

# Collectivity and flow in small systems at RHIC PHENIX perspectives

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University of Colorado  
Boulder



THE UNIVERSITY of NORTH CAROLINA  
**GREENSBORO**

# A very brief history of recent heavy ion physics

1980s and 1990s—AGS and SPS... QGP at SPS!

Early 2000s—QGP at RHIC! No QGP at SPS. d+Au as control.

Mid-late 2000s—Detailed, quantitative studies of strongly coupled QGP. d+Au as control.

2010—Ridge in high multiplicity p+p (LHC)! Probably CGC!

Early 2010s—QGP in p+Pb!

Early 2010s—QGP in d+Au!

Mid 2010s and now-ish—QGP in high multiplicity p+p? QGP in mid-multiplicity p+p??

QGP in d+Au even at low energies???

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“Twenty years ago, the challenge in heavy ion physics was to find the QGP. Now, the challenge is to not find it.” —Jürgen Schukraft, QM17

## Particle production in small systems

- Final state effects are observed
- Photon modification consistent with QGP formation

## Small systems geometry scan

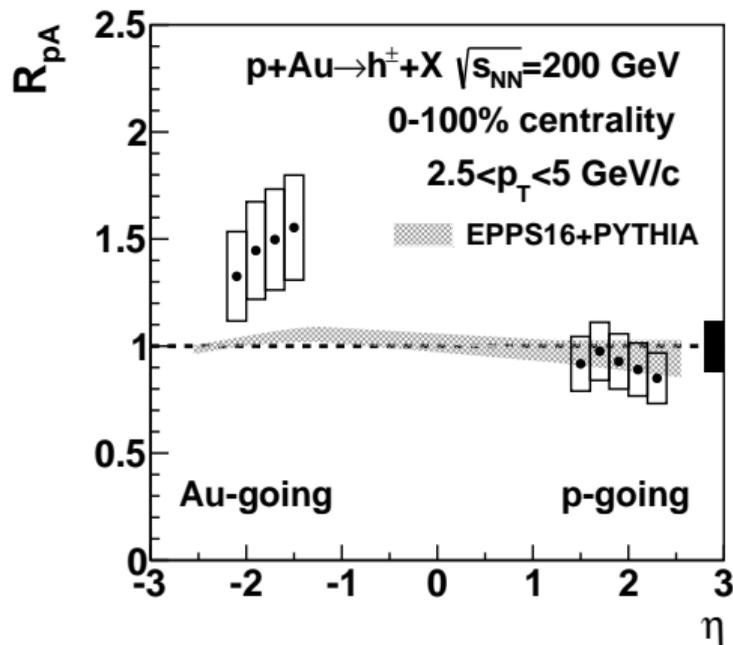
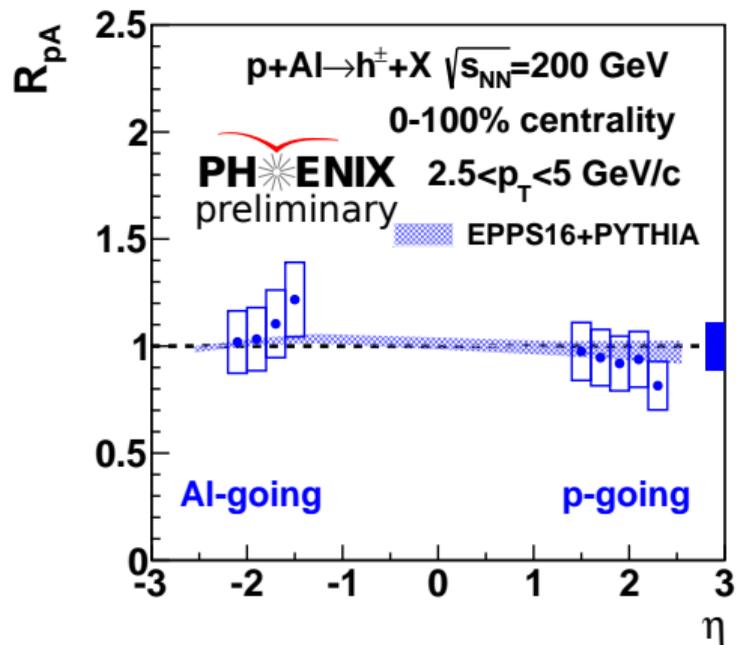
- Observation that correlations are geometrical in origin
- Data well-reproduced by hydro
- CGC calculations somewhat describe the data

## Small systems energy scan

- Similar correlations for all energies
- Non-trivial fluctuations

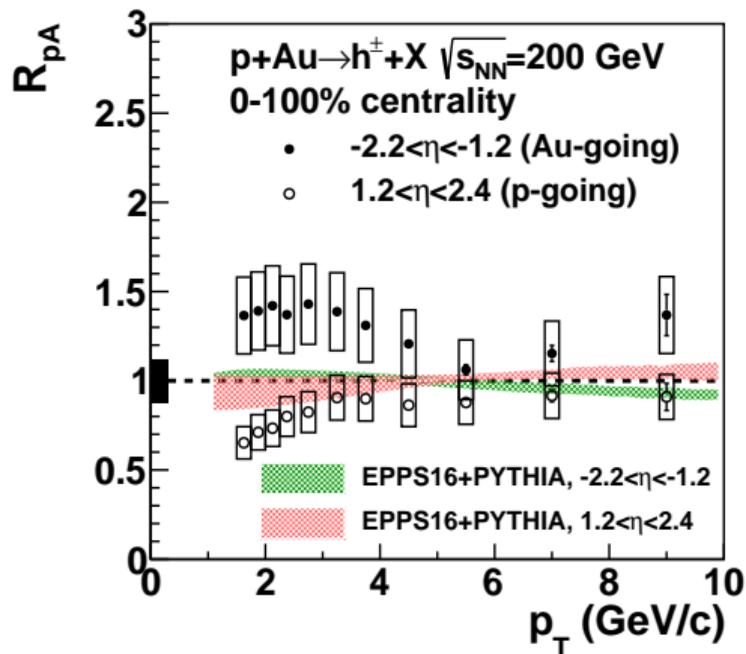
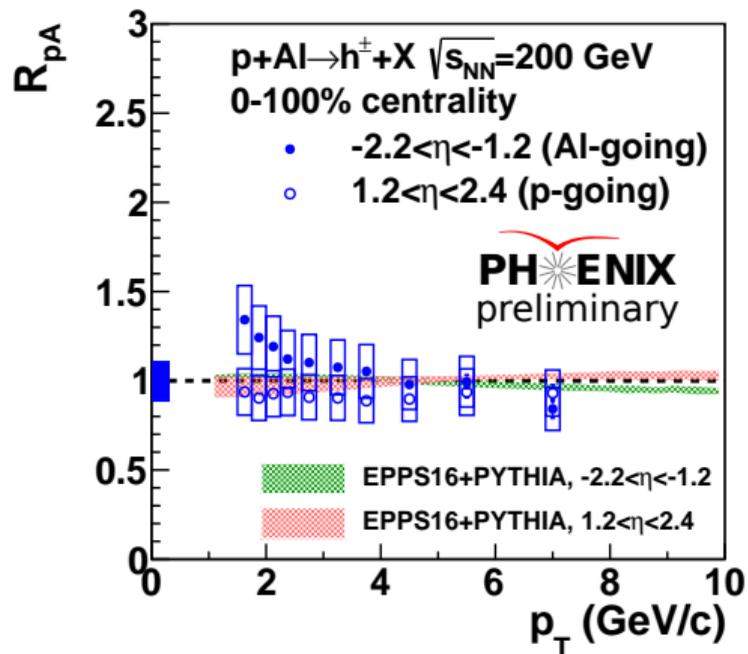
Particle production in small systems

# Small systems nuclear modification



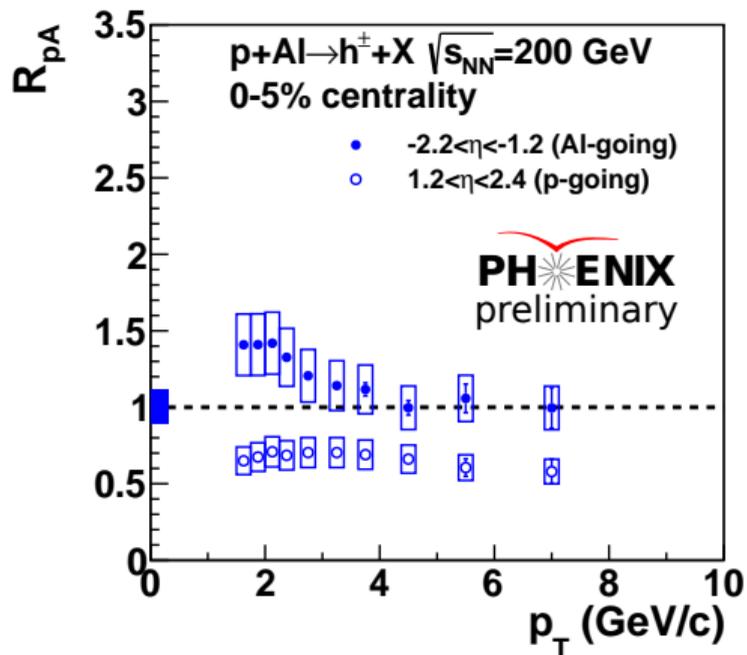
Forward modification consistent with nPDF effects (EPPS16)

# Small systems nuclear modification

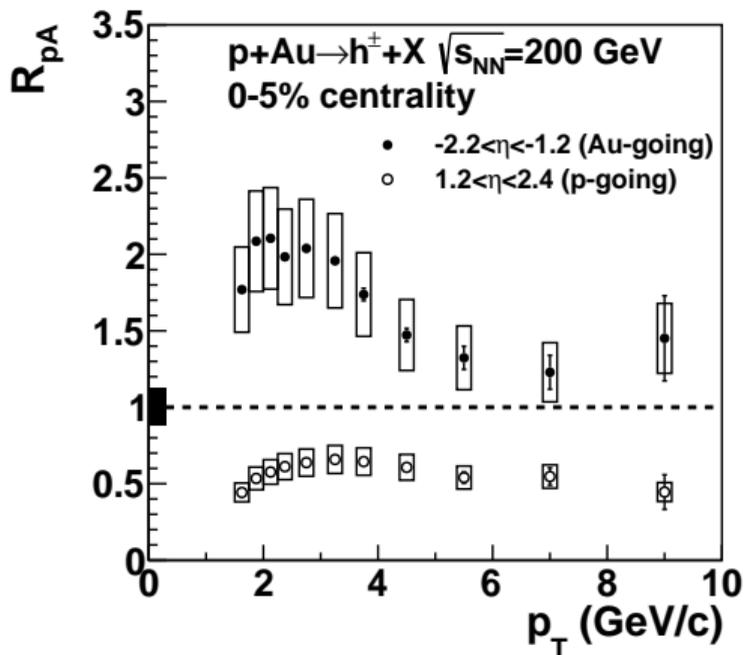


High- $p_T$  modification consistent with nPDF effects (EPPS16)

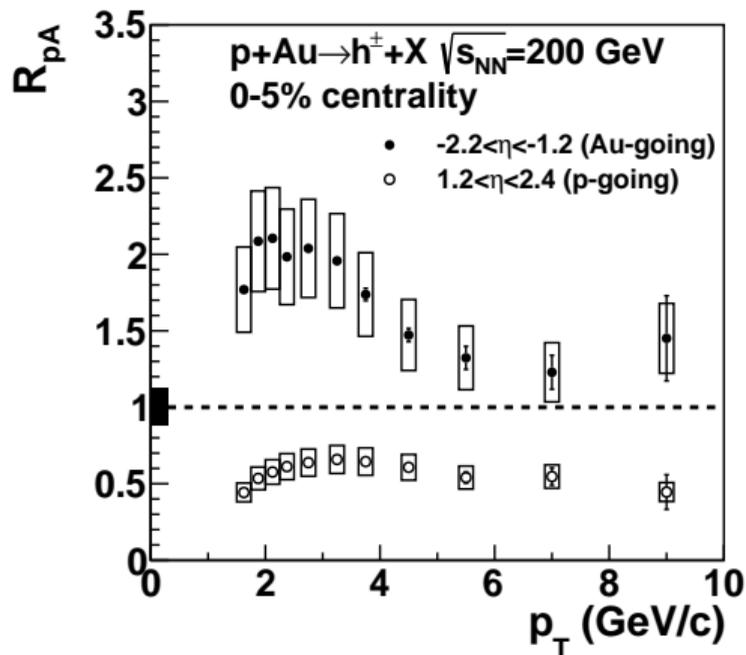
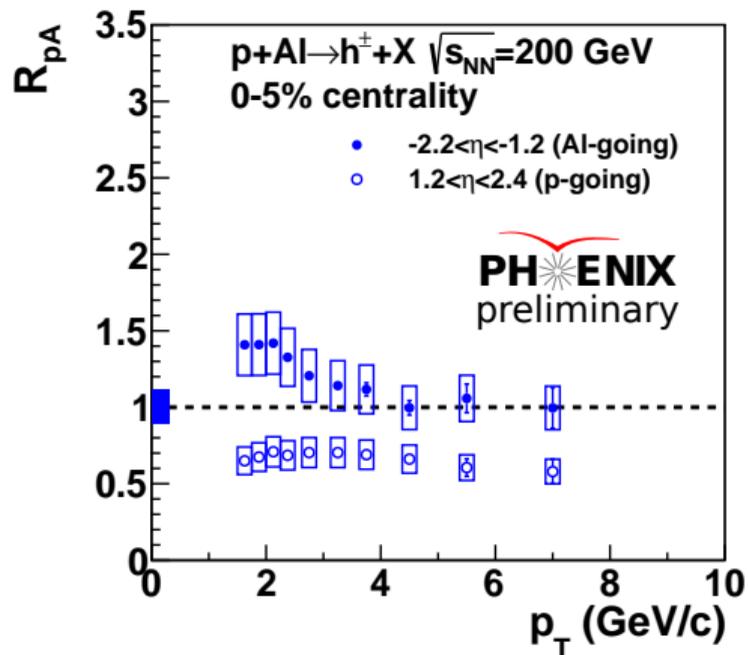
# Small systems nuclear modification



Stronger effects in central collisions

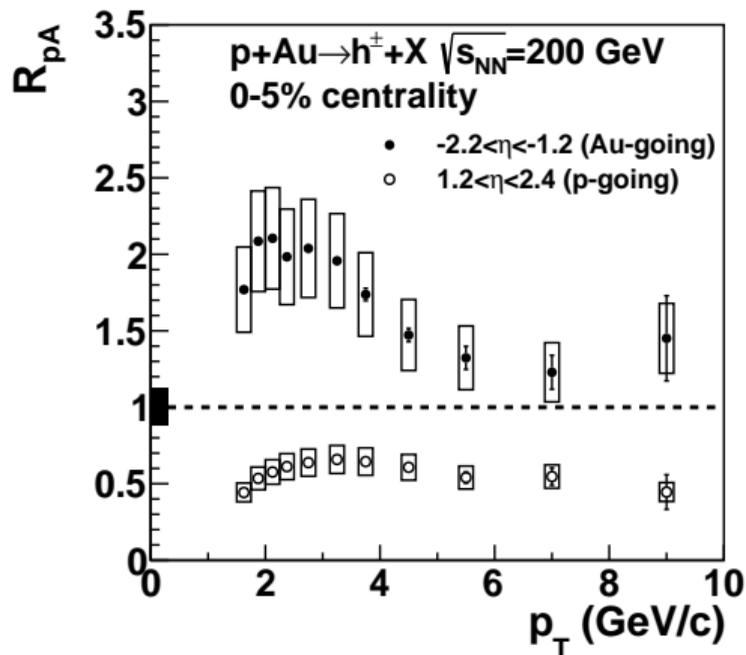
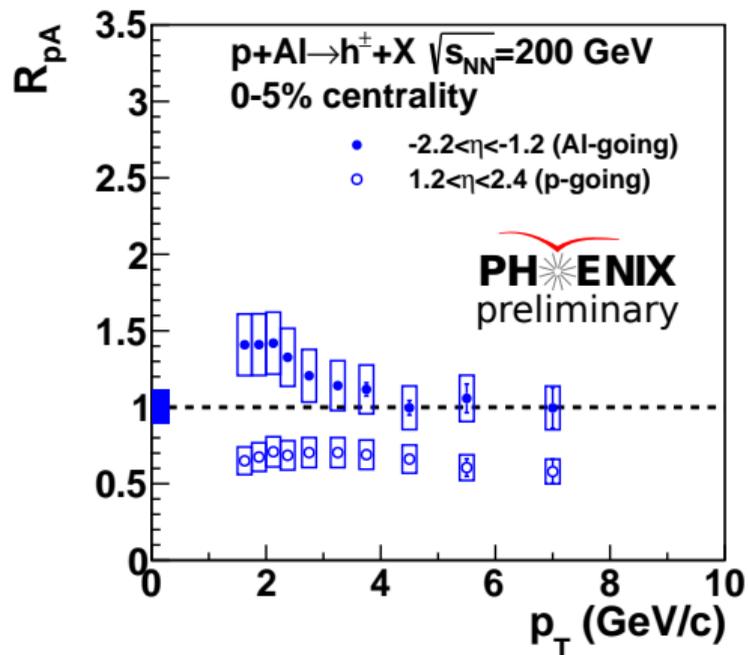


# Small systems nuclear modification



Strong enhancement for backward at intermediate  $p_T$ —why?

# Small systems nuclear modification

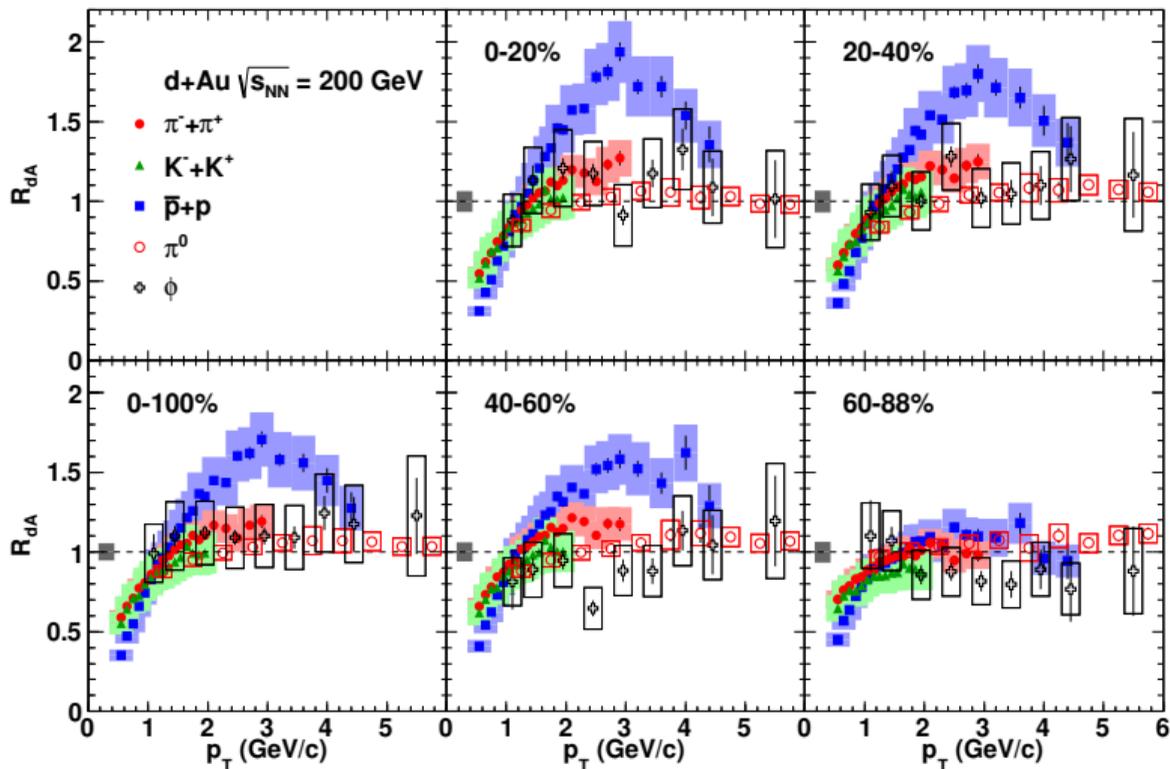


Strong enhancement for backward at intermediate  $p_T$ —why?

Don't forget: particle species dependence of Cronin! There must be final state effect(s)...

# Particle species dependence of “Cronin enhancement”

PHENIX, Phys. Rev. C 88, 024906 (2013)



$\pi^+$ ,  $\pi^-$ ,  $\pi^0$ ,

$K^+$ ,  $K^-$ ,

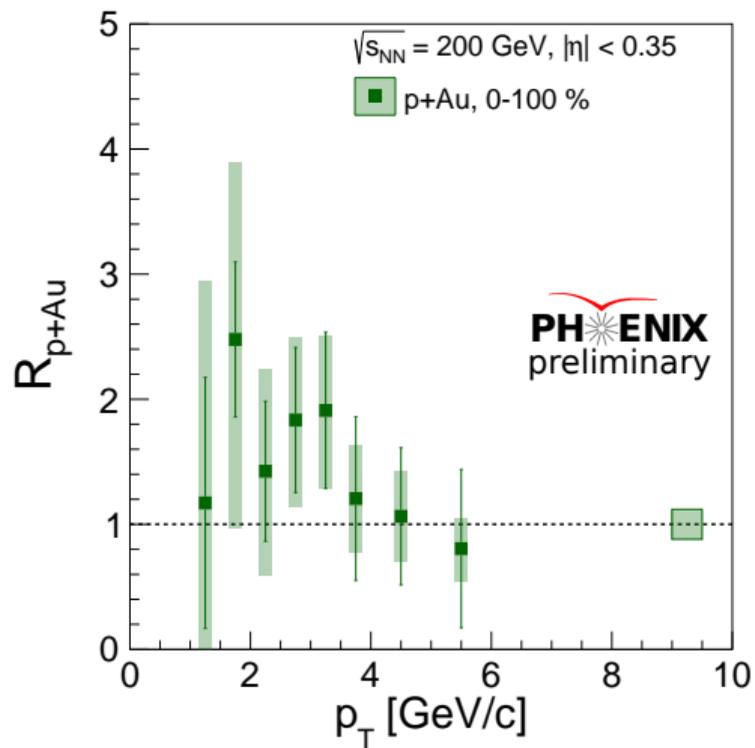
$p$ ,  $\bar{p}$ ,

$\phi$

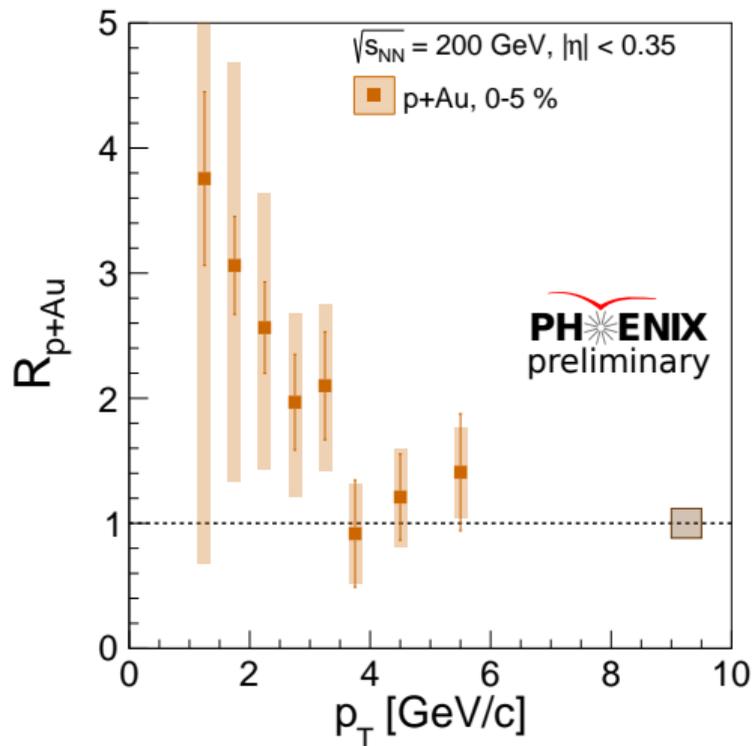
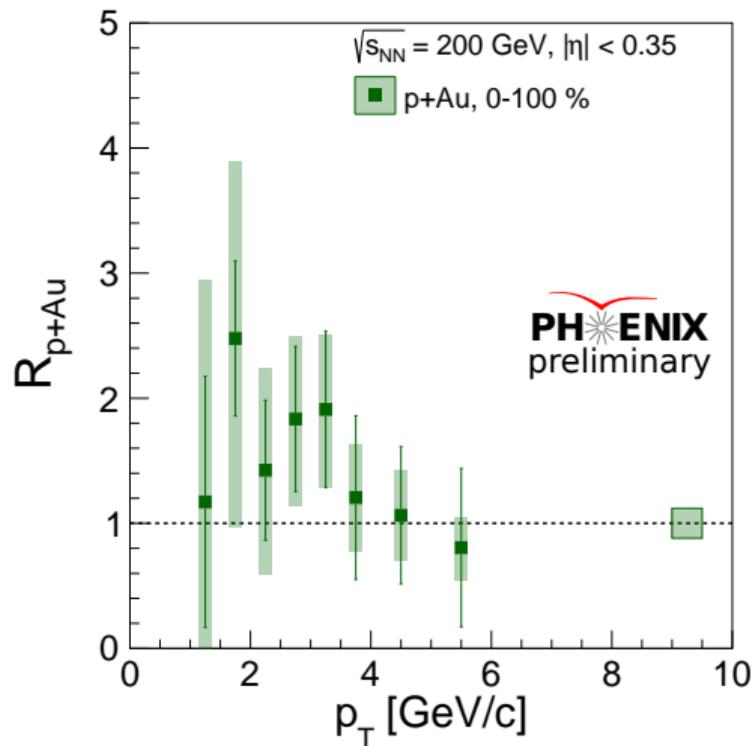
Protons much more strongly  
modified than pions

$\phi$  mesons confusing as always...

