

# Charge dependent flow measurements and the search for the Chiral Magnetic Wave in ALICE

Ron Belmont  
Wayne State University  
On behalf of the ALICE Collaboration

QCD Chirality Workshop  
Los Angeles  
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# Outline

- Physics motivation
- Previous results on CMW
- Proposal for new observable
- Experimental details
- Results
- Conclusions and outlook

# Утро в сосновом лесу

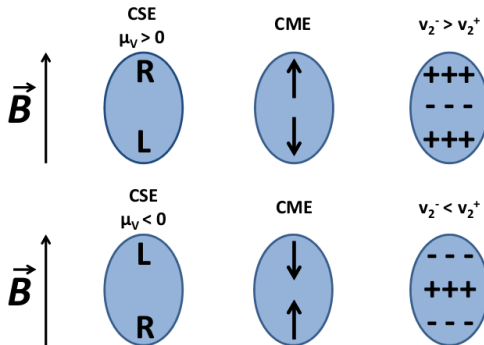


# Утро в сосновом лесу



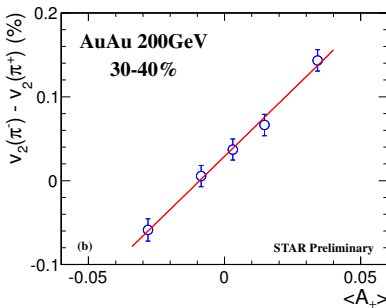
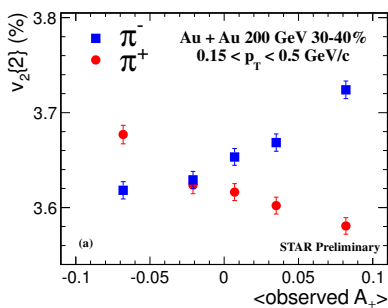


# Physics Motivation: the Chiral Magnetic Wave



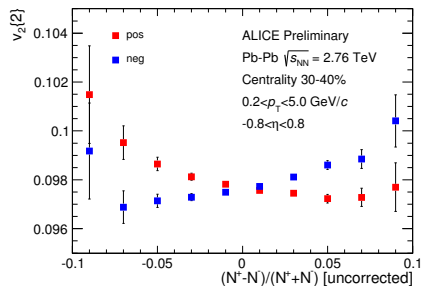
- Coupling between Chiral Magnetic Effect (CME) and Chiral Separation Effect (CSE) leads to wave propagation of electric quadrupole moment, which leads to charge dependence of elliptic flow as a function of charge asymmetry
- Kharzeev and Yee, Phys. Rev. D83, 085007 (2011)
- Burnier, Kharzeev, Liao, and Yee, Phys. Rev. Lett. 107, 052303 (2011)

# STAR results on $v_2^\pm$ and $\Delta v_2$ vs $A$ , 30–40% centrality

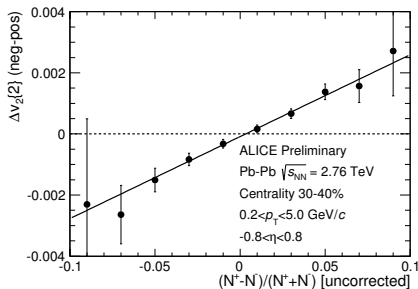


- STAR preliminary, arXiv:1211.3216
- Charge asymmetry  $A_{\pm} = A = (N^+ - N^-)/(N^+ + N^-)$
- Note change in x-axis scale on right plot—correction for efficiency/acceptance
- Qualitatively consistent with CMW picture

