# Transverse Single Spin Asymmetry in $J/\psi$ Production in Run15 Polarized p + p, p + Al and p + Au Collision at $\sqrt{s} = 200 \text{GeV}$

# Chen Xu, Jin Huang, Haiwang Yu, Stephen Pate, vassilios papavassiliou, Xiaorong Wang

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#### Abstract

The transverse single spin asymmetry of high  $p_T$  muons from  $J/\psi$  production in polarized p + p and p + Au collisions at  $\sqrt{s} = 200$  GeV has been measured from Run15 data. The Run15 pp data recorded luminosity is 50  $pb^{-1}$  with average beam polarization about 55% and the recorded luminosity of  $1.27pb^{-1}$  with average beam polarization about 60% for pAu data which is given by Run summery from CAD.

# 1 Run selection

# 1.1 Run selection with pp data

Following runs are excluded:

• Remove runs due to the missing of Spin patterns and GL1p scalar in Spin Database:

Remove runs due to abnormal GL1p scalar in Spin Database:
426308 426353 431831 431832 431833 431834 431835 431837 431840 431845
431846 431859 431860 431886 431888

• Remove the runs due to Zero BBCin count in Spin Database: 426313 426315 426316 426319 426320 431854

 $\bullet$  Remove the runs due to high number of dead packets or dimuon yield per minimum bias events is too low or too high: 427670 427671 427672 427673 427674 427708 427710 427711 427712 427713 427805 427806 427807 427811 427813 427814 427815 427829 427878 427879 427881 427882 427885 427886 427887 427964 430402 430519 427656 425423 429886 429887 430402 430519 427656

• Remove runs due to increasing polarization in same fill: 424227

• Remove runs due to no diumuon events after cut:

#### 424439

• Remove runs due to the short duration (less than about 10 mins): 422074 422084 422319 422531 422562 422640 423041 423311 423546 423549 423576 424443 424627 424759 424886 425168 425290 425583 425688 426443 427129 427136 427264 427362 427366 427377 427657 427658 427673 427709 427810 427883 427968 427979 428211 428255 428260 428264 428266 428318 428323 428324 428451 428601 428728 428730 428733 428737 428754 428758 428892 429022 429024 429127 429365 429595 429678 429680 429696 429798 429888 430119 430121 430136 430137 430239 430494 430522 430563 430594 430600 430905 430906 431125 431137 431437 431608 431609 431836 431839 431844 431894

### **1.2 Run selection with** *p*Au data

Following runs are excluded:

• Remove runs due to the missing of Spin patterns and GL1p scalar in Spin Database:

 $\bullet$  Remove runs due to abnormal GL1p scalar in Spin Database: 435361

• Remove runs due to increasing polarization in same fill:

### **1.3** Run selection with pAl data

Following runs are excluded:

• Remove runs due to abnormal GL1p scalar in Spin Database: 437101 437714 438033 438153

• Remove the runs due to high number of dead packets or dimuon yield per minimum bias events is too low or too high:

 $South Arm: 437353 \ 437356 \ 437358 \ 437361 \ 437362 \ 437417 \ 437421 \ 437430 \ 437431 \\ 437433 \ 437434 \ 437435 \ 437440 \ 437474 \ 437478 \ 437483 \ 437484 \ 437486 \ 437487 \\ 437488 \ 437568 \ 437569 \ 437572 \ 437573 \ 437574 \ 437575 \ 437583 \ 437649 \ 437650 \\ 437659 \ 437659$ 

North Arm: 437433

# 2 Event and track selection

Analysis cuts are placed on a track by track basis. The same cuts are applied for both *pp*, *p*Al and *p*Au case. The details for those cuts are shown as following:

• Kinematic Cut for dimuon:  $0.42GeV < p_T < 10GeV$ ,  $p_z < 100GeV$ , charge = 0, Forward and backward pseudo-rapidity (1.2 < |y| < 2.2).

• Track Quality Cut for single muon: DG0 < 25cm(N), DG0 < 30cm(S), DDG0 < 10, ntrhits > 9, nidhits > 5, lastgap > 2, MuTr  $DCA_r < 10$ .

• Track Quality Cut for dimuon:  $BBCz-vertex : -30 < z < 30cm, Evt_vtxchi2 < 5.$ 

• Trigger Selection: 2D LL1 trigger and SG3&MUIDLL1( $1D \parallel 1H$ ) trigger

A  $p_T < 0.42 GeV$  low side cut is applied considering the resolution of forward muon arms. The resolution is got from PYTHIA6 simulation where the difference between input and output  $p_x$  and  $p_y$  distributions are plotted and shown in figure 1. This cut will just cut off less than 1% dimuons as we can see in the  $p_T$  distribution plots in figure 2.



δp distribution

Figure 1:  $\delta p_x$  and  $\delta p_y$  are got by finding the difference between input and output  $p_x$ ,  $p_y$  in PYTHIA6 simulation. A 2- $\sigma$  cut ( $\tilde{0}.3$  GeV) is made.

