

*Pulling Apart the Strong  
Force by  
Peering Into the Proton*

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*University of Michigan*

*REU Seminar*

*July 12, 2016*

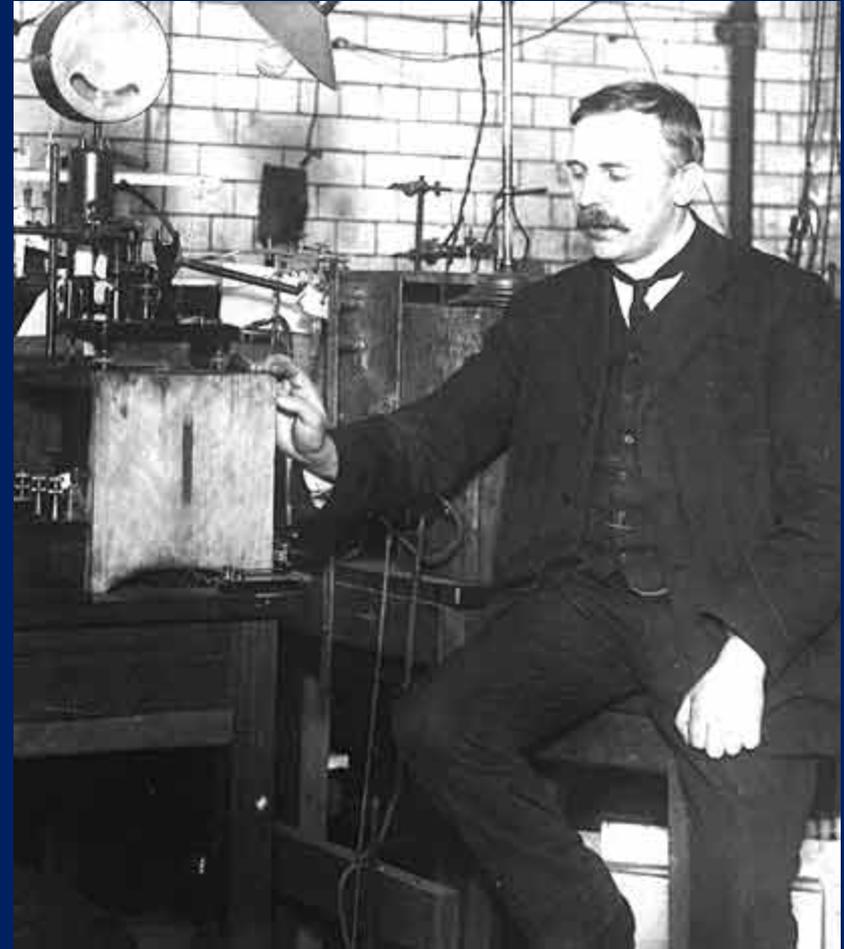
# *Probing inside atoms: mostly empty space!*

1911: Ernest Rutherford, Hans Geiger, Ernest Marsden scatter alpha particles from radioactive decay off of a thin gold foil

- Most went right through
- *But*—about 1/8000 bounced back!

“It was quite the most incredible event that has ever happened to me in my life. It was almost as incredible as if you fired a 15-inch shell at a piece of tissue paper and it came back and hit you.” - Rutherford

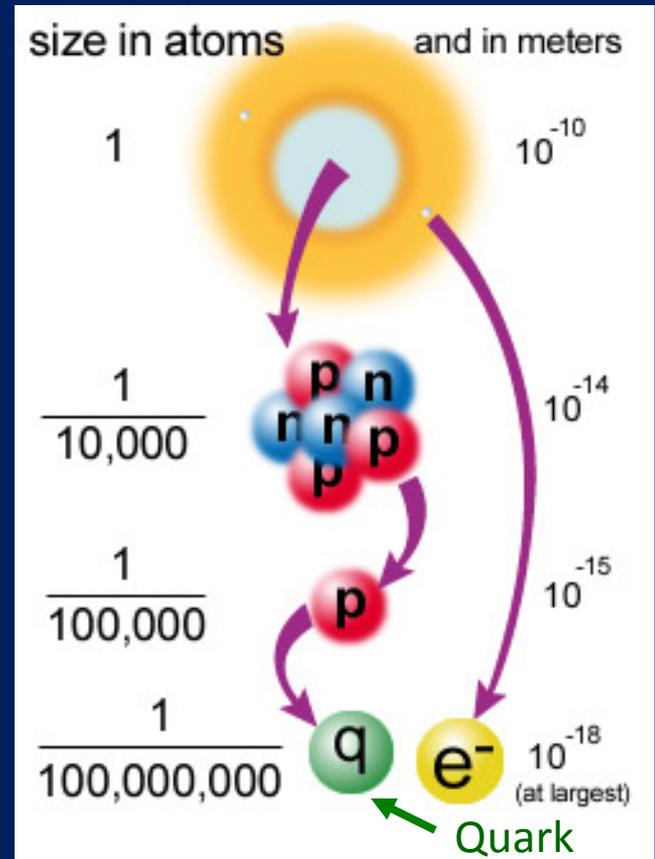
So atoms have a small, positively charged core → the nucleus



# Probing inside protons . . .

Late 1960s, Stanford Linear Accelerator Center: scatter electrons off of protons

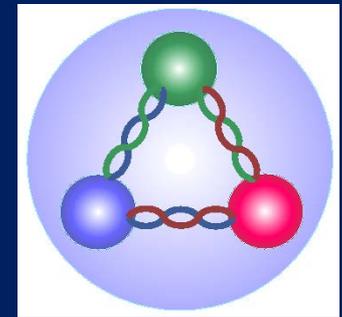
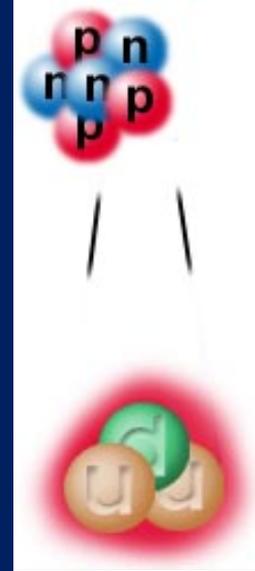
- Many bounced back sharply . . .
- But weren't bouncing off of the whole proton → subcomponents!
  - Protons *not* solid lumps of positive charge
  - Constituents that make up proton now called “quarks,” or slightly more generally, “partons”

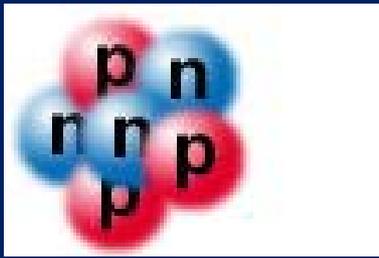


Quarks	u up	c charm	t top
	d down	s strange	b bottom

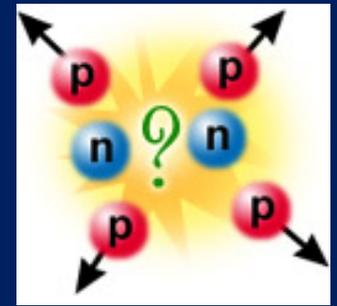
# Quark-Parton Model

- Simplest model - proton made of three “valence” quarks: 2 up “flavored” quarks and 1 down “flavored” quark
  - “Flavor” – charge that couples to the weak force
- But these quarks not completely free in nucleon
  - Bound by force-carrier particles called “gluons”
  - “Sea quarks” also present: short-lived quark-antiquark pairs from quantum mechanical fluctuations
- Hit proton with more energy  $\rightarrow$  resolve shorter-lived fluctuations: gluons and sea quarks





## *Strong force*



- How does nucleus stay together?  
Electromagnetic force should cause protons to repel one another
- Protons and neutrons interact via *strong force*, carried by gluons
  - Much stronger than electromagnetic force ( $\sim 100x$ ) and waaayyy stronger than gravity ( $\sim 10^{38}x!!$ ) (thus the name!)
  - But—very, very short range! ( $\sim 10^{-15}$  m)

# “Color” charge and Quantum Chromodynamics

- Strong force acts on particles with *color* charge
  - Quarks, plus gluons themselves! (Contrast with photons, which are electrically neutral)
- “Color” because three different “charges” combine to make a neutral particle:

red + blue + green = white

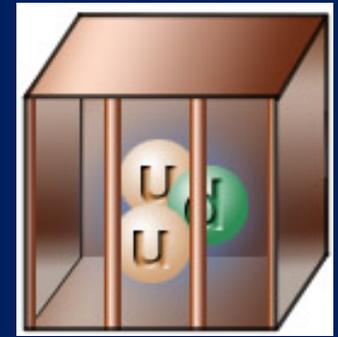
- Quantum **Chrom**odynamics (QCD)—theory describing strong force

Quarks also carry *fractional* electric charge!!

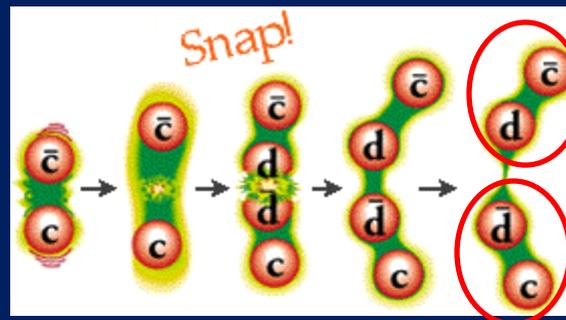
Proton = up + up + down quarks  
 $+1 = (+2/3) + (+2/3) + (-1/3)$

Neutron = down + down + up  
 $0 = (-1/3) + (-1/3) + (+2/3)$

# Quark confinement



- Never see quarks or gluons directly
  - *Confined* to composite, color-neutral particles
  - Groups of three quarks (**rgb**), called *baryons*, or quark-antiquark pairs (**red-antired**, . . .), called *mesons*
- If you try to pull two quarks apart, energy between them increases until you produce a new quark-antiquark pair (good old  $E=mc^2$ )



“D<sup>-</sup> meson”

“D<sup>+</sup> meson”

# *For more information*

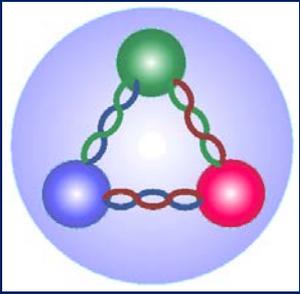
- For more info on quarks, gluons, and the strong force, see

<http://www.particleadventure.org/>

(Many pictures on previous pages borrowed from this site)

*How do we understand the visible matter in our universe in terms of the quarks and gluons described by our theory of the strong force, quantum chromodynamics?*

*How can studying QCD systems teach us more about fundamental aspects of QCD as a theory?*



## *Studying proton structure*

- If can't see individual quarks and gluons, how to determine proton structure?
- Inelastic scattering—shoot high-energy beam (e.g. of electrons) at proton to break it up, and try to understand what happens
  - Electron exchanges photon with quarks, because quarks carry electromagnetic charge as well as color

# *Probes sensitive to different length scales*



What size potholes will bother you if you're driving/riding a . . .