# Photons in small systems

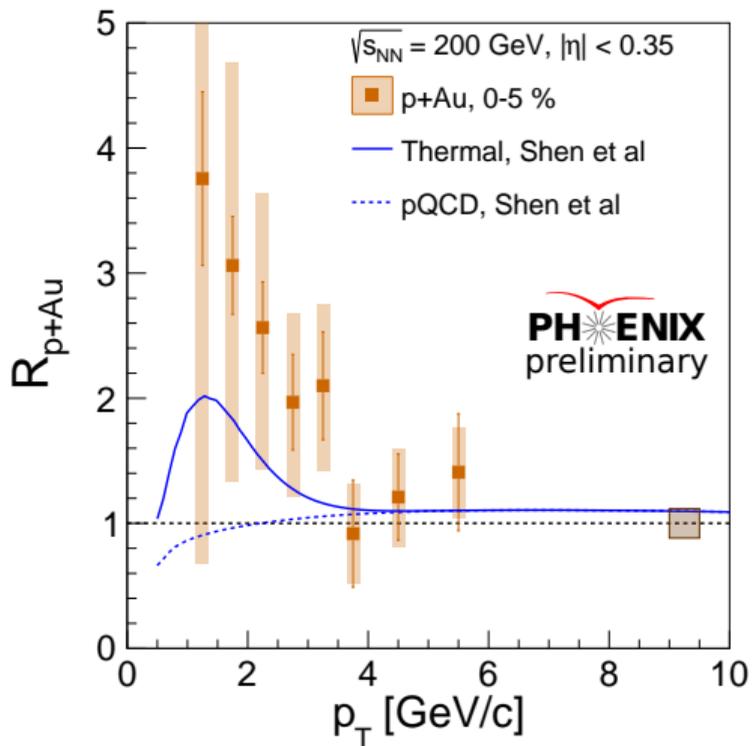
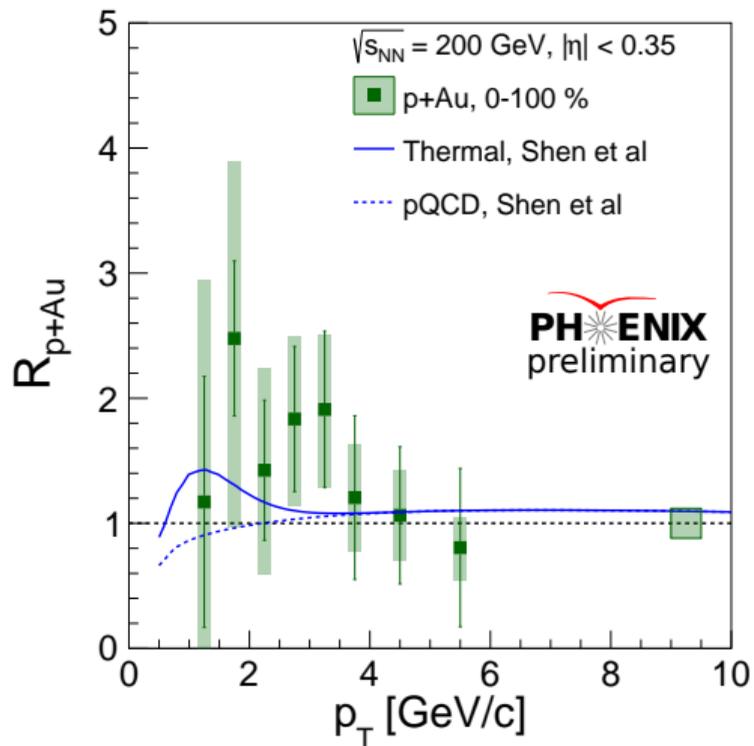


# Photons in small systems



Thermal photons in  $p+Au$ ?

# Photons in small systems



Thermal photons in  $p+Au$ ? Theory from Phys. Rev. C 95, 014906 (2017)

# Brief summary: particle production in small systems

Strong modifications at forward & backward rapidities

- Not nPDF effects alone
- Additional initial state effects possible (e.g. the usual multiple scattering)

Nuclear modification strongly dependent on particle species

- Must be final state effect(s)
- Hadronization, radial flow, etc...

Observation of low- $p_T$  enhancement of photons

- Consistent with QGP formation in small systems
- Other explanations possible

Small systems geometry scan

# Testing hydro by controlling system geometry

arXiv:1805.02973, submitted to Nature Physics

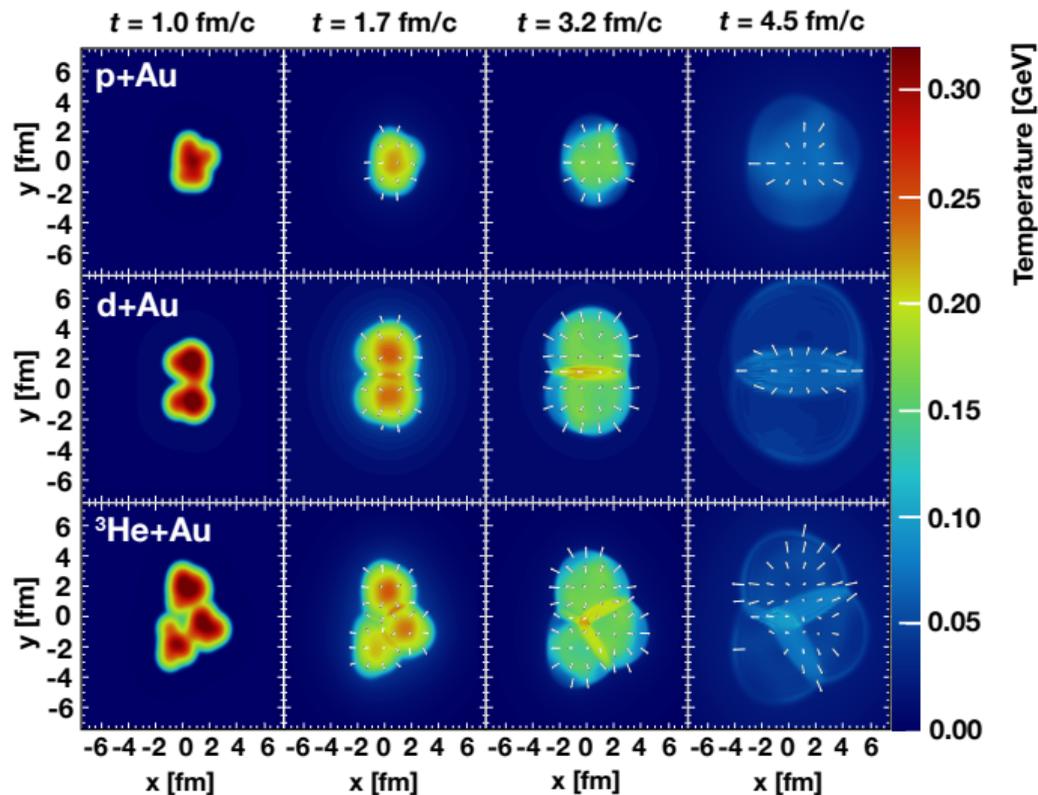
Hydrodynamics translates  
initial geometry into final  
state

Test hydro hypothesis by  
varying initial state

	$\epsilon_2$	$\epsilon_3$
$p+Au$	0.24	0.16
$d+Au$	0.57	0.17
${}^3He+Au$	0.48	0.23

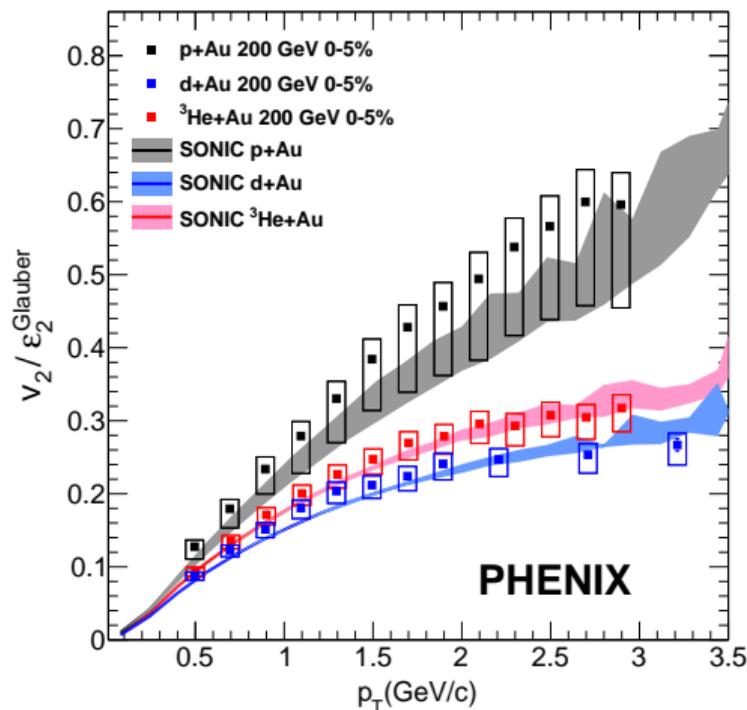
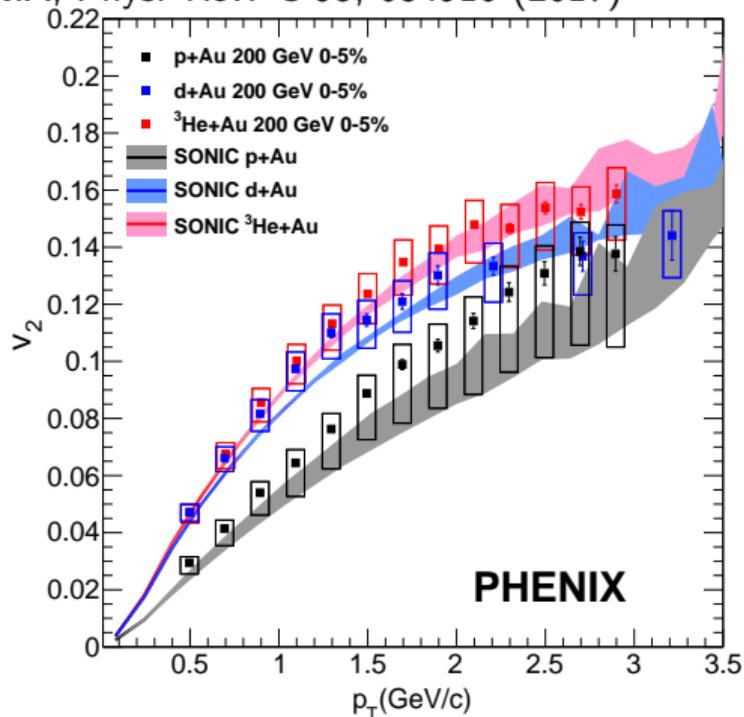
$$\epsilon_2^{p+Au} < \epsilon_2^{d+Au} \approx \epsilon_2^{{}^3He+Au}$$

$$\epsilon_3^{p+Au} \approx \epsilon_3^{d+Au} < \epsilon_3^{{}^3He+Au}$$



# Small systems geometry scan

PHENIX, Phys. Rev. C 95, 034910 (2017)

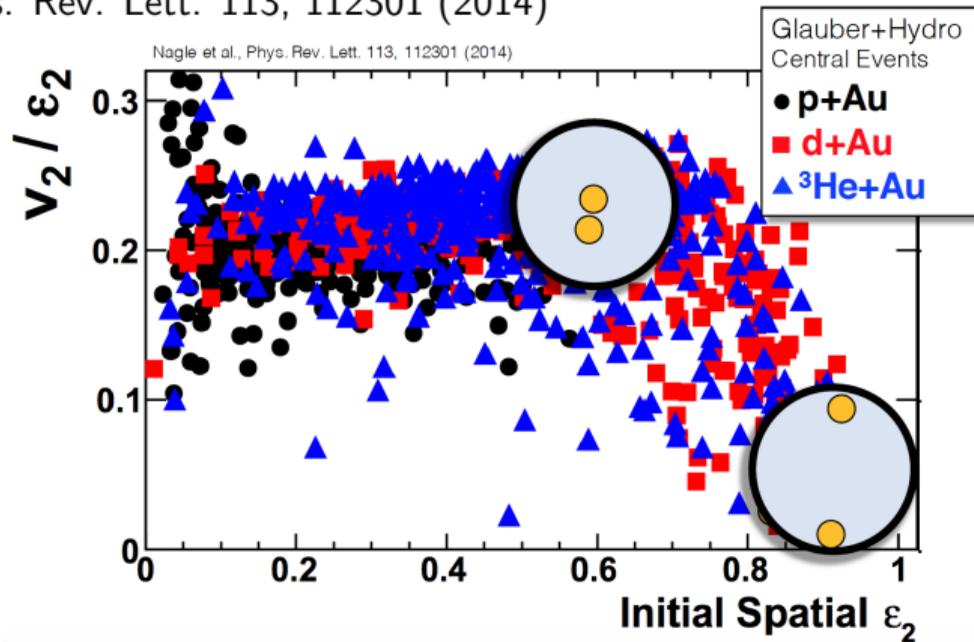


Hydro theory describes the data extremely well

Imperfect scaling with  $\epsilon_2$  captured by hydro—disconnected hot spots

# Small systems geometry scan

J.L. Nagle et al, Phys. Rev. Lett. 113, 112301 (2014)

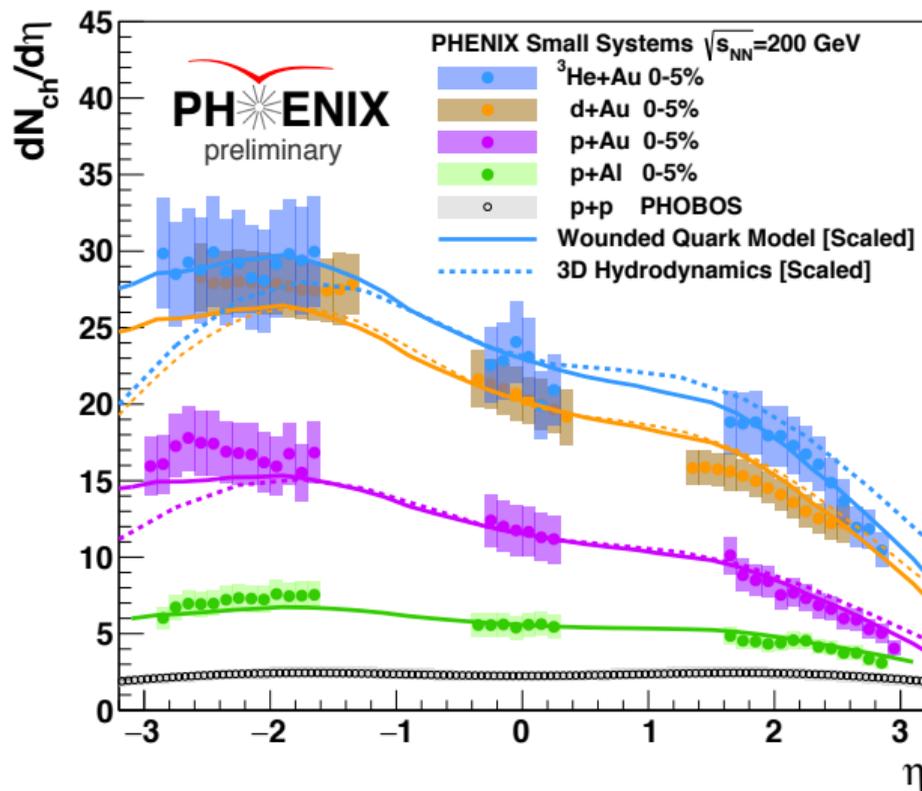


$v_2/\epsilon_2$  relationship breaks for very large  $\epsilon_2$

The hydro hotspots are so far apart that they never connect

—Efficiency to translate  $\epsilon_2$  into  $v_2$  goes down

# Longitudinal dynamics in small systems

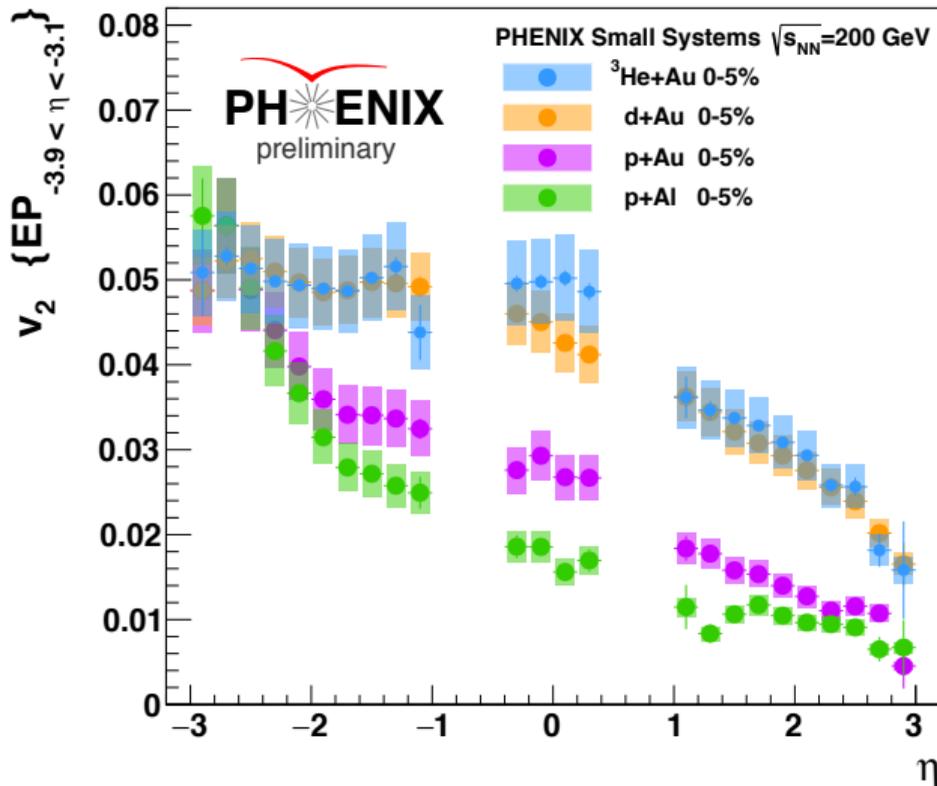


$p+\text{Al}$ ,  $p+\text{Au}$ ,  $d+\text{Au}$ ,  $^3\text{He}+\text{Au}$

Good agreement with wounded quark model

Good agreement with 3D hydro

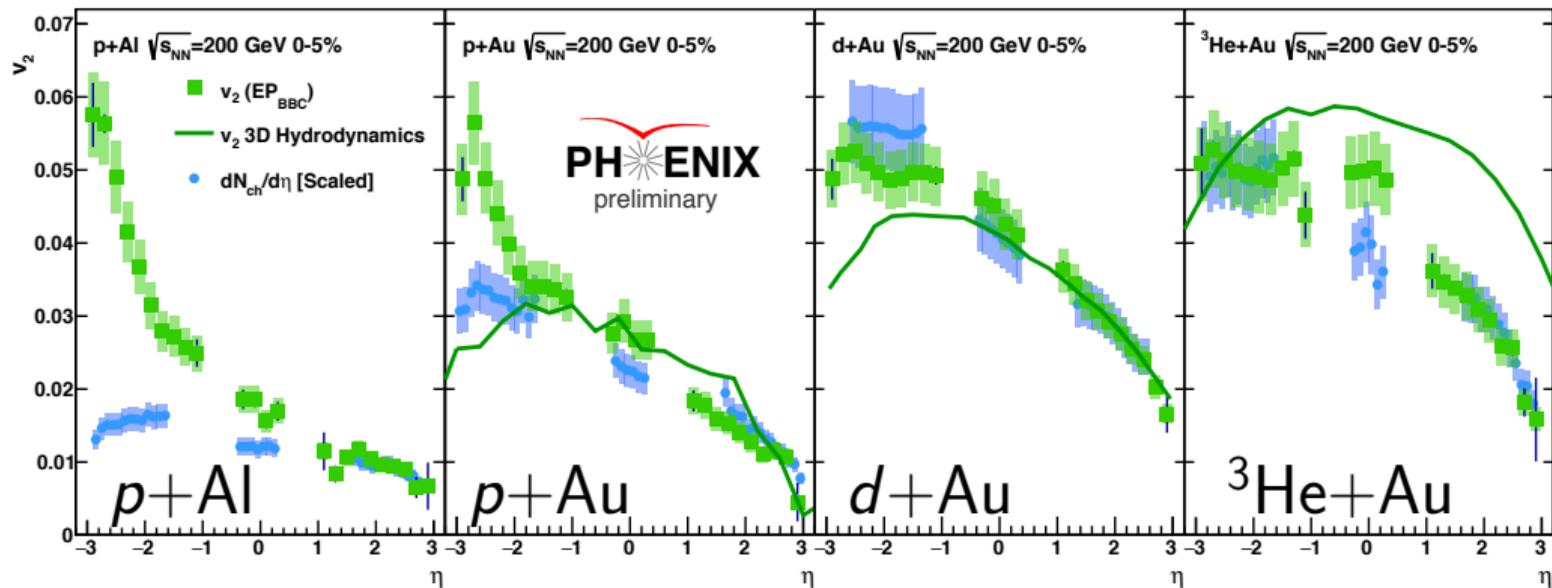
# Longitudinal dynamics in small systems



$p+\text{Al}$ ,  $p+\text{Au}$ ,  $d+\text{Au}$ ,  $^3\text{He}+\text{Au}$

Also have  $v_2$  vs  $\eta$

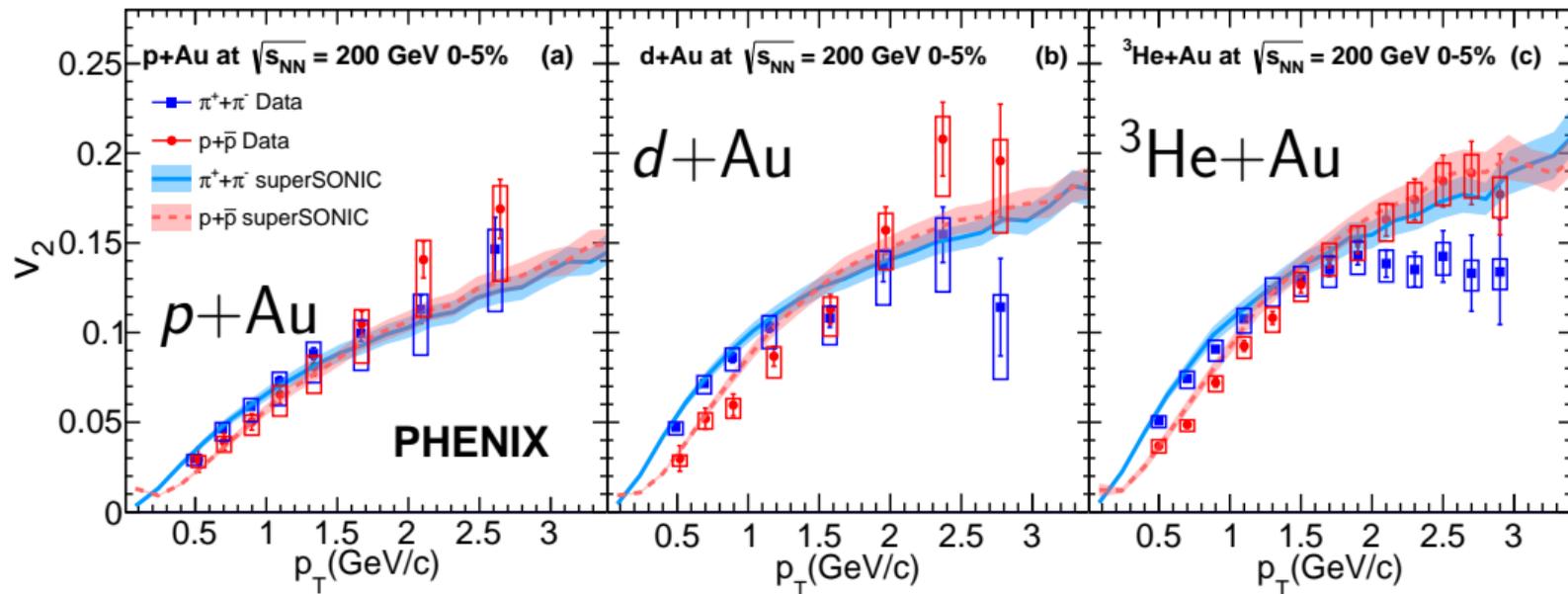
# Longitudinal dynamics in small systems



Good agreement with 3D hydro for  $p+Au$  and  $d+Au$   
Apparent scaling between  $v_2$  and  $dN_{ch}/d\eta$ —coincidence?