# **3** Background Fraction

Gaussian Process Regression(GPR) method is used to fit the background shapes without supposing a prior functional form. More details about GPR method can be found in Analysis Note AN1145.

The GPR method is trained on the data points in the 1.5-2.2 GeV and 4.3-6.0 GeV mass ranges in order to exclude the  $J/\psi$  and  $\psi'$  contributions to the mass spectrum and include only the data points that should correspond to background for the analysis.

For  $J/\psi$  invariant mass fit, the background which is got from GPR is extracted



Figure 2:  $p_T$  distribution for North arm(top) and South arm( bottom) in pp data.

from real data point. Then  $J/\psi$  is fitted with Crystal Ball function while  $\psi'$  is fitted with a Gaussian function.

The Crystal Ball function is a gaussian which has been joined smoothly with a power law on one side such that it and the first and second derivative are continuous functions as defined in equation 11 in AN1178.

In this analysis, we fit dimuon invariant mass in three different  $p_T$  bins for both North and South arm which are  $p_T \in (0 - 10)$  GeV,  $p_T \in (0 - 2)$ GeV,  $p_T \in (2 - 10)$ GeV for pp, pAl and pAu data. At the same time, two  $x_F$  bins were picked by making the statistic of each  $x_F$  bin in  $2 - \sigma J/\psi$  mass window equal. The  $x_F$  binning for pp, pAl and pAu data is  $x_F \in (0.05 - 0.11)$  and  $x_F \in (0.11 - 0.30)$ . The background fraction is calculated within  $2 - \sigma J/\psi$  mass window.

Figure 3 to 7 show the GPR fitting for pp data, figure 8 to 12 show the GPR fitting for pAu data and figure 13 to 17 show the GPR fitting for pAl data.

Table 1 shows the background fraction in  $p_T$  bins from GPR for pp data Table 2 shows the background fraction in  $p_T$  bins from GPR for pAu data Table 3 shows the background fraction in  $p_T$  bins from GPR for pAl data Table 4 shows the background fraction in  $x_F$  bins from GPR for pp data Table 5 shows the background fraction in  $x_F$  bins from GPR for pAu data Table 6 shows the background fraction in  $x_F$  bins from GPR for pAu data



Figure 3: MuTr mass spectrum fits with GPR background estimation for  $p_T = 0 - 10$  GeV bin for the north(top) and south(bottom) arm with pp data



Figure 4: MuTr mass spectrum fits with GPR background estimation for  $p_T = 0 - 2$  GeV bin for the north(top) and south(bottom) arm with pp data



Figure 5: MuTr mass spectrum fits with GPR background estimation for  $p_T = 2 - 10$  GeV bin for the north(top) and south(bottom) arm with pp data



Figure 6: MuTr mass spectrum fits with GPR background estimation for  $x_F = 0.05 - 0.11$  bin for the north(top) and south(bottom) arm with pp data



Figure 7: MuTr mass spectrum fits with GPR background estimation for  $x_F = 0.11 - 0.30$  bin for the north(top) and south(bottom) arm with pp data



Figure 8: MuTr mass spectrum fits with GPR background estimation for  $p_T = 0 - 10$  GeV bin for the north(top) and south(bottom) arm with pAu data



Figure 9: MuTr mass spectrum fits with GPR background estimation for  $p_T = 0 - 2$  GeV bin for the north(top) and south(bottom) arm with pAu data



Figure 10: MuTr mass spectrum fits with GPR background estimation for  $p_T = 2 - 10$  GeV bin for the north(top) and south(bottom) arm with pAu data



Figure 11: MuTr mass spectrum fits with GPR background estimation for  $x_F = 0.05 - 0.11$  bin for the north(top) and south(bottom) arm with pAu data



Figure 12: MuTr mass spectrum fits with GPR background estimation for  $x_F = 0.11 - 0.30$  bin for the north(top) and south(bottom) arm with pAu data



Figure 13: MuTr mass spectrum fits with GPR background estimation for  $p_T = 0 - 10$  GeV bin for the north(top) and south(bottom) arm with pAl data



Figure 14: MuTr mass spectrum fits with GPR background estimation for  $p_T = 0 - 2$  GeV bin for the north(top) and south(bottom) arm with pAl data



Figure 15: MuTr mass spectrum fits with GPR background estimation for  $p_T = 2 - 10$  GeV bin for the north(top) and south(bottom) arm with pAl data



Figure 16: MuTr mass spectrum fits with GPR background estimation for  $x_F = 0.05 - 0.11$  bin for the north(top) and south(bottom) arm with pAl data



Figure 17: MuTr mass spectrum fits with GPR background estimation for  $x_F = 0.11 - 0.30$  GeV bin for the north(top) and south(bottom) arm with pAl data

