

# System-size & beam energy dependence of the space-time extent of the pion emission source in HI collisions



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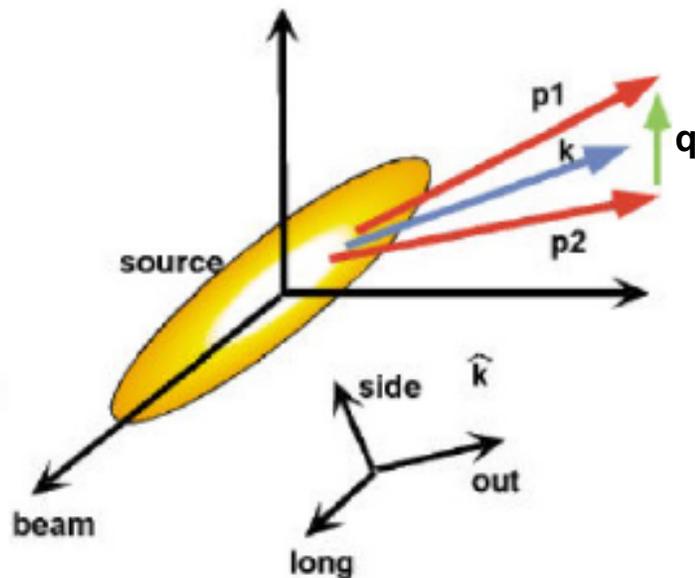
4<sup>th</sup> Joint DNP Meeting  
of APS and JPS  
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# HBT methodology

- Construct 2 pion correlation function:  $C_2(\mathbf{q}) = A(\mathbf{q})/B(\mathbf{q})$ 
  - $A(\mathbf{q})$ : measured distribution of relative momentum difference  $\mathbf{q}$
  - $B(\mathbf{q})$ : uncorrelated distribution for pairs from mixed events
- Measured  $\mathbf{q}$ 's determine HBT Gaussian radii,  $R$ 's

$\mathbf{q} = \mathbf{p}_2 - \mathbf{p}_1$  is relative momentum difference between pion pairs  
 $k_T = |\mathbf{p}_{T2} + \mathbf{p}_{T1}|/2$  is pion-pair transverse momentum