# $v_2^\pm$ and $\Delta v_2$ vs $A$ , 30–40% centrality in ALICE



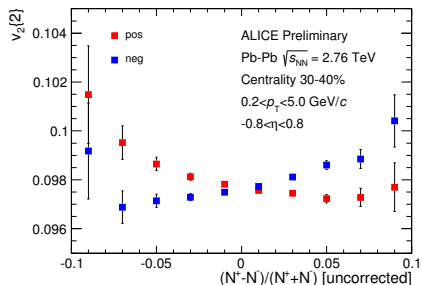
ALI-PREL-70889



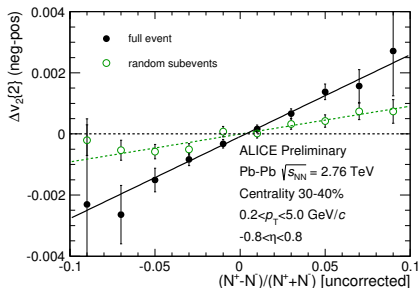
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- Strong, clear signal
- Qualitatively consistent with STAR results

# $v_2^\pm$ and $\Delta v_2$ vs $A$ , 30–40% centrality in ALICE



ALI-PREL-70889



ALI-PREL-70897

- Strong, clear signal
- Qualitatively consistent with STAR results
- Using random subevents with half the track population weakens signal
- Observable has significant efficiency dependence

# Proposal for new measurement: 3-particle correlator

- $v_2$  as a function of  $A$  is very interesting, but requires efficiency correction due to negative binomial sampling
- So what else can we do? Measure the covariance!  $\langle v_2 A \rangle - \langle v_2 \rangle \langle A \rangle$
- $v_2$  is a 2-point correlation, so this is a 3-point correlation
- Can also generalize  $A$  to the charge of a third particle  $q_3$ , since  $\langle q_3 \rangle_{\text{event}} \equiv A$
- Putting it together, the general 3-point correlator is

$$\langle \cos(n(\varphi_1 - \psi_n)) q_3 \rangle - \langle q_3 \rangle \langle \cos(n(\varphi_1 - \psi_n)) \rangle$$

- Similar correlator reported in this analysis

$$\langle \cos(n(\varphi_1 - \varphi_2)) q_3 \rangle - \langle q_3 \rangle \langle \cos(n(\varphi_1 - \varphi_2)) \rangle$$

- We use 2-particle Q-cumulant to calculate  $\langle \cos(n(\varphi_1 - \varphi_2)) \rangle$   
 $c_n\{2\}$  integral,  $d_n\{2\}$  differential

# Experimental details

Detector subsystems:

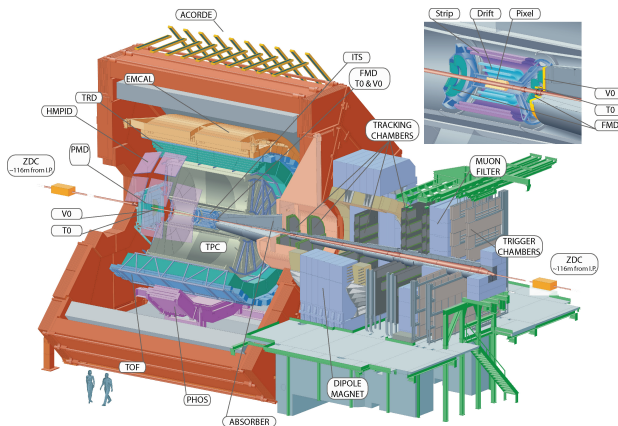
- ITS: vertex, tracking
- V0A+C: trigger, centrality
- TPC: centrality, tracking

Data sample:

- Year 2010 data set
- Pb-Pb collisions at  $\sqrt{s_{NN}} = 2.76$  TeV
- $\approx 12$  M events analyzed

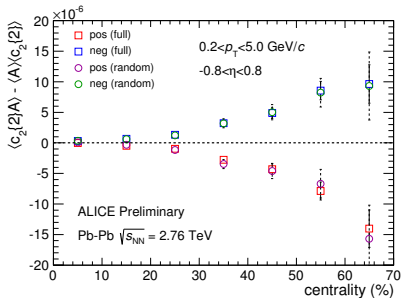
Track selection:

- $0.2 < p_T < 5.0$  (GeV/c)
- $-0.8 < \eta < 0.8$
- $0 < \varphi < 2\pi$



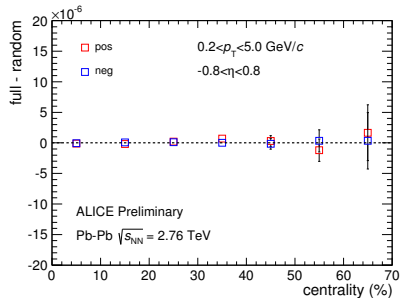
# 3-particle correlator: efficiency independent

## Full and Random together



ALI-PREL-70901

## Difference Full–Random

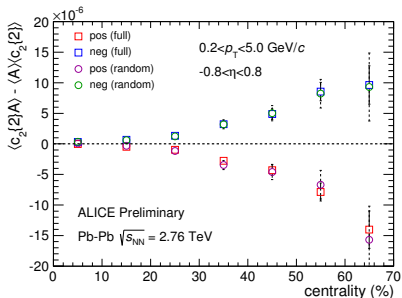


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- The correlator is identical when using random subevents (half the tracks are selected randomly), indicating it is unaffected by detector efficiency

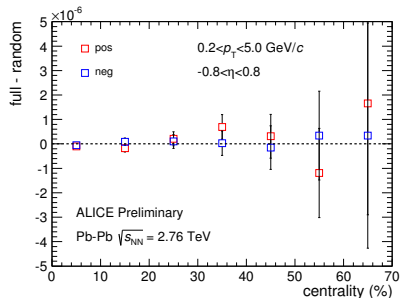
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ALI-PREL-70901

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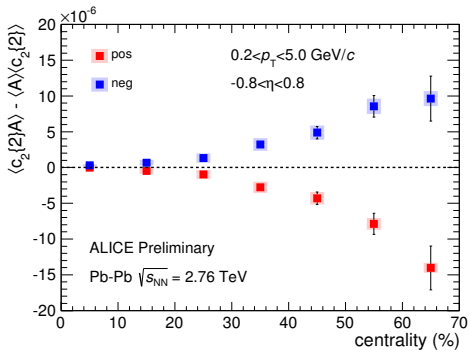


ALI-PREL-71655

- The correlator is identical when using random subevents (half the tracks are selected randomly), indicating it is unaffected by detector efficiency



# 3-particle correlator: 2<sup>nd</sup> harmonic

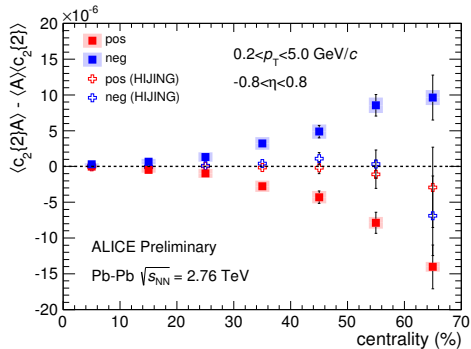


ALI-PREL-70910

What causes the increased charge separation as the collisions become more peripheral?

- Peripheral  $\rightarrow$  stronger magnetic field  $\rightarrow$  stronger CMW effect?
- Central  $\rightarrow$  more combinatoric pairs  $\rightarrow$  trivial dilution of local charge conservation (LCC) effects?
- Dependence on magnitude of  $v_2$  or  $dN/dy$ ?
- Some combination of these (and possibly other) effects?