# *Probes sensitive to different length scales*



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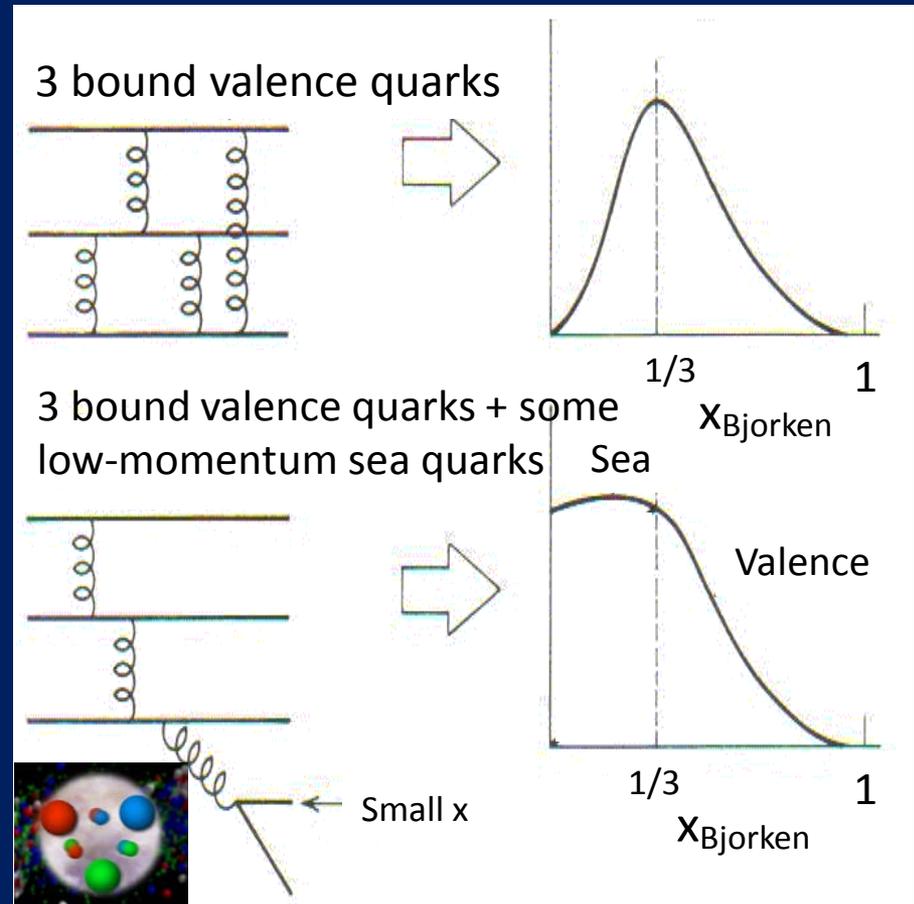
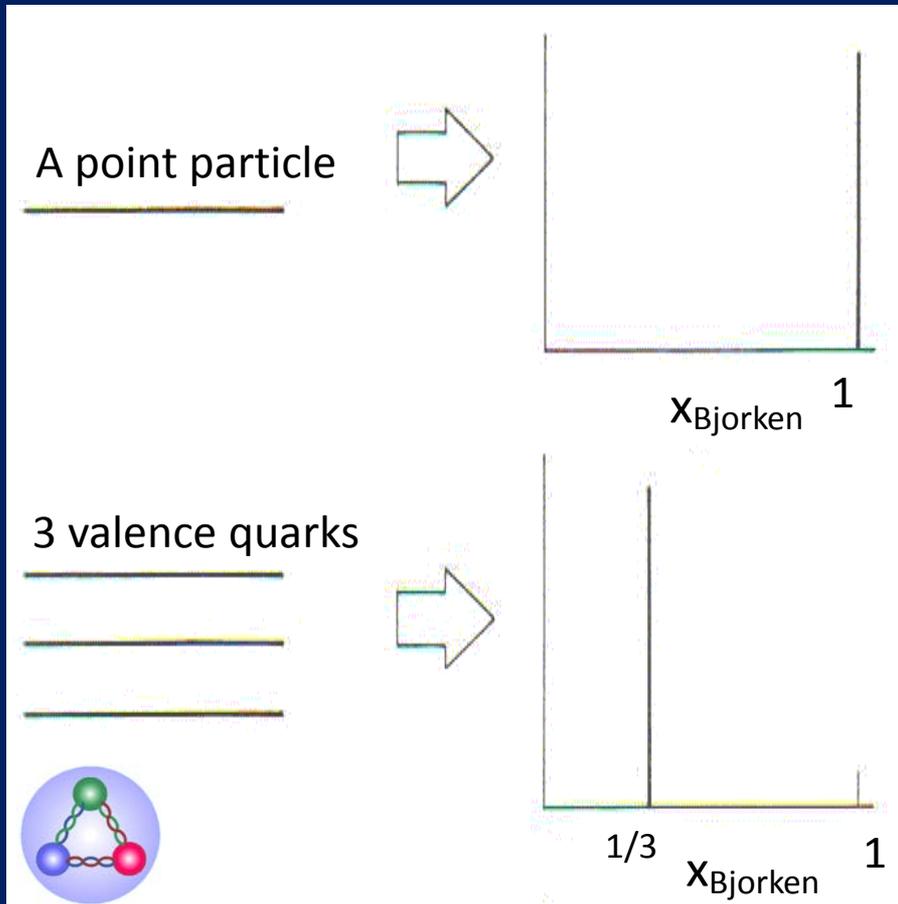


# *High-energy particle accelerators*

- *Molecular and atomic* structure of matter: study using
  - ultraviolet light (wavelengths 10-400 nanometers)
  - x-rays (wavelengths 0.01-10 nanometers)
- *Nuclei and protons*: 10,000× to 100,000× smaller than atoms → Need high-energy particle accelerators to see inside them

# Proton structure, momentum fraction, and “parton distribution functions”

What momentum fraction would the scattering particle carry if the proton were made of ...

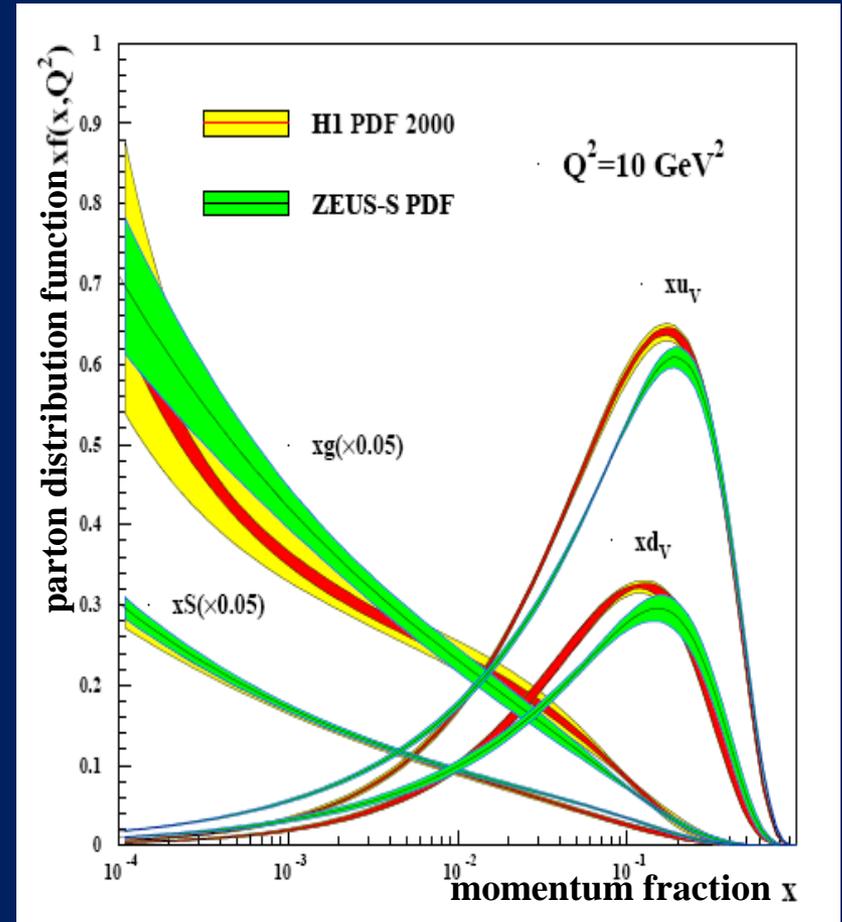


Halzen and Martin, “Quarks and Leptons”, p. 201

Christine Aidala, REU Seminar, 7/12/2016

# *So what do the parton distribution functions look like?*

- Wealth of data largely thanks to proton-electron collider, HERA, in Hamburg, Germany (1992-2007)
- Up and down valence quark distributions peaked at a little less than  $1/3$
- Lots of sea quark-antiquark pairs and even more gluons (scaled down by  $20\times$  in figure!)



PRD67, 012007 (2003)

# *What have we learned?*

- Conclusions from decades of inelastic scattering data investigating proton momentum structure:
  - 3 “valence” quarks carry (on average) the largest single momentum fractions of the proton
  - But lots of gluons and “sea” quark-antiquark pairs in the proton as well! Gluons carry ~50% of total momentum of proton

***Despite all the recent excitement about the Higgs boson, gluon interactions are actually responsible for more than 98% of the mass of the visible universe!!***

# *Mapping out the proton: Other questions to ask!*

What does the proton look like in terms of the quarks and gluons inside it?

- *Position*
- *Momentum*
- *Spin*
- *Flavor*
- *Color*

Vast majority of past four decades focused on *1-dimensional* momentum structure! Since 1990s starting to consider other directions . . .

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Polarized protons first studied in 1980s. How angular momentum of quarks and gluons add up still not well understood!

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- *Color*

Good measurements of flavor distributions in valence region. Flavor structure at lower momentum fractions still yielding surprises!

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What does the proton look like in terms of the quarks and gluons inside it?

- *Position*
- *Momentum*
- *Spin*
- *Flavor*
- *Color*

Theoretical and experimental concepts to describe and access position only born in mid-1990s. Pioneering measurements over past decade.

# *Mapping out the proton: Other questions to ask!*

What does the proton look like in terms of the quarks and gluons inside it?

- *Position*
- *Momentum*
- *Spin*
- *Flavor*
- *Color*

Accounted for by theorists from beginning of QCD, but more detailed, potentially observable effects of color have come to forefront since 2010 . . .

# What is spin?

Spin is a quantum mechanical property of fundamental particles or combinations of particles.

It's called "spin" because it's a type of angular momentum and is described by equations treating angular momentum.

The units of angular momentum are the same as Planck's constant,  $\hbar$ , and can only have values that are integer : 0, 1, 2, 3, . . .  
or half-integer: 1/2, 3/2, 5/2, . . .



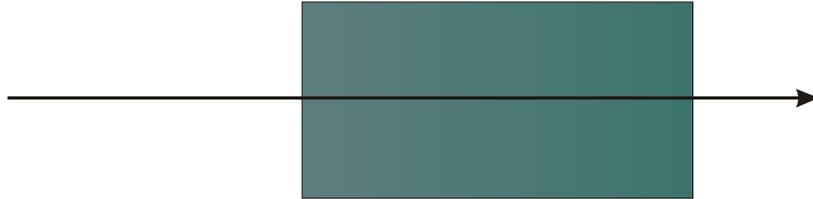
Quarks, like protons, have spin 1/2.

In a magnetic field, different spin states have different energies but have the same magnitude of the angular momentum.

*Proton spin is what makes the medical diagnostic technique of MRI possible!*

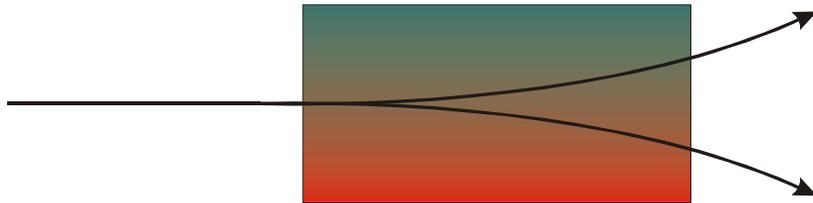
# Stern-Gerlach experiment

Any  
particle  
with spin



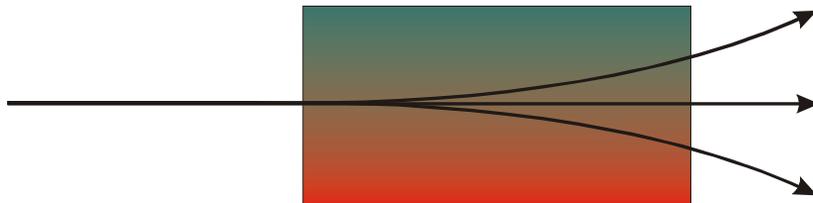
$$\frac{\partial \mathbf{B}}{\partial z} = 0$$

Spin  $\frac{1}{2}$  particle  
(e.g.  $^{107}\text{Ag}$  or  
 $^1\text{H}$ )



$$\uparrow \frac{\partial \mathbf{B}}{\partial z} \neq 0$$

Spin 1 particle  
(e.g.  $^2\text{H}$ )



$$\uparrow \frac{\partial \mathbf{B}}{\partial z} \neq 0$$

Spin  $\frac{3}{2}$   
particle (e.g.  
 $^7\text{Li}$ )



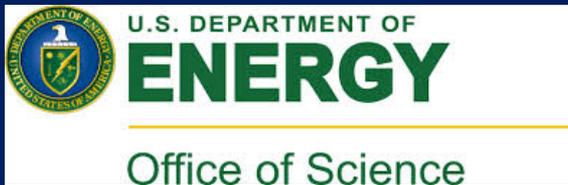
$$\uparrow \frac{\partial \mathbf{B}}{\partial z} \neq 0$$