# Small systems geometry scan

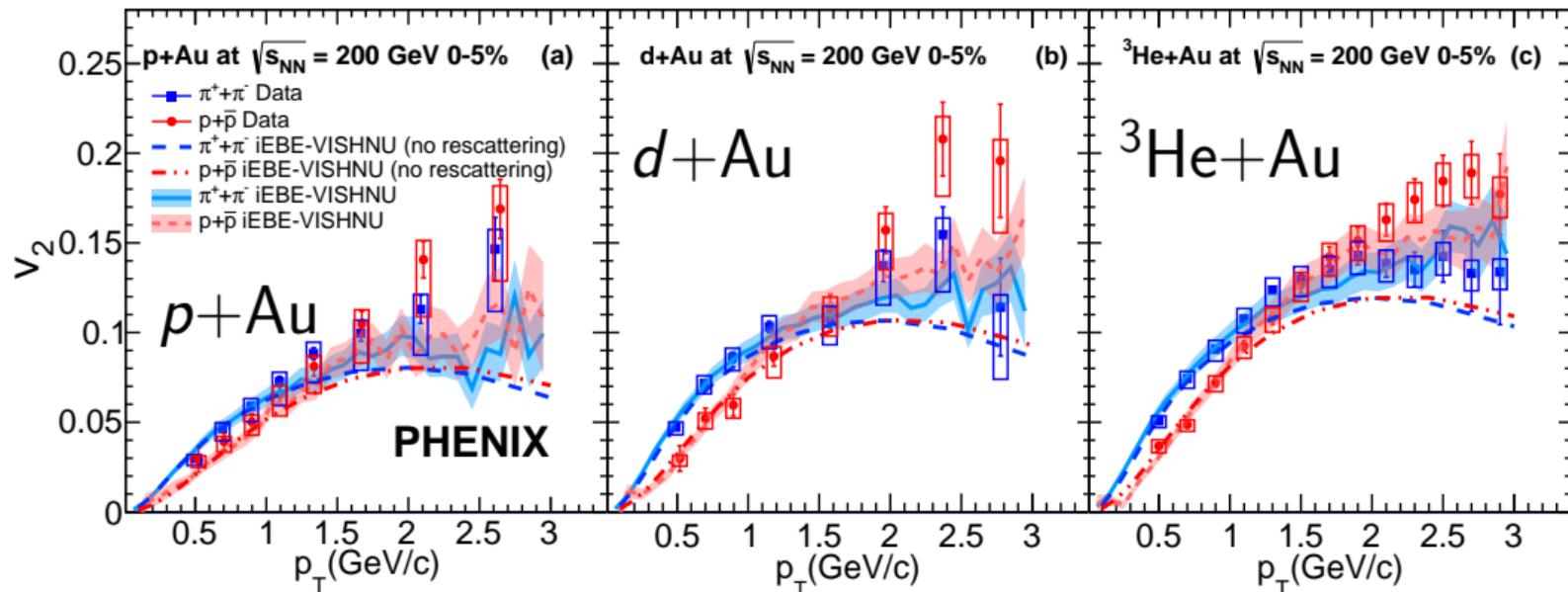
arXiv:1710.09736, accepted by Phys. Rev. C



Identified particle  $v_2$  vs  $p_T$  in  $p+Au$ ,  $d+Au$ , and  $^3He+Au$   
—Mass ordering well-described by hydro

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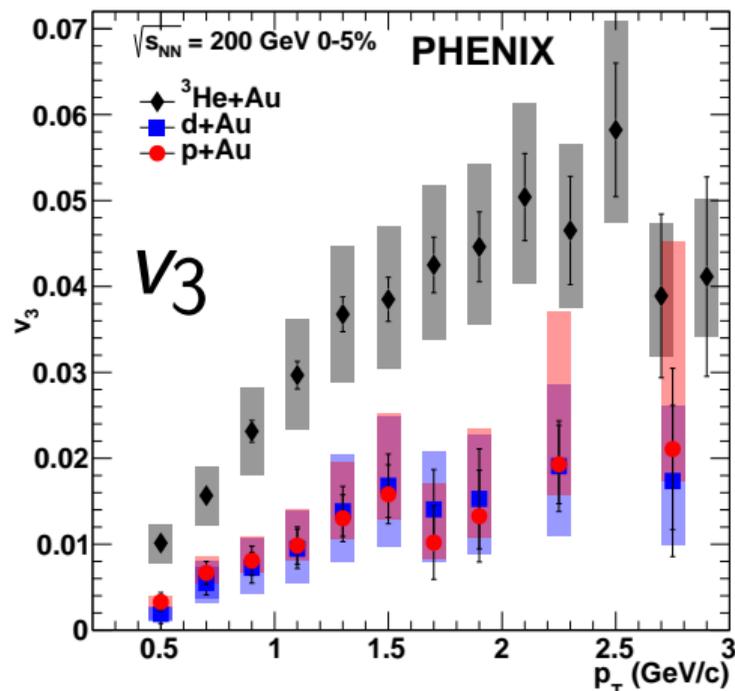
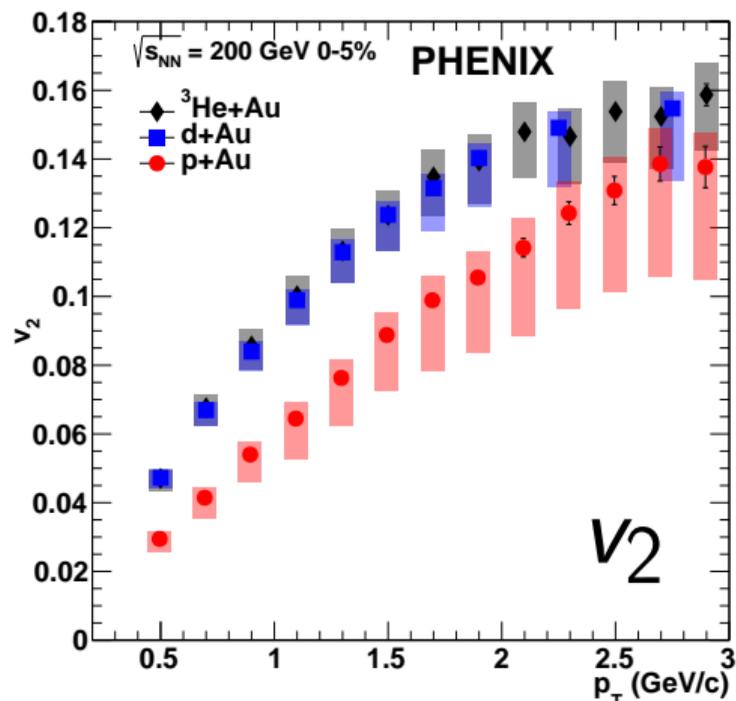
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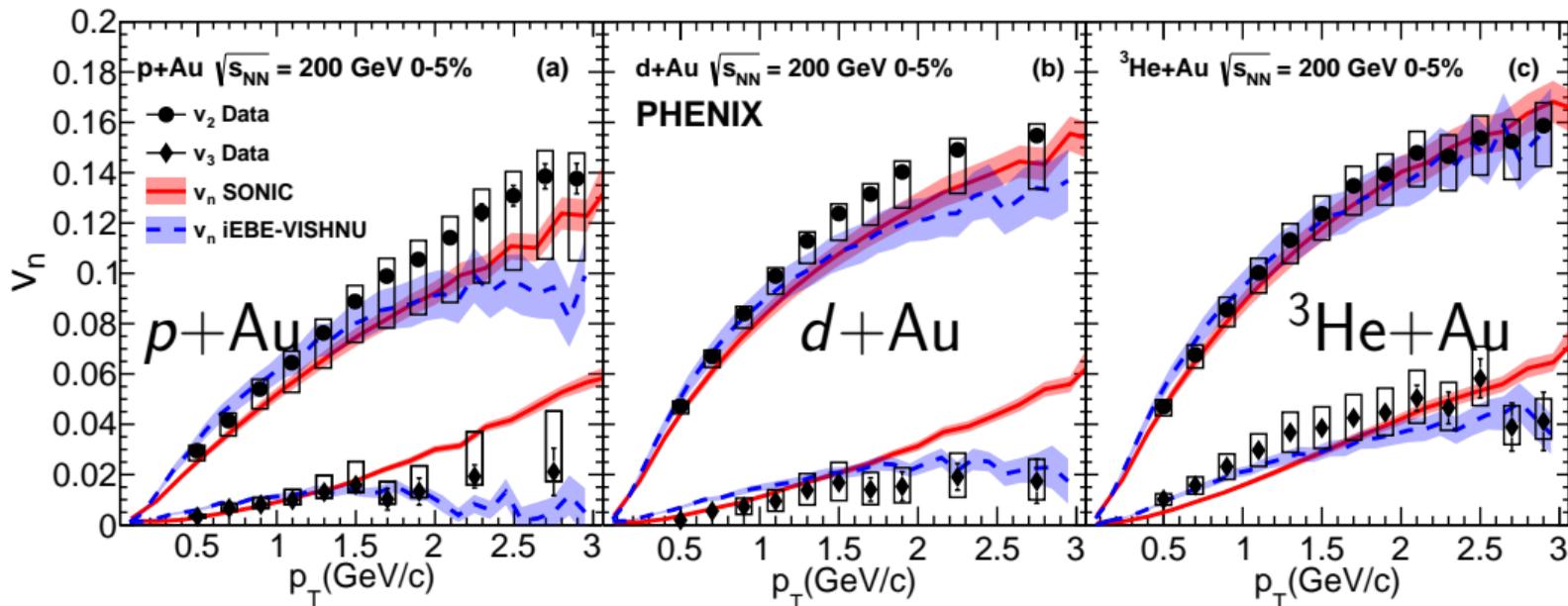
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$v_2$  and  $v_3$  ordering matches  $\varepsilon_2$  and  $\varepsilon_3$  ordering in all three systems  
—Regardless of mechanism, the correlation is geometrical

# Testing hydro by controlling system geometry

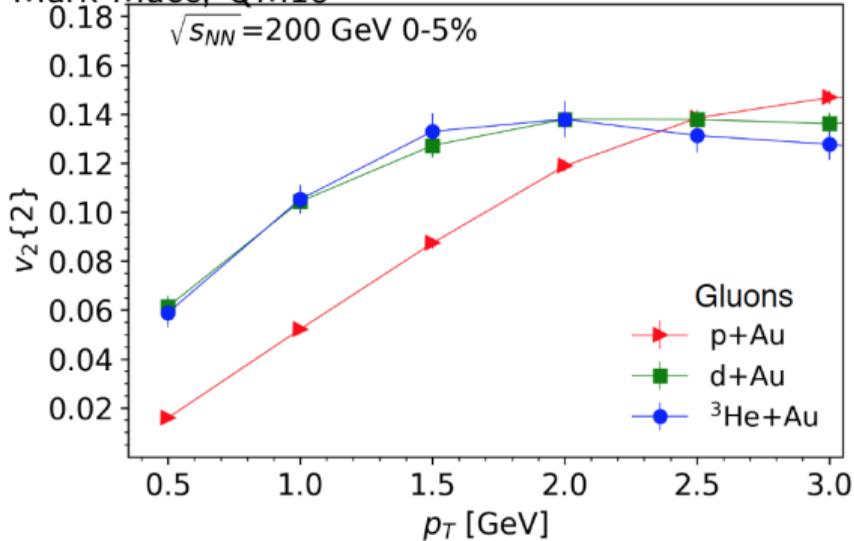
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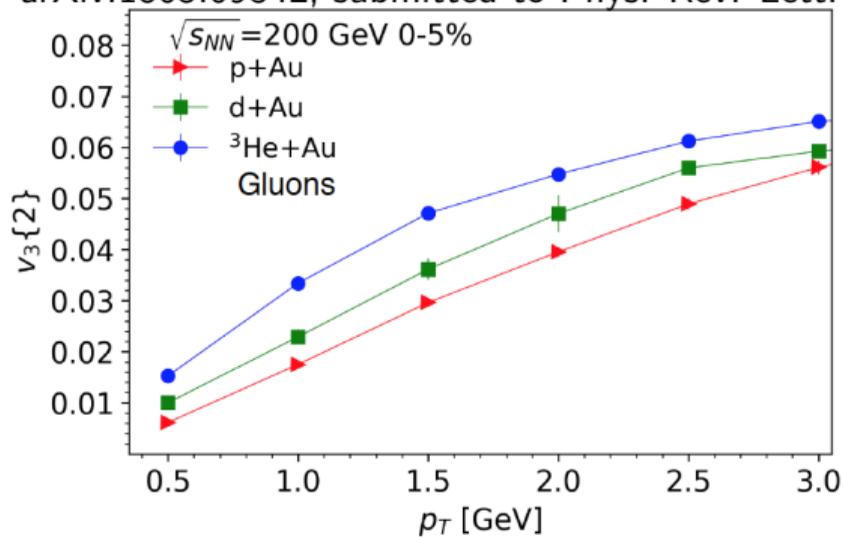
$v_2$  and  $v_3$  vs  $p_T$  described very well by hydro in all three systems  
—Strongly suggests QGP droplets in hydro evolution

# CGC results on small systems

Mark Mace, QM18



arXiv:1805.09342, submitted to Phys. Rev. Lett.

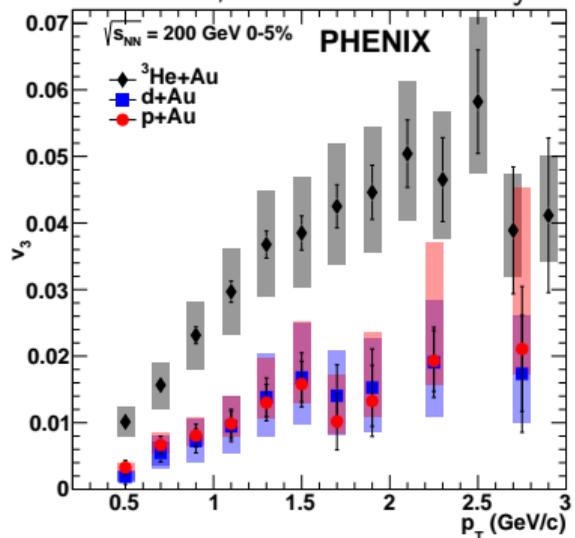
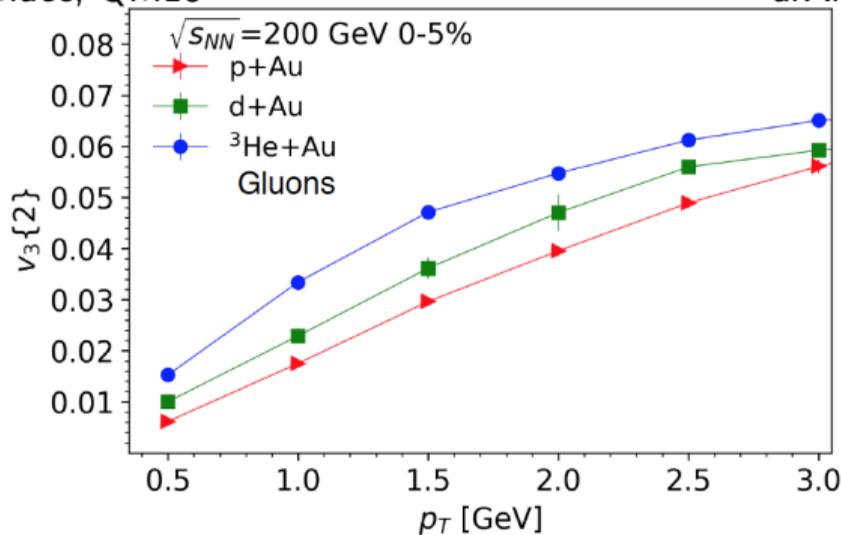


New for QM18: full calculation using dilute-dense framework,  $v_2$  and  $v_3$  for small systems geometry scan

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arXiv:1805.09342, submitted to Phys. Rev. Lett.



New for QM18: full calculation using dilute-dense framework,  $v_2$  and  $v_3$  for small systems geometry scan

$v_3$  ordering is not quite right

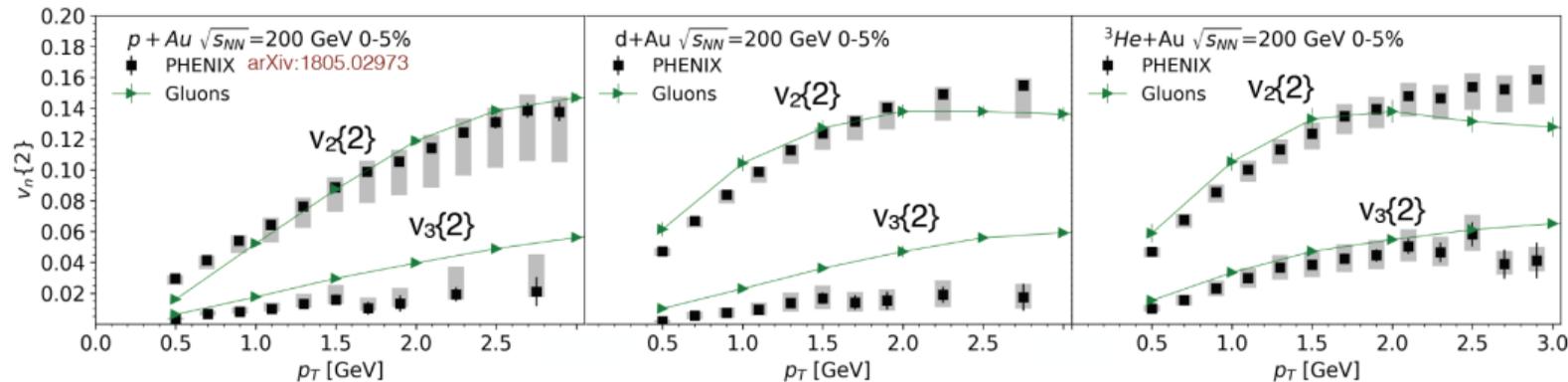
—CGC:  $p+Au < d+Au < {}^3He+Au$

—Data:  $p+Au \approx d+Au < {}^3He+Au$

# CGC results on small systems

Mark Mace, QM18

arXiv:1805.09342, submitted to Phys. Rev. Lett.



$v_2$  is quite close for the three systems

$v_3$  is rather far off

## Brief summary: small systems geometry scan

Comprehensive set of measurements for longitudinal dynamics

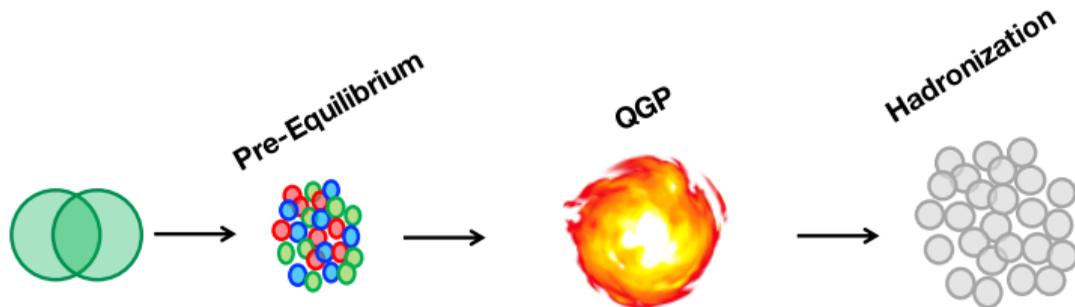
$v_2$  and  $v_3$  match  $\varepsilon_2$  and  $\varepsilon_3$  ordering in  $p+Au$ ,  $d+Au$ ,  $^3\text{He}+Au$   
—Correlation is definitively geometrical in origin

$v_2$  and  $v_3$  in  $p+Au$ ,  $d+Au$ ,  $^3\text{He}+Au$  are well-described by hydro theory  
—Strongest evidence to date for QGP formation in small systems

New CGC calculations show some good agreement with data but also some considerable discrepancies

Small systems beam energy scan

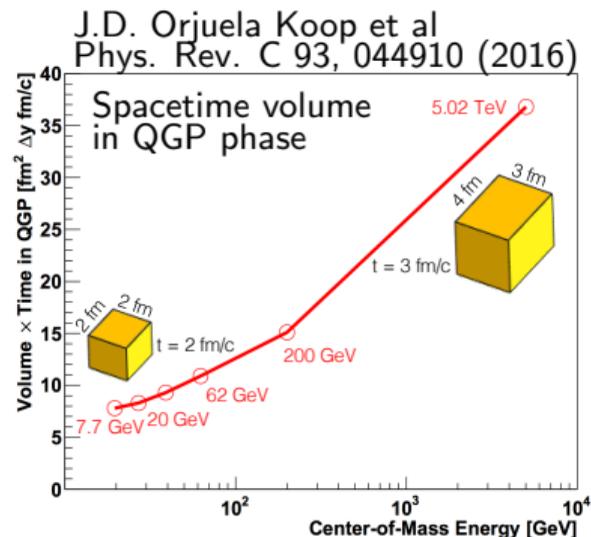
# Testing hydro by controlling system size and life time



Standard picture for A+A:  
QGP in hydro evolution

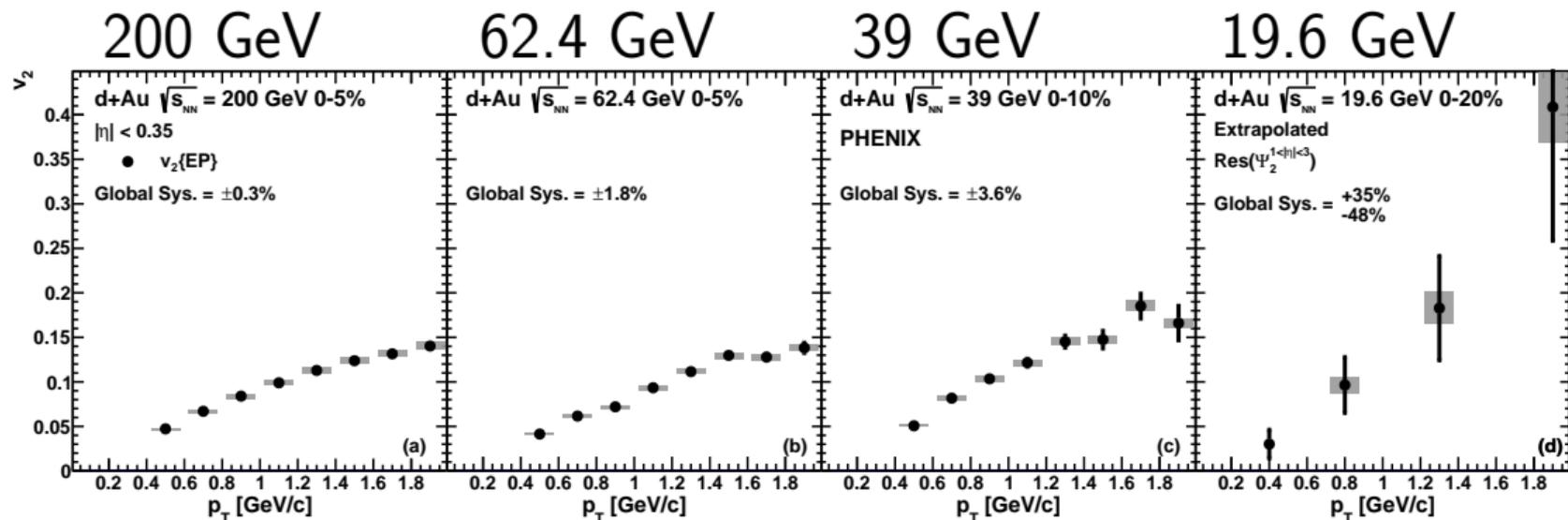
What about small systems?  
And lower energies?