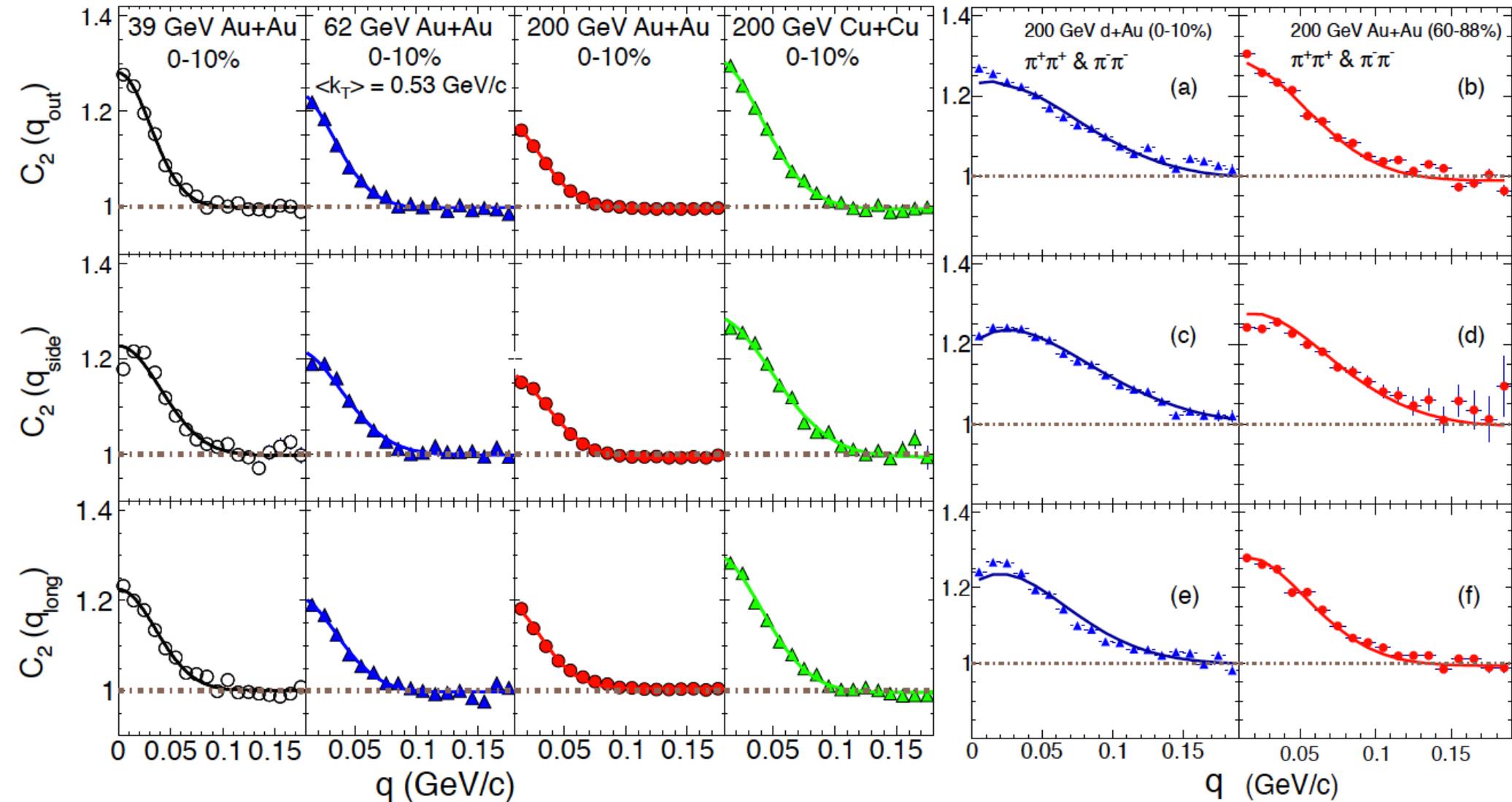


Calculated in longitudinally co-moving frame

Bertsch-Pratt convention:

- $q_{\text{out}}$  parallel to  $k_T$
- $q_{\text{long}}$  parallel to beam direction
- $q_{\text{side}}$  perpendicular to beam &  $k_T$

# 3D 2 pion HBT correlation functions



Coulomb corrected fits as in PLB **432**, 248 (1998):