$p_T$	$f_{Bgr} \pm \delta f_{Bgr}(Stat.)(\%)$ North	$f_{Bgr} \pm \delta f_{Bgr}(Stat.)(\%)$ South
$p_T \in 0-2$	$9.9 \pm 1.0$	$10.3 \pm 1.1$
$p_T \in 2 - 10$	$6.8\pm0.7$	$5.3 \pm 0.6$

Table 1: Background Fraction in  $p_T$  bins for pp data

$p_T$	$f_{Bgr} \pm \delta f_{Bgr}(Stat.)(\%)$ North	$f_{Bgr} \pm \delta f_{Bgr}(Stat.)(\%)$ South
$p_T \in 0-2$	$9.7 \pm 1.6$	$19.4 \pm 2.2$
$p_T \in 2 - 10$	$7.5\pm~0.5$	$9.1 \pm 1.1$

Table 2:	Background	Fraction	in $p_T$	bins fo	or pAu	data
			r 1			

$$p_T$$
 $f_{Bgr} \pm \delta f_{Bgr}(Stat.)(\%)$  North $f_{Bgr} \pm \delta f_{Bgr}(Stat.)(\%)$  South $p_T \in 0-2$  $8.2 \pm 1.6$  $16.3 \pm 1.5$  $p_T \in 2-10$  $7.5 \pm 0.6$  $11.0 \pm 0.7$ 

Tab	le 3:	Bac	kground	Fraction	in $p_T$	bins	for <i>p</i>	bAl	data
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Table 4:	Background	Fraction	in $x_F$	bins :	for $pp$	data
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$x_F$	$f_{Bgr} \pm \delta f_{Bgr}(Stat.)(\%)$ North	$f_{Bgr} \pm \delta f_{Bgr}(Stat.)(\%)$ South
$x_F \in 0.05 - 0.11$	$13.3 \pm 1.6$	$18.9 \pm 1.6$
$x_F \in 0.11 - 0.30$	$3.6 \pm 0.2$	$7.2 \pm 0.6$

Table 5: Background Fraction in  $x_F$  bins for  $p\mathrm{Au}$  data

$x_F$	$f_{Bgr} \pm \delta f_{Bgr}(Stat.)(\%)$ North	$f_{Bgr} \pm \delta f_{Bgr}(Stat.)(\%)$ South
$x_F \in 0.05 - 0.11$	$11.2 \pm 2.5$	$15.7 \pm 1.6$
$x_F \in 0.11 - 0.30$	$5.3 \pm 0.6$	$5.3 \pm 0.5$

Table 6: Background Fraction in  $x_F$  bins for pAl data

# 4 $J/\psi$ Transverse Single Spin Asymmetry

Equation 1, 2 shows how we extract the physics  $J/\psi$  double spin Asymmetry

$$A_N^{J/\psi} = \frac{A_N^{incl} - f \cdot A_N^{bgr.}}{1 - f} \tag{1}$$

$$\delta A_N^{J/\psi} = \frac{\sqrt{(\delta A_N^{incl})^2 + f^2 \cdot (\delta A_N^{bgr})^2}}{1 - f}$$
(2)

where  $f = N^{BG}/N^{incl}$  is the background fraction which comes from section 3.  $A_N^{inc}$  is the inclusive dimuon asymmetry within 2  $\sigma$  mass window cut.  $A_N^{bgr.}$  is the background asymmetry which we estimate from the low side band dimuon and the mass range of which is from 1.5GeV to 2.4GeV.

# 5 Maximum Likelihood method

Maximum likelihood method has been used in the previous  $J/\psi A_N$  analysis and it has the advantage of dealing with low statistic situation. A detailed description of this method can be found in K. Oleg Eyser's analysis note 1018. Here exactly the same likelihood function is used here and shown in equation 11 and 12. As we have described in section 6.1, when dealing with yellow bin,  $\pi - \phi$  is put into the equations below instead of  $\phi$ .

For spin up:

$$-logL(\phi) = -\sum log(1 + \epsilon * cos(\phi_i))$$
(3)

For spin down:

$$-logL(\phi) = -\sum log(1 - \epsilon * cos(\phi_i))$$
(4)

A scanning of  $\epsilon$  from -0.6 to 0.6 with 1200 steps has been proceeded for finding the best estimator ( $\epsilon_{best}$ ). Having got the best estimator, the asymmetry can be calculated by  $A_N = \epsilon_{best}$ /Polarization, where Polarization is the average polarization of each run weighted by run luminosity.

One more thing needed to be mentioned here is the spin value read from Spin Data Base. The values in the spin DB are taken from CDEV packets, which is provided by CAD. CDEV data has spin information at 12'o clock, where the RHIC polarimeters are located. Therefore, +1(-1) in the spin DB means spin-down (spin-up) at 12 o'clock.

