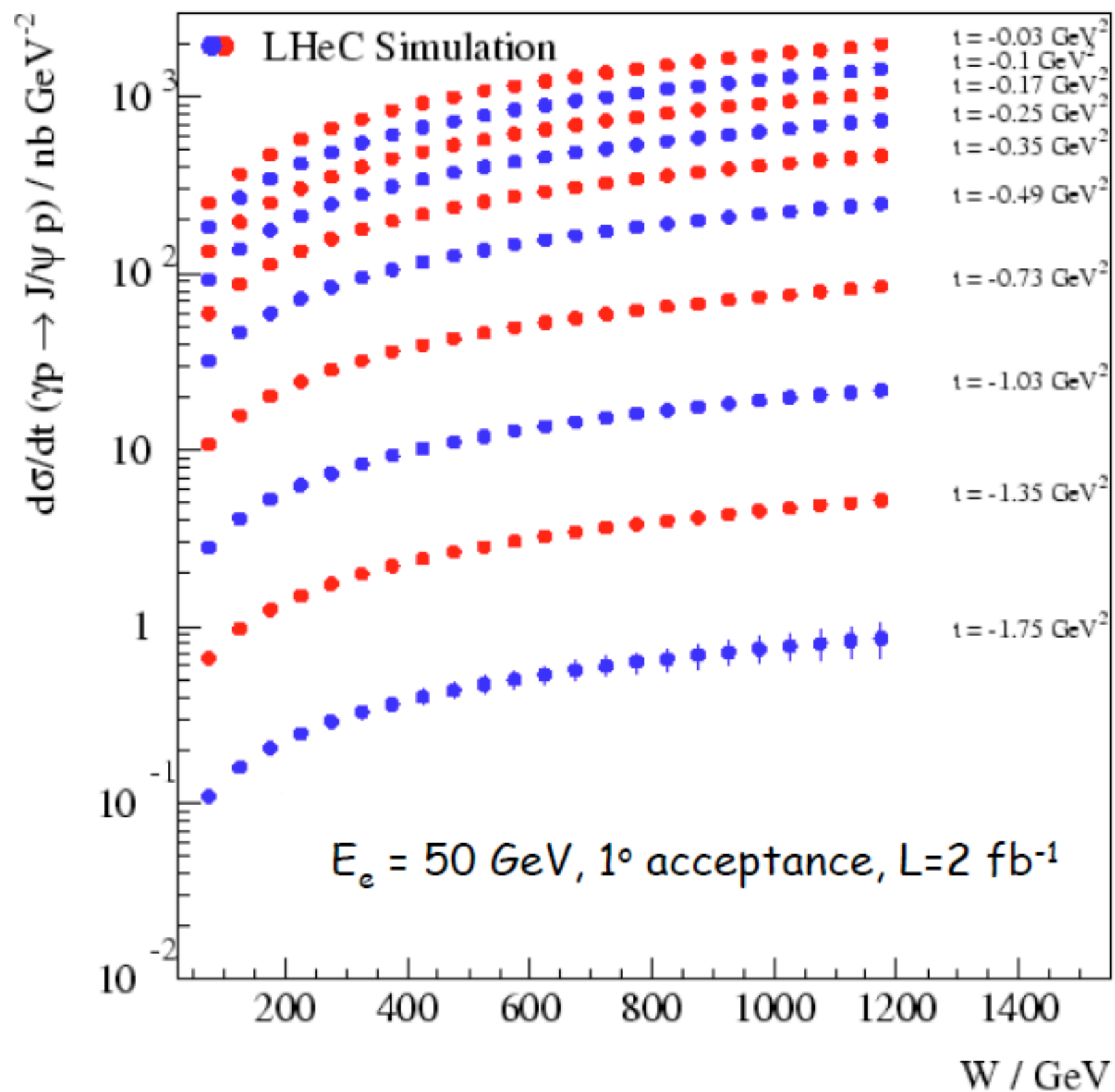
"eikonalised": with impact-parameter dependent saturation

"1 Pomeron": non-saturating



Significant non-linear effects expected even for t-integrated cross section in LHeC kinematic range.

Elastic J/ψ Production more Differentially



J/ψ photoproduction
double differentially
in W and t ...