$$C_2(\mathbf{q}) = N[(\lambda(1 + G(\mathbf{q})))F_c + (1 - \lambda)]$$

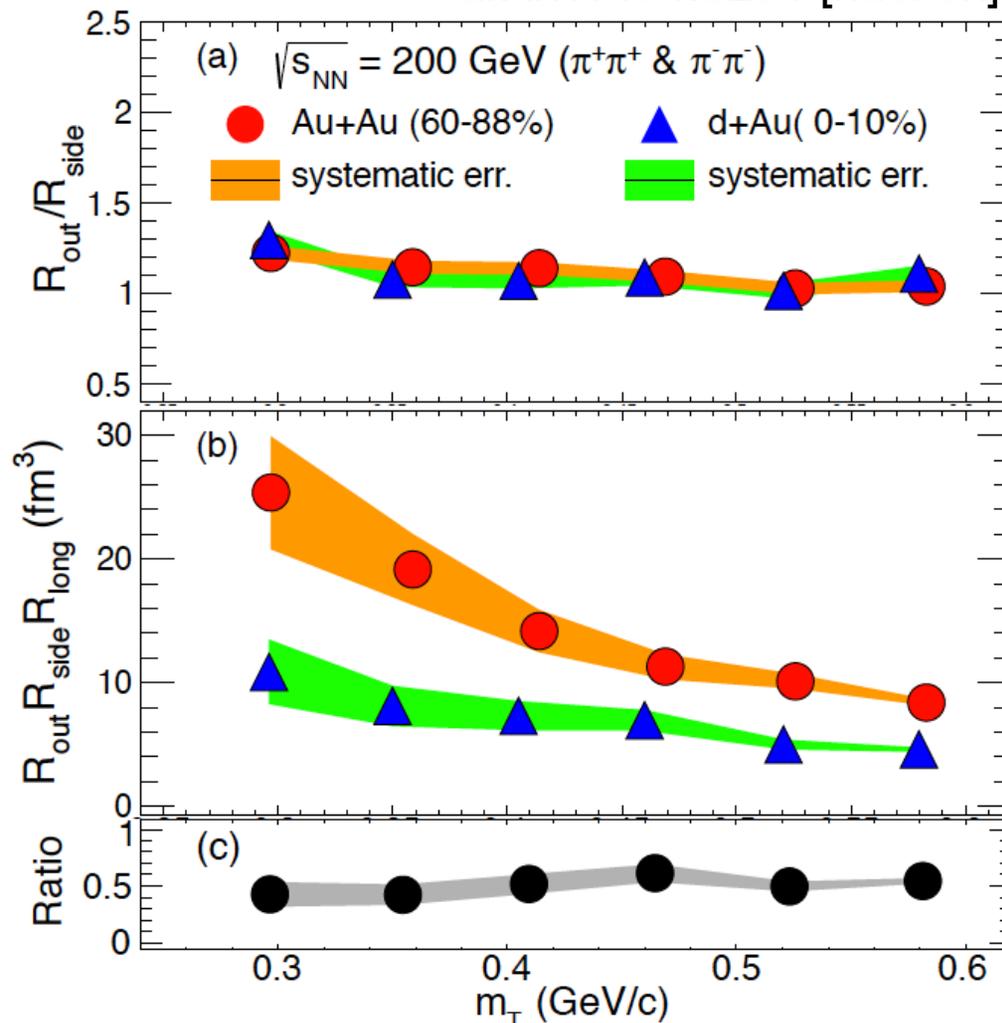
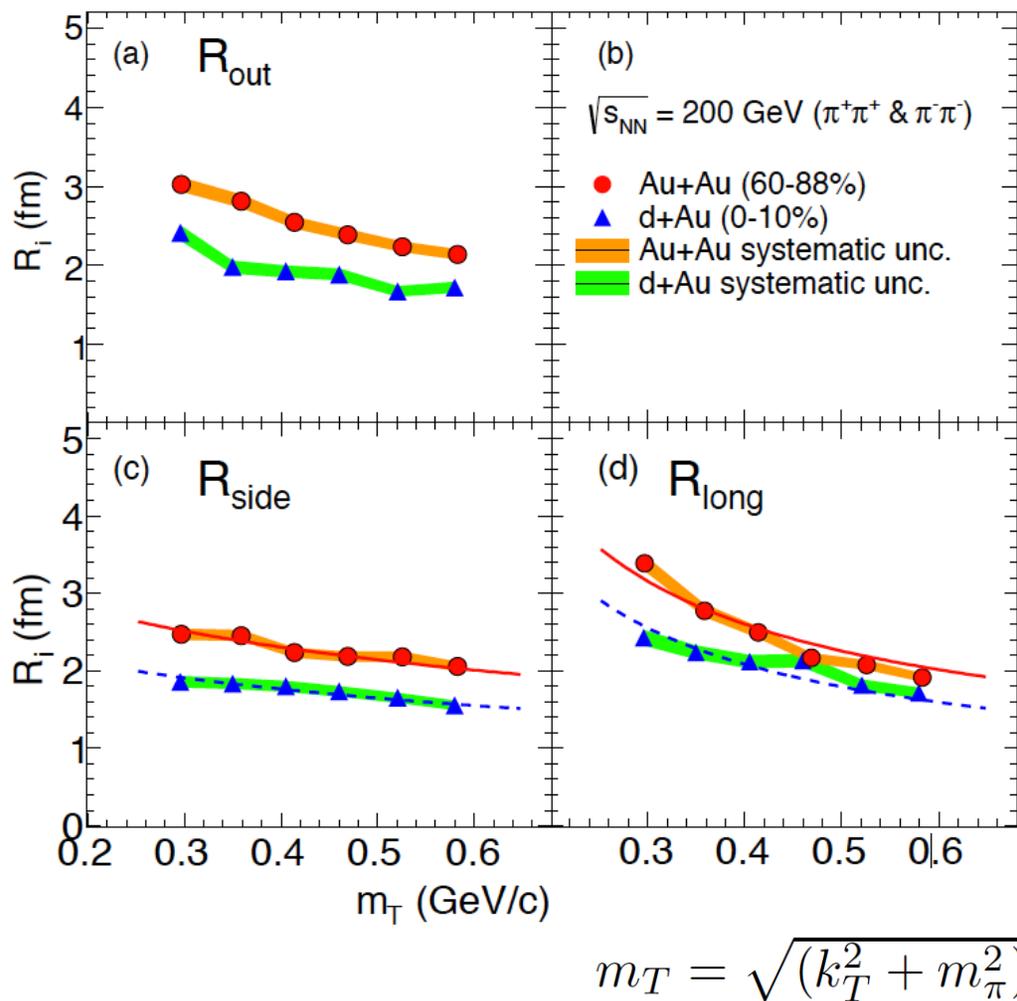
$$G(\mathbf{q}) \cong \exp(-R_{\text{side}}^2 q_{\text{side}}^2 - R_{\text{out}}^2 q_{\text{out}}^2 - R_{\text{long}}^2 q_{\text{long}}^2)$$

broader width  $\longrightarrow$  smaller HBT radius

# $m_T$ dependence of HBT radii

position-momentum correlations reduce R's  
as in PRC **70**, 044907 (2004):

arXiv:1404.5291 [nucl-ex]



- characteristic signature for expansion of emitting source of short emission duration
- indication for final-state rescattering effects in reaction dynamics for  $d+Au$