The spin direction is reversed at PHENIX after the proton beam passed the Siberian snakes(helical magnets) between 12'o clock and PHENIX (there are two places where the Siberian snakes are in the RHIC, so the spin direction is back to original after each rotation). Therefore, +1(-1) in the spin DB means spin-down(spin-up) at PHENIX.

### 5.1 Maximum Likelihood method with pp data

In pp collision, both blue beam and yellow beam are polarized. In Run15, the transverse polarization direction is along Y-axis. So when  $A_N(\phi)$  is calculated w.r.t blue beam, the azimuthal angle is already under PHENIX coordinate system. However, this is not the case for yellow beam since yellow beam is traveling towards South Arm which is along the negative Z direction in PHENIX coordinate system. The azimuthal angle under PHENIX coordinate system is  $\pi - \phi$  w.r.t yellow beam. Therefore, instead of fitting with  $\cos(\phi)$  we fit  $A_N(\phi)$  with  $\cos(\pi - \phi)$  when dealing with yellow beam related  $A_N$ .

Table 7 and 8 list the inclusive (background)  $A_N$  with all the bins for Blue and Yellow beam. The difference of  $A_N^{Incl.(bgr)}$  between Spin Analyzer and Maximum Likelihood method for each bin is around 0.1 sigma which is in a reasonable range.

Arm (Blue Beam)	$A_N^{incl}$	$A_N^{bgr}$
$North(0 < p_T < 2GeV)$	$0.007 \pm 0.015$	$0.032 \pm 0.035$
$North(2 < p_T < 10 GeV)$	$0.016 \pm 0.021$	$0.111 \pm 0.058$
$North(0.05 < x_F < 0.11 GeV)$	$0.005 {\pm} 0.015$	$0.035 {\pm} 0.032$
$North(0.11 < x_F < 0.30 GeV)$	$0.016 {\pm} 0.019$	$0.178 {\pm} 0.087$
$South(0 < p_T < 2Gev)$	$0.004 \pm 0.013$	$0.023 \pm 0.028$
$South(2 < p_T < 10Gev)$	$0.011 \pm 0.020$	$0.005 \pm 0.056$
$South(0.05 < x_F < 0.11 GeV)$	$0.004{\pm}0.013$	$0.025 {\pm} 0.026$
$South(0.11 < x_F < 0.30 GeV)$	$0.015 \pm 0.020$	$-0.023 \pm 0.096$

Table 7: List of Inclusive and background  $A_N$  from Maximum Likelihood for Blue beam with pp data

Arm(Yellow Beam)	$A_N^{incl}$	$A_N^{bgr}$
$North(0 < p_T < 2GeV)$	$0.021 \pm 0.015$	$0.018 \pm 0.035$
$North(2 < p_T < 10 GeV)$	$0.053 \pm 0.021$	$0.072 \pm 0.058$
$North(0.05 < x_F < 0.11 GeV)$	$0.026{\pm}0.015$	$0.021{\pm}0.032$
$North(0.11 < x_F < 0.30 GeV)$	$0.040{\pm}0.019$	$0.117{\pm}0.087$
$South(0 < p_T < 2Gev)$	$0.005 \pm 0.013$	$0.032 \pm 0.030$
$South(2 < p_T < 10Gev)$	$0.004 \pm 0.020$	$0.060\pm0.056$
$South(0.05 < x_F < 0.11 GeV)$	$0.009 {\pm} 0.013$	$0.029{\pm}0.028$
$South(0.11 < x_F < 0.30 GeV)$	$-0.005 \pm 0.020$	$0.137{\pm}0.096$

Table 8: List of Inclusive and background  $A_N$  from Maximum Likelihood for Yellow beam with pp data

### 5.2 Maximum Likelihood method with pAu data

In pAu, only proton is polarized and traveling towards positive Z direction so the azimuthal angle is already under PHENIX coordinate system.

#### 5.2.1 Tilt angle correction

Figure 18 Shows the  $FVTX_X vs.FVTX_Z$  distribution in pp collision where two proton are moving along z-axis and no tilt angle exist there. In that case, the highlight band is perpendicular to x-axis. In pAu collision, it is still head-down collision. But we observed a tilt angle in X-Z plane which can be seen from figure 19. And the tilt angle is 3.6 mrad which is given by CAD published paper.

This tilt angle makes the CM frame of collision no longer in PHENIX coordinate system. Since every quantity is recorded under PHENIX coordinate system, we need to transform 3-D vector, momentum in this case, into CM frame. Since it is still head-down collision, only rotation transformation is needed for this purpose. The transformation is shown as following:



Figure 18: This plot shows FVTX\_X vs. FVTX\_Z distribution in *pp* collision. The tilt highlight band is perpendicular to x-axis which indicates that *pp* collision in Run15 is along Z-axis.

$$p'_{y} = p_{y} \tag{5}$$

$$p'_x = \cos(\alpha) * p_x - \sin(\alpha) * p_z \tag{6}$$

$$p'_{z} = \sin(\alpha) * p_{x} + \cos(\alpha) * p_{z} \tag{7}$$

where  $p_{x,y,z}$  is the momentum recorded in pDST and  $p'_{x,y,z}$  is the momentum in CM frame and  $\alpha$  is 3.6 mrad as mentioned above.