Apply a magnetic field

$2s+1$  Energy Levels

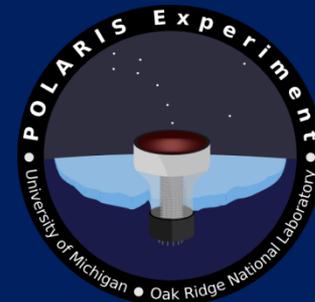
# *My current research efforts*

- Spin-momentum correlations within the proton
  - Can think of as quantum mechanical spin-orbit couplings
- Searching for experimental evidence of an exciting recent prediction of *quantum color entanglement* of quarks across two colliding protons
- Studies for light sensing and electronics for calorimeters of proposed large new experiment
- R&D for a novel neutron detector



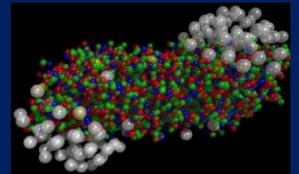
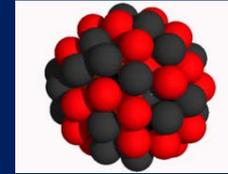
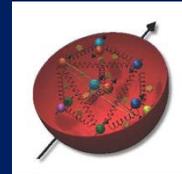
# My experiments

- Polarized proton-proton collisions to a variety of final states at the PHENIX experiment at Brookhaven National Lab (BNL) on Long Island, NY
  - Very flexible, multi-purpose experiment
  - “sPHENIX” is proposed follow-up experiment
- Quark-antiquark annihilation to muon pairs at the SeaQuest experiment at Fermilab outside Chicago
  - Dedicated measurement of simple final state—doesn’t carry color! (Muons are like heavy electrons)
- POLARIS neutron detector R&D experiment



# *The Relativistic Heavy Ion Collider at Brookhaven National Laboratory*

- A great place to be to study QCD!
- An accelerator-based program, but not designed to be at the energy (or intensity) frontier. More closely analogous to many areas of condensed matter research—create a system and study its properties!
- What systems are we studying?
  - “Simple” QCD bound states—the proton is the simplest stable bound state in QCD (and conveniently, nature has already created it for us!)
  - Collections of QCD bound states (nuclei, also available out of the box!)
  - QCD deconfined! (“quark-gluon plasma”, some assembly required!)

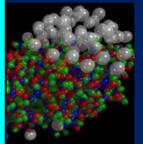


# *The Relativistic Heavy Ion Collider at Brookhaven National Laboratory*

- A great place to be to study QCD!
- An accelerator-based program, but not designed to be at the energy (or intensity) frontier. More closely analogous to many areas of condensed matter research, create a

***Understand more complex QCD systems within  
the context of simpler ones***

→ RHIC was designed from the start as a *single* facility capable of nucleus-nucleus, proton-nucleus, and proton-proton collisions



able

- Collections of QCD bound states (nuclei, also available out of the box!)
- QCD deconfined! (“quark-gluon plasma”, some assembly required!)

# *RHIC at Brookhaven National Laboratory*

Long Island,  
New York



# *RHIC at Brookhaven National Laboratory*

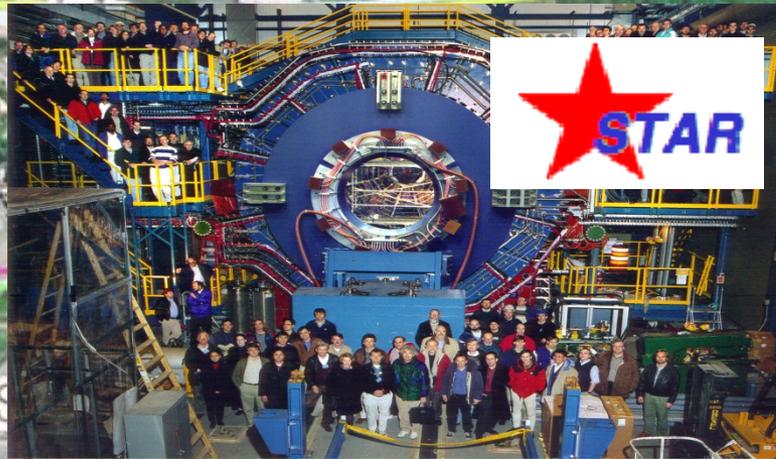
Long Island,  
New York



# *RHIC's experiments*



Just finished taking data June 27, after 16 years of running!



# PHENIX

**14 Countries; 74 Institutions;  
~500 Participants**



# PHENIX Detector

## Philosophy:

- ✓ Fast data acquisition & high granularity
- Trade-off area covered

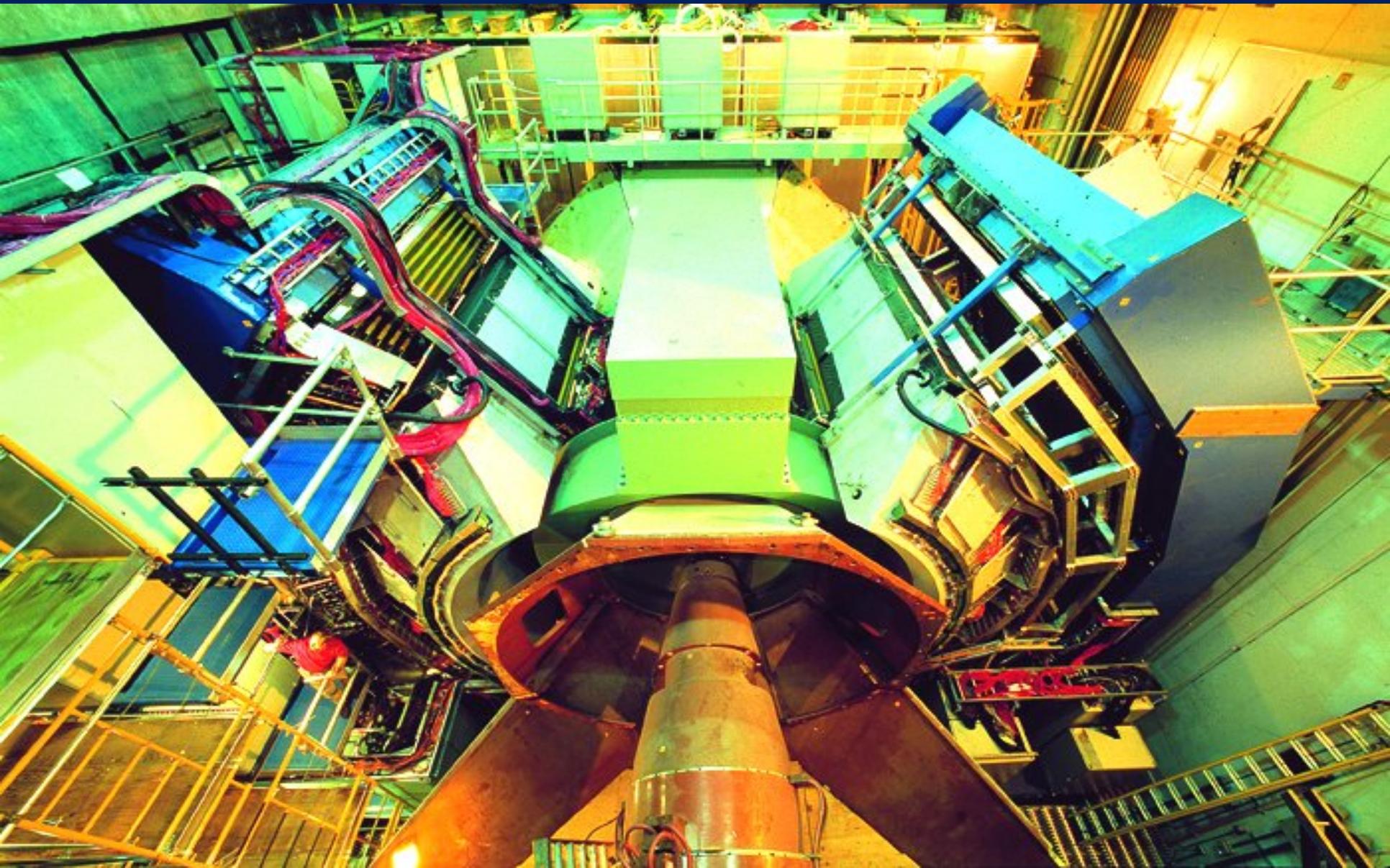


2 central arms  
- Track charged particles and detect electromagnetic processes

2 forward muon arms  
- Identify and track muons

2 forward electromagnetic calorimeters

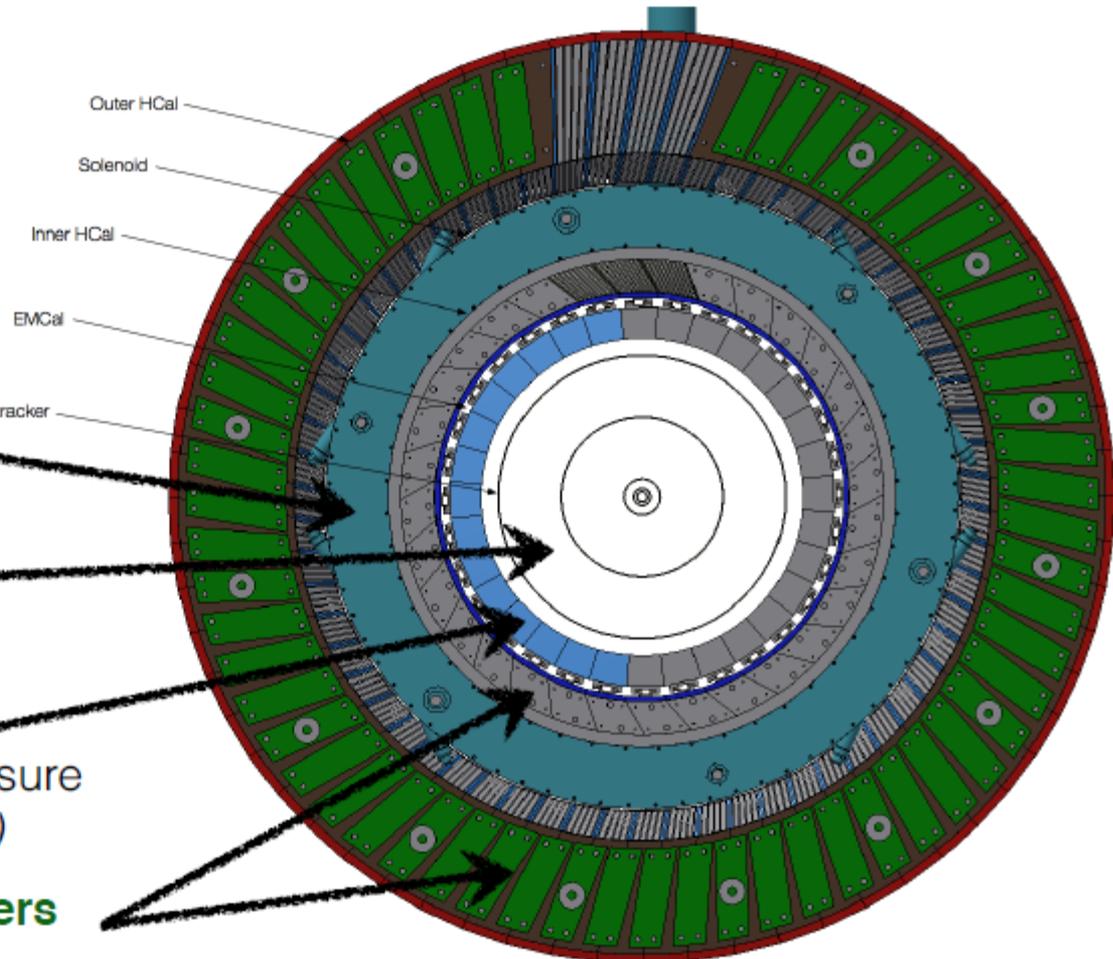
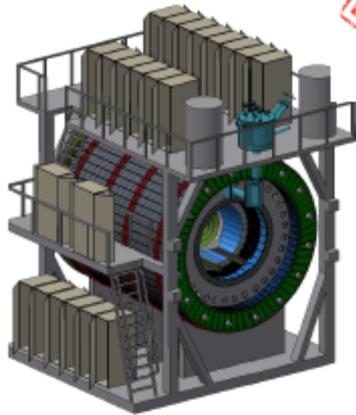
# *PHENIX Detector*



# Proposed *s*PHENIX detector



## Detector design



- 1.5 Tesla **magnet** from BaBar epxt.
- **vertex / tracker** (to measure *charged particles*)
- **electromagnetic calorimeter** (to measure *photons & electrons*)
- **hadronic calorimeters** (to measure *jets*)