# centrality ( $N_{\text{part}}$ ) dependence of HBT radii

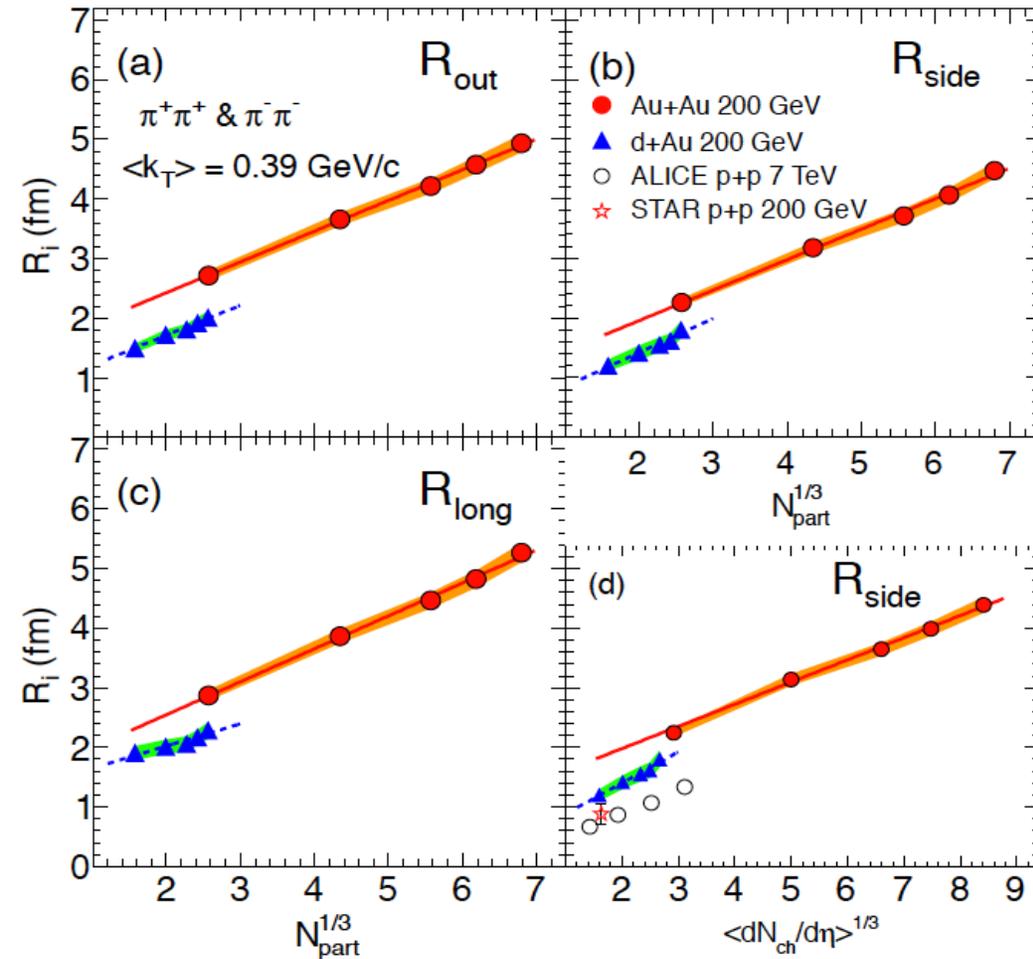
smaller transverse freeze-out size  
for  $d$ +Au emission source from blast  
wave fits as in PRC **52**, 2694 (1995):

	$d$ +Au	Au+Au
$\tau_0$ (fm/c)	$3.2 \pm 0.04 \pm 0.4$ (syst)	$3.8 \pm 0.04 \pm 0.3$ (syst)
$\chi^2/ndf$	26/5	24/5
$R_{\text{geom}}$ (fm)	$2.2 \pm 0.03 \pm 0.2$ (syst)	$2.8 \pm 0.03 \pm 0.2$ (syst)
$\chi^2/ndf$	6/5	4/5

blast wave fit functions:

$$R_{\text{side}} = R_{\text{geom}} / \sqrt{1 + \beta^2 (m_T/T)}$$

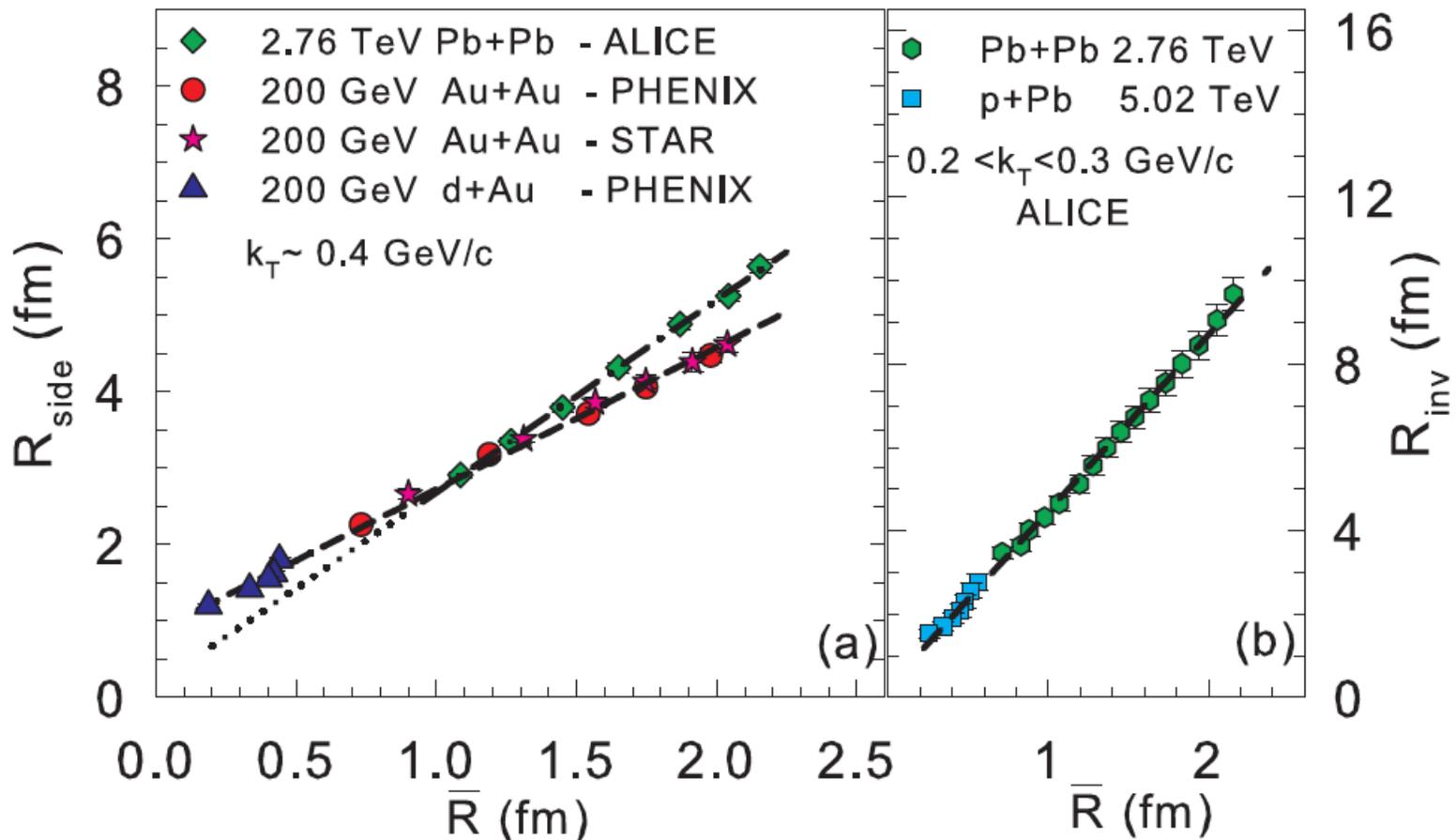
$$R_{\text{long}} = \tau_0 \sqrt{(T/m_T) [(K_2(m_T/T)) / (K_1(m_T/T))]}$$



suggests correlation between  
transverse freeze-out size and  
initial geometric size

# geometric scaling of HBT radii

arXiv:1404.5291 [nucl-ex]



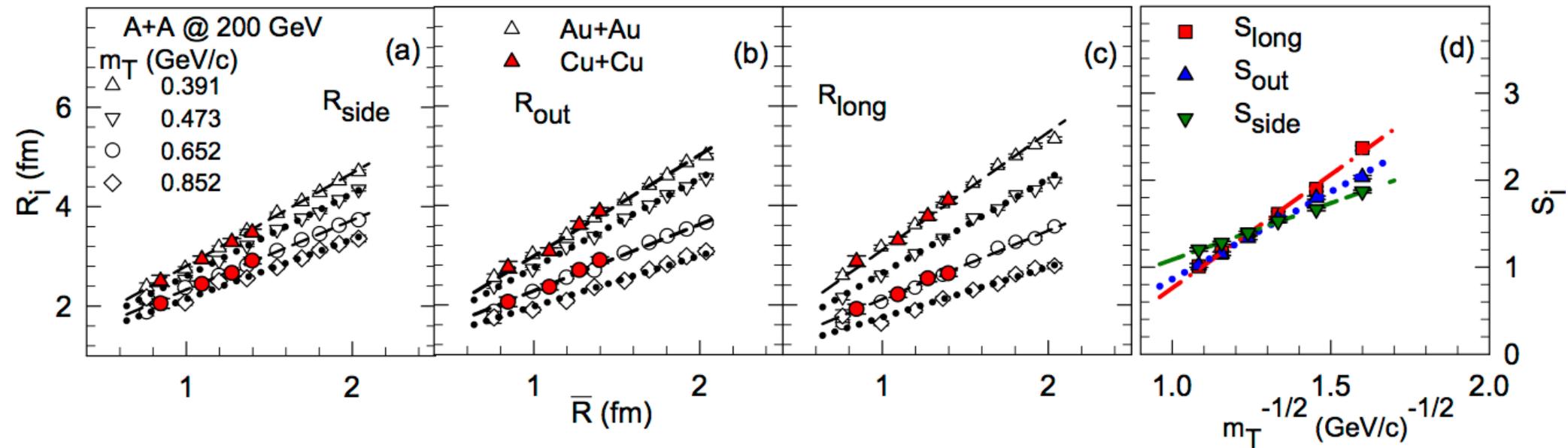
$$1/\bar{R} = \sqrt{(1/\sigma_x^2 + 1/\sigma_y^2)} \quad \sigma_x \text{ and } \sigma_y \text{ are RMS widths of density distributions}$$