This tilt angle will not affect the result in the leading order. A comparison has been made between inclusive and background  $A_N$  before and after tilt angle



Figure 19: This plot shows FVTX\_X vs. FVTX\_Z distribution in pAu collision. The tilt highlight band indicates that pAu collision is not exactly along Z-axis.

correction. Figure 20 shows the inclusive and background  $A_N$  in  $x_F$  bin before tilt angle correction. The fluctuation due to the tilt angle correction is about 0.1 sigma.

# 5.2.2 Inclusive and background $A_N$ with pAu data after tilt angle correction

Figure 21 shows inclusive and background asymmetry scanning with Maximum Likelihood method for p + Au data. Table 9 and 10 list the inclusive and background  $A_N$  that we found from the scanning.

$p_T$	$A_N^{Inc.} \pm \delta A_N^{Inc.}(Stat.)$ North	$A_N^{Inc.} \pm \delta A_N^{Inc.}(Stat.)$ South
$p_T \in 0-2$	$-0.061 \pm 0.022$	$-0.056 \pm 0.023$
$p_T \in 2 - 10$	$0.010 \pm 0.028$	$0.010 \pm 0.028$
$x_F \in 0.05 - 0.11$	$-0.025 \pm 0.023$	$-0.045 \pm 0.021$
$x_F \in 0.11 - 0.30$	$-0.045 \pm 0.027$	$-0.021 \pm 0.033$

Table 9:  $A_N^{Inc.}$  in different  $p_T$  and  $x_F$  bins with pAu data

# 5.3 Maximum Likelihood method with pAl data

Similar with what has been saw in pAu data, there is also a tilt angle in pAl collision and the tilt angle in pAl case is 2.5mrad. The result shown in this



Figure 20:  $A_N$  for all  $x_F$  before tilt angle correction.



Figure 21: Epsilon scanning with pAu dataset. Top(bottom) left: epsilon scanning for inclusive(background)  $A_N$  in North arm with  $0.05 < x_F < 0.11$ . Top(bottom) right: epsilon scanning for inclusive(background)  $A_N$  in South arm with  $0.05 < x_F < 0.11$ .

$p_T$	$A_N^{Bgr.} \pm \delta A_N^{Bgr.}(Stat.)$ North	$A_N^{Bgr.} \pm \delta A_N^{Bgr.}(Stat.)$ South
$p_T \in 0-2$	$-0.005 \pm 0.043$	$0.020 \pm 0.028$
$p_T \in 2 - 10$	$-0.026 \pm 0.055$	$-0.017 \pm 0.046$
$x_F \in 0.05 - 0.11$	$-0.010 \pm 0.036$	$0.015 \pm 0.025$
$x_F \in 0.11 - 0.30$	$-0.036 \pm 0.093$	$-0.051 \pm 0.097$

Table 10:  $A_N^{Bgr.}$  in different  $p_T$  and  $x_F$  bins with pAu data

section is the inclusive and background  $A_N$  after the tilt angle correction.

Figure 21 and 22 show inclusive and background asymmetry scanning with Maximum Likelihood method for p + Al data. Table 11 and 12 lists the inclusive and background  $A_N$  that we found from the scanning.



Figure 22: Epsilon scanning with pAl dataset. Top(bottom) left: epsilon scanning for inclusive  $A_N$  in North arm with  $0 < p_T < 2GeV$ . Top(bottom) right: epsilon scanning for background  $A_N$  in North arm with  $2 < p_T < 10GeV$ .

$p_T$	$A_N^{Inc.} \pm \delta A_N^{Inc.}(Stat.)$ North	$A_N^{Inc.} \pm \delta A_N^{Inc.}(Stat.)$ South
$p_T \in 0-2$	$0.031 \pm 0.027$	$-0.018 \pm 0.026$
$p_T \in 2 - 10$	$0.002 \pm 0.037$	$0.051 \pm 0.036$
$x_F \in 0.05 - 0.11$	$0.023 \pm 0.029$	$-0.009 \pm 0.025$
$x_F \in 0.11 - 0.30$	$0.025 \pm 0.037$	$0.042 \pm 0.038$

Table 11:  $A_N^{Inc.}$  in different  $p_T$  and  $x_F$  bins with pAl data



Figure 23: Epsilon scanning with pAl dataset. Top(bottom) left: epsilon scanning for inclusive  $A_N$  in South arm with  $0 < p_T < 2GeV$ . Top(bottom) right: epsilon scanning for background  $A_N$  in South arm with  $2 < p_T < 10GeV$ .