# 3-particle correlator: comparison to HIJING

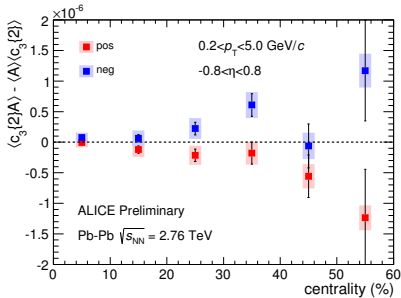


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- No observed effect in HIJING
- Note that HIJING has 3 particle correlations like 3 body decays

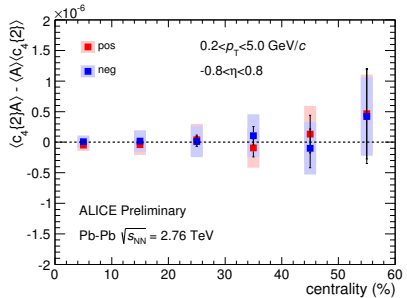
# 3-particle correlator: higher harmonics

## 3<sup>rd</sup> harmonic



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## 4<sup>th</sup> harmonic



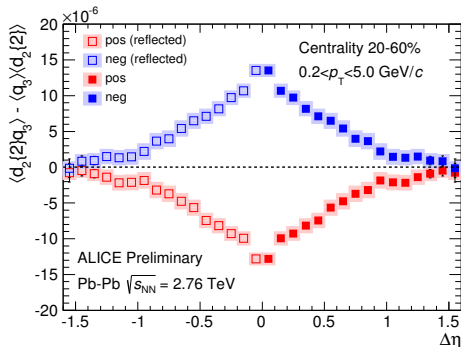
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- CMW quadrupole expected to affect only 2<sup>nd</sup> harmonic, LCC expected to affect all harmonics
- Small effect for 3<sup>rd</sup> harmonic, no observed effect for 4<sup>th</sup> harmonic  
—Note y-axis scale reduced by  $\times 10$  compared to 2<sup>nd</sup> harmonic
- Higher order multipole effects for CMW or harmonic interference? LCC only?

# Intermission

- What kind of differential studies can we do with this correlator?

# 3-particle correlator vs $\Delta\eta$

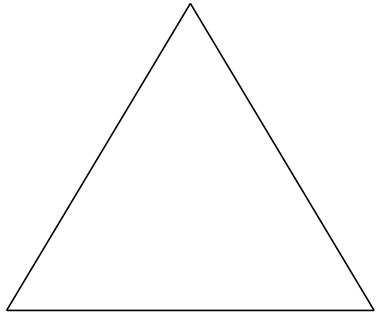


ALI-PREL-70961

- Generalizing from  $A$  to  $q_3$  as discussed, we can measure the correlator as a function of the separation between particles 1 and 3,  $\Delta\eta = \eta_1 - \eta_3$
- Doing so we can directly measure the  $\eta$  range and dependence of the charge dependent effect
- LCC and CMW correlations may have different  $\eta$  ranges, providing an additional experimental constraint
- However, we're missing something very important...

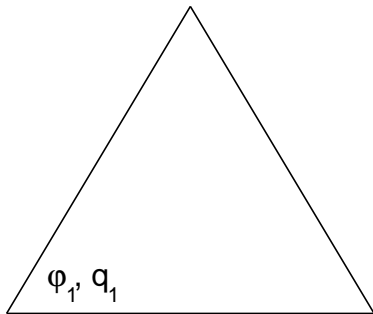
## 3-particle correlator: a closer look

- Let us examine the three particles more carefully



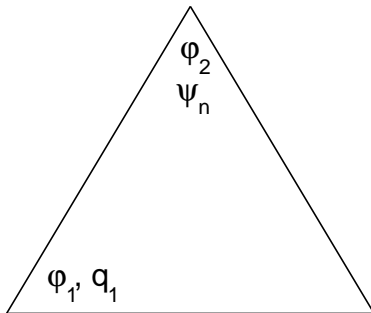
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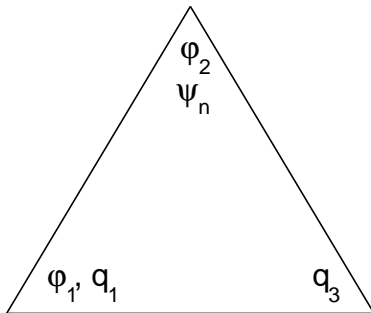
- Let us examine the three particles more carefully
- 1 is the particle of interest, and we consider both  $\varphi_1$  and  $q_1$
- 2 is the reference particle for estimating the flow of particle 1