Inclusive cross sec
probes to $x_g \sim 6 \cdot 10^{-6}$

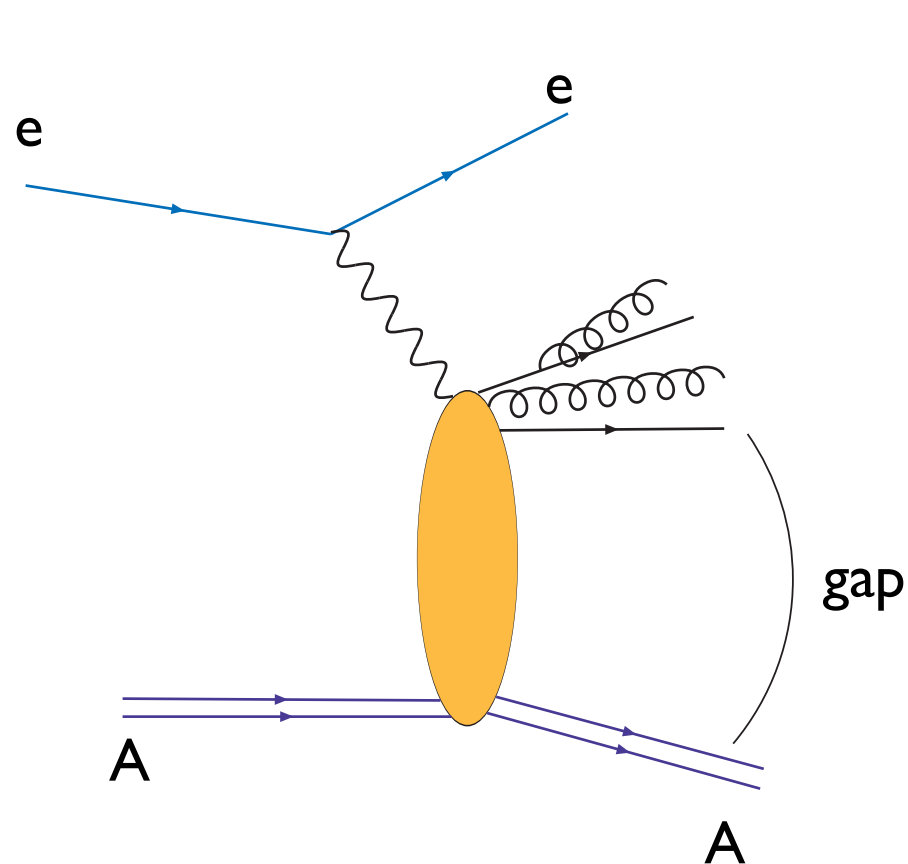
$Q_s^2 \sim 3 \text{ GeV}^2 \sim m_\psi^2/4$

Precise t dependence
will be crucial to
study satⁿ effects!