# *Officially became new RHIC collaboration in 2015 – Efforts ramping up!*



**superconducting magnet**  
arriving at BNL, January 2016

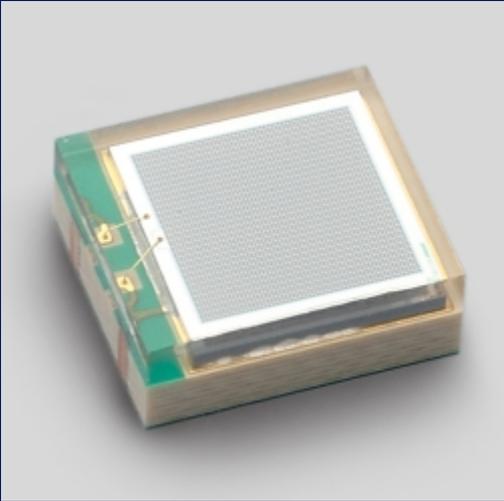


**EM+HCal** prototype,  
April 2016 beam tests



**inaugural sPHENIX Collaboration**  
Meeting December 2015

# *Silicon photomultipliers for sPHENIX*



Silicon photomultipliers (SiPMs) are new single-photon sensor technology

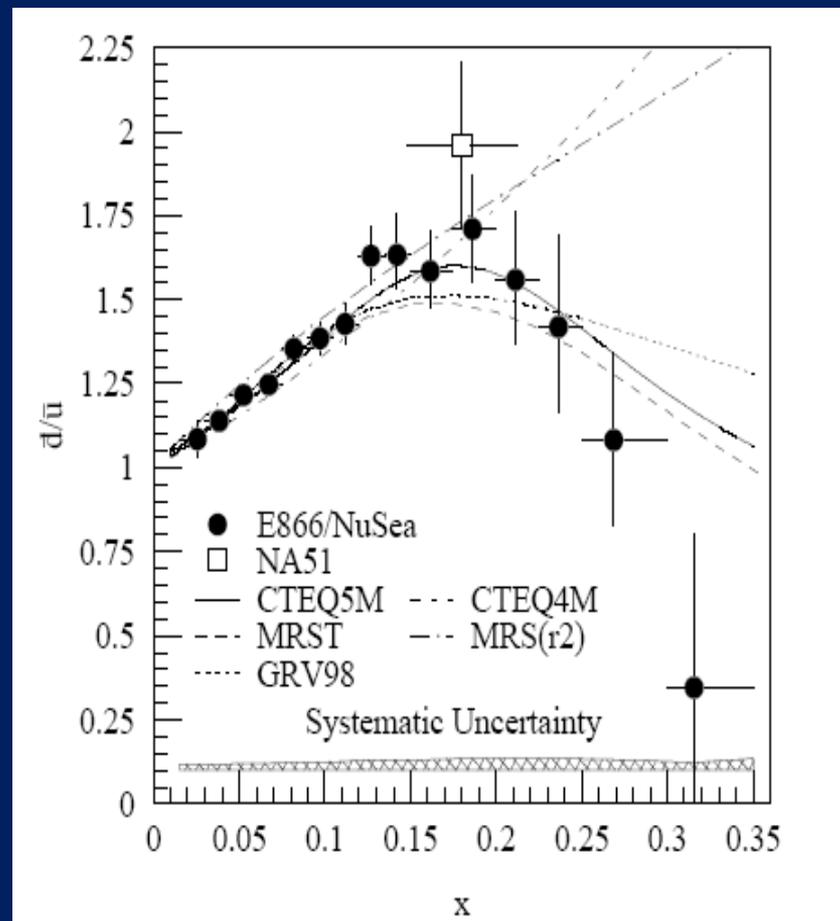
- Advantages compared to photomultiplier tubes (PMTs):
  - Insensitive to magnetic fields
  - Smaller → more flexible geometry
  - Lower operating voltage:  $<100$  V instead of  $>1000$  V
- Disadvantages:
  - Damaged in high-radiation environments
  - Temperature-dependent
- Will use SiPMs to collect light generated by electromagnetic and hadronic showers in the sPHENIX calorimeters

# 2001: A surprising discovery in the proton flavor structure

- Fermilab Experiment NuSea used proton-hydrogen and proton-deuterium collisions to probe nucleon structure via the Drell-Yan process

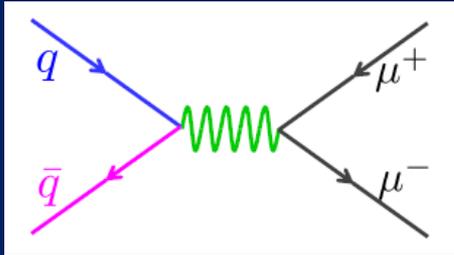


- Anti-up/anti-down asymmetry in the quark sea!
  - Previously expected to be ~constant at 1
  - Implies antiquarks not just generated by “perturbative” gluon splitting to quark-antiquark pairs

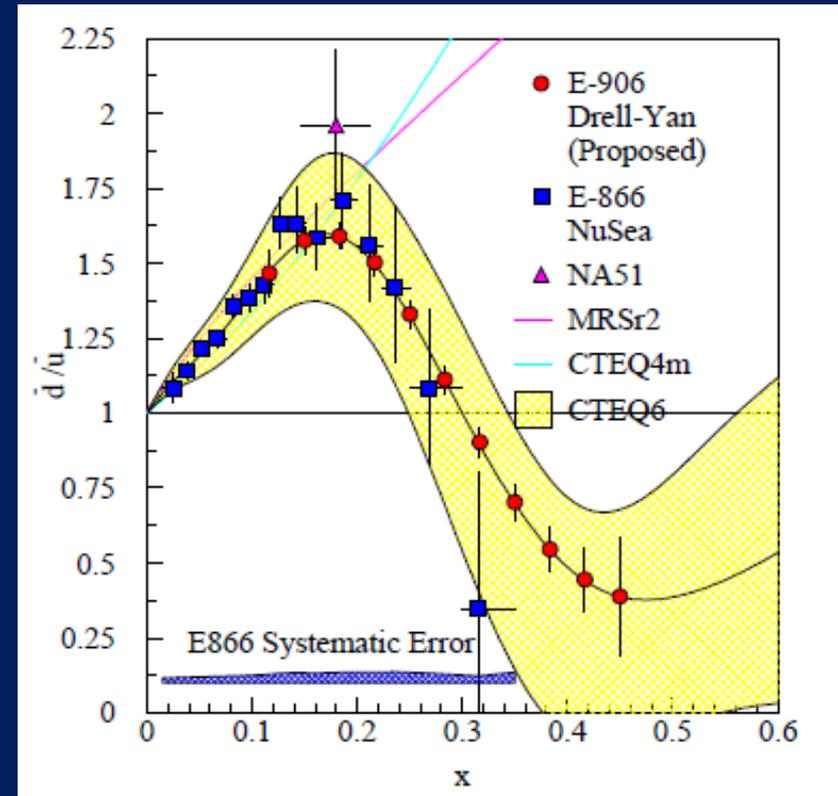


PRD64, 052002 (2001)

# *Fermilab SeaQuest: To understand this flavor structure better*



- Follow-up experiment to Fermilab NuSea with main goal of extending measurements to higher momentum fraction  $x$
- 120 GeV proton beam from Fermilab Main Injector + proton, deuteron (proton+neutron), and nuclear targets (C, Fe, W)

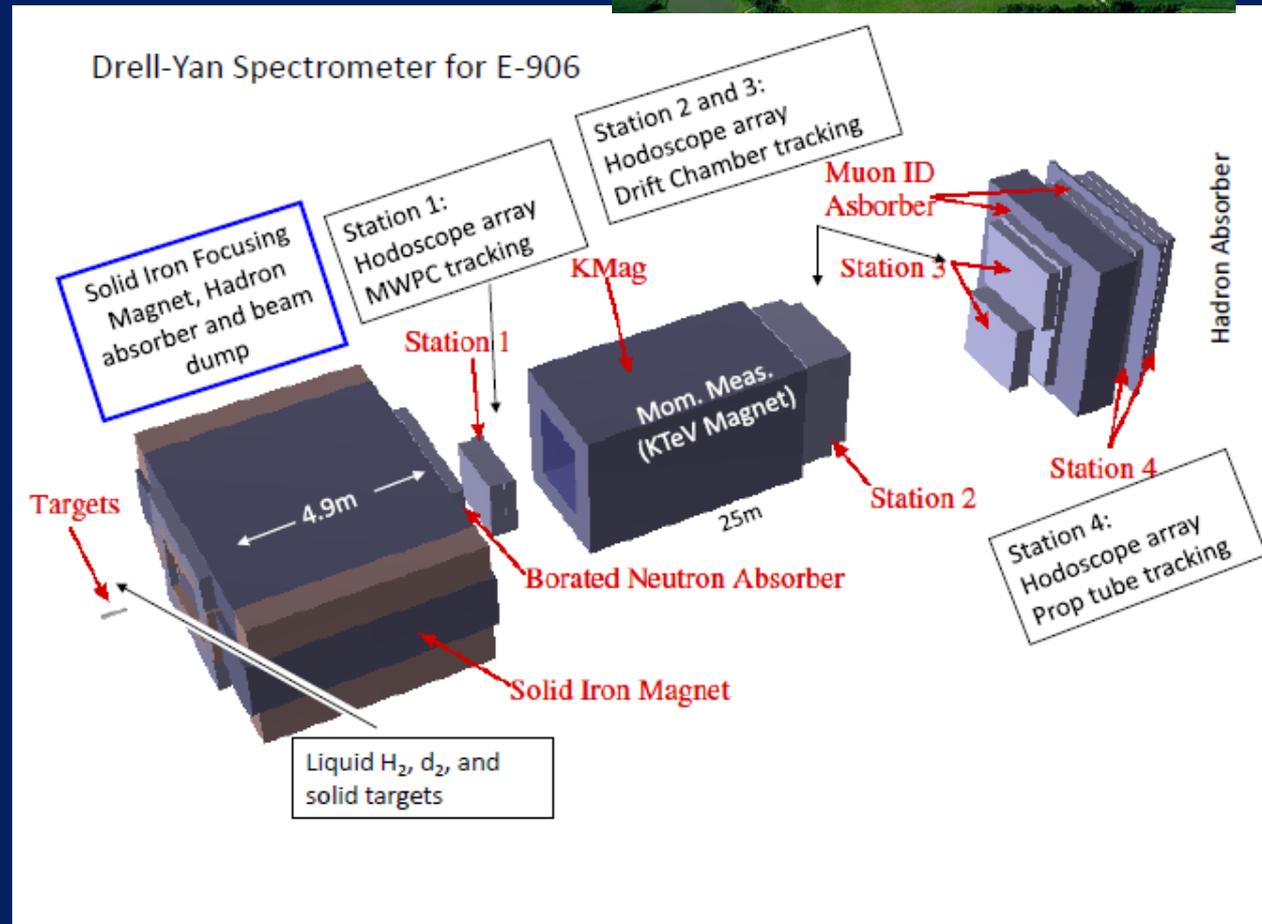


# *Fixed-target (SeaQuest) vs. collider (PHENIX/sPHENIX) experiments*

- Earliest experiments studying proton structure used electron beams to probe stationary (“fixed”) proton targets (think of tube of hydrogen gas)
  - Typically easier and cheaper to perform fixed-target experiments
- Collider experiments allow you to reach higher energy
  - Can use different theoretical tools to interpret results (“perturbative QCD”)
  - Can produce heavier particles ( $E=mc^2$  again!)
  - Can access different kinematic region (e.g. lower momentum fraction,  $x_{Bjorken}$ )

# Fermilab SeaQuest

- Targets: Liquid hydrogen and deuterium (U-M responsibility!), and C, Fe, W nuclei
- Commissioned 2012, physics data-taking 2014-17
- ~65 participants from 14 institutions