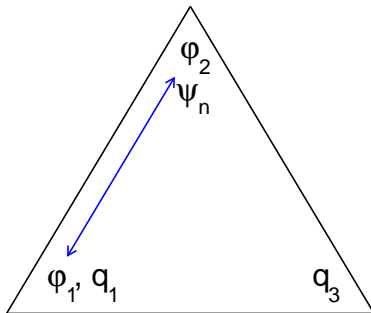
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- 3 is the charged particle



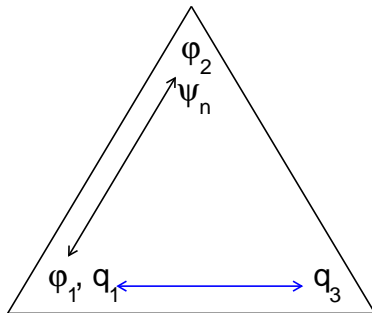
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- 3 is the charged particle
- The correlation between 1 and 2 is the harmonic coefficient



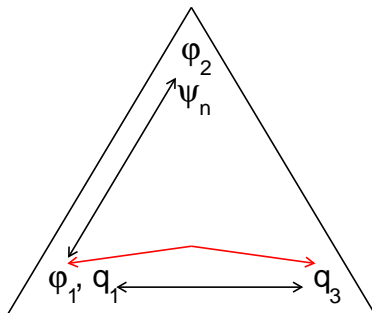
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- The correlation between 1 and 2 is the harmonic coefficient
- The correlation between 1 and 3 is the balance function



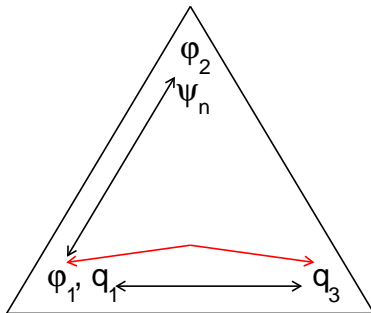
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- The correlation between 1 and 3 is the balance function
- Both correlations must be fully taken into account to get at potentially new physics

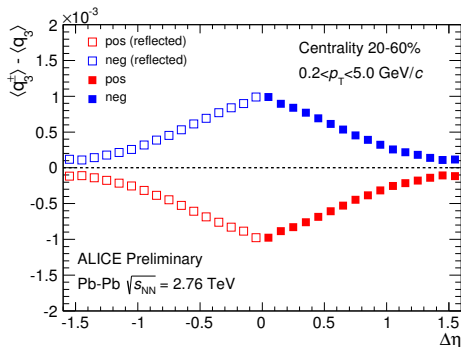


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- The correlation between 1 and 2 is the harmonic coefficient
- The correlation between 1 and 3 is the balance function
- Both correlations must be fully taken into account to get at potentially new physics
  - When removing the charge correlation between 1 and 3, all reducible correlations have been removed and the correlator is a cumulant  $\langle\langle \cos(n(\varphi_1 - \varphi_2)) q_3 \rangle\rangle$
  - S.A. Voloshin and R. Belmont, arXiv:1408.0714



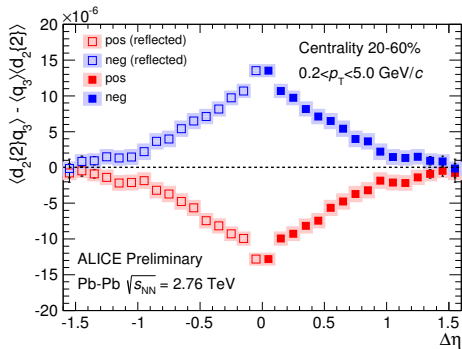
# Understanding mean charge vs $\Delta\eta$



ALI-PREL-73382

- $\langle q_3 \rangle$  denotes mean charge (independent of  $q_1$ )
- $\langle q_3^\pm \rangle$  denotes mean charge depending on charge of particle 1  $q_1$
- The mean charge of the third particle is affected by the charge of the first particle due to charged pair production (the balance function)
- How does this affect the three particle correlator?