Use collisions species and  
energy to control system  
size, test limits of hydro  
applicability



# $d+Au$ beam energy scan

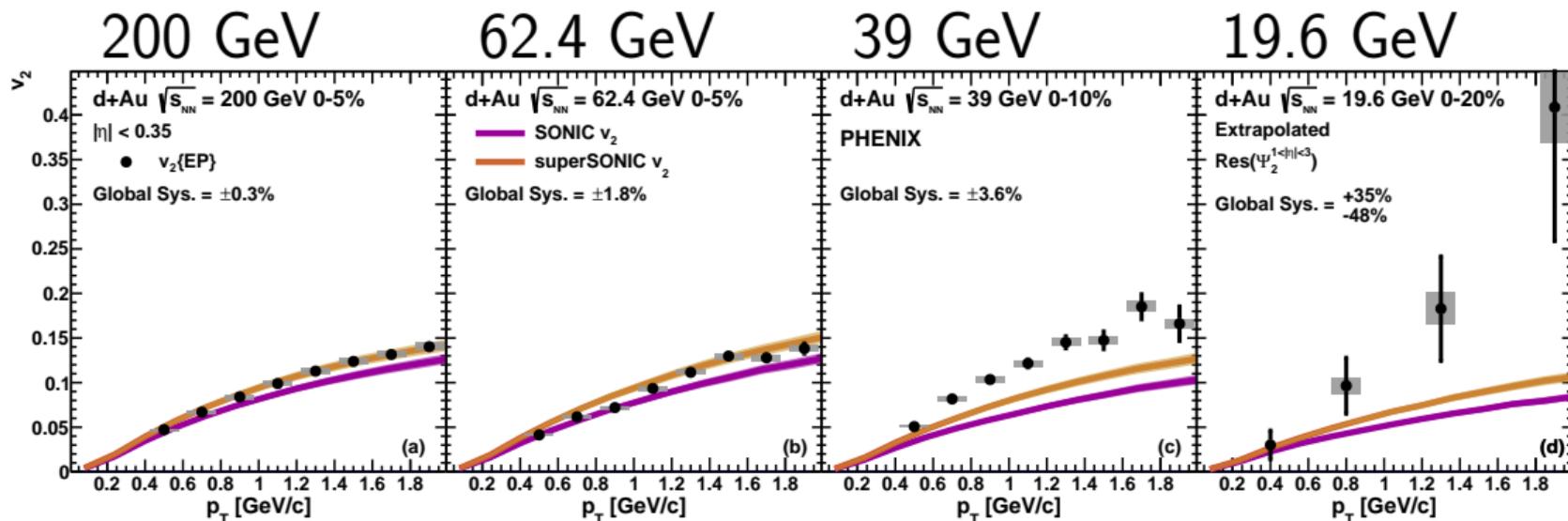
Phys. Rev. C 96, 064905 (2017)



Event plane  $v_2$  vs  $p_T$  measured for all energies

# $d+Au$ beam energy scan

Phys. Rev. C 96, 064905 (2017)

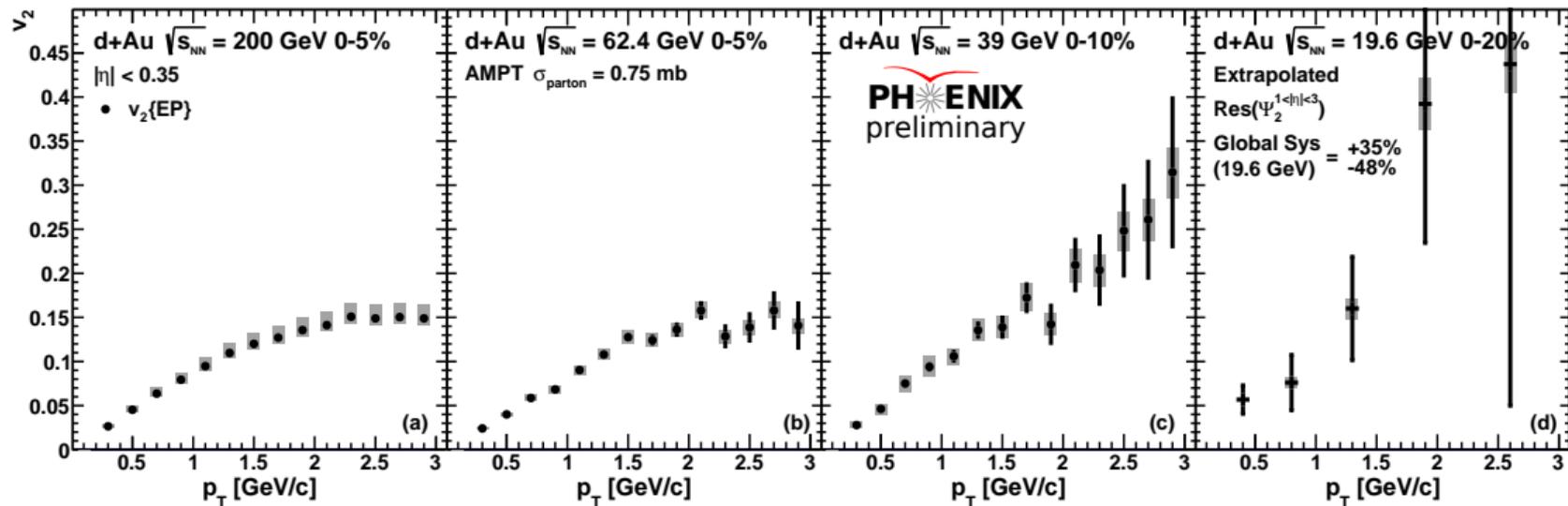


Event plane  $v_2$  vs  $p_T$  measured for all energies

Hydro theory agrees with higher energies very well,  
underpredicts lower energies—nonflow?

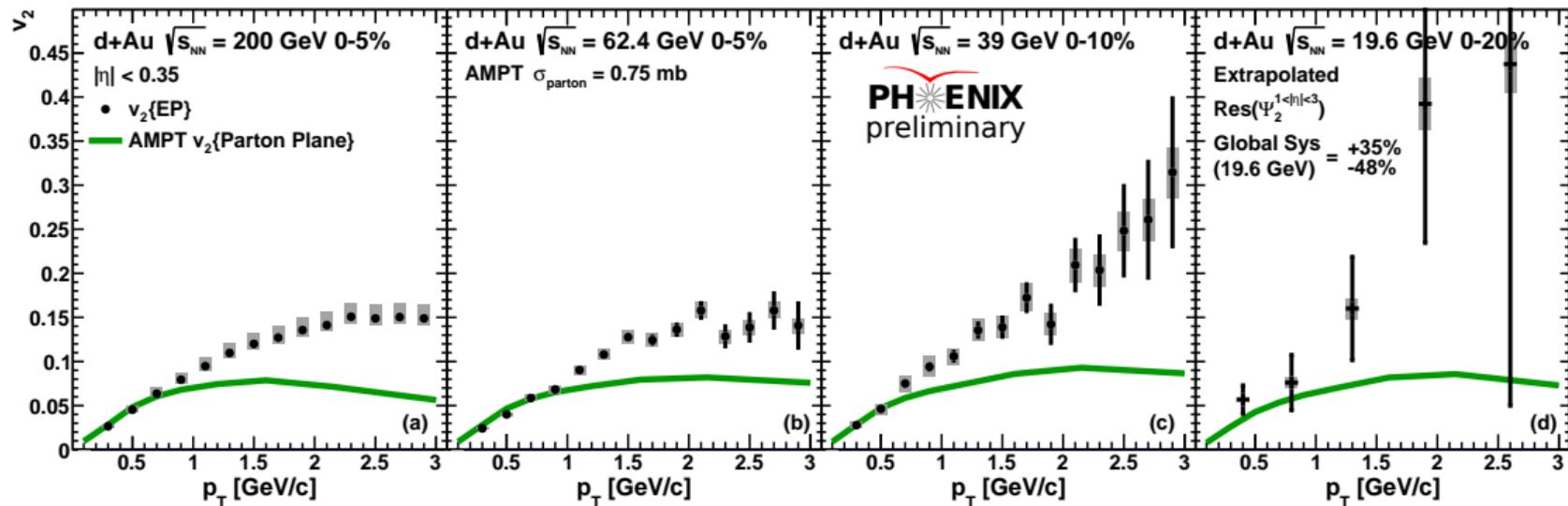
# $v_2$ vs $p_T$ , comparisons to AMPT

Phys. Rev. C 96, 064905 (2017)



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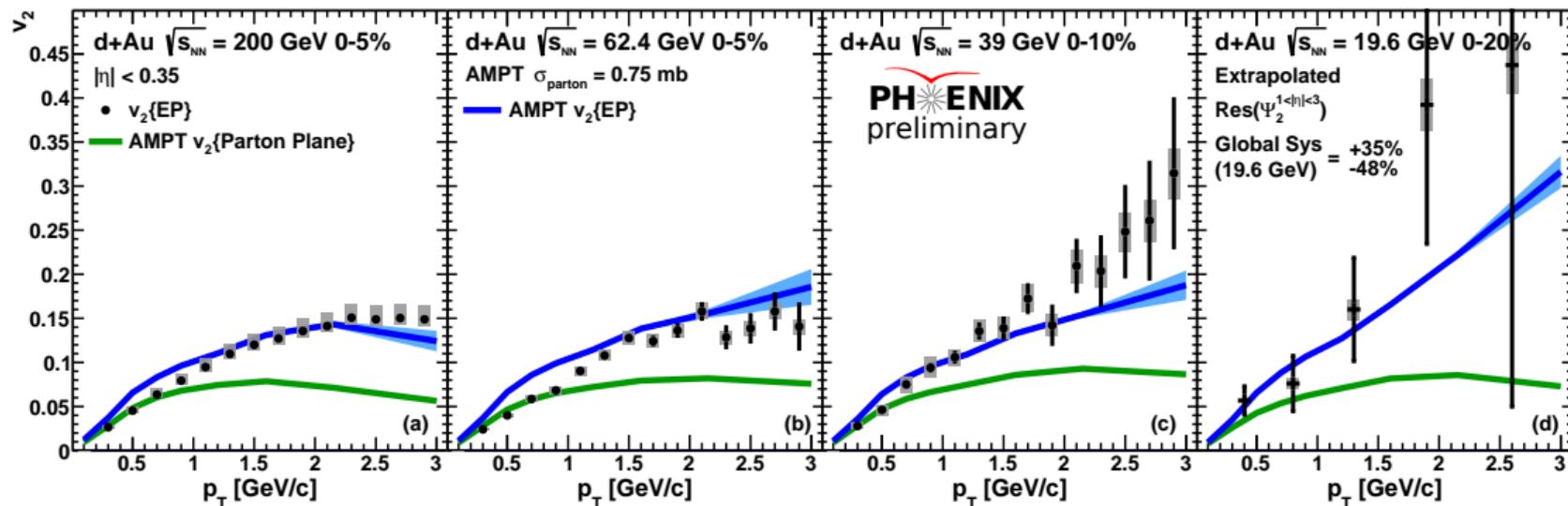
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AMPT flow only shows good agreement at low  $p_T$  and all energies

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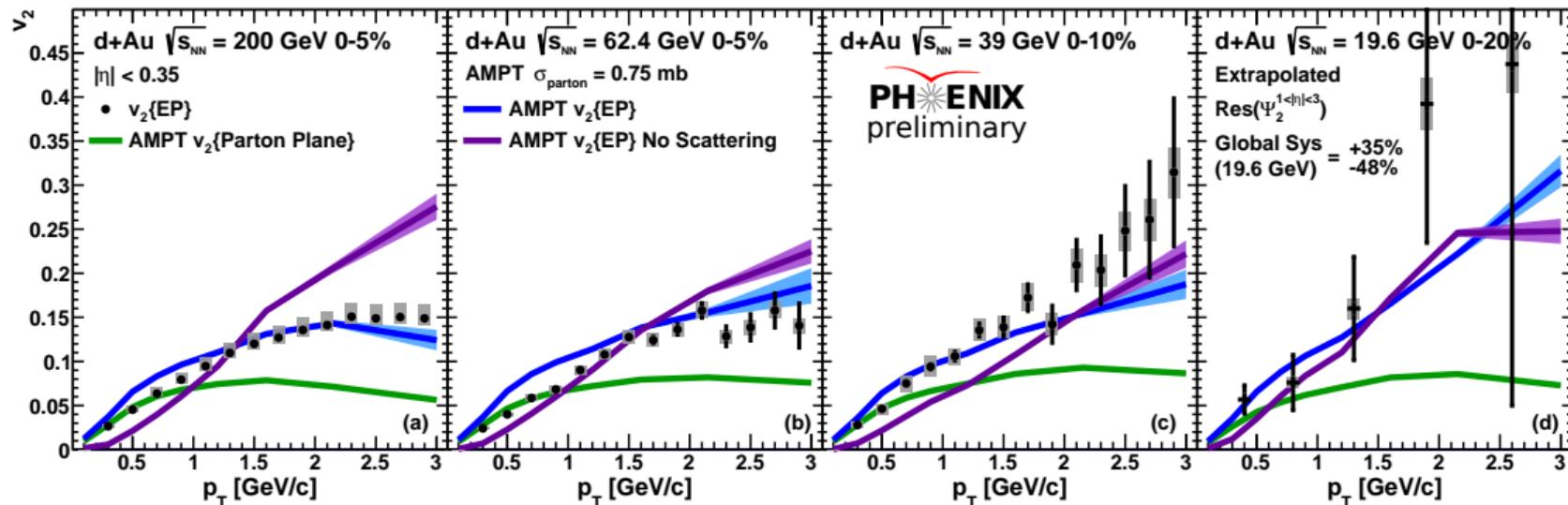


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AMPT flow+non-flow shows reasonable agreement for all  $p_T$  and all energies

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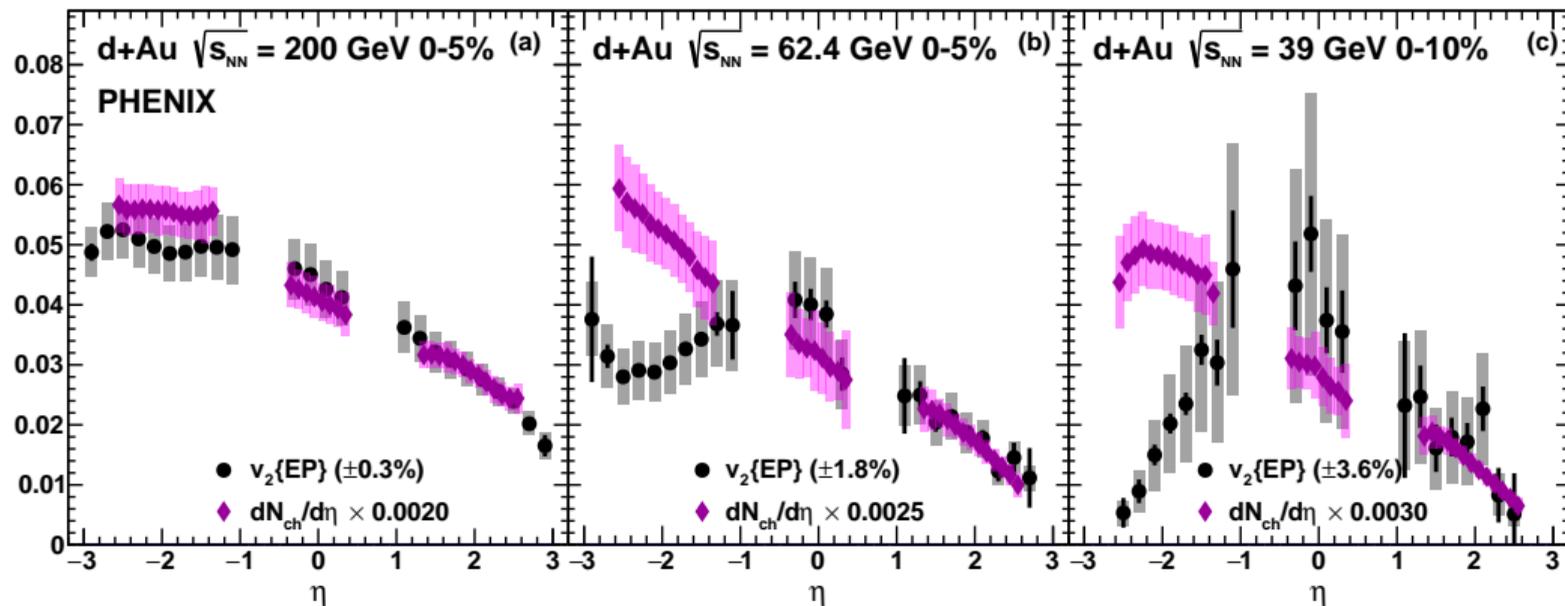
AMPT flow only shows good agreement at low  $p_T$  and all energies

AMPT flow+non-flow shows reasonable agreement for all  $p_T$  and all energies

AMPT non-flow only far under-predicts for low  $p_T$ , too high for high  $p_T$

# $v_2$ and $dN_{ch}/d\eta$ vs $\eta$

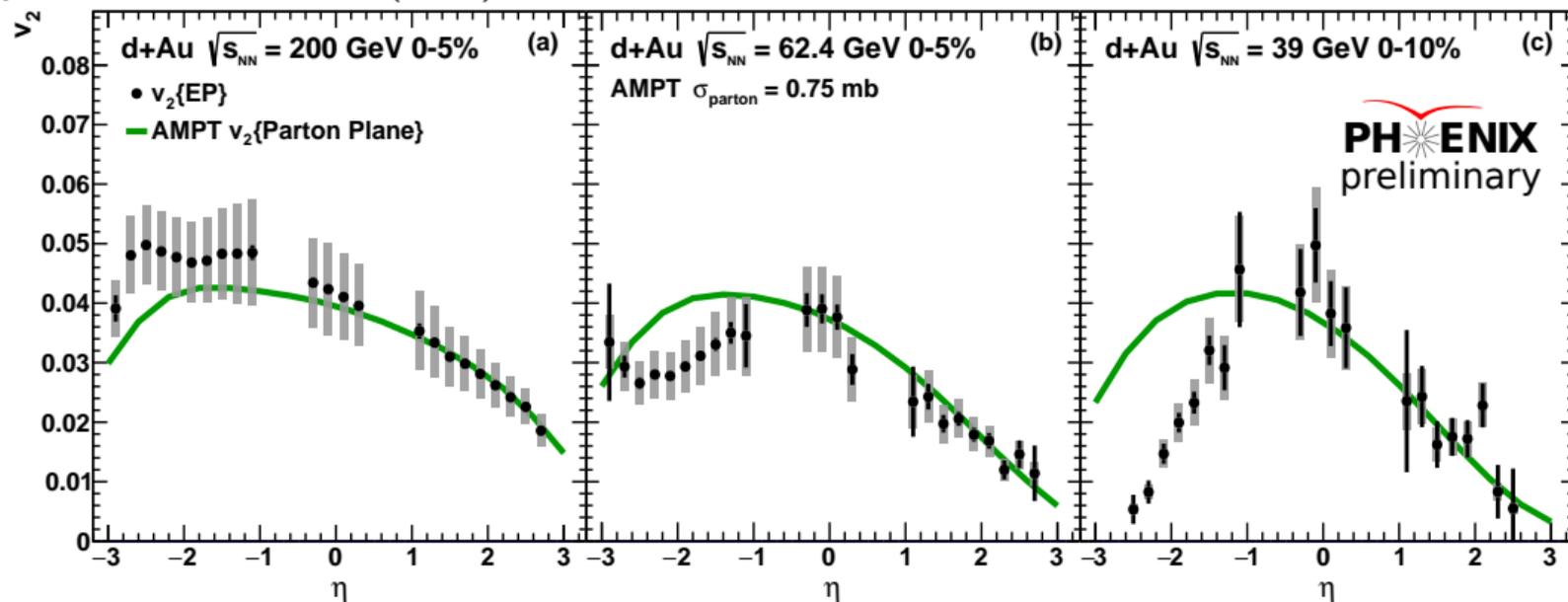
Phys. Rev. C 96, 064905 (2017)



BBC south ( $-3.9 < \eta < -3.1$ ) used to estimate the event plane  
200 GeV shows strong forward/backward asymmetry in  $v_2$  and  $dN_{ch}/d\eta$   
Asymmetry is large for  $dN_{ch}/d\eta$  at all energies, but not for  $v_2$

# $v_2$ vs $\eta$ , comparison with AMPT

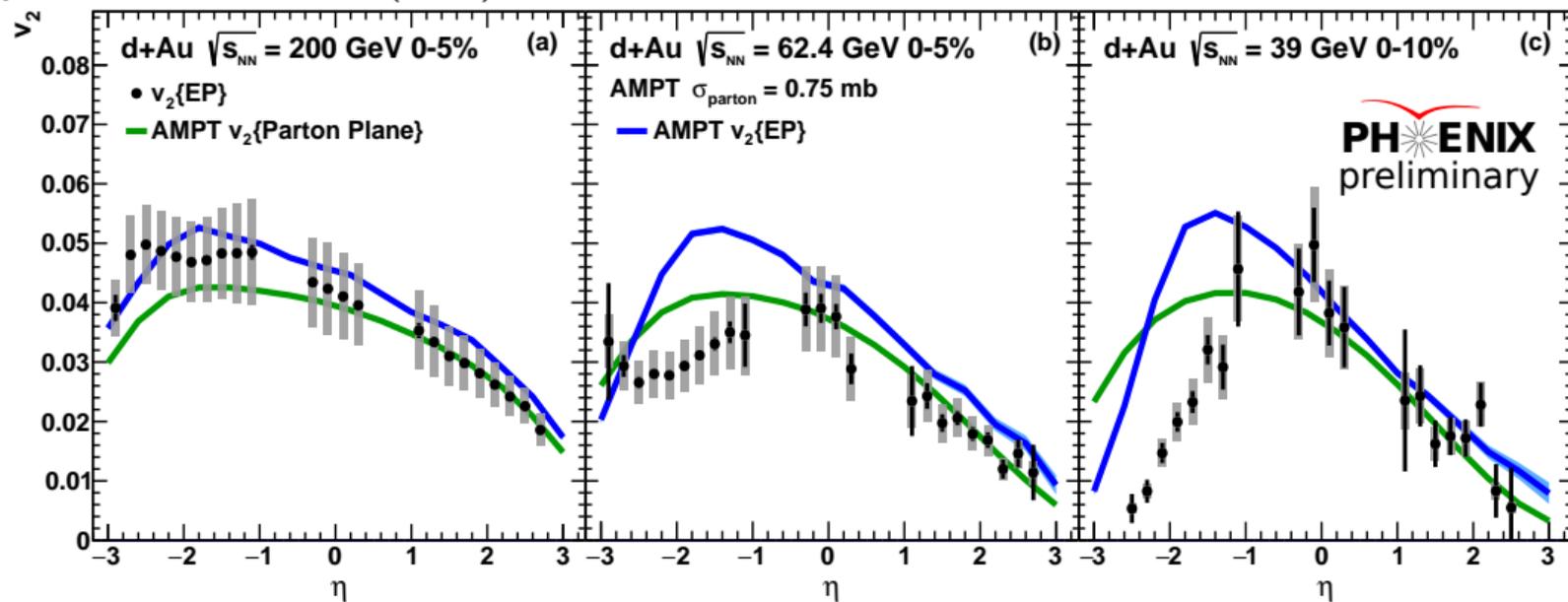
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AMPT flow only agrees with mid and forward rapidity very well, misses backward rapidity