- HBT radii scale with initial transverse size for both  $p(d)+A$  and  $A+A$  collisions
- larger slope corresponds to larger expansion rate for LHC data
- final state rescattering effects are important in  $p(d)+A$  collisions also

# geometric scaling of HBT radii in HI collisions

arXiv: 1408.1343 [nucl-ex]

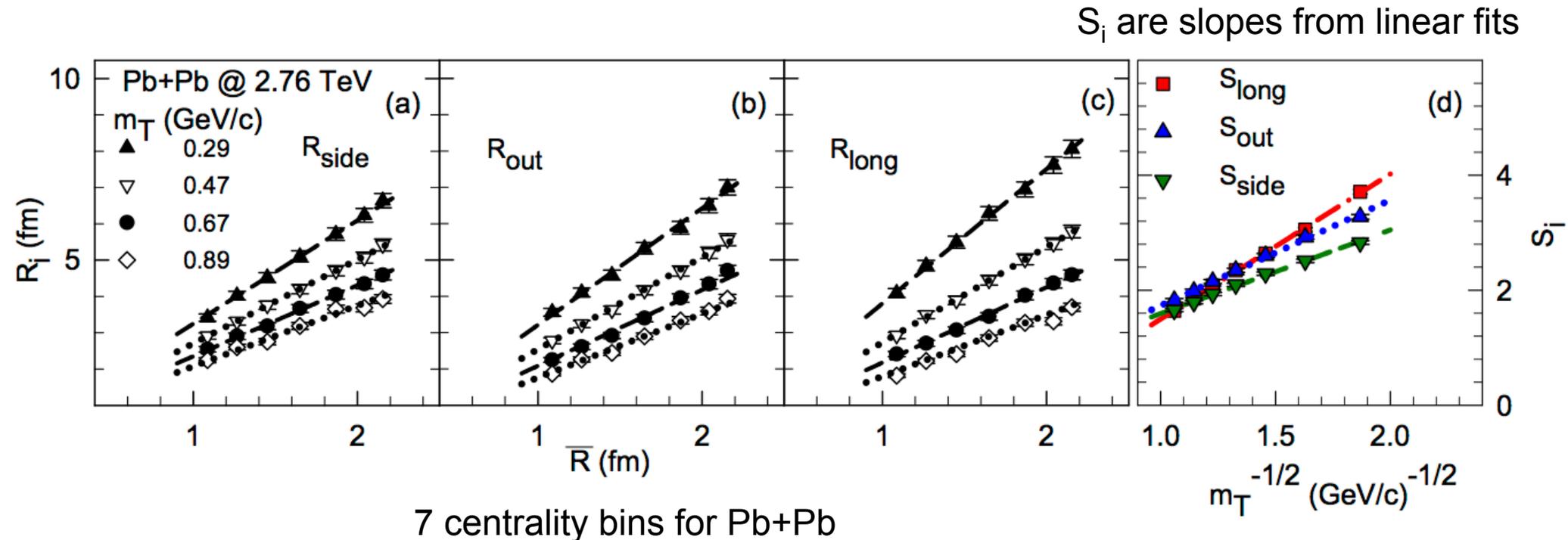
$S_i$  are slopes from linear fits



9 centrality bins for Au+Au & 4 centrality bins for Cu+Cu

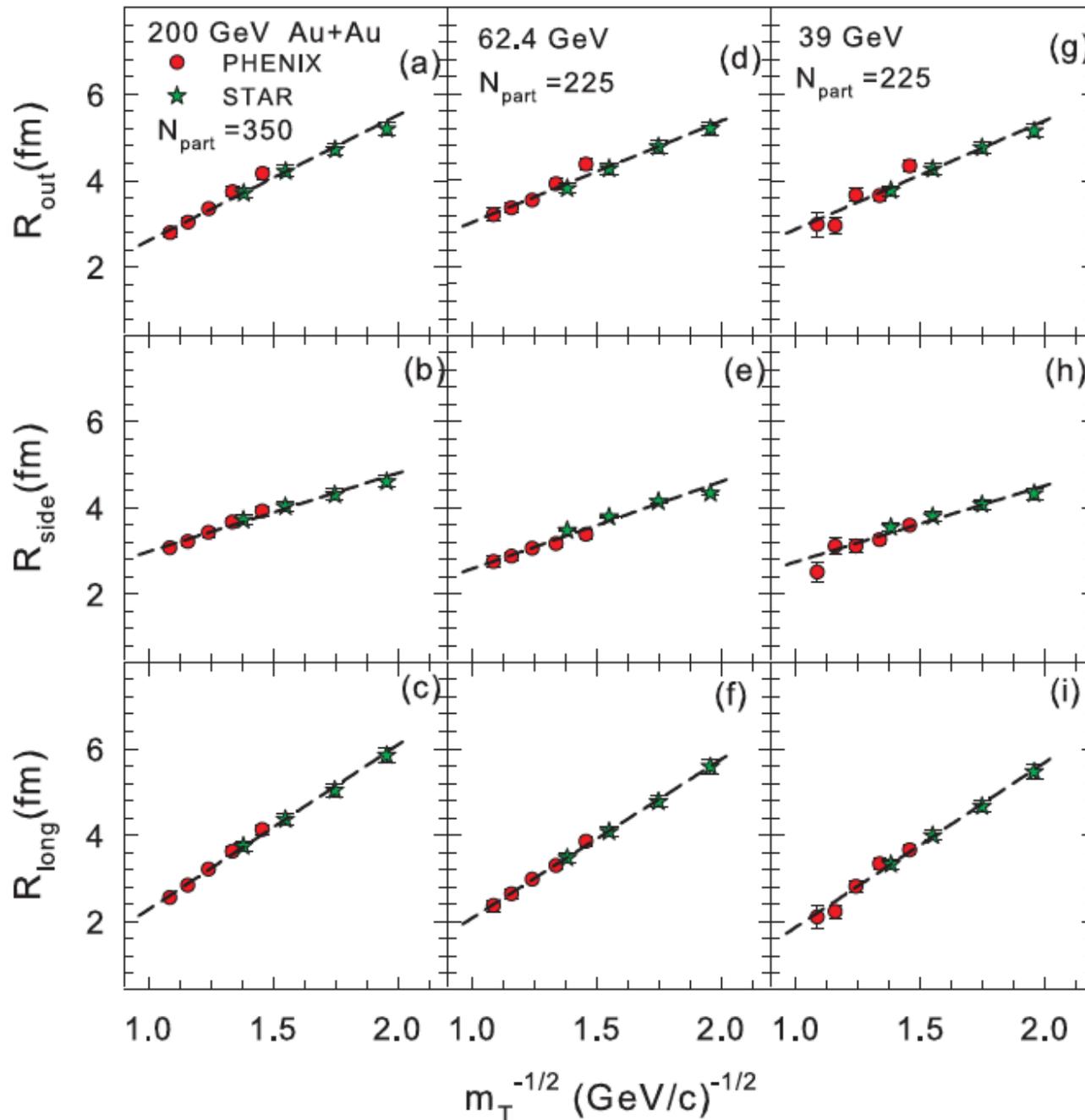