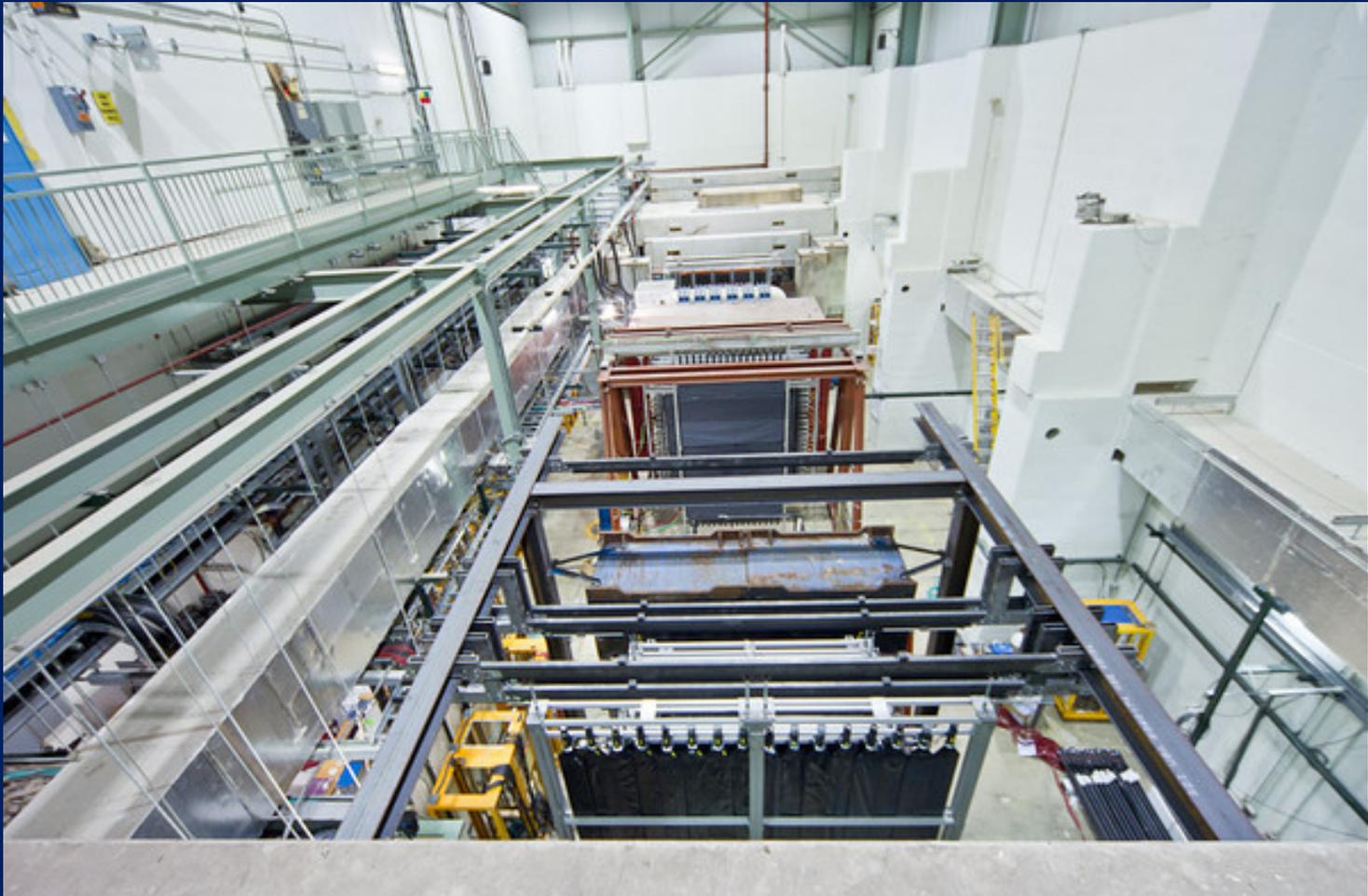


# *SeaQuest model: Reuse, recycle!*

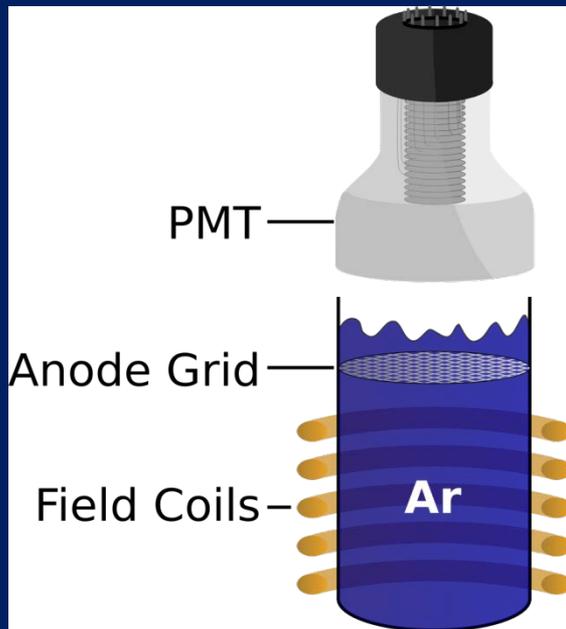
Station 4  
tracking plane  
assembled from  
old proportional  
tubes scavenged  
from LANL  
“threat  
reduction”  
experiments!



# *View of SeaQuest experimental hall from downstream platform*



# *POLARIS: A scintillating liquid argon time projection chamber for neutron detection*

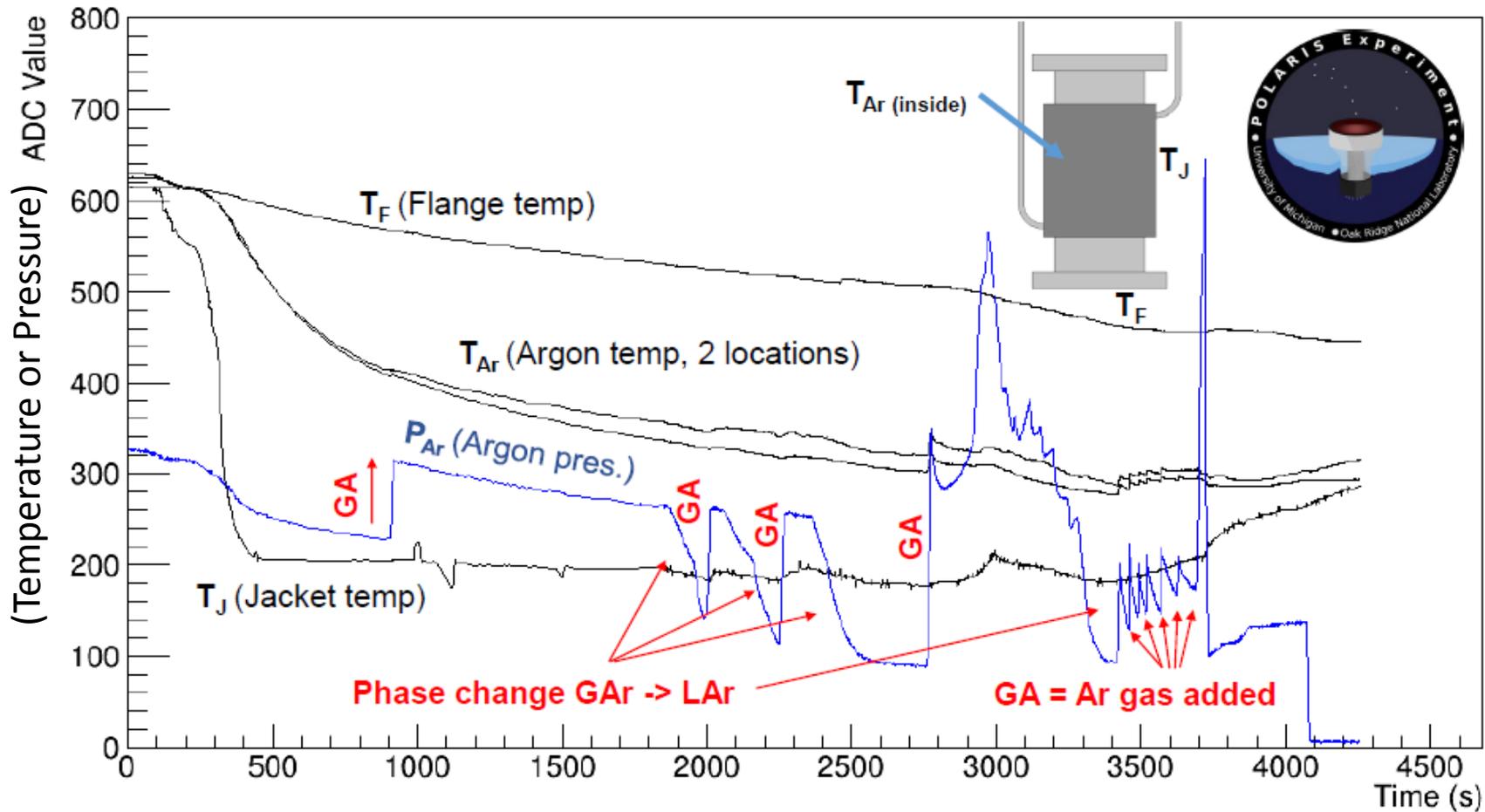


- Adapting existing technology used by neutrino and dark matter communities to optimize for neutron detection
- Neutron strikes Ar nucleus, knocking off some electrons and exciting others
  - Recoil Ar creates additional ionization and excitation
- Excited electrons return to ground state, emitting scintillation light, collected by a photomultiplier tube
- Ionization electrons are drifted by an external electric field to an anode charge collection grid
- Amount of light plus charge collected gives neutron energy
- Time difference between light and charge collection in combination with known electric field gives position of neutron-Ar collision along field direction
- In collaboration with nuclear astrophysics group at Oak Ridge National Lab



Liquid argon, boiling

# Temperature and pressure as argon is liquefied



# *Undergraduate group members*

- Meghan Tanner – sPHENIX silicon photomultiplier test stand setup, sPHENIX simulations
- Puyang Ma – SeaQuest statistical uncertainty checks, background simulations
- Emily Camras – reconstruction of simulated jets in PHENIX; POLARIS neutron detector
- Nick Kamp – POLARIS neutron detector
- Ezra Lesser – POLARIS neutron detector

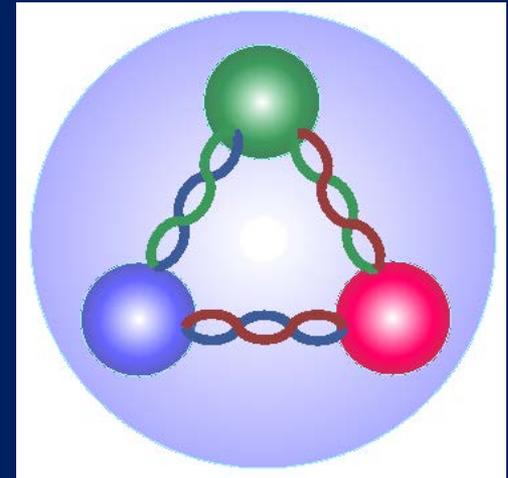
# Summary

- We still have a ways to go from the quarks and gluons of the theory of the strong force to full descriptions of the protons and nuclei of the world around us!
- Since the late 1990s things have been developing rapidly as we've discovered new questions we can ask about proton structure and have come up with ideas to perform relevant measurements
- Different experiments at BNL, Fermilab, and other world facilities are working to unravel the mysteries of the proton . . .
  - And with new detectors, we'll be able to learn even more!

# *Extra*

# *Nucleon structure: The early years*

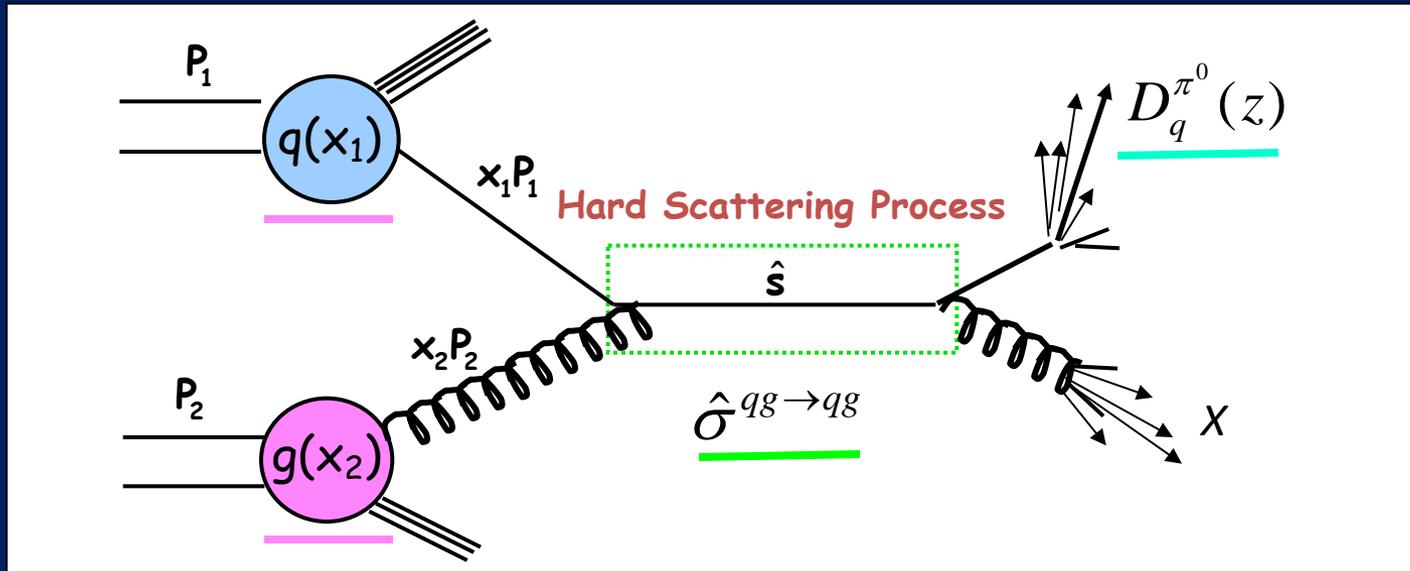
- 1932: Estermann and Stern measure proton anomalous magnetic moment  
→ proton not a pointlike particle!
- 1960s: Quark structure of the nucleon
  - SLAC inelastic electron-nucleon scattering experiments by Friedman, Kendall, Taylor → Nobel Prize
  - Theoretical development by Gell-Mann → Nobel Prize
- 1970s: Formulation of QCD . . .