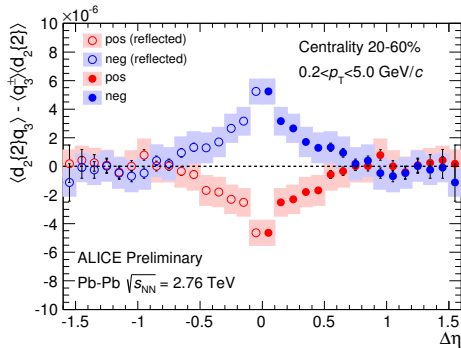
# 3-particle correlator vs $\Delta\eta$



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- Charge independent subtraction (charge correlation not considered)

# 3-particle correlator vs $\Delta\eta$

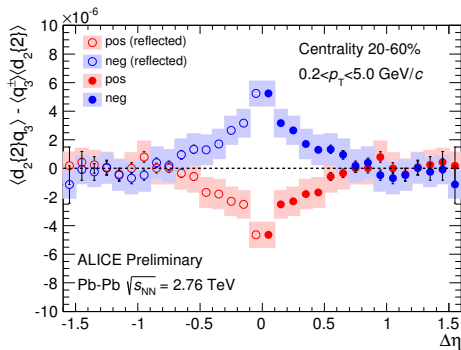


ALI-PREL-70978

- Charge dependent subtraction (charge correlation considered)



# 3-particle correlator vs $\Delta\eta$

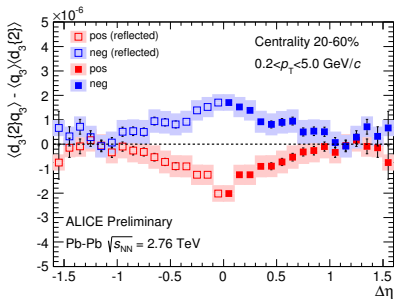


ALI-PREL-70978

- Charge dependent subtraction (charge correlation considered)
- The observed effect has a large contribution from the dependence of  $q_3$  on  $q_1$
- Both the strength and range are significantly reduced, but a pronounced charge dependent effect remains
- How much contribution from charge conservation has been removed? Is there some way to remove all LCC effects leaving only CMW?

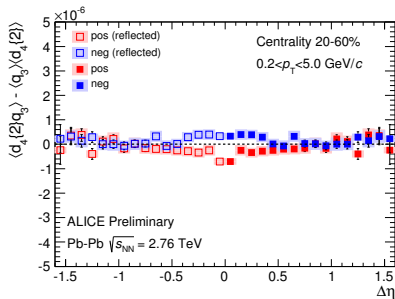
# 3-particle correlator vs $\Delta\eta$ for higher harmonics

## 3<sup>rd</sup> harmonic



ALI-PREL-70970

## 4<sup>th</sup> harmonic

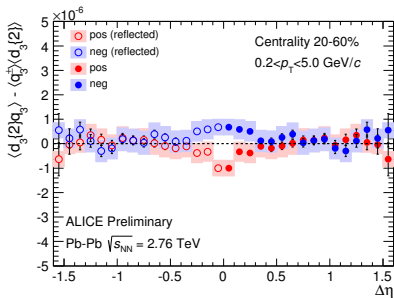


ALI-PREL-70974

- Charge *independent* subtraction
- Moderate effect for 3<sup>rd</sup>, minimal effect for 4<sup>th</sup>