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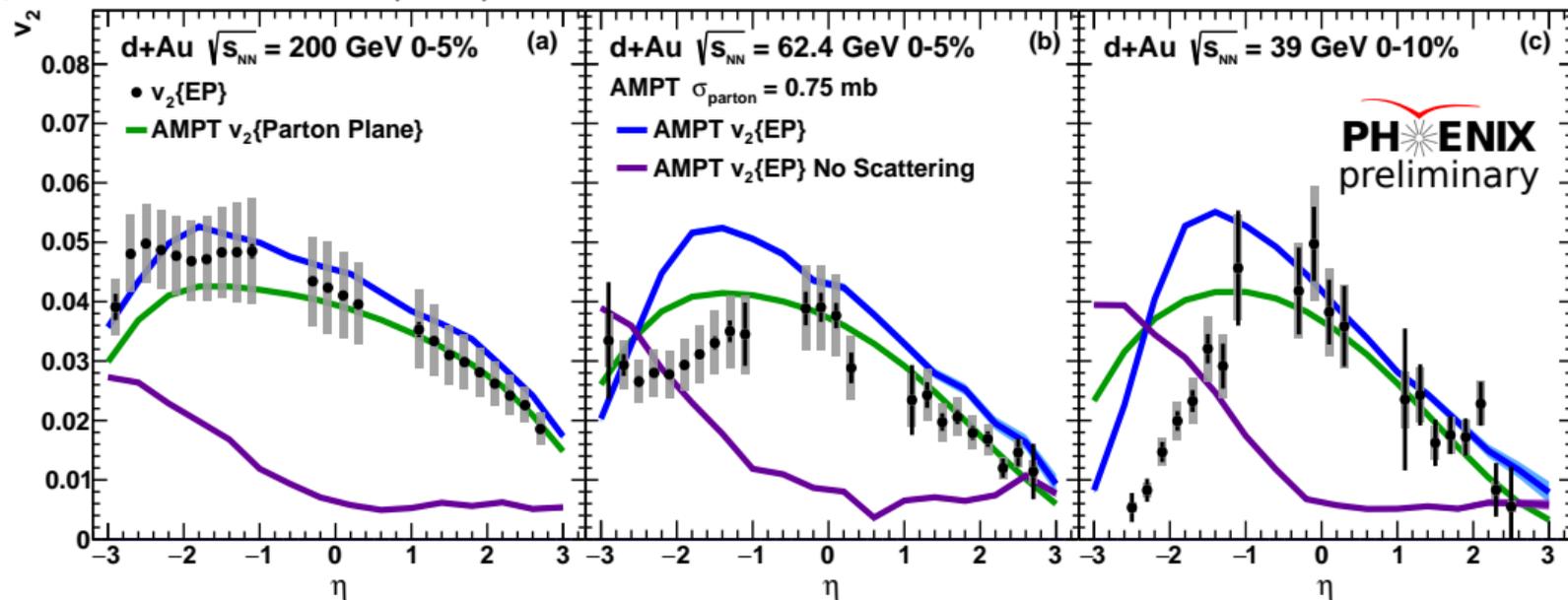
Phys. Rev. C 96, 064905 (2017)



- AMPT flow only agrees with mid and forward rapidity very well, misses backward rapidity
- AMPT flow+non-flow is very similar at mid and forward
- AMPT flow+non-flow shows striking anti-correlation at backward rapidity

# $v_2$ vs $\eta$ , comparison with AMPT

Phys. Rev. C 96, 064905 (2017)



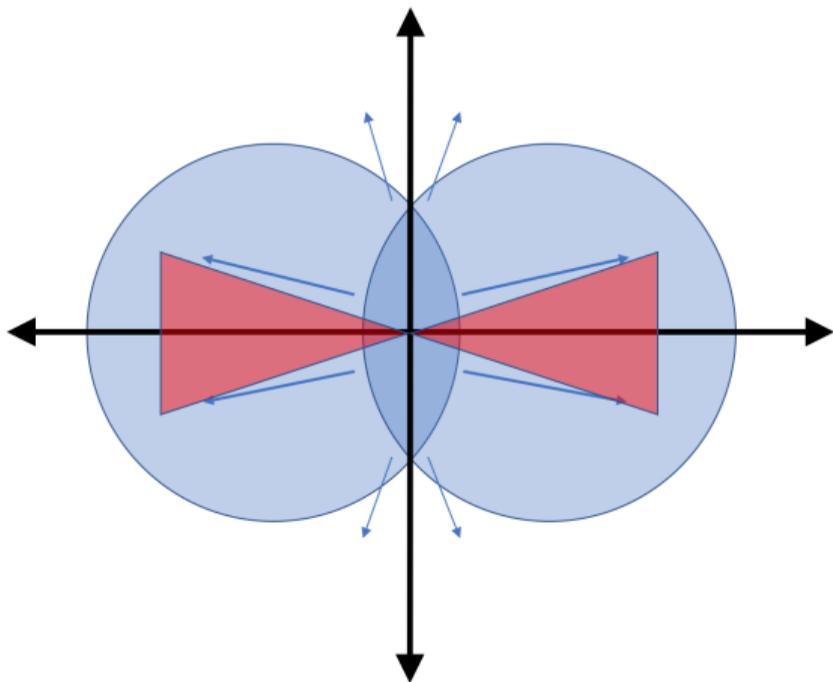
AMPT flow only agrees with mid and forward rapidity very well, misses backward rapidity

AMPT flow+non-flow is very similar at mid and forward

AMPT flow+non-flow shows striking anti-correlation at backward rapidity

AMPT non-flow only shows nothing at mid and forward, large  $v_2$  at backward rapidity near the

## flow and nonflow



$$v_n = \langle \cos(n(\phi_{\text{some particle}} - \psi_n)) \rangle$$

$$v_n^2 = \langle \cos(n(\phi_{\text{some particle}} - \phi_{\text{some other particle}})) \rangle$$

How to deal with “fake flow”?

—Kinematics

—Combinatorics

$$v_n^2 = \langle \cos(n(\phi_a - \phi_b)) \rangle$$

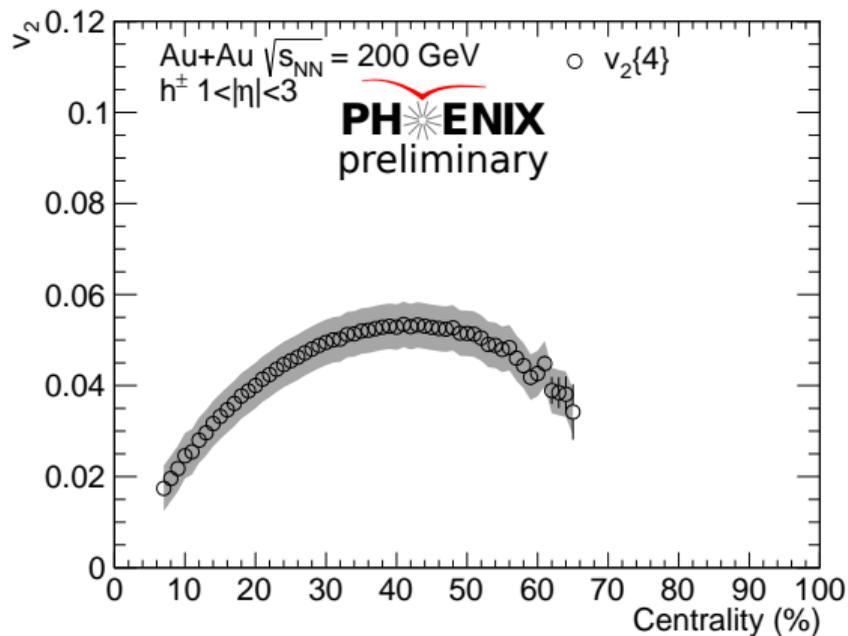
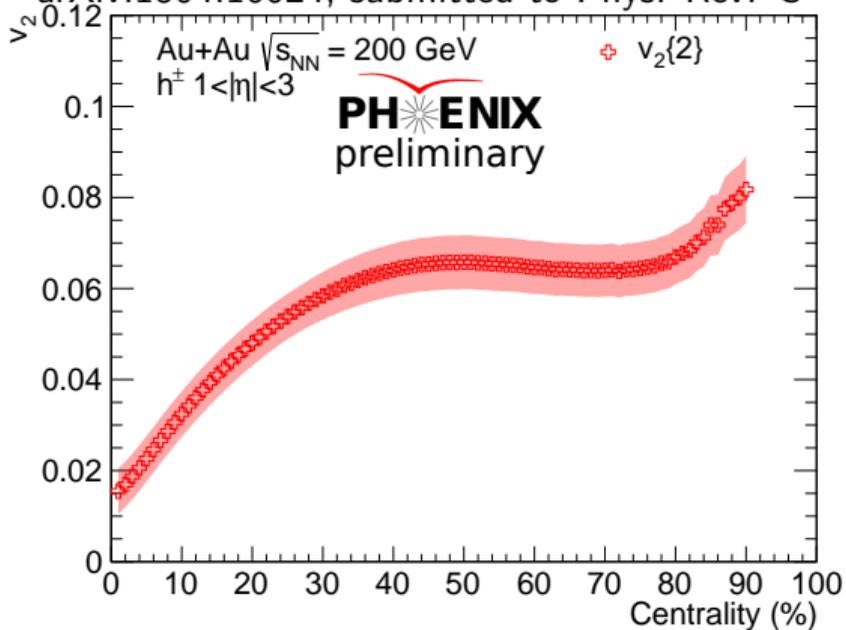
$$v_n^4 = \langle \cos(n(\phi_a + \phi_b - \phi_c - \phi_d)) \rangle$$

$$v_n^6 = \langle \cos(n(\phi_a + \phi_b + \phi_c - \phi_d - \phi_e - \phi_f)) \rangle$$

$$v_n^8 = \dots$$

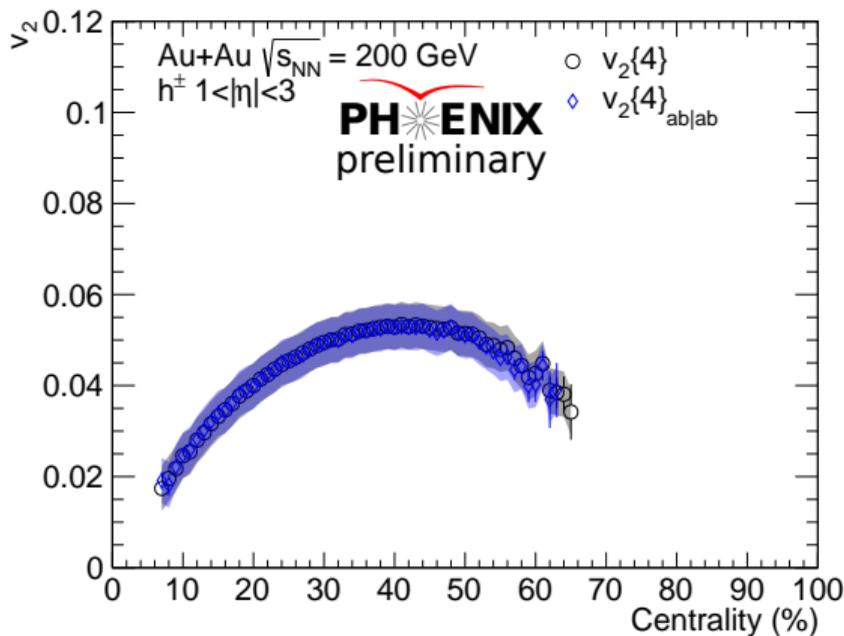
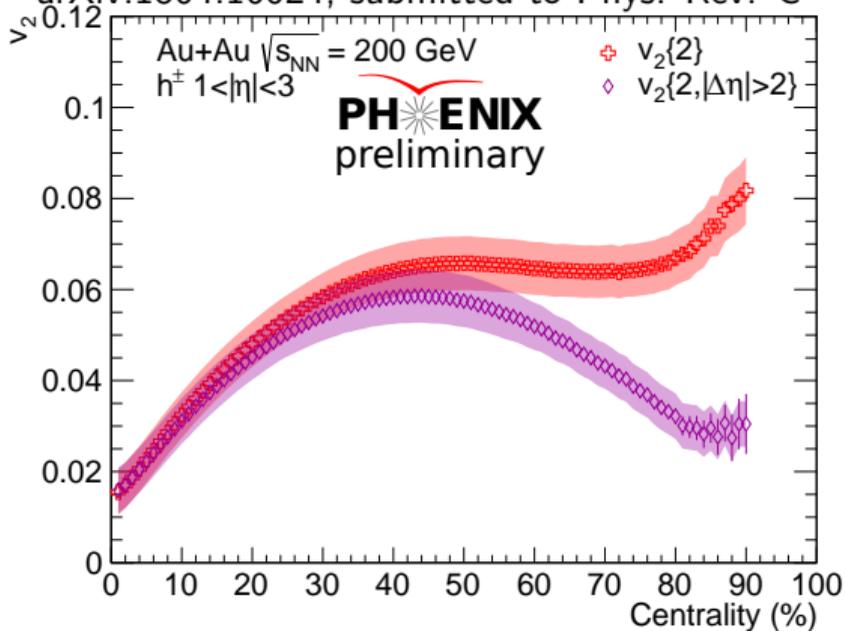
# Nonflow approaches in AuAu

arXiv:1804.10024, submitted to Phys. Rev. C



# Nonflow approaches in AuAu

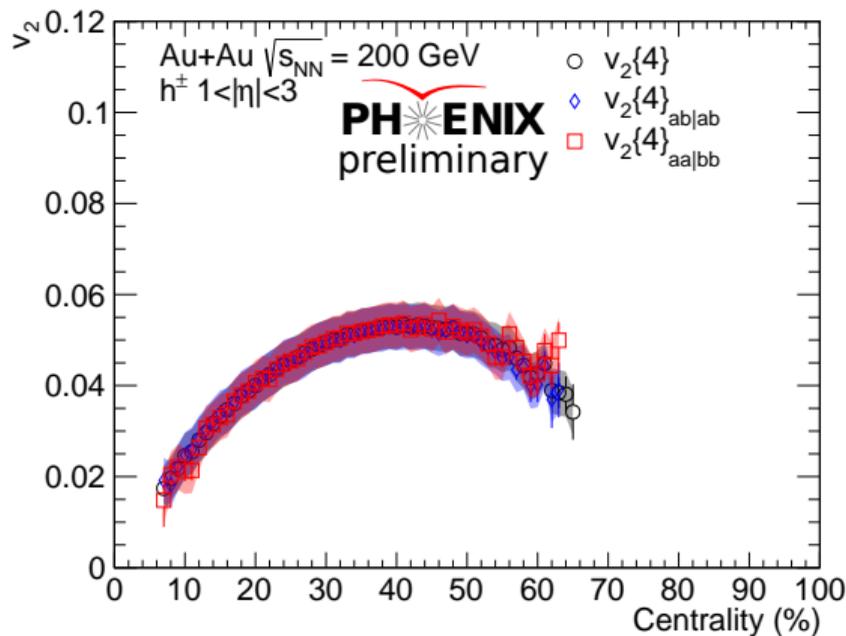
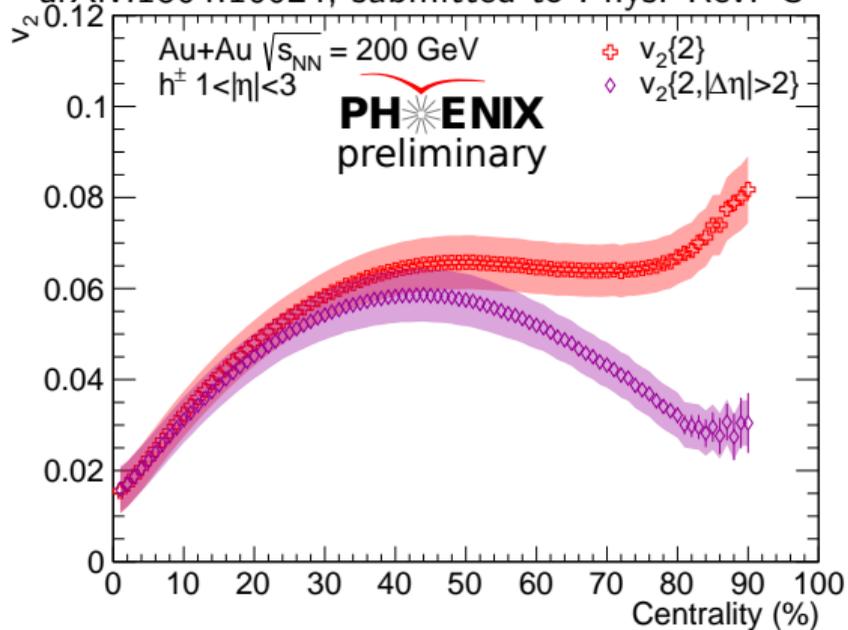
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- Large pseudorapidity separation
- Big difference for 2-particle (good)
- No difference for 4-particle (good)

# Nonflow approaches in AuAu

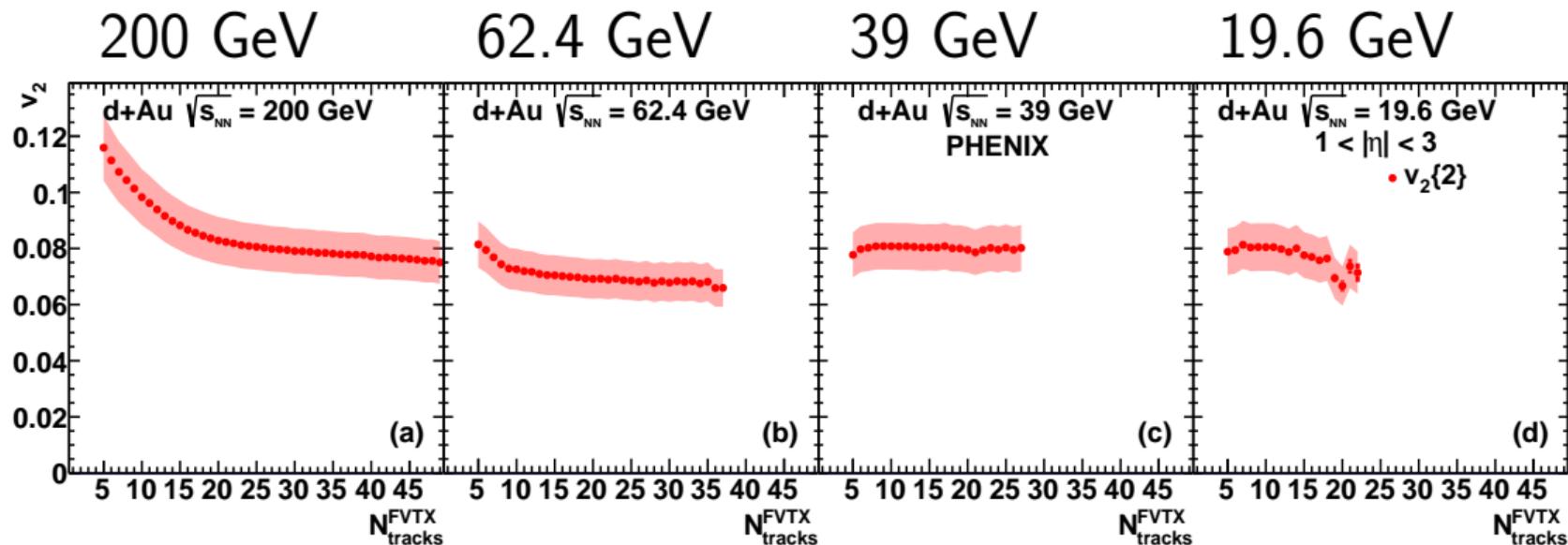
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- Large pseudorapidity separation
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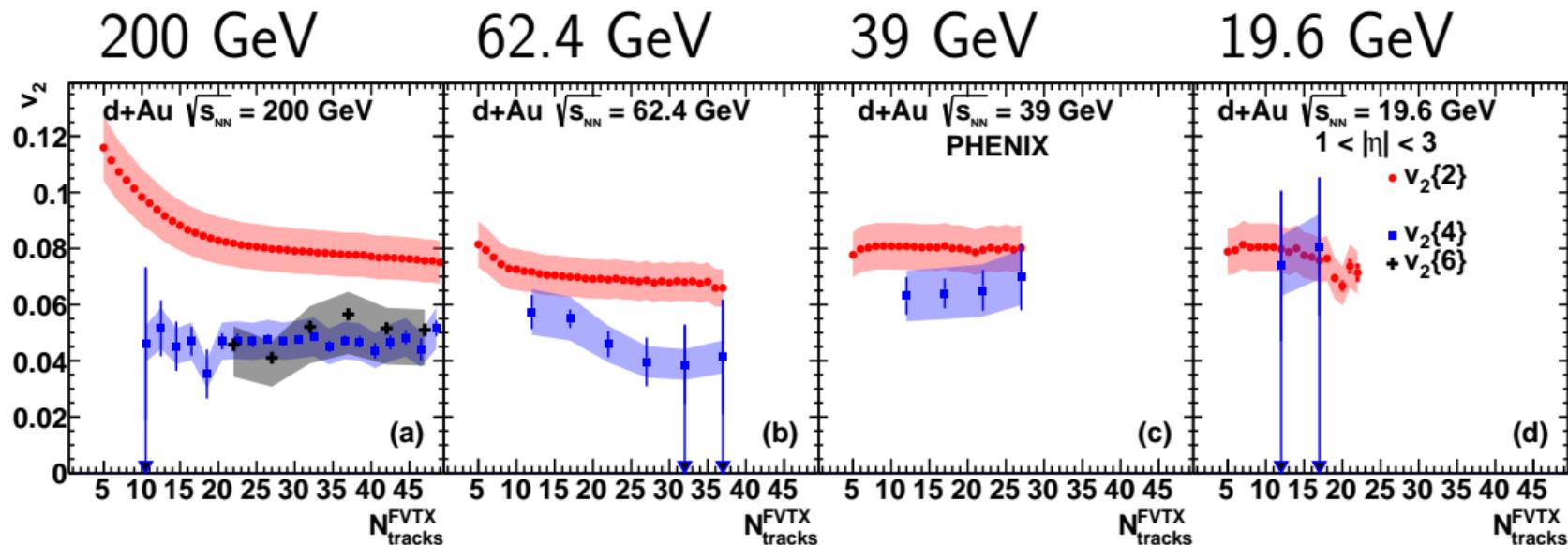
# $d+Au$ beam energy scan

Phys. Rev. Lett. 120, 062302 (2018)



# $d+Au$ beam energy scan

Phys. Rev. Lett. 120, 062302 (2018)



Measurement of  $v_2\{6\}$  in  $d+Au$  at 200 GeV and  $v_2\{4\}$  in  $d+Au$  at all energies