$p_T$	$A_N^{Bgr.} \pm \delta A_N^{Bgr.}(Stat.)$ North	$A_N^{Bgr.} \pm \delta A_N^{Bgr.}(Stat.)$ South
$p_T \in 0-2$	$0.090 \pm 0.050$	$-0.029 \pm 0.048$
$p_T \in 2 - 10$	$0.113 \pm 0.077$	$0.009 \pm 0.084$
$x_F \in 0.05 - 0.11$	$0.091 \pm 0.044$	$-0.040 \pm 0.043$
$x_F \in 0.11 - 0.30$	$0.093 \pm 0.129$	$0.234{\pm}0.152$

Table 12:  $A_N^{Bgr.}$  in different  $p_T$  and  $x_F$  bins with pAl data

# 5.4 $J/\psi A_N$

Having obtained the inclusive and background asymmetries the signal asymmetry can be calculated from Equation 1 and Equation 2. Figure 24 to 25 show  $J/\psi A_N$  in different  $p_T$  and  $x_F$  bins with pp data. Figure 30 and 31 show  $J/\psi A_N$  in different  $p_T$  and  $x_F$  bins with pAl data and figure 27 and 28 show  $J/\psi A_N$  in different  $p_T$  and  $x_F$  bins with pAu data. And table 13, 14, 15 and 16 list the  $J/\psi A_N$  in each arm for each  $p_T$  and  $x_F$  bin with pp, pAl and pAu data.

$p_T$	$A_N^{J/\psi} \pm \delta A_N^{J/\psi}(Stat.)$ North	$A_N^{J/\psi} \pm \delta A_N^{J/\psi}(Stat.)$ South
$p_T \in 0-2$	$0.004 \pm 0.017$	$0.013 \pm 0.011$
$p_T \in 2 - 10$	$0.009 \pm 0.023$	$0.011 \pm 0.021$
$x_F \in 0.05 - 0.11$	$0.002 \pm 0.027$	$0.001 \pm 0.015$
$x_F \in 0.11 - 0.30$	$0.008 \pm 0.021$	$0.017 \pm 0.021$

Table 13:  $A_N^{J/\psi}$  in different  $p_T$  and  $x_F$  bins for Blue beam with pp data

$p_T$	$A_N^{J/\psi} \pm \delta A_N^{J/\psi}(Stat.)$ North	$A_N^{J/\psi} \pm \delta A_N^{J/\psi}(Stat.)$ South
$p_T \in 0-2$	$0.021 \pm 0.017$	$0.002 \pm 0.015$
$p_T \in 2 - 10$	$0.051 \pm 0.023$	$0.000 \pm 0.021$
$x_F \in 0.05 - 0.11$	$0.027 \pm 0.018$	$0.006 \pm 0.015$
$x_F \in 0.11 - 0.30$	$0.037 \pm 0.021$	$-0.010 \pm 0.021$

Table 14:  $A_N^{J/\psi}$  in different  $p_T$  and  $x_F$  bins for Yellow beam with pp data

$p_T$	$A_N^{J/\psi} \pm \delta A_N^{J/\psi}(Stat.)$ North	$A_N^{J/\psi} \pm \delta A_N^{J/\psi}(Stat.)$ South
$p_T \in 0-2$	$0.018 \pm 0.037$	$-0.013 \pm 0.037$
$p_T \in 2 - 10$	$-0.008 \pm 0.045$	$0.031 \pm 0.046$
$x_F \in 0.05 - 0.11$	$0.018 \pm 0.039$	$0.062 \pm 0.037$
$x_F \in 0.11 - 0.30$	$0.022 \pm 0.039$	$-0.076 \pm 0.042$

Table 15:  $A_N^{J/\psi}$  in different  $p_T$  and  $x_F$  bins for Blue beam with pAl data

$p_T$	$A_N^{J/\psi} \pm \delta A_N^{J/\psi}(Stat.)$ North	$A_N^{J/\psi} \pm \delta A_N^{J/\psi}(Stat.)$ South
$p_T \in 0-2$	$-0.067 \pm 0.025$	$-0.074 \pm 0.029$
$p_T \in 2 - 10$	$0.013 \pm 0.031$	$0.012 \pm 0.033$
$x_F \in 0.05 - 0.11$	$-0.027 \pm 0.027$	$-0.058 \pm 0.027$
$x_F \in 0.11 - 0.30$	$-0.045 \pm 0.029$	$-0.019 \pm 0.037$

Table 16:  $A_N^{J/\psi}$  in different  $p_T$  and  $x_F$  bins for Blue beam with pAu data

# 6 Cross Check

First of all, it is necessary to cross check the BBC counts and dimuon yield (figure 32 to 35) for each bunch in each run. Make sure that we deal with the