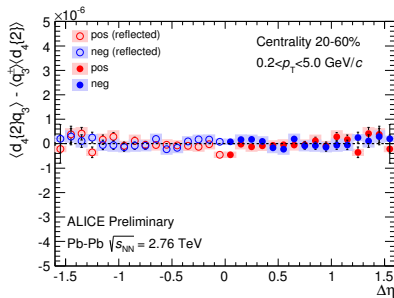
# 3-particle correlator vs $\Delta\eta$ for higher harmonics

## 3<sup>rd</sup> harmonic



ALI-PREL-70982

## 4<sup>th</sup> harmonic



ALI-PREL-70986

- Charge *dependent* subtraction
- Very little effect for either

# Summary

- Integrated 3 particle correlator has strong centrality dependence  
—LCC and dilution? CMW and B-field strength? Magnitude of  $v_2$ ,  $dN/dy$ ?  
Other?
- Differential 3 particle correlator directly measures the  $\eta$  range, providing additional constraints
- Selection on  $q_1$  for subtraction influences the differential correlator  
—How much of the LCC effect has been removed? Input from theory needed!
- Differential correlator is the best (though not only) way to compare across experiments with different  $\eta$  acceptance
- Small but non-negligible charge dependence of third harmonic  
—Higher order multipole moments of P-violating effects, interference from flow harmonics? LCC only?

# Outlook

## Use of identified particles

- The three-particle correlator can be analyzed with identified particles—and not just the flow particle but any particle or all three particles
- PID of first particle could be used to examine whether there's any flavor or mass dependence of the observed effect
- PID of second and third particles may also be interesting to study
- The current data may not have enough statistics for a detailed PID study, but LHC Run-II is coming soon

## Cross-experiment comparisons

- This correlator guarantees “fair” comparisons across experiments
- CMS and ATLAS can measure the differential correlator to larger  $\Delta\eta$
- STAR can (and should!) analyze this correlator for all available RHIC energies, as they have done with the CME correlator

Additional material

# Physics Motivation: the Chiral Magnetic Wave

Chiral Magnetic, Separation Effect:

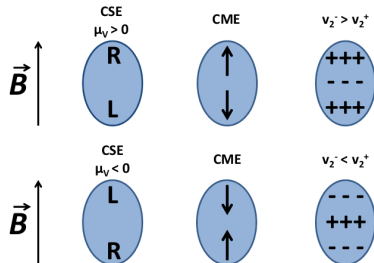
$$\vec{J}_V = \frac{N_c e}{2\pi^2} \mu_A \vec{B}, \quad \vec{J}_A = \frac{N_c e}{2\pi^2} \mu_V \vec{B}$$

Thermodynamics:

$$\vec{J}_V = \frac{N_c e}{2\pi^2} \chi \rho_A \vec{B}, \quad \vec{J}_A = \frac{N_c e}{2\pi^2} \chi \rho_V \vec{B}$$

Chiral basis:

$$\vec{J}_L = -\frac{N_c e}{2\pi^2} \chi \rho_L \vec{B}, \quad \vec{J}_R = \frac{N_c e}{2\pi^2} \chi \rho_R \vec{B}$$



- Kharzeev and Yee, Phys. Rev. D83, 085007 (2011)
- Burnier, Kharzeev, Liao, and Yee, Phys. Rev. Lett. 107, 052303 (2011)

# Physics Motivation: the Chiral Magnetic Wave

Azimuthal distribution of charges:

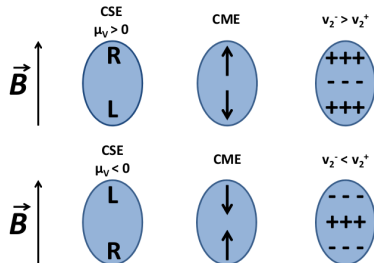
$$\frac{dQ}{d\varphi} = Q[1 - r_e \cos(2\varphi)]$$