## *Proton-proton scattering vs. electron-proton scattering*

- Studying the proton by breaking it up with another proton is much more complicated than probing it with an electron beam!
  - Two composite objects colliding and breaking up
- Rely on some input from experiments performed in simpler systems
- One specific advantage: *Direct access to gluons*, which cannot be probed directly via electron beams (no electromagnetic charge)

# Predictive power of perturbative QCD



$$\sigma(pp \rightarrow \pi^0 X) \propto \underline{q(x_1)} \otimes \underline{g(x_2)} \otimes \underline{\hat{\sigma}^{qg \rightarrow qg}(\hat{s})} \otimes \underline{D_q^{\pi^0}(z)}$$

High-energy processes have predictable rates given:

- Partonic hard scattering rates (calculable in pQCD)
- Parton distribution functions (need experimental input)
- Fragmentation functions (need experimental input)

} Universal non-perturbative factors

# *Factorization and universality in perturbative QCD*

- Need to systematically *factorize* short- and long-distance physics—observable physical QCD processes always involve at least one long-distance scale (confinement)!
- Long-distance (i.e. non-perturbative) functions need to be *universal* in order to be portable across calculations for many processes (and to be meaningful in describing hadron structure!)

# *Factorization and universality in perturbative QCD*

- Need to systematically *factorize* short- and long-distance physics—observable physical QCD processes always involve at least one long-distance scale (confinement)!
- Measure observables sensitive to parton distribution functions (pdfs) and fragmentation functions (FFs) in many colliding systems over a wide kinematic range → constrain by performing *simultaneous fits to world data*

# PHENIX detector

## Philosophy:

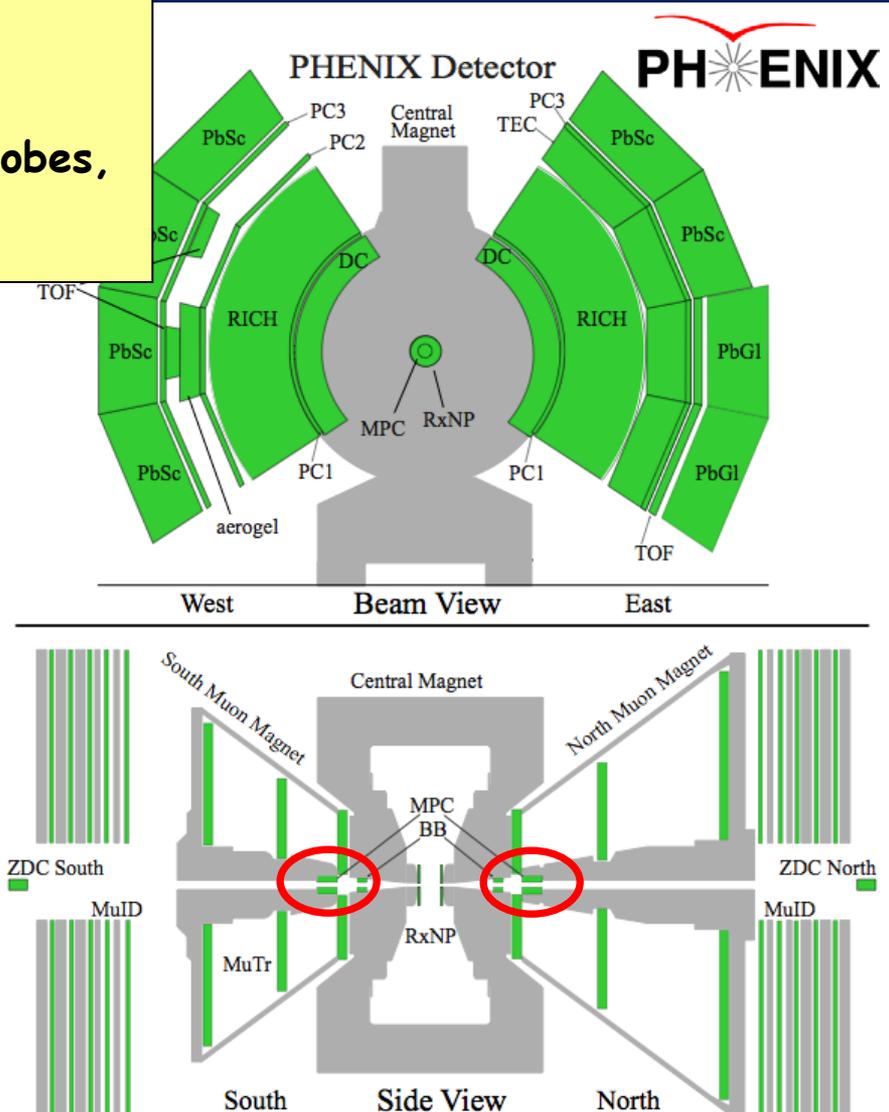
High rate capability to measure rare probes,  
limited acceptance.

- 2 central spectrometers
  - Track charged particles and detect electromagnetic processes

$|\eta| < 0.35$   
 $90^\circ + 90^\circ$  azimuth
- 2 forward muon spectrometers
  - Identify and track muons

$1.2 < |\eta| < 2.4$   
 $2\pi$  azimuth
- 2 forward calorimeters (as of 2007)
  - Measure forward pions, etas

$3.1 < |\eta| < 3.7$   
 $2\pi$  azimuth
- Relative Luminosity
  - Beam-Beam Counter (BBC)
  - Zero-Degree Calorimeter (ZDC)



# *Gold-Gold Collision in PHENIX Central Arms*

Thousands of tracks!

Proton-proton collisions only produce ~5-10 tracks at the energies I study



# *First and only polarized proton collider*

Broadcast Messages - Nucleon

RHC Experimenter Status	Beam Lifetime 1358.25 588
BRAHMS (ZDC): 0.00	PHENIX (ZDC): 3.21
STAR (ZDC): 0.20	PHOBOS (ZDC): 5.41

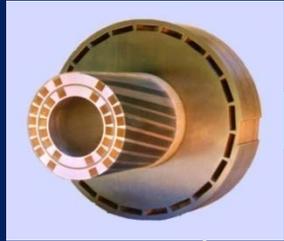
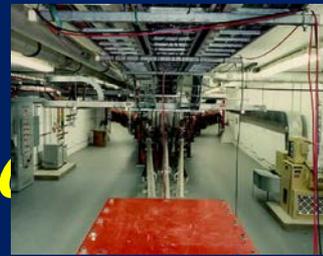
Tuesday December 11, 2001

2230: Significant polarization has been measured in RHIC, at 100 GeV

MACHINE



# RHIC polarized collider

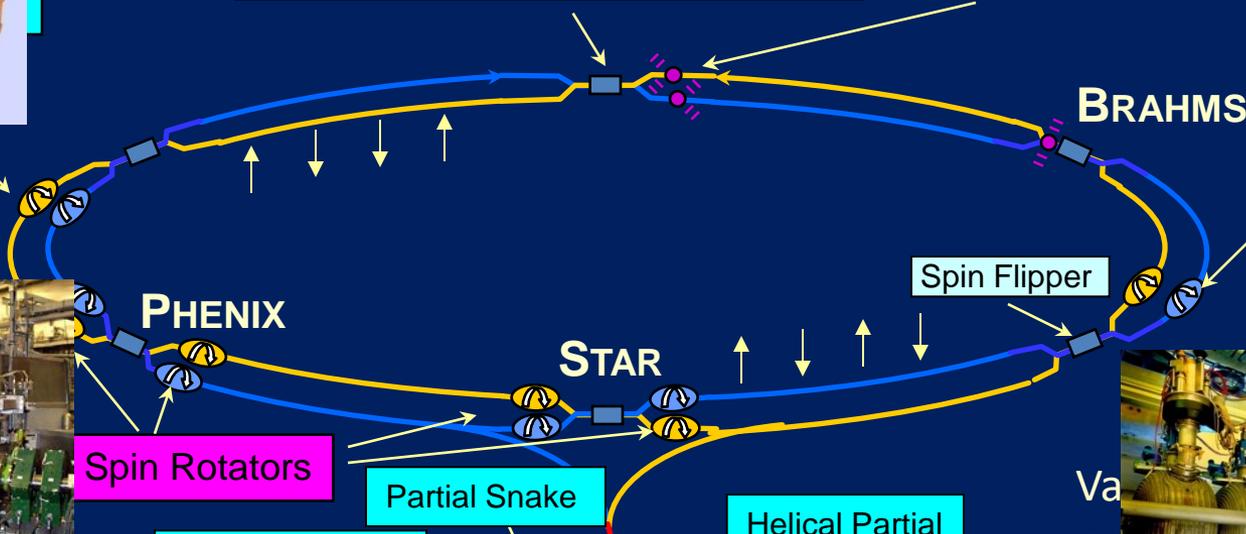


Absolute Polarimeter (H jet)

RHIC pC Polarimeter



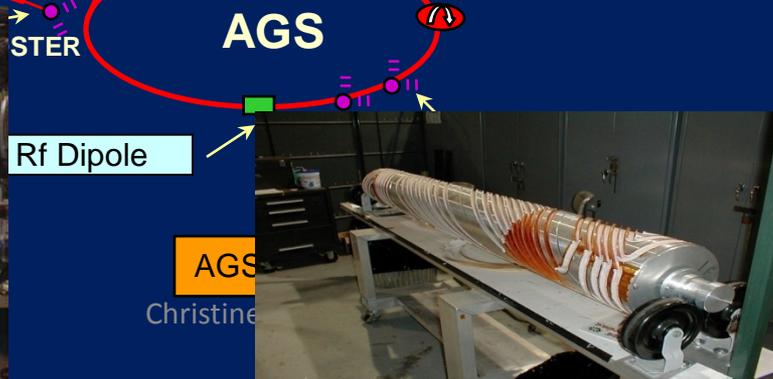
Siberian Snakes



Polarized Source



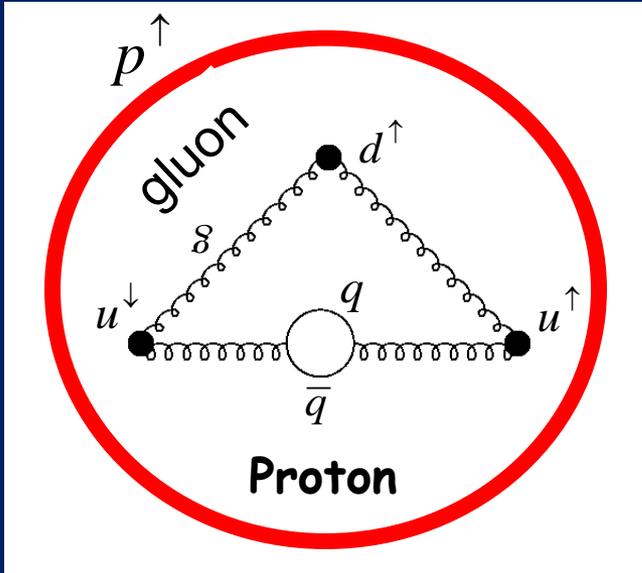
Variable magnetic field for high acceleration and storage



AGS Rf Dipole  
Christine



# The Proton Spin Crisis



Say you have a proton with total spin  $+1/2$  along some axis. You'd expect it to contain two quarks with spin  $+1/2$  and one with spin  $-1/2$ .  
 $1/2 + 1/2 - 1/2 = +1/2$

Surprising data from late 1980s!

1987: Only 12%  $\pm$  16% of proton's spin carried by quarks' spins!