Figure 24:  $pp A_N^{J/\psi}$  vs.  $p_T$  bins



Figure 25:  $pp \; A_N^{J/\psi}$  vs.  $x_F$ 



Figure 26:  $p{\rm Au}\;A_N^{J/\psi}$  in combined  $p_T$  bin



Figure 27:  $p{\rm Au}\;A_N^{J/\psi}$  vs.  $p_T$ 



Figure 28:  $p{\rm Au}\;A_N^{J/\psi}$ vs.  $x_F$ 



Figure 29: pAl  $A_N^{J/\psi}$  in combined  $p_T$  bin



Figure 30: pAl $A_N^{J/\psi}$  vs.  $p_T$ 



Figure 31: pAl  $A_N^{J/\psi}$  vs.  $x_F$ 

bunch crossing number correctly and the BBC counts read from Spin Database is reasonable.

From those plots, the abort gap can be clearly seen there and it is placed in the right crossing bunch range.



Figure 32: The left plot(North arm) and right plot(South arm) show dimuon yields for each bunch in each run in pp collision. Where X axis is PHENIX crossing and Y axis is run sequence

## 6.1 Crosscheck with Spin Analyzer

Due to the low statistic issue of background in the second  $x_F$  bin, the Spin Analyzer is used as a cross check for Maximum Likelihood Method which has been described in last section. The results got from Spin Analyzer are considered as one source of systematic uncertainties.

An overview introduction about Spin Analyzer frame work can be found in Haiwang's analysis note 1194. The most relative features of Spin Analyzer to this analysis are:

1. The spin information is directly loaded from the Spin Database through the standard USpin interface (offline/packages/uspin/). The newest database QA level is used at the time when SpinAnalyzer is run.



Figure 33: pp BBC in cross check: A 2-D plot filled with BBC in counts reading from Spin Database. X-axis is RHIC crossing and Y-axis is Run sequence



Figure 34: The left plot(North arm) and right plot(South arm) show dimuon yields for each bunch in each run in pAu collision. Where X axis is PHENIX crossing and Y axis is run sequence



Figure 35: *p*Au BBCin cross check: A 2-D plot filled with BBCin counts reading from Spin Database. X-axis is RHIC crossing and Y-axis is Run sequence

- 2. The output from SpinAnalyzer is histograms of counts which is categorized with respect to spin combinations. If chosen, it will also outputs histograms containing the single and double spin-asymmetry results.
- 3. Haiwang Yu developed a patch to make Spin Analyzer capable to do single polarized beam case such as *p*Au collision.

# 6.2 Extract $A_N^{incl(bgr)}$ from Spin Analyzer

Equation 3 shows the definition of  $A_N$  as a function of  $\phi$ 

$$A_N(\phi) = \frac{\sigma^{\uparrow}(\phi) - \sigma^{\downarrow}(\phi)}{\sigma^{\uparrow}(\phi) + \sigma^{\downarrow}(\phi)} = \frac{1}{P} * \frac{N^{\uparrow}(\phi) - R * N^{\downarrow}(\phi)}{N^{\uparrow}(\phi) + R * N^{\downarrow}(\phi)}$$
(8)

Where R is relative luminosity and P is the beam polarization.

For spin = 1/2:

$$\sigma^{\uparrow}(\phi) = \sigma_0 * (1 + A_N * Cos(\phi)) \tag{9}$$

For spin = -1/2:

$$\sigma^{\downarrow}(\phi) = \sigma_0 * (1 - A_N * Cos(\phi)) \tag{10}$$

Insert equation (4) and equation (5) into equation (3), we will get:

$$A_N(\phi) = A_N * Cos(\phi) \tag{11}$$

From Spin Analyzer,  $A_N^{incl(bgr)}$  versus  $\phi$  distribution for each  $p_T$  bin in both North and South arm will be got automatically after running Spin Analyzer.

For extracting  $A_N^{incl(bgr)}$ , a cosine modulation fitting function is used and both the value and the uncertainty of  $A_N^{incl(bgr)}$  can be extracted from the fitting.

In my analysis, 16 even  $\phi$  bins is set with different  $p_T$  bins for both pp and pAu cases. The azimuthal angle  $\phi$  is recorded and calculated under PHENIX coordinate system.

# 6.3 Spin Analyzer with pp data

## 6.3.1 Inclusive and Background Asymmetry

The inclusive and background asymmetries extracted from Spin Analyzer are shown from figure 36 to 40. The inclusive asymmetry is calculated from like-sign dimuon within  $2\sigma$  invariant mass range got from GPR fitting in section 3. The background asymmetry is calculated from the low side band dimuon the mass range of which is from 1.5 to 2.4 GeV.



Figure 36: pp Inclusive and background  $A_N$  with  $0 < p_T < 2 GeV$  bin in North arm

# 6.4 Spin Analyzer with pAu data

In pAu, only proton is polarized and traveling towards positive Z direction so the azimuthal angle is already under PHENIX coordinate system and we can use  $\cos(\phi)$  for fitting purpose.