Decrease in slope with  $m_T$  confirms influence of position-momentum correlations resulting from collective expansion in HI collisions.

# geometric scaling of HBT radii in HI collisions



- larger radii at LHC due to larger emission lifetime and expansion rate
- same scaling pattern at RHIC and LHC

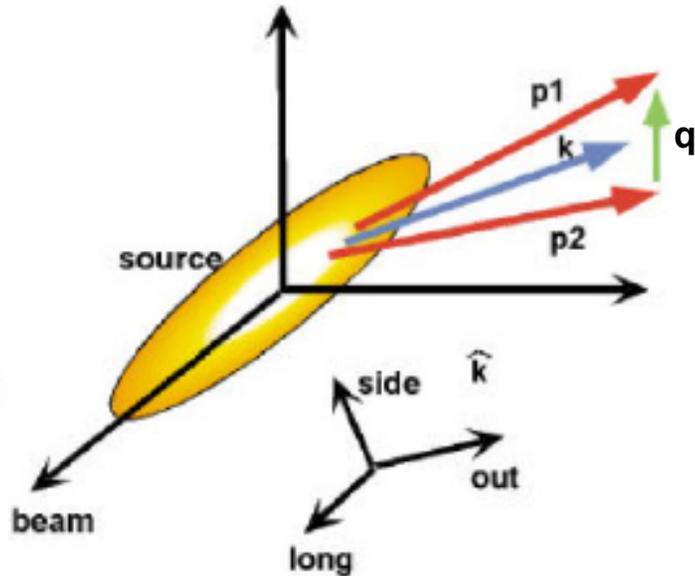
# comparison of PHENIX & STAR HBT radii



STAR data from  
arXiv:1403.4972 [nucl-ex]

- agreement between PHENIX and STAR datasets
- PHENIX data provide sizable extension in  $m_{\text{T}}$

# expansion dynamics from HBT radii



From the literature:

- ZPC **39**, 69 (1988)
- PRL **74**, 4400 (1995)
- PRL **75**, 4003 (1995)
- NPA **608**, 479 (1996)
- PRC **53**, 918 (1996)

$$R_{\text{long}} \propto \tau$$

$$(R_{\text{side}} - \sqrt{2}\bar{R})$$

$$(R_{\text{out}}^2 - R_{\text{side}}^2) \propto \Delta\tau^2$$

$$(R_{\text{side}} - \sqrt{2}\bar{R})/R_{\text{long}}$$

emission lifetime

expansion radius for small  $m_T$

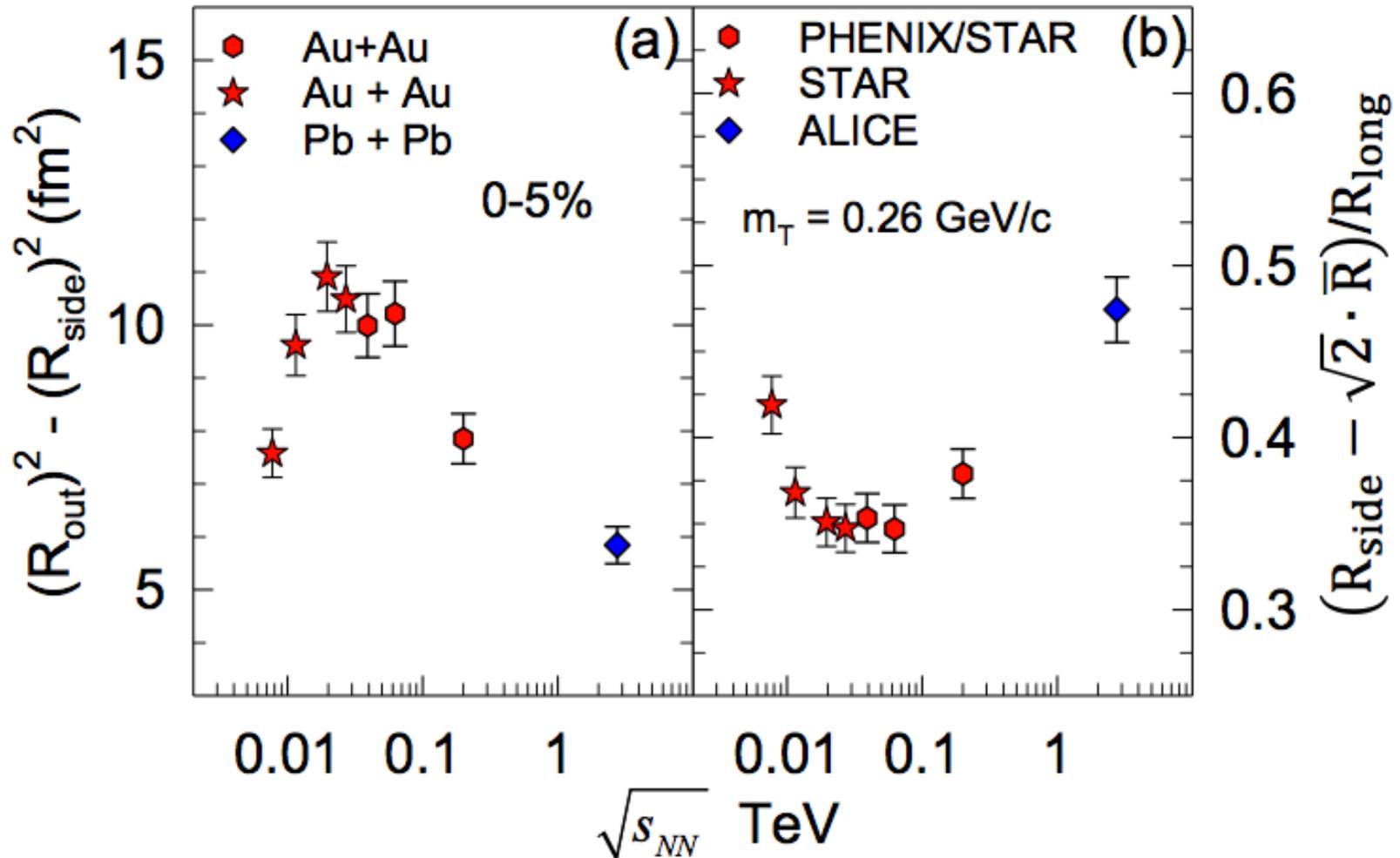
emission duration

expansion rate

An emitting system produced in the vicinity of a 1<sup>st</sup> order transition of the phase diagram for nuclear matter could show a stalling of the mean expansion speed and a longer emission duration due to a “softening” of the equation of state (resulting in  $R_{\text{out}} > R_{\text{side}}$ ).

# beam energy dependence

arXiv: 1408.1343 [nucl-ex]



Nonmonotonic behavior with a maximum in emission duration  $\Delta\tau$  and corresponding minimum in expansion rate in this beam energy range

# Summary, Outlook and Acknowledgement

- From HBT radii in  $d+Au$  collisions:
  - linear dependence of  $R_{\text{side}}$  on initial transverse size
  - smaller freeze-out size compared to Au+Au
  - final state rescattering effects are important
- From HBT radii in HI collisions:
  - nonmonotonic behavior in this beam energy range of emission duration and expansion rate
  - change in expansion dynamics in this energy range
- Improved measurement of HBT radii w.r.t. event plane during BES II at RHIC in store
- Special thanks to Alex Mwai, Ajit & Roy @ SBU