Definition of charge asymmetry  $A$ :

$$A = \frac{Q}{N^{total}} = \frac{N^+ - N^-}{N^+ + N^-}$$

Azimuthal distribution of particles:

$$\frac{dN^\pm}{d\varphi} = N^\pm [1 + (2v_2 \mp r_e A) \cos(2\varphi)]$$



- Kharzeev and Yee, Phys. Rev. D83, 085007 (2011)
- Burnier, Kharzeev, Liao, and Yee, Phys. Rev. Lett. 107, 052303 (2011)



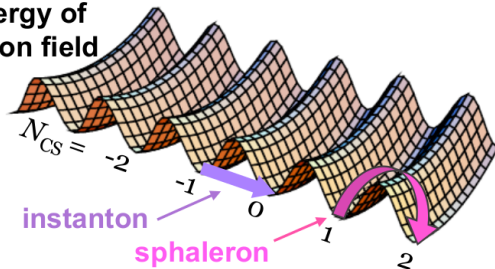
# Physics Motivation: Topological Charge

QCD vacuum is highly non-trivial!

Topological charge, winding number, Chern-Simons number:

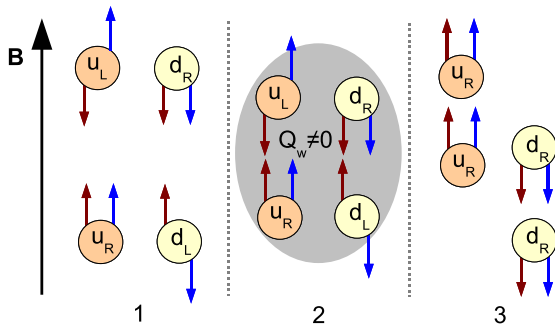
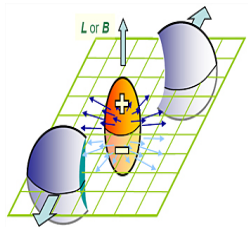
$$Q_w = \frac{g^2}{32\pi^2} \int d^4x F_{\mu\nu}^a \tilde{F}_a^{\mu\nu} \in \mathbb{Z}.$$

**Energy of  
gluon field**



- Instanton: tunneling through barrier (all energies/temperatures, including 0)
- Sphaleron: jumping over barrier (only sufficiently high temperatures/energies)

# Physics Motivation: the Chiral Magnetic Effect



- Kharzeev, McLerran, and Warringa, Nucl. Phys. A803, 227 (2008)
- Presence of non-zero topological charge causes some chiralities to flip  
example:  $Q_w = -1 \Rightarrow L \rightarrow R, R \rightarrow R$
- Problem:  $Q_w$  fluctuates about 0, electric dipole averages to 0

# Methodology—Direct Cumulants

- Definition of flow vectors

$$Q_{n,x} = \sum_{i=1}^M \cos n\varphi_i = \Re Q_n$$
$$Q_{n,y} = \sum_{i=1}^M \sin n\varphi_i = \Im Q_n$$

- Direct cumulant method for integral flow

$$\begin{aligned} \langle \cos(n(\varphi_1 - \varphi_2)) \rangle &= \frac{Q_n Q_n^* - M}{M(M-1)} \\ &= c_n\{2\} \end{aligned}$$

- The flow coefficients can be calculated as  $v_n = \sqrt{c_n\{2\}}$
- In this analysis, particles 1 and 2 are always selected to be the same charge

# Methodology—Direct Cumulants

- Definition of single particle flow vectors

$$u_{n,x} = \cos n\varphi_i = \Re u_n$$

$$u_{n,y} = \sin n\varphi_i = \Im u_n$$

- Direct cumulant method for differential flow

$$\begin{aligned} \langle \cos(n(\varphi_1 - \varphi_2)) \rangle &= \frac{u_n Q_n^* - 1}{M - 1} \\ &= d_n\{2\} \end{aligned}$$

- The flow coefficients can be calculated as  $v_n = d_n\{2\} / \sqrt{c_n\{2\}}$
- In this analysis, the charge of particle 1 is selected while particle 2 is allowed to be from either charge