# $d+Au$ beam energy scan

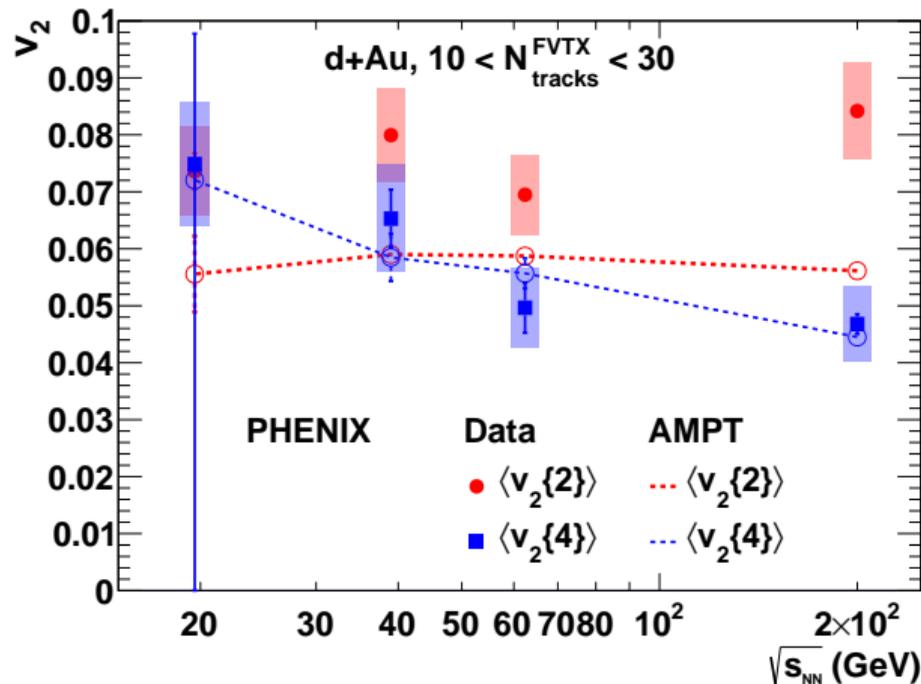
Phys. Rev. Lett. 120, 062302 (2018)

Select  $10 < N_{\text{tracks}}^{\text{FVTX}} < 30$ ,  
integrate

AMPT sees similar trend

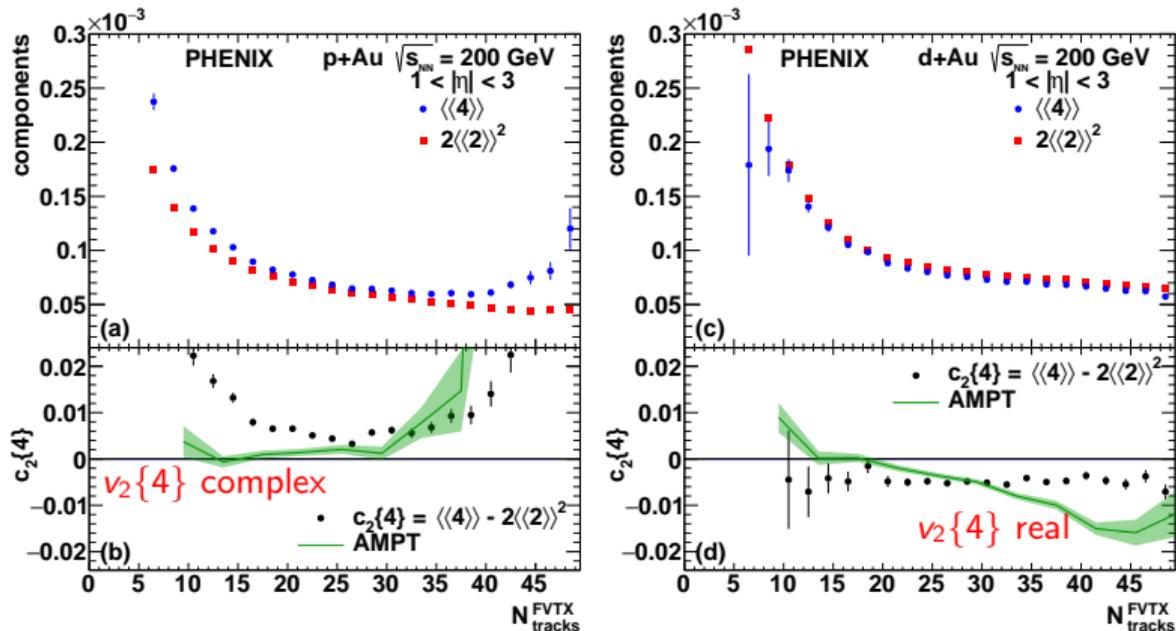
Fluctuations?

Not Bessel-Gaussian  
Not small-variance limit  
Need to understand  
fluctuations better



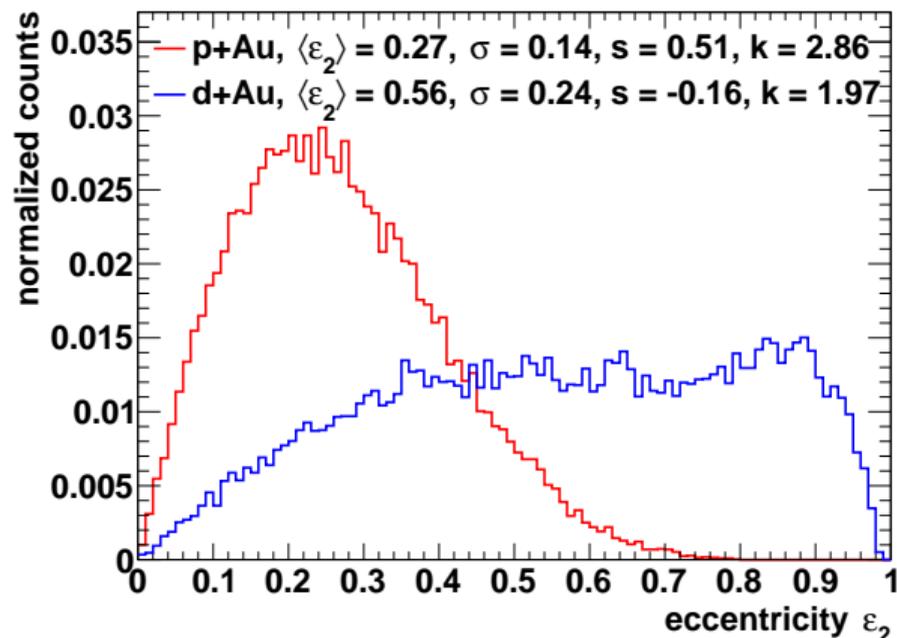
# Components and cumulants in p+Au and d+Au at 200 GeV

Phys. Rev. Lett. 120, 062302 (2018)



Is the sign of  $c_2\{4\}$  a good indicator of collectivity? No.  
Fluctuations could dominate in the p+Au...

# Eccentricity distributions and cumulants



$$\varepsilon_2\{4\} = (\varepsilon_2^4 - 2\varepsilon_2^2\sigma^2 - 4\varepsilon_2s\sigma^3 - (k-2)\sigma^4)^{1/4}$$

	p+Au	d+Au
$\varepsilon_2^4$	0.00531	0.0983
$2\varepsilon_2^2\sigma^2$	0.00277	0.0370
$4\varepsilon_2s\sigma^3$	0.00147	-0.0053
$(k-2)\sigma^4$	0.00031	-0.0001

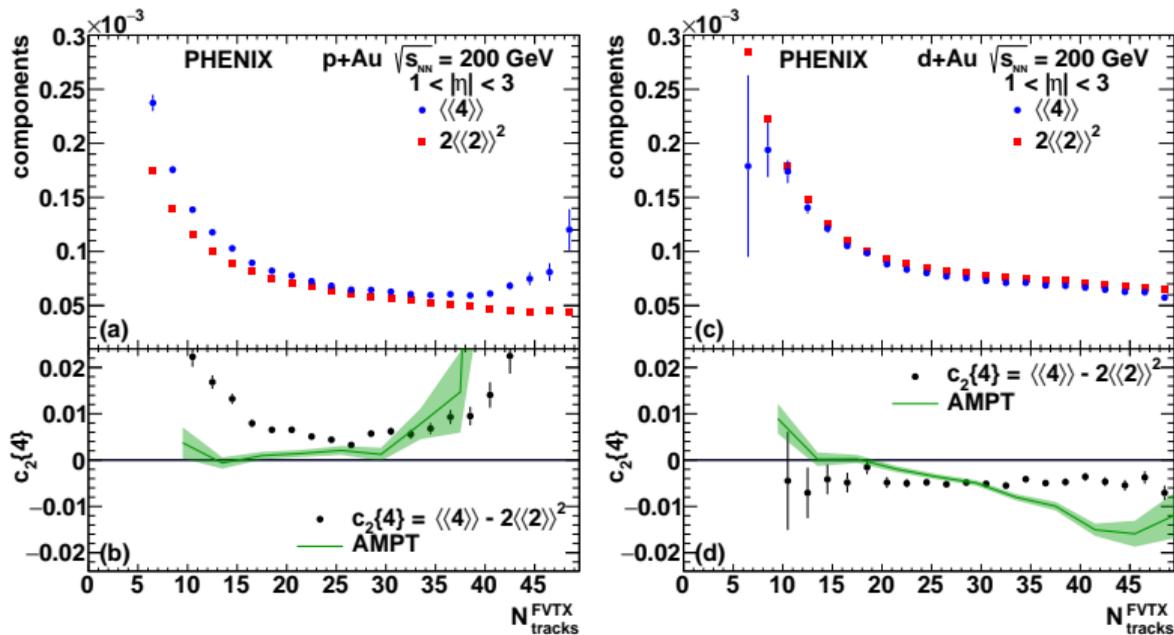
the variance brings  $\varepsilon_2\{4\}$  down (this term gives the usual  $\sqrt{v_2^2 - \sigma^2}$ )

positive skew brings  $\varepsilon_2\{4\}$  further down, negative skew brings it back up

kurtosis  $> 2$  brings  $\varepsilon_2\{4\}$  further down, kurtosis  $< 2$  brings it back up

—recall Gaussian has kurtosis = 3

# Eccentricity distributions and cumulants



$$v_2\{4\} = (v_2^4 - 2v_2^2\sigma^2 - 4v_2\sigma^3 - (k-2)\sigma^4)^{1/4}$$

Eccentricity fluctuations alone go a long way towards explaining this  
Additional fluctuations in the (imperfect) translation of  $\varepsilon_2$  to  $v_2$ ?

## Brief summary: small systems beam energy scan

Measurement of  $v_2$  vs  $p_T$  for  $d+Au$  at 200, 62.4, 39, and 19.6 GeV

—Hydro describes higher two energies well, misses lower two energies

—AMPT describes all data well with mix of flow and nonflow

Measurement of  $v_2$  vs  $\eta$  for  $d+Au$  at 200, 62.4, and 39 GeV

—Hydro theory at lower energies would be very useful

—Interesting anticorrelation between flow and nonflow at backward rapidity

Measurement of  $v_2\{6\}$  at 200 GeV and  $v_2\{4\}$  at all four energies

—Nonflow should be combinatorially suppressed

—Highly non-trivial fluctuations

# Final thoughts

Initial and final state effects are clear in the data  
—*Which* final state effects is perhaps not so clear

Low- $p_T$  photon enhancement observed in  $p+Au$   
—Consistent with EM radiation from QGP  
—Other explanations possible

Wealth of data from small systems beam energy and geometry scans  
—Higher energies described by hydro, all energies described by AMPT  
—All geometries described by hydro, also somewhat described by CGC

# Final thoughts

Initial and final state effects are clear in the data  
—*Which* final state effects is perhaps not so clear

Low- $p_T$  photon enhancement observed in  $p+Au$   
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—Other explanations possible

Wealth of data from small systems beam energy and geometry scans  
—Higher energies described by hydro, all energies described by AMPT  
—All geometries described by hydro, also somewhat described by CGC

“The optimist regards the future as uncertain.”—Eugene Wigner

Additional material

## Back to basics (a brief excursion)

The (raw) moments of a probability distribution function  $f(x)$ :

$$\mu_n = \langle x^n \rangle \equiv \int_{-\infty}^{+\infty} x^n f(x) dx$$

The moment generating function:

$$M_x(t) \equiv \langle e^{tx} \rangle = \int_{-\infty}^{+\infty} e^{tx} f(x) dx = \int_{-\infty}^{+\infty} \sum_{n=0}^{\infty} \frac{t^n}{n!} x^n f(x) dx = \sum_{n=0}^{\infty} \mu_n \frac{t^n}{n!}$$

Moments from the generating function:

$$\mu_n = \left. \frac{d^n M_x(t)}{dt^n} \right|_{t=0}$$

Key point: the moment generating function uniquely describe  $f(x)$

## Back to basics (a brief excursion)

Can also uniquely describe  $f(x)$  with the cumulant generating function:

$$K_x(t) \equiv \ln M_x(t) = \sum_{n=0}^{\infty} \kappa_n \frac{t^n}{n!}$$

Cumulants from the generating function:

$$\kappa_n = \left. \frac{d^n K_x(t)}{dt^n} \right|_{t=0}$$

Since  $K_x(t) = \ln M_x(t)$ ,  $M_x(t) = \exp(K_x(t))$ , so

$$\mu_n = \left. \frac{d^n \exp(K_x(t))}{dt^n} \right|_{t=0}, \quad \kappa_n = \left. \frac{d^n \ln M_x(t)}{dt^n} \right|_{t=0}$$

End result: (details left as an exercise for the interested reader)

$$\begin{aligned} \mu_n &= \sum_{k=1}^n B_{n,k}(\kappa_1, \dots, \kappa_{n-k+1}) && = B_n(\kappa_1, \dots, \kappa_{n-k+1}) \\ \kappa_n &= \sum_{k=1}^n (-1)^{k-1} (k-1)! B_{n,k}(\mu_1, \dots, \mu_{n-k+1}) && = L_n(\kappa_1, \dots, \kappa_{n-k+1}) \end{aligned}$$

## Back to basics (a brief excursion)

Evaluating the Bell polynomials gives

$$\langle x \rangle = \kappa_1$$

$$\langle x^2 \rangle = \kappa_2 + \kappa_1^2$$

$$\langle x^3 \rangle = \kappa_3 + 3\kappa_1\kappa_2 + \kappa_1^3$$

$$\langle x^4 \rangle = \kappa_4 + 4\kappa_1\kappa_3 + 3\kappa_2^2 + 6\kappa_1^2\kappa_2 + \kappa_1^4$$

One can tell by inspection (or derive explicitly) that  $\kappa_1$  is the mean,  $\kappa_2$  is the variance, etc.

## Back to basics (a brief excursion)

Subbing in  $x = v_n$ ,  $\kappa_2 = \sigma^2$ , we find

$$\begin{aligned} \left( \langle v_n^4 \rangle &= v_n^4 + 6v_n^2\sigma^2 + 3\sigma^4 + 4v_n\kappa_3 + \kappa_4 \right) \\ - \left( 2\langle v_n^2 \rangle^2 &= 2v_n^4 + 4v_n^2\sigma^2 + 2\sigma^4 \right) \\ &\rightarrow \\ \langle v_n^4 \rangle - 2\langle v_n^2 \rangle^2 &= -v_n^4 + 2v_n^2\sigma^2 + \sigma^4 + 4v_n\kappa_3 + \kappa_4 \end{aligned}$$

Skewness  $s$ :  $\kappa_3 = s\sigma^3$

Kurtosis  $k$ :  $\kappa_4 = (k - 3)\sigma^4$

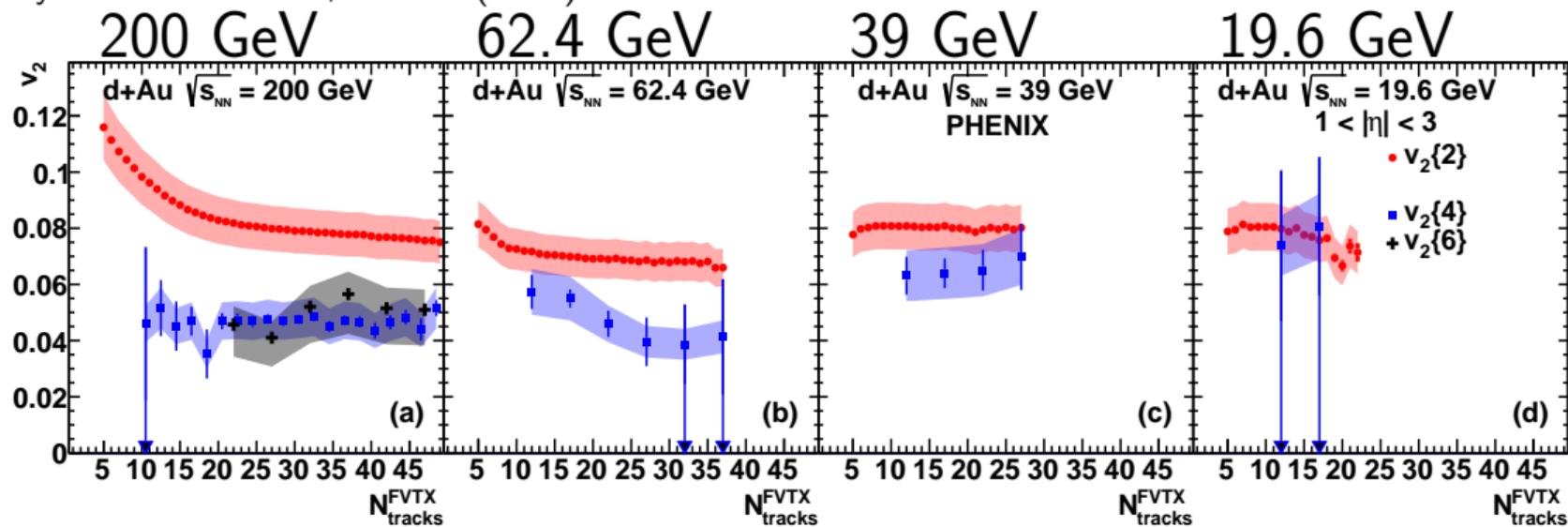
$$v_n\{2\} = (v_n^2 + \sigma^2)^{1/2}$$

$$v_n\{4\} = (v_n^4 - 2v_n^2\sigma^2 - 4v_n s\sigma^3 - (k - 2)\sigma^4)^{1/4}$$

So the fully general form is a bit more complicated than we tend to think...

# $d+Au$ beam energy scan

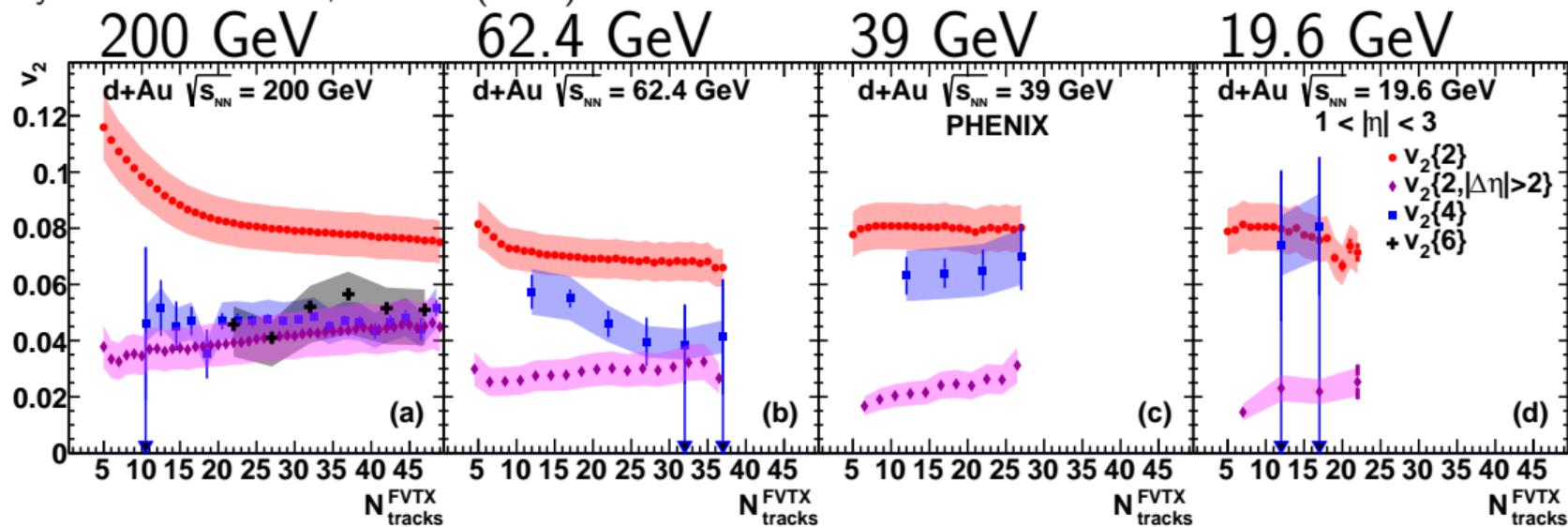
Phys. Rev. Lett. 120, 062302 (2018)



$v_2\{2\}$  and  $v_2\{4\}$  vs  $N_{\text{tracks}}^{\text{FVTX}}$ , all tracks anywhere in FVTX

# $d+Au$ beam energy scan

Phys. Rev. Lett. 120, 062302 (2018)

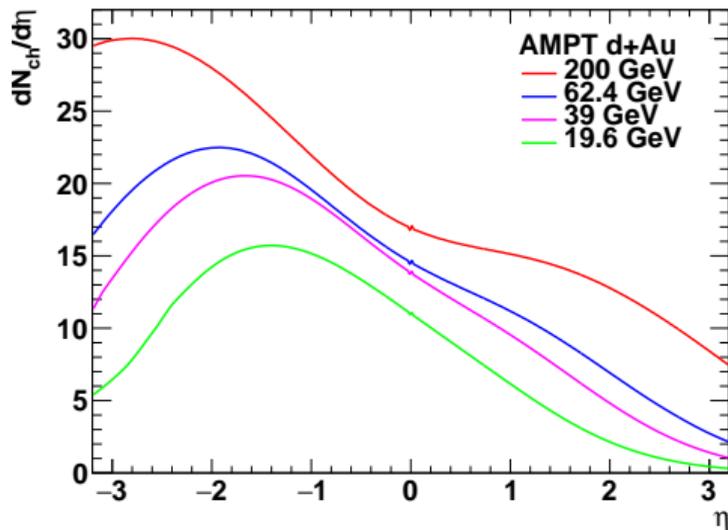


$v_2\{2\}$  and  $v_2\{4\}$  vs  $N_{\text{tracks}}^{\text{FVTX}}$ , all tracks anywhere in FVTX

$v_2\{2, |\Delta\eta| > 2\}$  vs  $N_{\text{tracks}}^{\text{FVTX}}$ , one track backward, the other forward

How is  $v_2\{4\} > v_2\{2, |\Delta\eta| > 2\}$  possible? Can blame fluctuations to a point, but...