## The Proton Spin Crisis begins!!

The rest now expected to be from gluon spin and orbital angular momentum of quarks and gluons, but this hasn't been easy to measure!

Spin

$$\frac{1}{2} = \frac{1}{2} \Delta\Sigma + \Delta G + L_z$$

Quark Spin      Gluon Spin

Orbital Angular Momentum

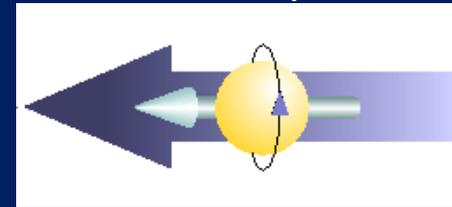
# Polarized Parton Distribution Functions

- Describe spin structure in terms of *polarized* parton distribution functions
- Helicity distributions—*difference* in probability of scattering off of a quark or gluon with *same vs. opposite helicity* of proton

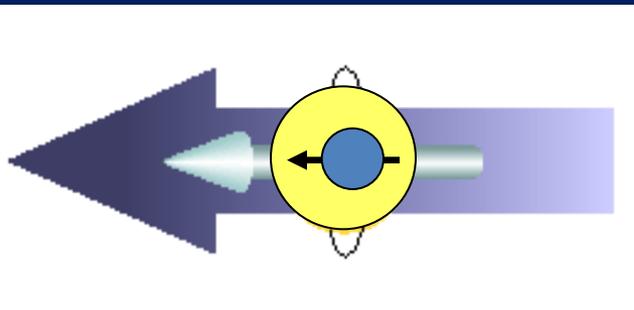
Helicity: Projection of spin vector onto momentum vector for particles polarized longitudinally, i.e. parallel to direction of motion.

Either positive or negative.

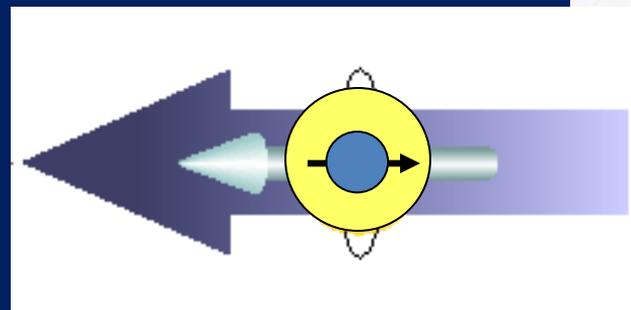
Positive helicity



Negative helicity



VS.



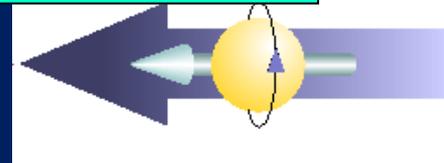
Christine Aidala,

# Polarized Parton Distribution Functions

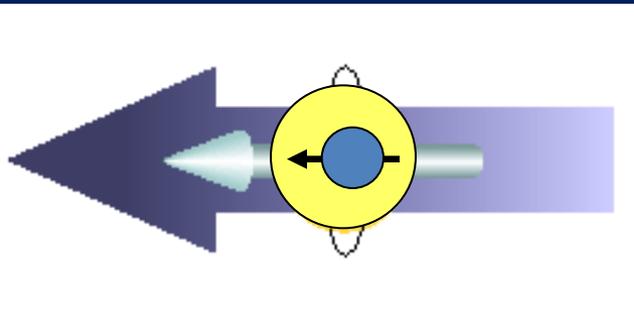
- Describe spin structure in terms of *polarized* parton distribution functions
- To study the *spin* structure of the proton:  
Do inelastic scattering with *polarized* protons!  
(spin directions all aligned)  $\frac{1}{2}S_z$ .

Helicity: Projection of spin vector onto momentum vector for particles polarized longitudinally, i.e. parallel to direction of motion.

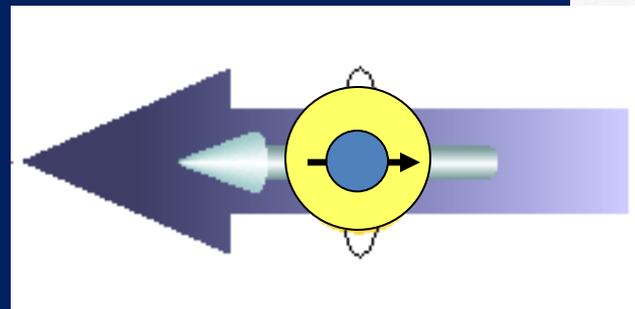
Either positive or negative.



Negative helicity



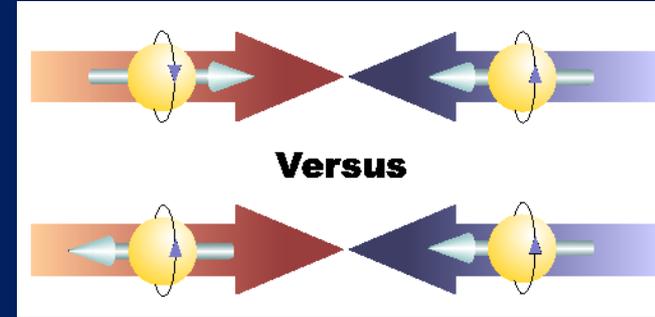
VS.



Christine Aidala,

# How Can We Investigate the Proton's Spin at RHIC?

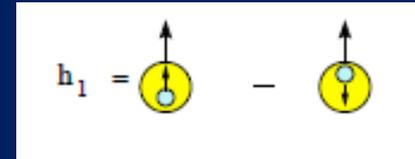
$$\text{Asymmetry} \propto \frac{B - C}{B + C}$$



- Collide polarized protons in different configurations and see what we observe in our detector
- Most often examining *asymmetries*
  - *e.g.* difference in the number of a certain particle produced when the beams have the same vs. opposite polarization
  - Same number produced gives asymmetry = 0.
  - All from one configuration and none from the other gives +1 or -1.
- Knowing what processes involving quarks and gluons led to production of the observed particle gives us a handle on the quarks' and gluons' contribution to the spin.

# Spin-momentum correlations and the proton as a QCD “laboratory”

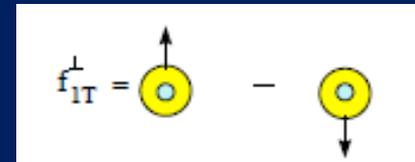
“Transversity” pdf:



Correlates *proton transverse spin* and *quark transverse spin*

$S_p$ - $S_q$  coupling

“Sivers” pdf:



Correlates *proton transverse spin* and *quark transverse momentum*

$S_p$ - $L_q$  coupling

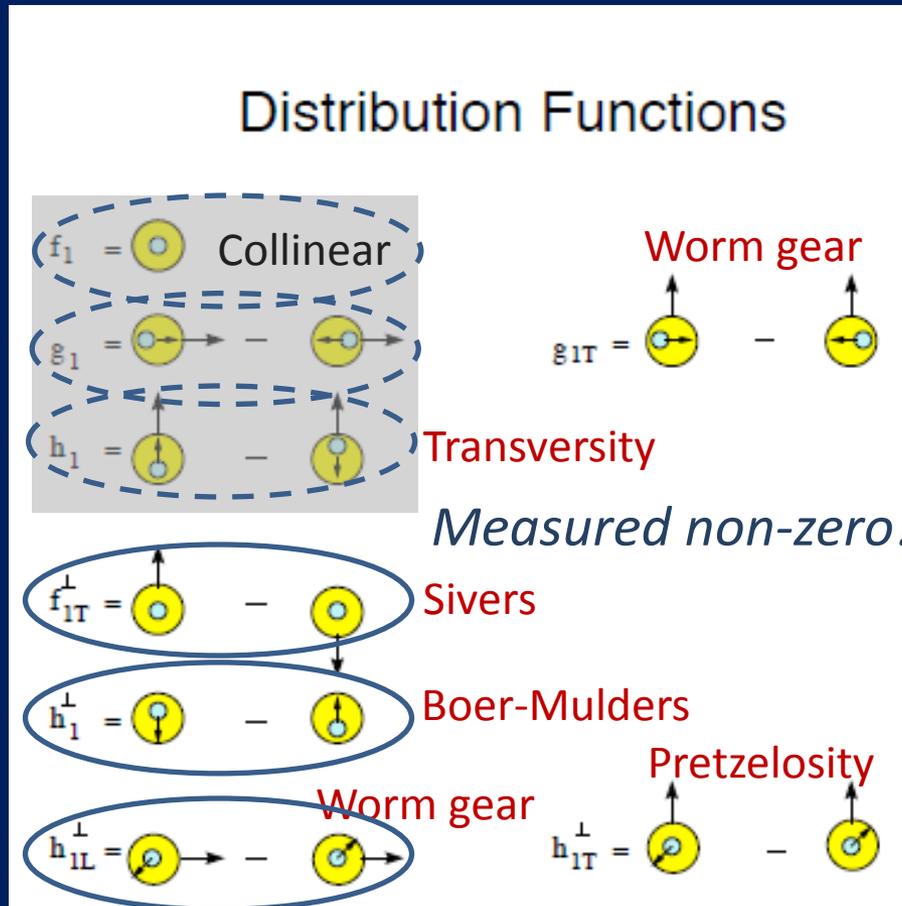
“Boer-Mulders” pdf:



Correlates *quark transverse spin* and *quark transverse momentum*

$S_q$ - $L_q$  coupling

# Spin-momentum correlations in proton! A recent and rapidly developing area of QCD research



# Transverse single-spin asymmetries in $p+p$ collisions: From low to high energies!

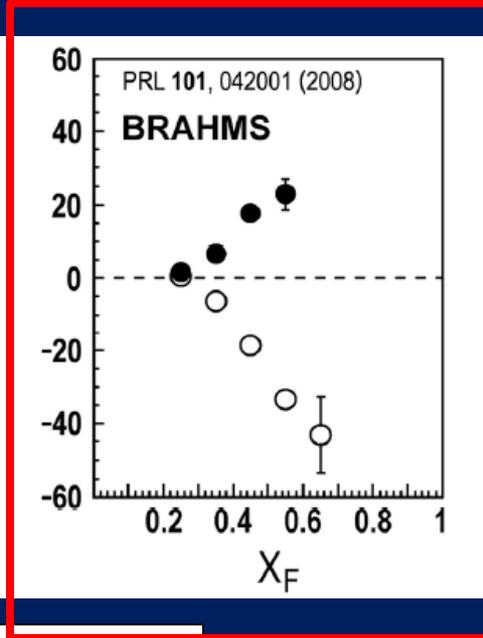
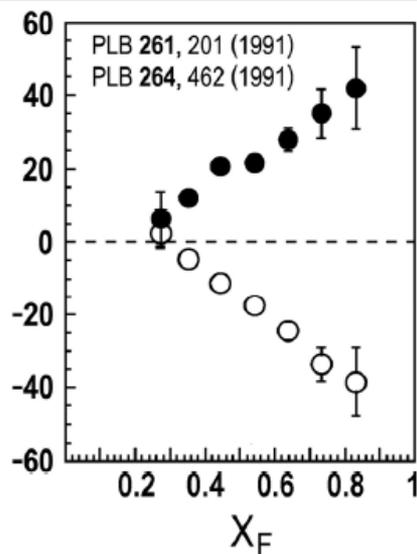
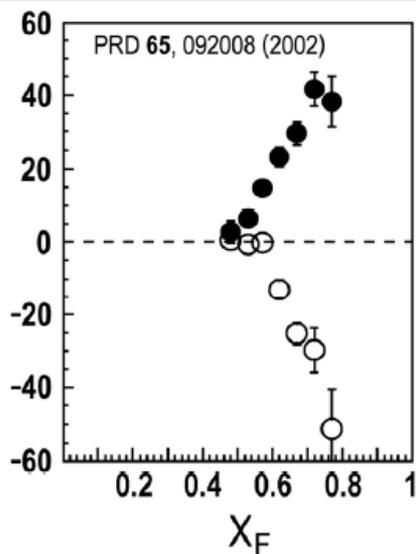
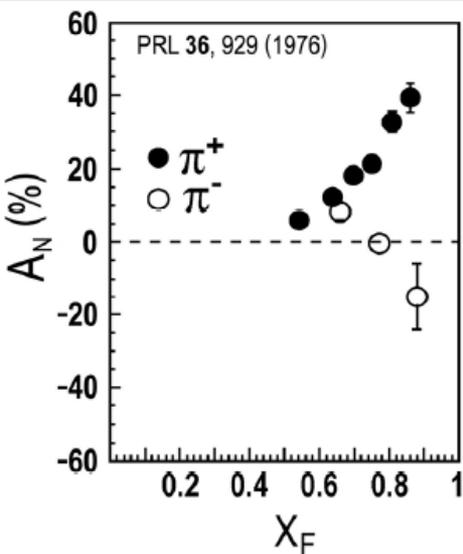