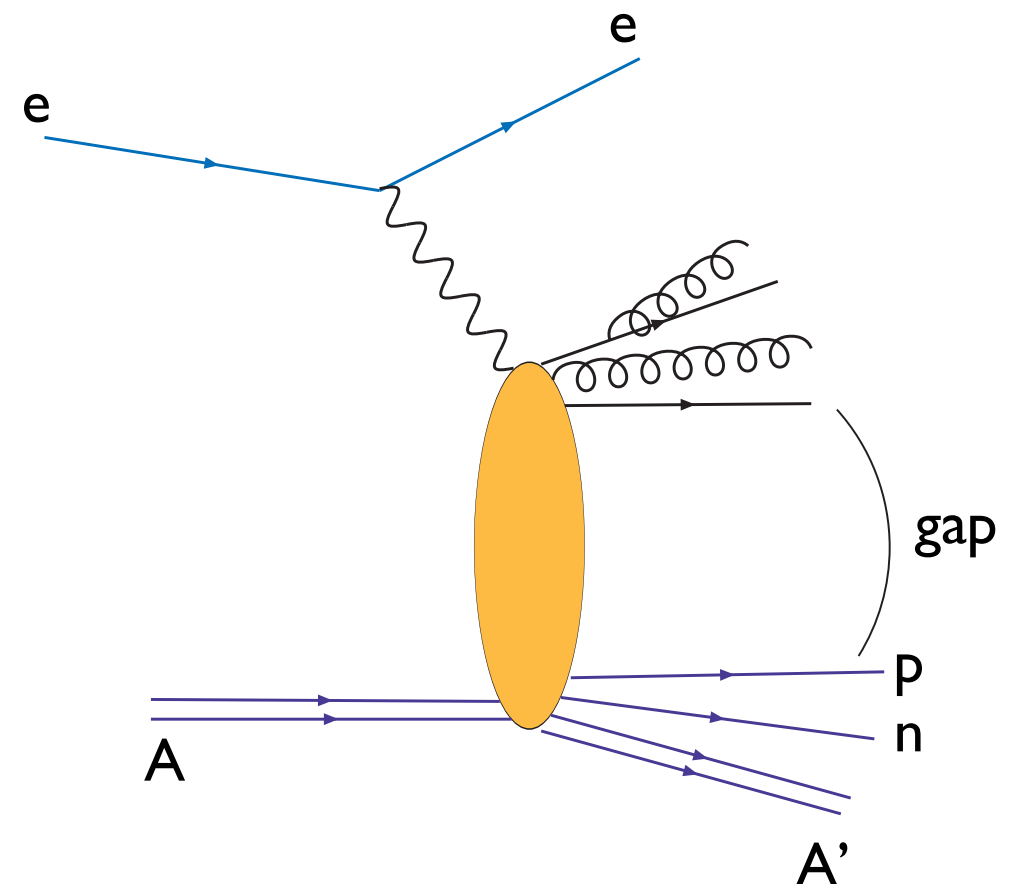
Also possible in
several Q^2 bins

Diffraction in eA

Two possibilities for the diffractive events in nuclei:

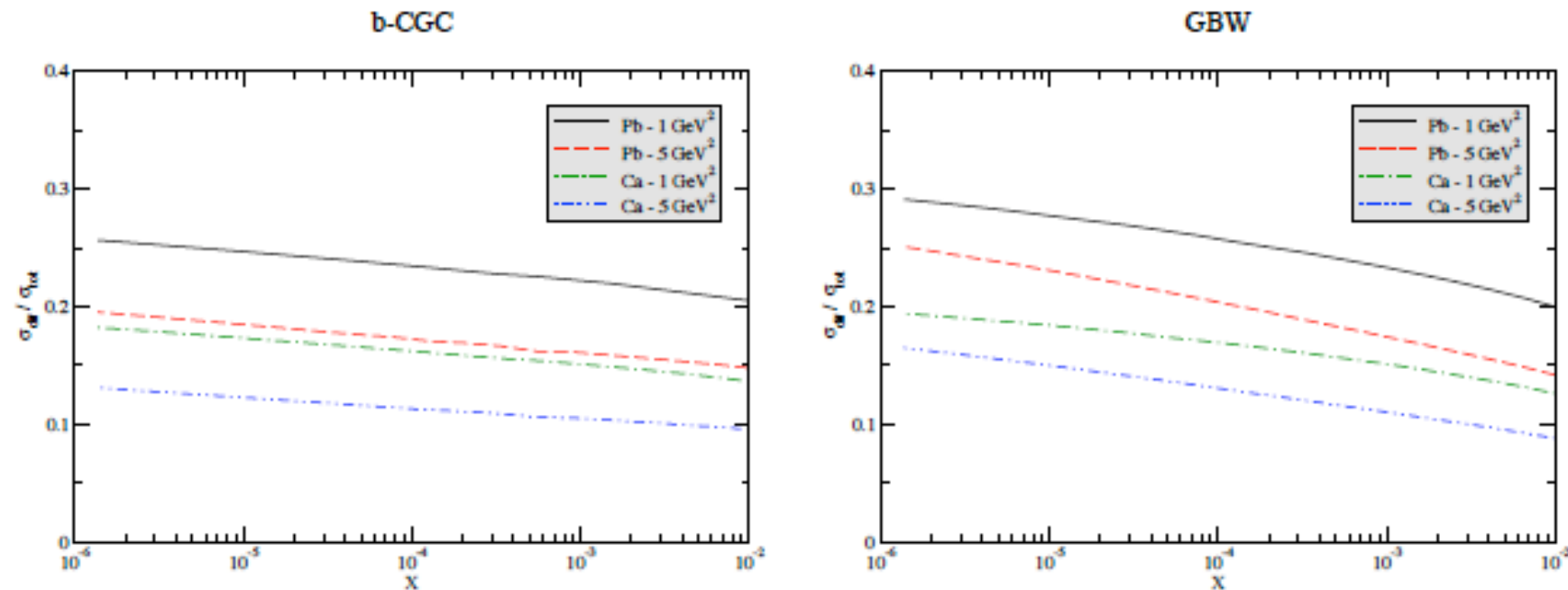


Coherent
No-breakup



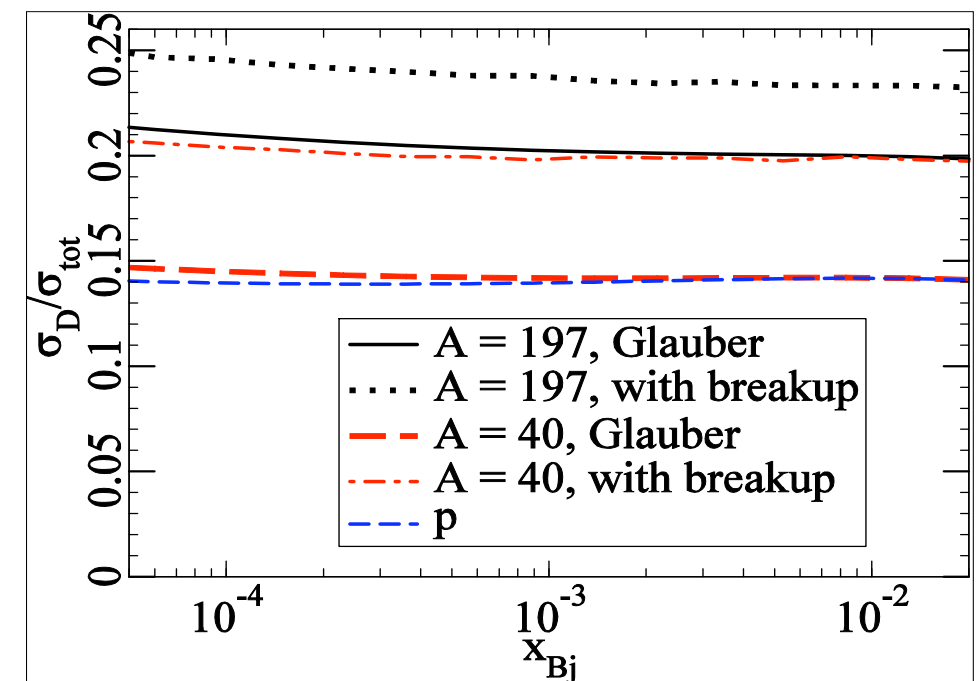
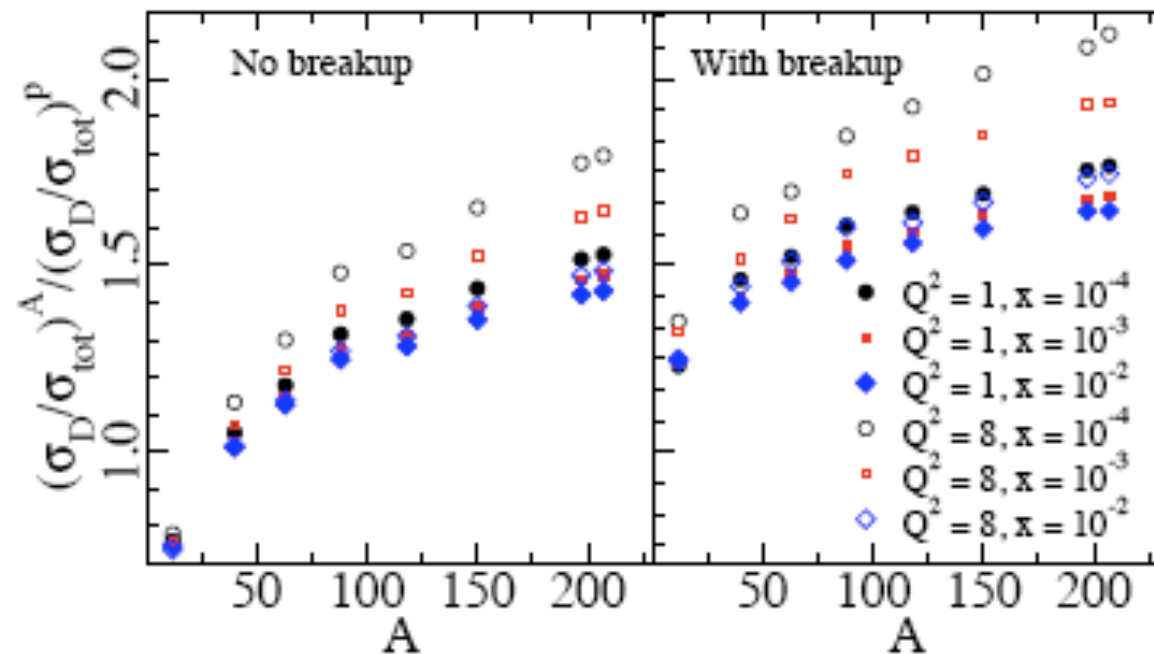
Incoherent
With breakup into nucleons
The gap is still there

Diffractive to inclusive ratio in eA



Predictions give
20%-40% for $\sigma_{\text{diff}} / \sigma_{\text{tot}}$
in the regime down
to 10^{-6}

Cazaroto, Carvalho, Goncalves, Navarra



Kowalski, Lappi, Venugopalan

Summary

- What have we learned from DIS at HERA:
 - fast growth of structure functions at small x
 - large gluon density
 - large number of diffractive events
- New ep/eA collider needed to:
 - explore new kinematic regime at yet smaller values of x
 - pin down the position of the saturation scale, establish the transition region between dilute and dense regime
 - measure the initial state for AA collisions, parton densities in nuclei
 - measure the transverse shape of the nucleus
 - impact of high densities on spin structure