# $d+Au$ beam energy scan

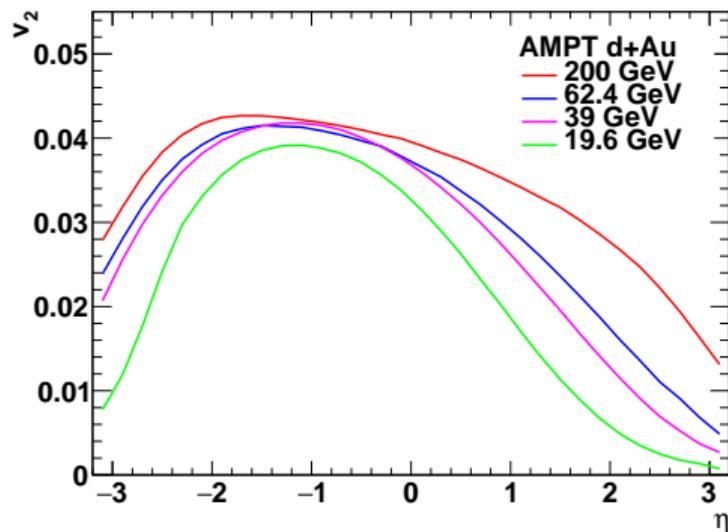
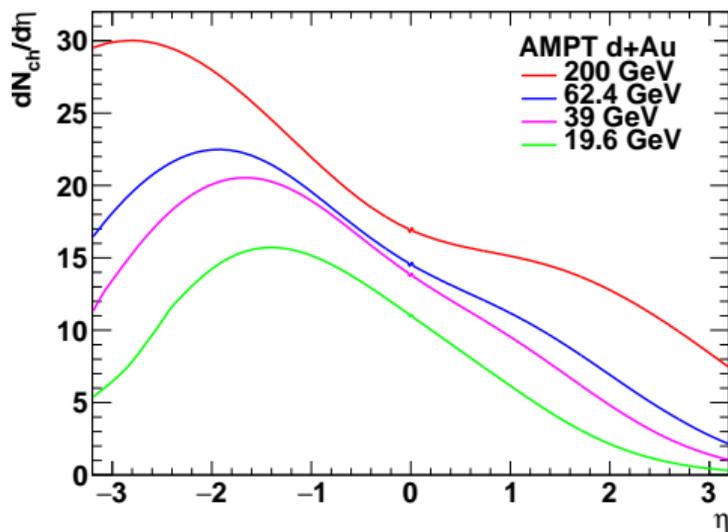


Asymmetric  $dN_{\text{ch}}/d\eta$  and asymmetric  $v_2$  vs  $\eta$

The single subevent is weighted by  $dN_{\text{ch}}/d\eta$  towards backward rapidity, where  $v_2$  is also higher—the effect is more pronounced at lower energies

The two subevent is equally weighted between forward and back:  $\sqrt{\langle v_2^B v_2^F \rangle}$

# $d+Au$ beam energy scan

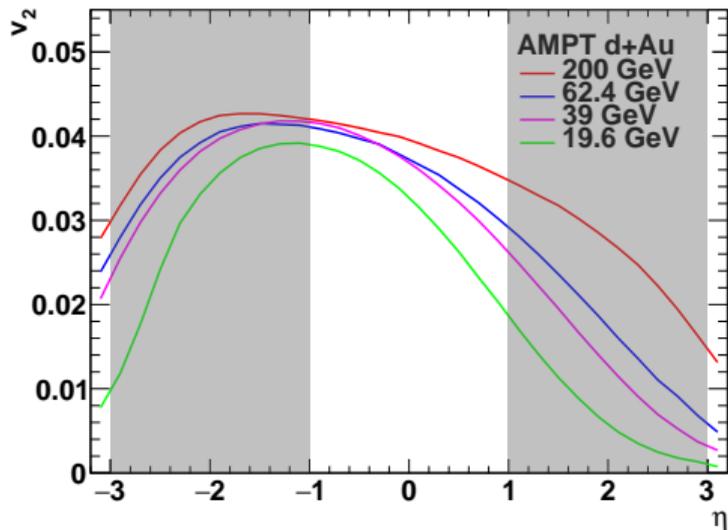
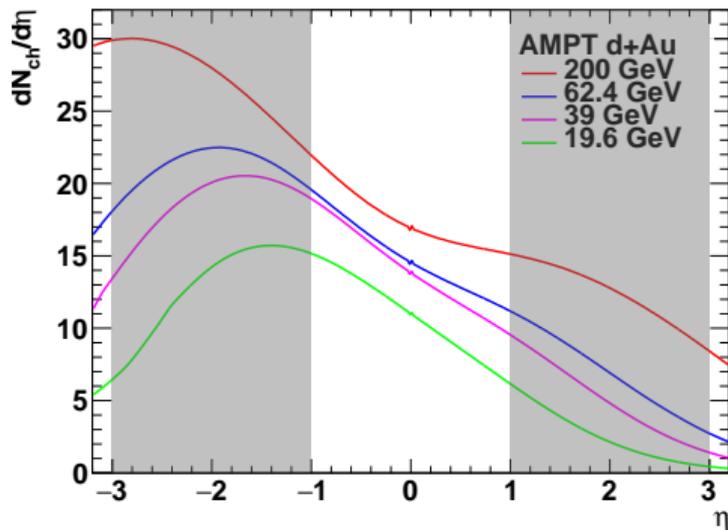


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# $d+Au$ beam energy scan



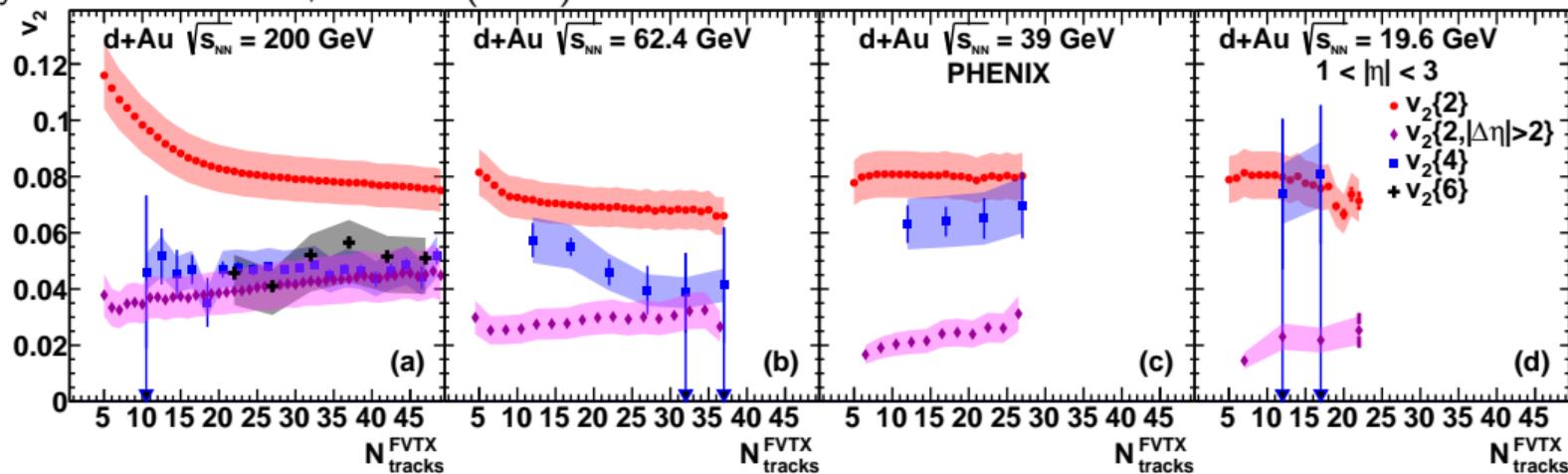
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# d+Au beam energy scan

Phys. Rev. Lett. 120, 062302 (2018)



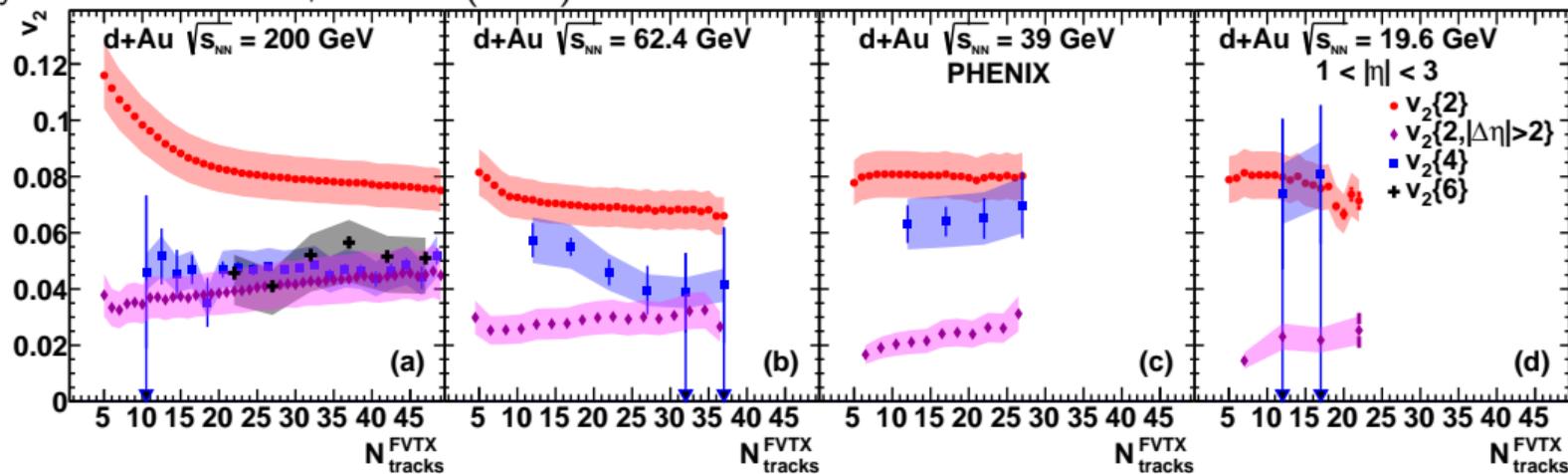
$v_2\{2\}$  and  $v_2\{4\}$  vs  $N_{\text{tracks}}^{\text{FVTX}}$ —weighted average of  $v_2^B$  and  $v_2^F$

$v_2\{2, |\Delta\eta| > 2\}$  vs  $N_{\text{tracks}}^{\text{FVTX}}$ —fixed, equal weighting  $\sqrt{\langle v_2^B v_2^F \rangle}$

$dN_{\text{ch}}/d\eta$  and  $v_2$  vs  $\eta$  alone may explain these results

# d+Au beam energy scan

Phys. Rev. Lett. 120, 062302 (2018)



$v_2\{2\}$  and  $v_2\{4\}$  vs  $N_{\text{tracks}}^{\text{FVTX}}$ —weighted average of  $v_2^B$  and  $v_2^F$

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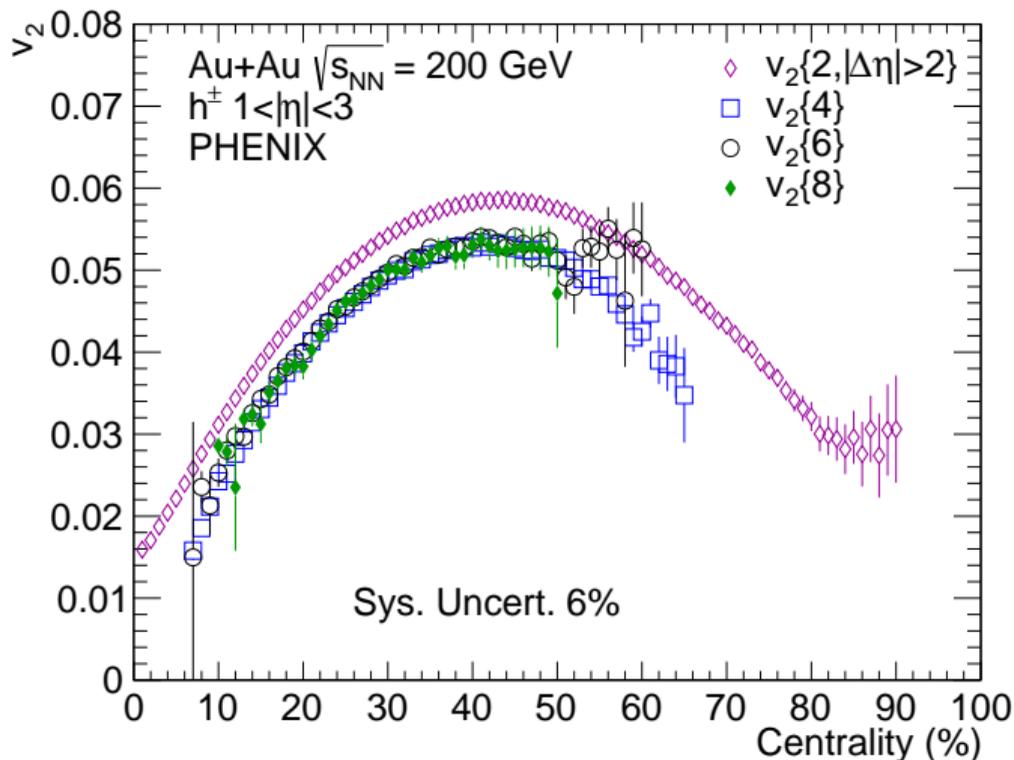
$dN_{\text{ch}}/d\eta$  and  $v_2$  vs  $\eta$  alone may explain these results

There can also be some event plane decorrelation, e.g.

$$v_2\{2, |\Delta\eta| > 2\} = \sqrt{\langle v_2^B v_2^F \rangle \cos(2(\psi_2^B - \psi_2^F))}$$

# Collectivity in large systems

arXiv:1804.10024 (submitted to Phys. Rev. C)



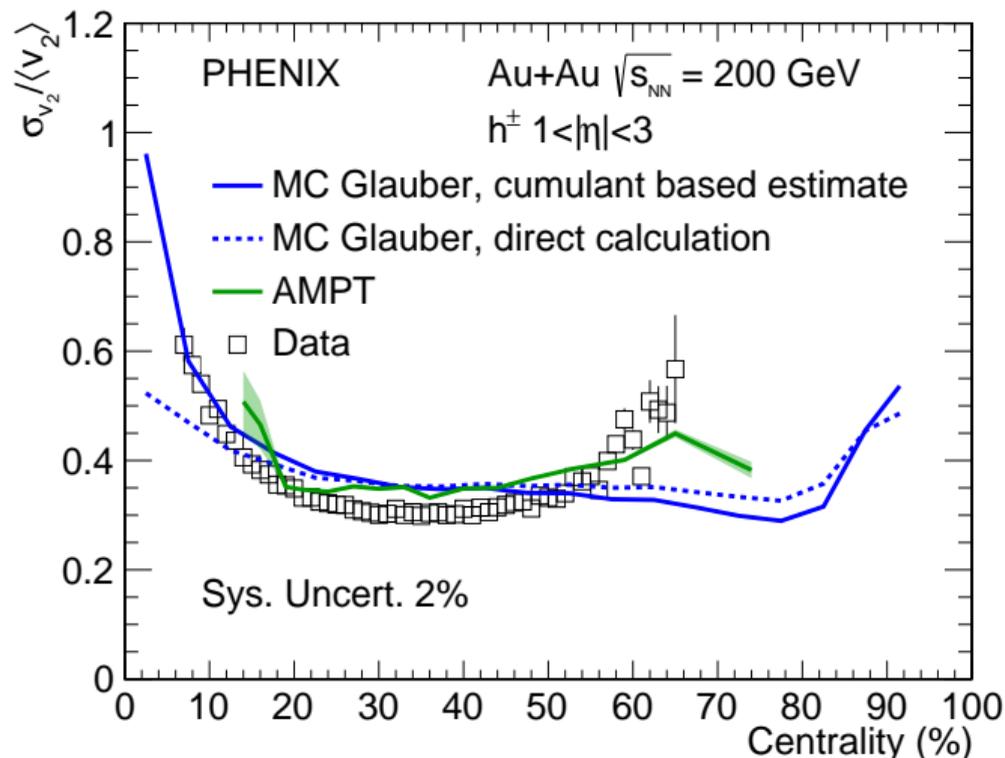
$$1 < |\eta| < 3$$

$$v_2\{2\}, v_2\{4\}, v_2\{6\},$$

$$v_2\{8\}$$

# Collectivity in large systems

arXiv:1804.10024 (submitted to Phys. Rev. C)



$$1 < |\eta| < 3$$

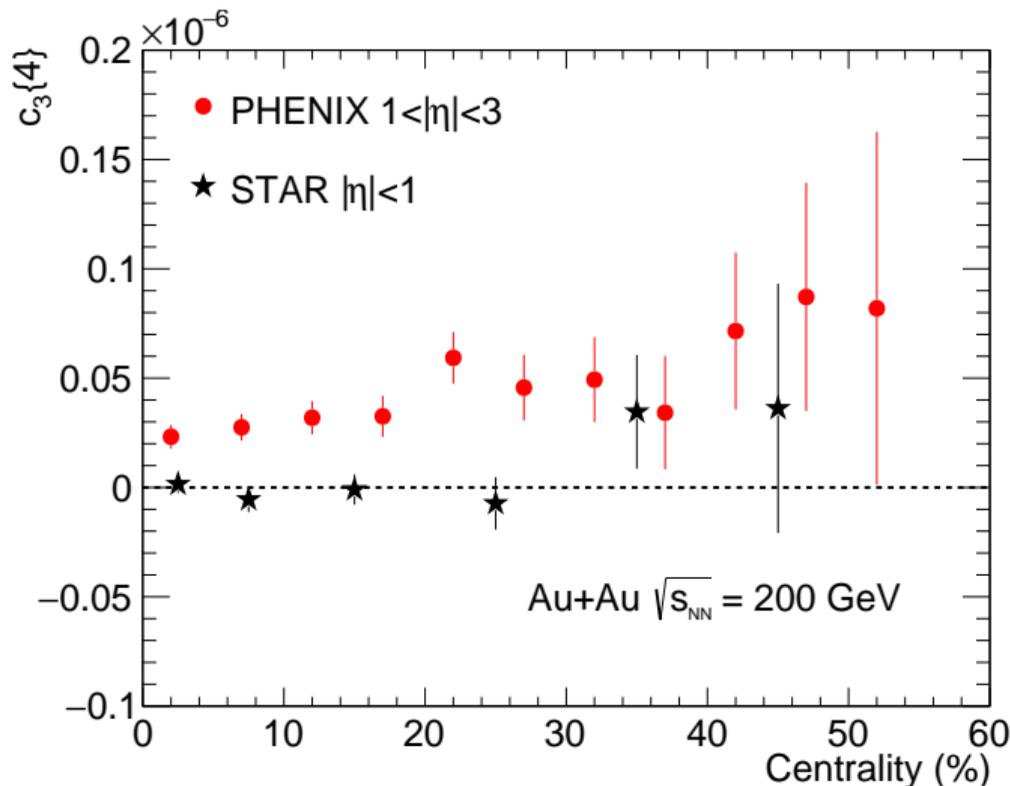
$$\sigma_{v_2} / \langle v_2 \rangle$$

Central: breakdown of small-variance limit

Peripheral: non-linearity in hydro response (e.g. J. Noronha-Hostler et al Phys. Rev. C 93, 014909 (2016))

# Collectivity in large systems

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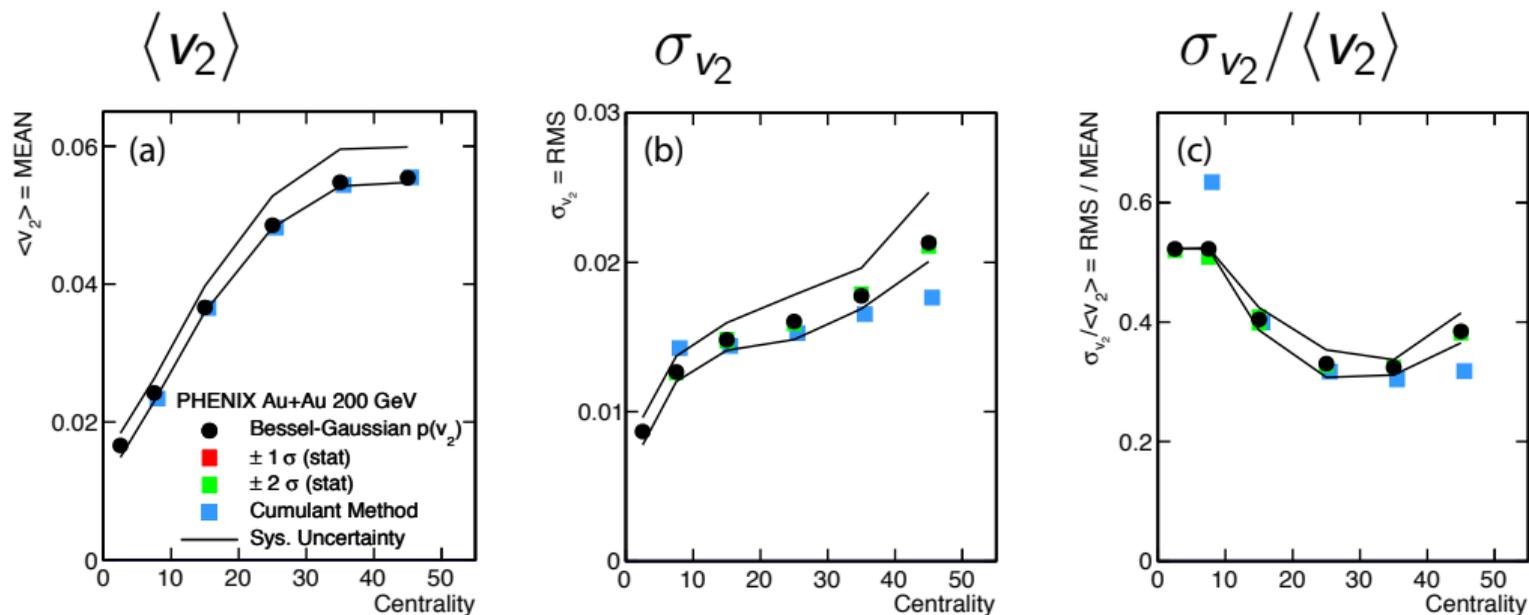
$$1 < |\eta| < 3$$

Cannot extract

$$\sigma_{v_3} / \langle v_3 \rangle$$

# Collectivity in large systems

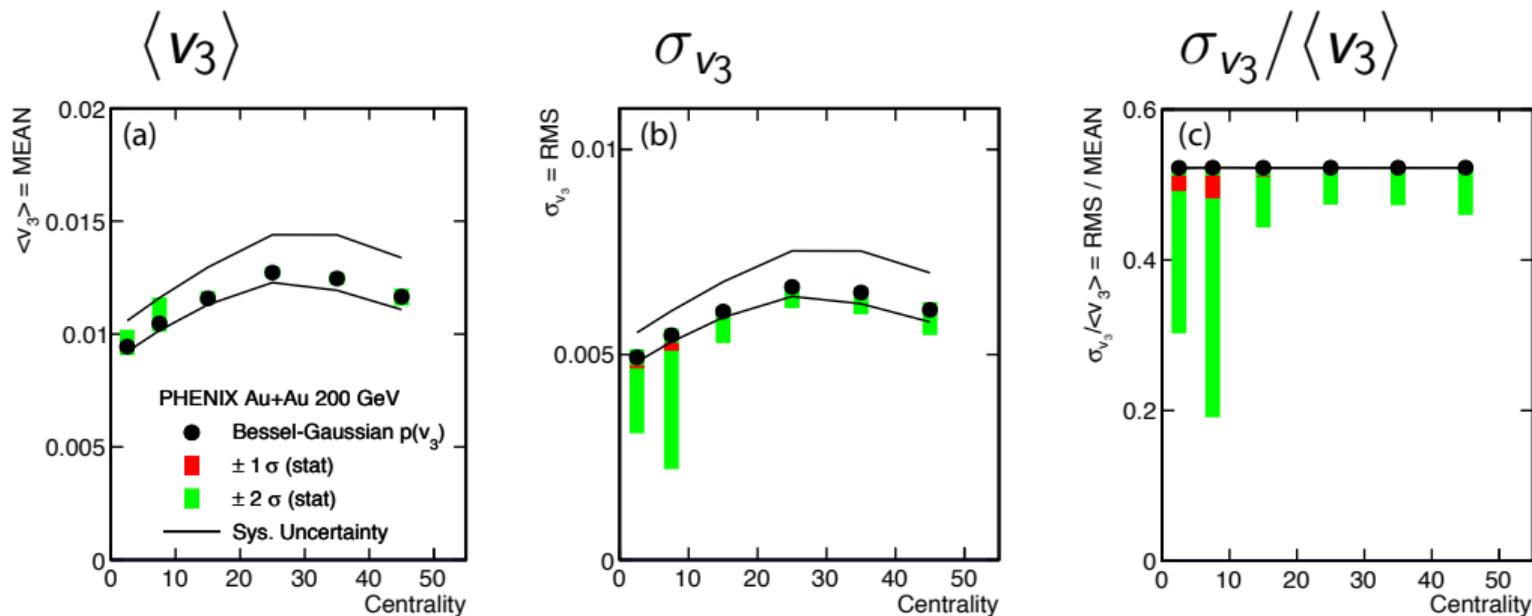
arXiv:1804.10024 (submitted to Phys Rev C)



Can extract  $\langle v_2 \rangle$  and  $\sigma_{v_2}$  separately using forward-fold