ANL  
 $\sqrt{s}=4.9$  GeV

BNL  
 $\sqrt{s}=6.6$  GeV

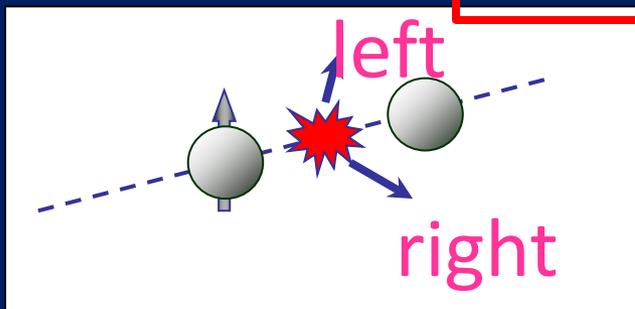
FNAL  
 $\sqrt{s}=19.4$  GeV

RHIC  
 $\sqrt{s}=62.4$  GeV



$$x_F = 2p_{long} / \sqrt{s}$$

$$= x_1 - x_2$$



# Transverse single-spin asymmetries in $p+p$ collisions: From low to high energies!

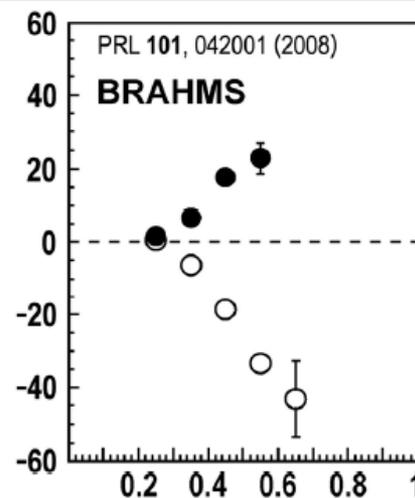
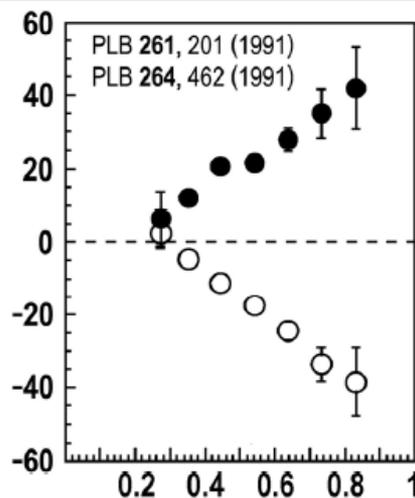
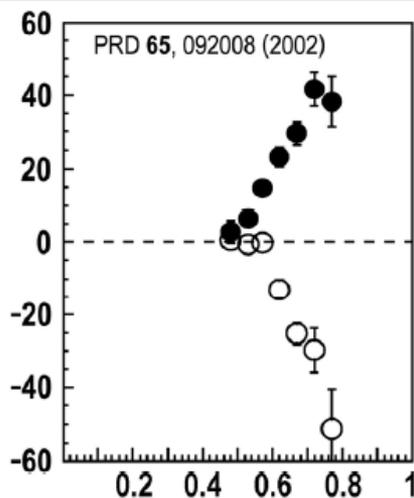
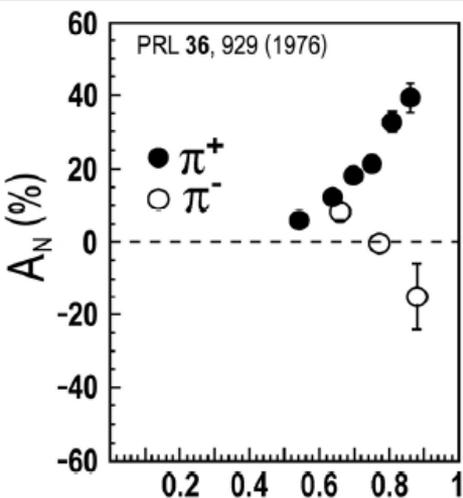


ANL  
 $\sqrt{s}=4.9$  GeV

BNL  
 $\sqrt{s}=6.6$  GeV

FNAL  
 $\sqrt{s}=19.4$  GeV

RHIC  
 $\sqrt{s}=62.4$  GeV



*Effects persist to RHIC energies*

$\rightarrow$  *Can probe this striking spin-momentum correlation in a calculable regime and extract physics by comparing experiment to theory!*

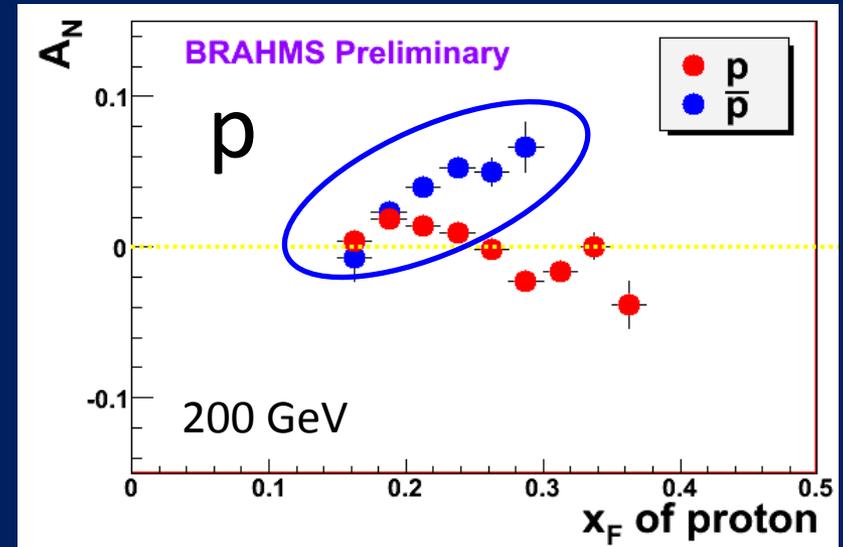
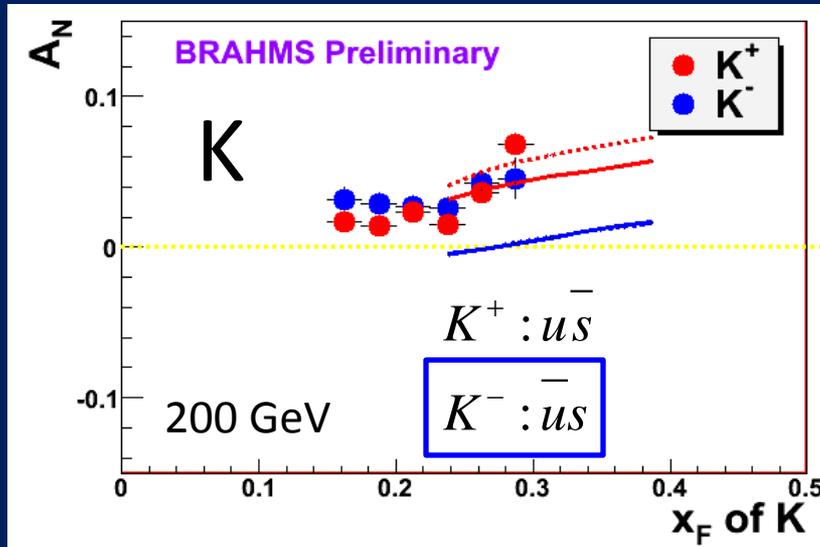
$x_F$

# High- $x_F$ asymmetries, but not valence quarks??



$$x_F = 2p_{long} / \sqrt{s}$$

$$= x_1 - x_2$$



Negative kaons same as positive??

Large antiproton asymmetry?!

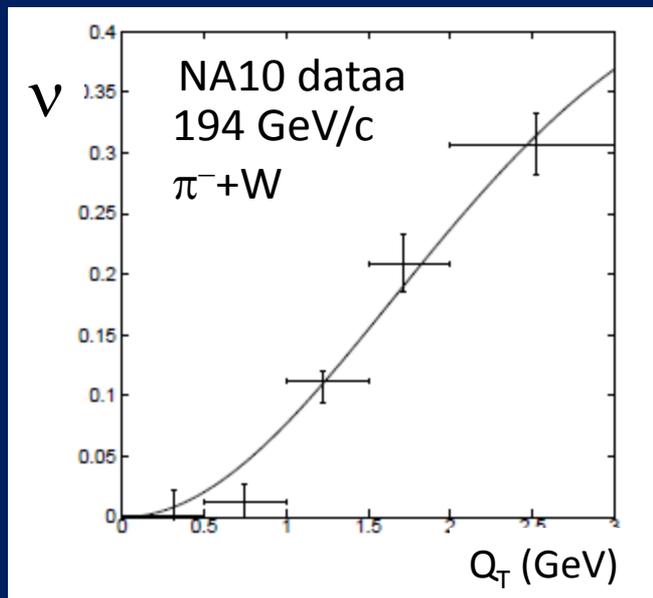
Pattern of pion species asymmetries in the forward direction  
→ valence quark effect.

But this conclusion confounded by kaon and antiproton  
asymmetries from RHIC!

***Lots of interesting effects to be explored!***

# *My own physics focus on SeaQuest: Azimuthal dependence of unpolarized Drell-Yan cross section*

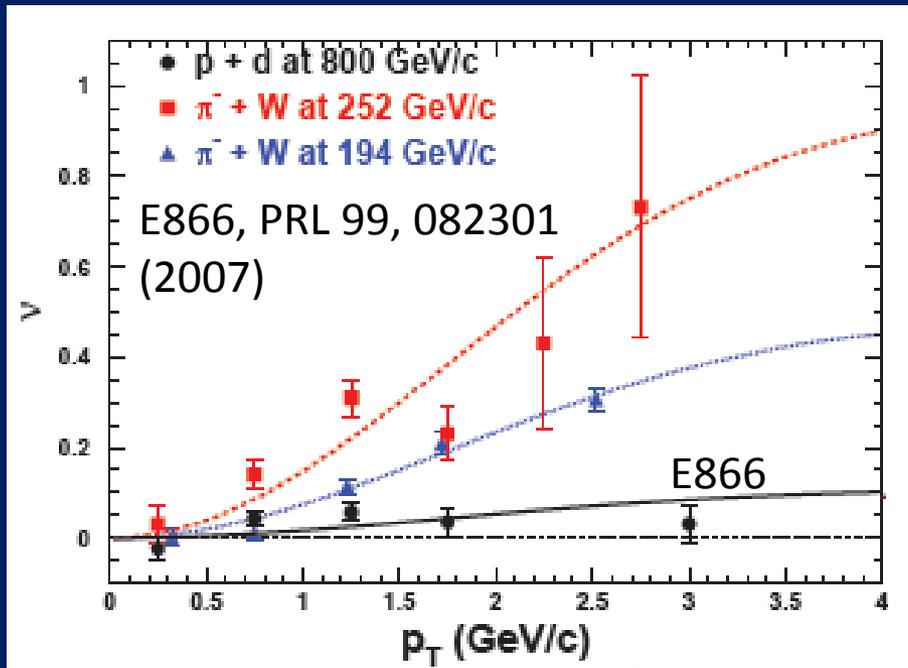
$$\frac{d\sigma}{d\Omega} \propto 1 + \lambda \cos^2 \theta + \mu \sin 2\theta + \frac{\nu}{2} \sin^2 \theta \cos 2\phi$$



D. Boer, PRD60, 014012 (1999)

- $\cos 2\phi$  term sensitive to *correlations between quark transverse spin and quark transverse momentum!*
- Large  $\cos 2\phi$  dependence seen in pion-induced Drell-Yan

# What about proton-induced Drell-Yan?



- Significantly reduced  $\cos 2\phi$  dependence in proton-induced Drell-Yan observed by E866
- Suggests sea quark transverse spin-momentum correlations small?
- Will be interesting to measure for higher- $x$  sea quarks in SeaQuest!

Boer - Mulders function  $h_1^\perp$

$$v(\pi W \rightarrow \mu^+ \mu^- X) \sim [\text{valence } h_1^\perp(\pi)] * [\text{valence } h_1^\perp(p)]$$

$$v(pd \rightarrow \mu^+ \mu^- X) \sim [\text{valence } h_1^\perp(p)] * [\text{sea } h_1^\perp(p)]$$