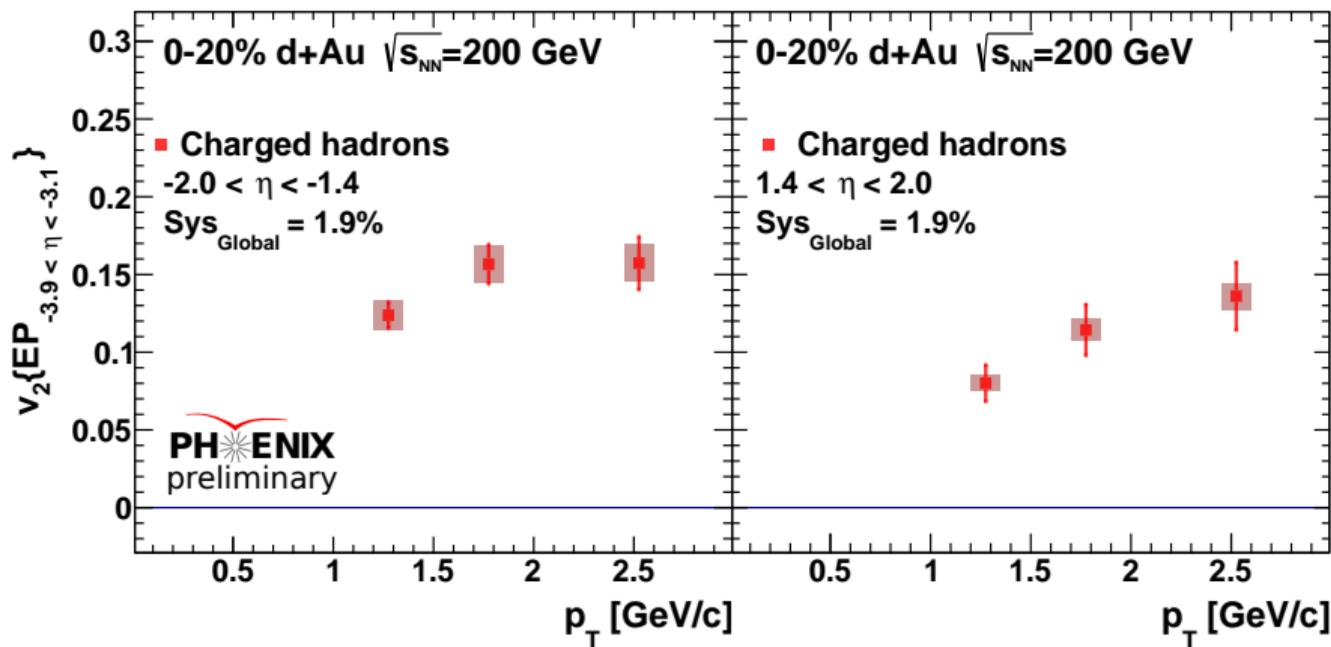
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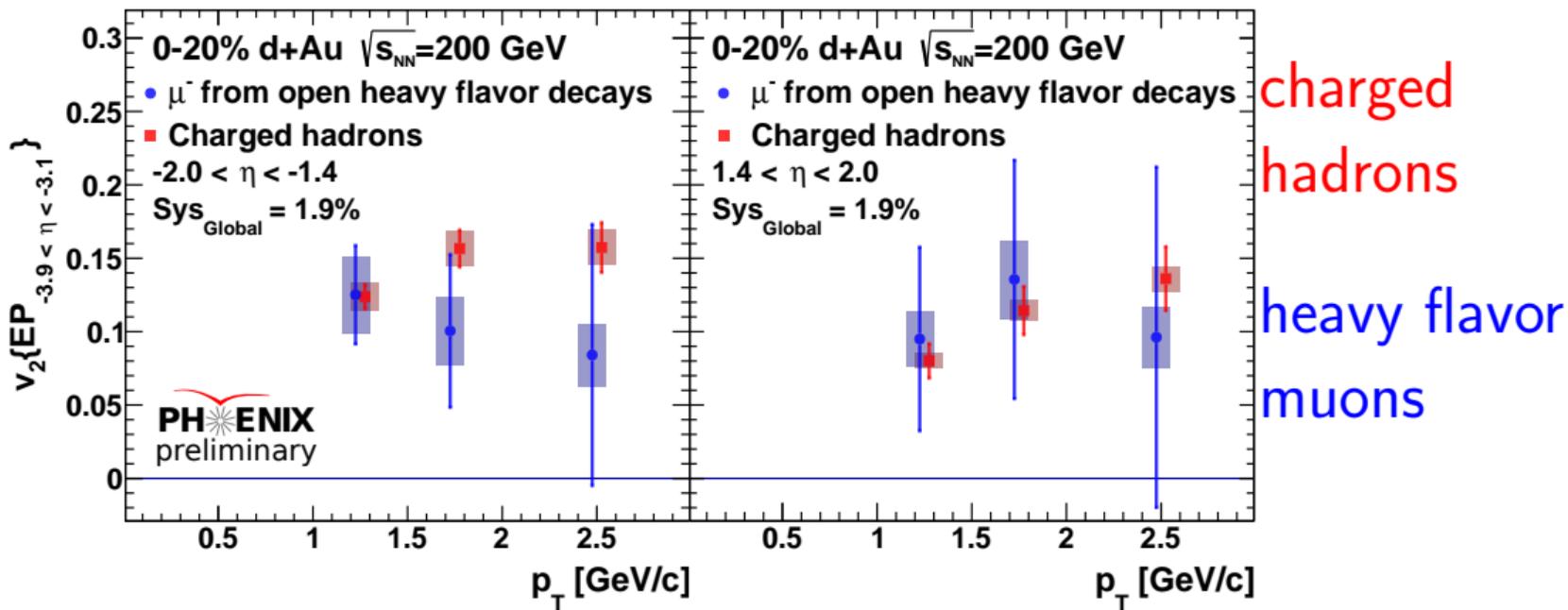
Can extract  $\langle v_3 \rangle$  and  $\sigma_{v_3}$  separately using forward-fold

# Small systems flow



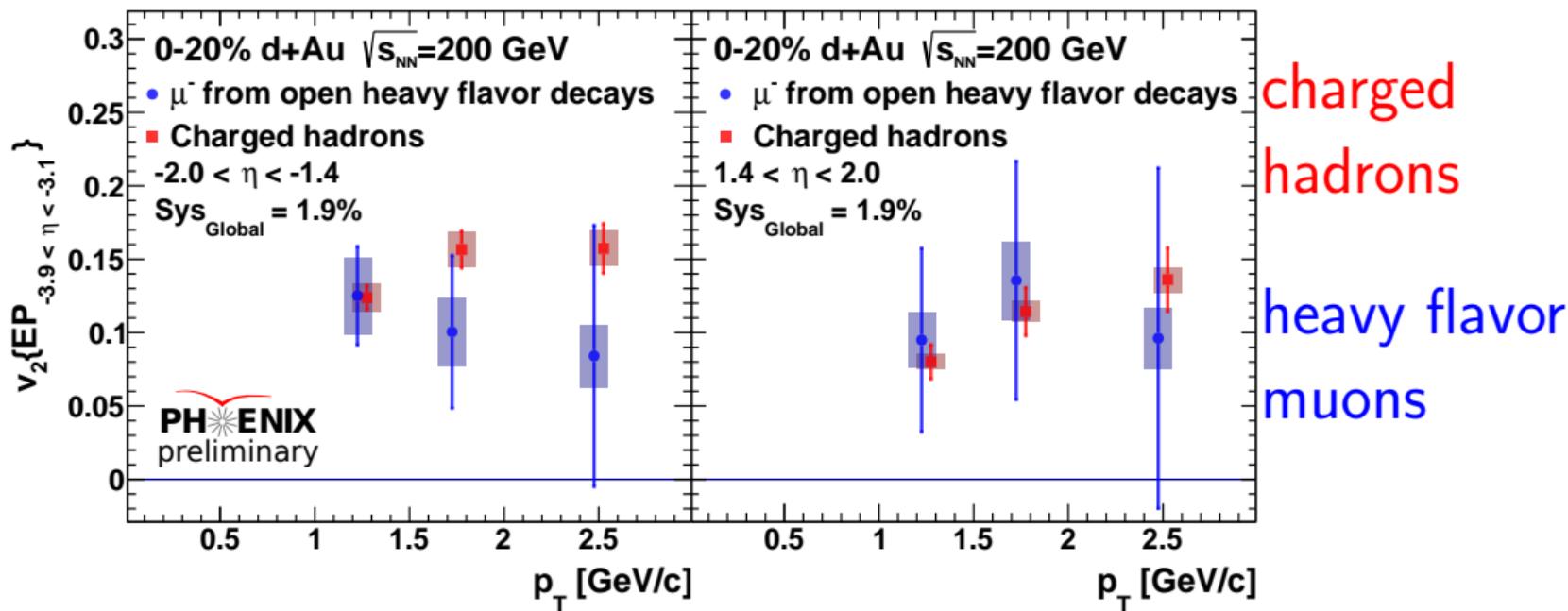
charged  
hadrons

# Small systems flow—heavy flavor



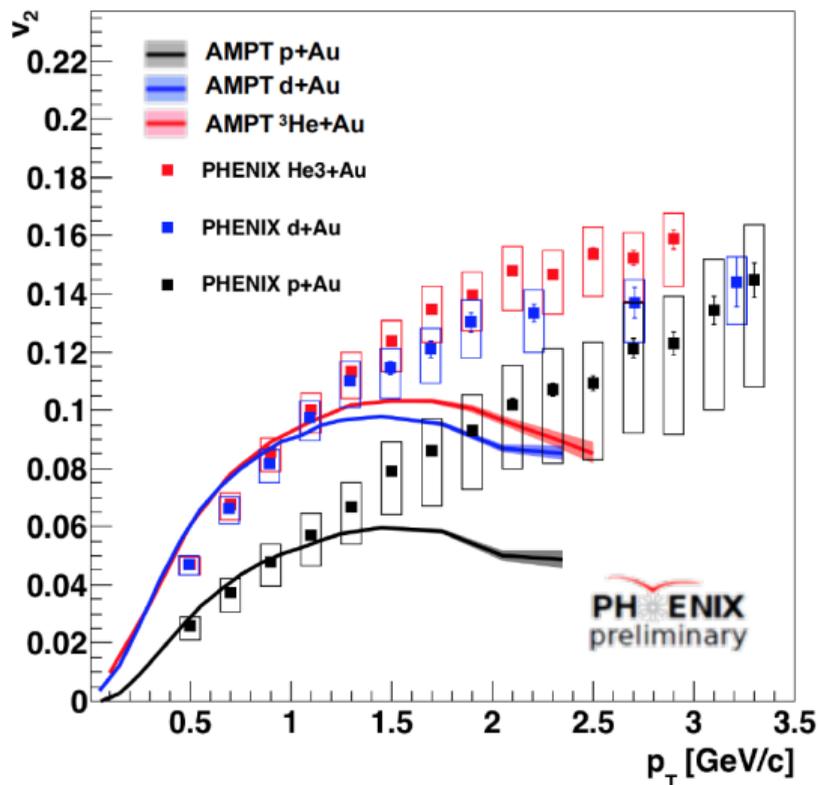
Nonzero  $v_2$  for heavy flavor in  $d+Au$

# Small systems flow—heavy flavor



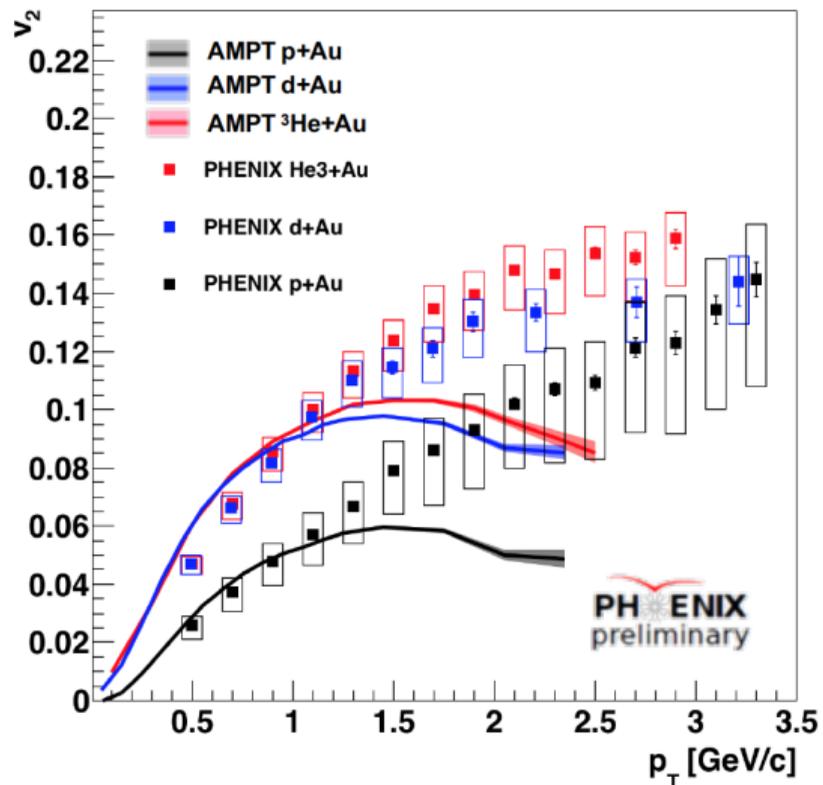
Nonzero  $v_2$  for heavy flavor in  $d+Au$

$3.22\sigma$ ,  $2.16\sigma$  for  $v_2 > 0$  at backward, forward (99.9%, 98.5% one-sided)



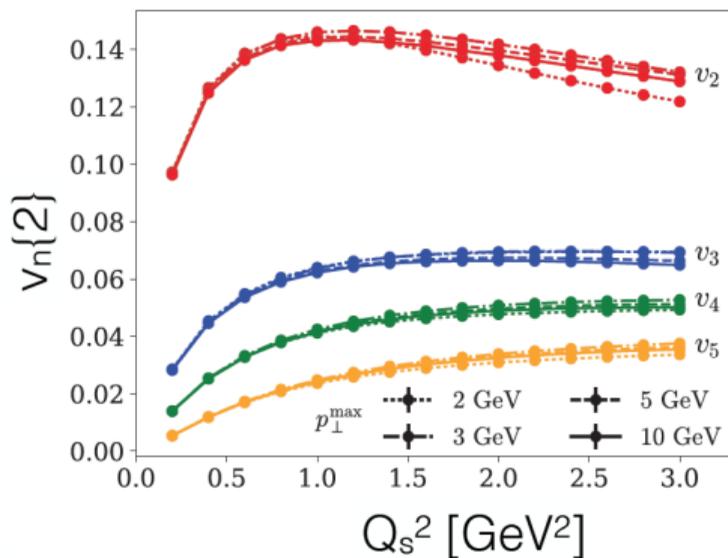
## AMPT basic features

Initial conditions	HIJING
Particle production	String melting
Pre-equilibrium	None
Expansion	Parton scattering (tunable)
Hadronization	Spatial coalescence
Final stage	Hadron cascade (tunable)



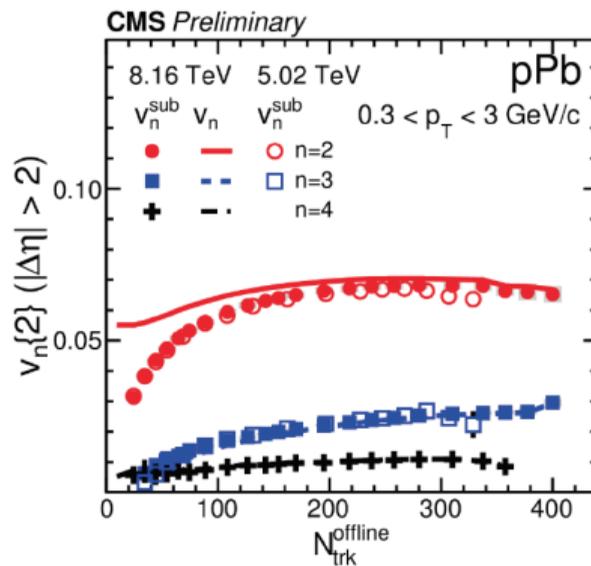
# CGC results on small systems

Mark Mace, QM18



Dusling, MM, Venugopalan PRL 120 (2018)

Phys. Rev. Lett. 120, 042002 (2018)

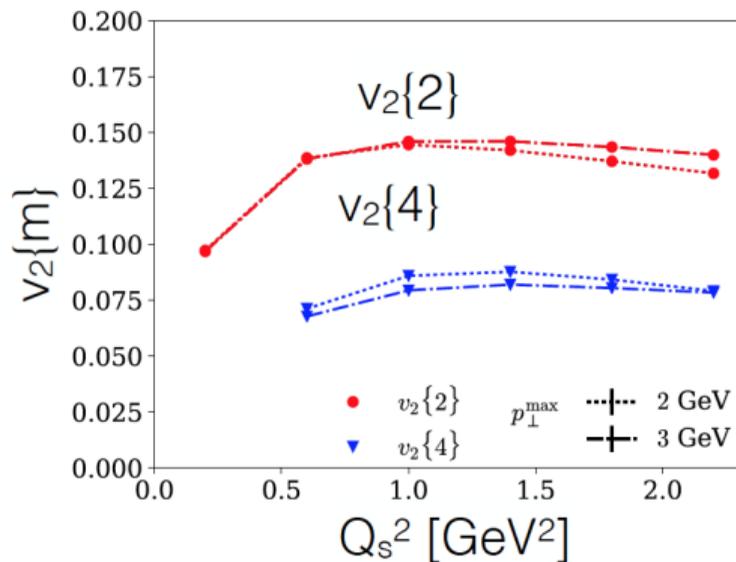


CMS-PAS-HIN-16-022

“Simple parton model” with quarks scattering off dense gluon field  
 Can qualitatively reproduce harmonic ordering  
 Off from data by a factor of 2 to 3

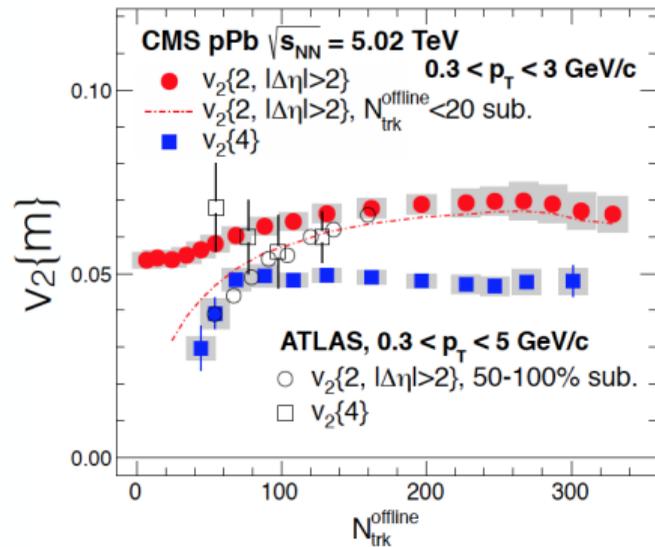
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Phys. Rev. Lett. 120, 042002 (2018)



CMS PLB 724 (2013) 213

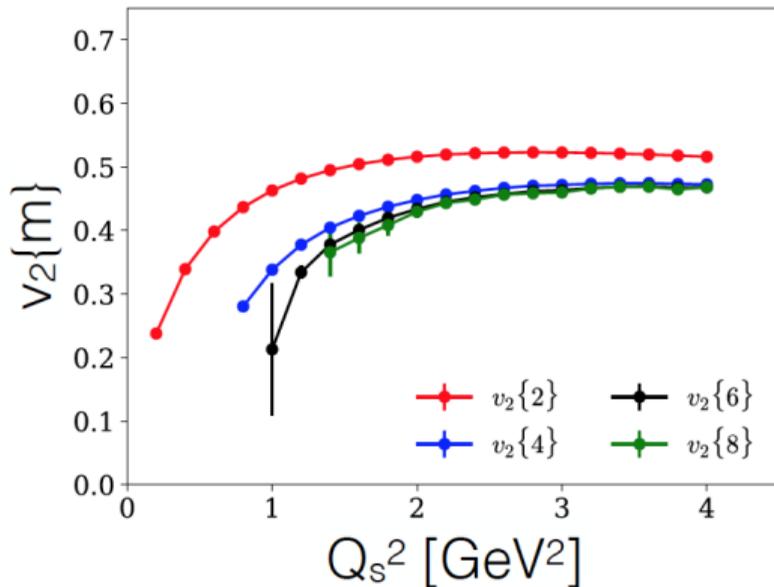
“Simple parton model” with quarks scattering off dense gluon field

Can reproduce  $v_2\{2\}$  and  $v_2\{4\}$

Disagreement with data by a factor of 2, but qualitative features match

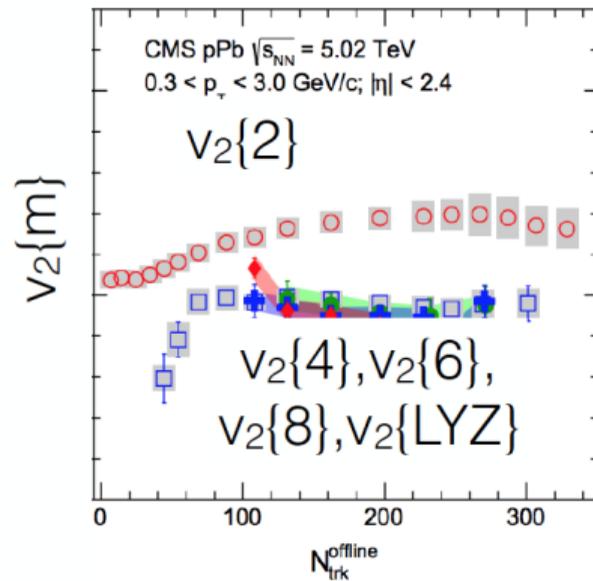
# CGC results on small systems

Mark Mace, QM18



Dusling, MM, Venugopalan PRL 120 (2018)

Phys. Rev. Lett. 120, 042002 (2018)



CMS PRL 115 (2015) 012301

Abelian calculations can produce  $v_2\{2\}$ ,  $v_2\{4\}$ ,  $v_2\{6\}$ ,  $v_2\{8\}$

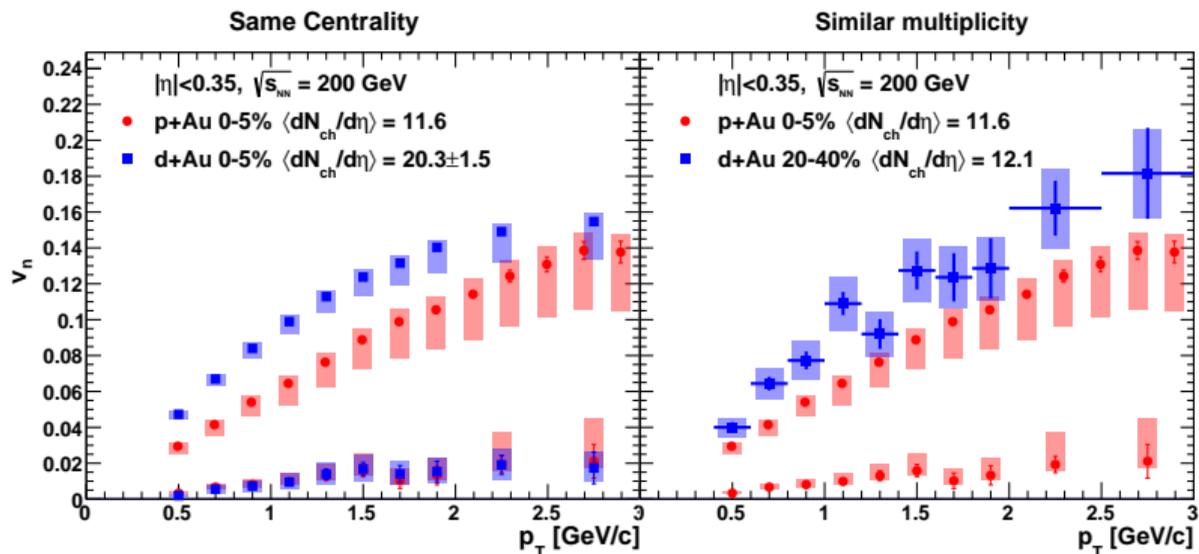
Disagreement with data by factor of 5, but qualitative features match

# CGC results on small systems

Data: Phys. Rev. C 96, 064905 (2017)

Theory: arXiv:1805.09342

“Our prediction would therefore be that  $v_{2,3}(p_{\perp})$  for high multiplicity events across small systems should be identical for the same  $N_{\text{ch}}$ .”



$v_3$  is same in  $p/d$ +Au for different  $N_{\text{ch}}$

$v_2$  looks different for  $p/d$ +Au for similar  $N_{\text{ch}}$ , but need nonflow estimate...