Figure 37: pp Inclusive and background  $A_N$  with  $2 < p_T < 10 GeV$  bin in North arm



Figure 38: pp Inclusive and background  $A_N$  with  $0 < p_T < 2 GeV$  bin in South arm



Figure 39: pp Inclusive and background  $A_N$  with  $2 < p_T < 10 GeV$  bin in South arm

# 6.4.1 Inclusive and background $A_N$ with pAu data after tilt angle correction

Similar with the procedure in pp case, inclusive and background asymmetries with pAu extracted from Spin Analyzer are shown from figure 41 to 44. The inclusive asymmetry is calculated from like-sign dimuon within  $2 - \sigma$  invariant mass range got from GPR fitting in section 3. The background asymmetry is calculated from the low side band dimuon the mass range of which is from 1.5 to 2.4GeV.

### 6.5 A crosscheck for Spin Analyzer with standalone code

I also wrote a standalone code to repeat what Spin Analyzer is doing in the background for both pp and pAu analysis. Then compare the result from standalone code with the result from Spin Analyzer.

### 6.5.1 Cross Check for *pp* with Standalone code

In pp, since both blue and yellow beam are polarized, equation(3) is rewritten as:

$$A_{N}(\phi) = \frac{\sigma^{\uparrow\uparrow}(\phi) + \sigma^{\uparrow\downarrow}(\phi) - (\sigma^{\downarrow\uparrow}(\phi) + \sigma^{\downarrow\downarrow}(\phi))}{\sigma^{\uparrow\uparrow}(\phi) + \sigma^{\uparrow\downarrow}(\phi) + \sigma^{\downarrow\downarrow}(\phi) + \sigma^{\downarrow\downarrow}(\phi)} = \frac{1}{P} * \frac{N^{\uparrow\uparrow}(\phi) + R_{1} * N^{\uparrow\downarrow}(\phi) - (R_{2} * N^{\downarrow\uparrow} + R_{3} * N^{\downarrow\downarrow})}{N^{\uparrow\uparrow}(\phi) + R_{1} * N^{\uparrow\downarrow}(\phi) - R_{2} * N^{\downarrow\uparrow} + R_{3} * N^{\downarrow\downarrow}}$$
(12)

Where  $R_1 = L^{\uparrow\uparrow}/L^{\uparrow\downarrow}$ ,  $R_2 = L^{\uparrow\uparrow}/L^{\downarrow\uparrow}$ ,  $R_3 = L^{\uparrow\uparrow}/L^{\downarrow\downarrow}$ .



Figure 40: pp Inclusive<br/>(top plot)&background(bottom plot) $A_N$  with one<br/>  $x_F$  bin



Figure 41: pAu Inclusive and background  $A_N$  with  $0 < p_T < 2 GeV$ 



Figure 42: pAu Inclusive and background  $A_N$  with  $2 < p_T < 10 GeV$ 



Figure 43: pAu Inclusive and background  $A_N$  with  $0.05 < x_F < 0.11$ 



Figure 44: pAu Inclusive and background  $A_N$  with  $0.11 < x_F < 0.30$ 

Polarization is the average polarization of all the runs weighted by the run luminosity with  $P_{blue} = 57\%$  and  $P_{yellow} = 57\%$ .

 $A_N(\phi)$ , relative luminosity  $(R_1, R_2, R_3)$  and polarization value for blue and yellow beam got from standalone code are exactly the same with those values calculated by Spin Analyzer.

Figure 45-48 show the inclusive/background  $A_N$  fitting result from standalone code. The variance of  $A_N^{incl(bgr)}$  with Spin Analyzer and standalone is about 2%  $\sigma$ . This slight discrepancy is due to the different uncertainty calculation for  $A_N$  in each  $\phi$  bin. In Spin Analyzer, only number of events are considered into statistical uncertainty while, in standalone code, the polarization is also taken into account.



Figure 45: Inclusive and background  $A_N$  got from standalone code with  $0 < p_T < 2GeV$  bin in North arm with pp data

#### 6.5.2 Cross check for pAu data with standalone code

For pAu collision, only blue beam is polarized. So  $A_N^{incl(bgr)}(\phi)$  can be calculated by equation(3). The polarization is the average polarization of all the runs weighted by the run luminosity with  $P_{blue} = 60\%$ .

Figure 49 to 51 show the inclusive/background  $A_N$  in different  $p_T$  and  $x_F$  bins. An approximately  $1\%\sigma$  shift is observed due to the same reason described in section 7.1.

### 6.5.3 Fill-by-Fill $A_N$ estimation with Maximum Likelihood method

A fill-by-fill  $A_N$  estimation is also covered by Maximum Likelihood method. This is a cross check that whether there is a bias with combined data analysis



Figure 46: Inclusive and background  $A_N$  got from standal one code with  $2 < p_T < 10 GeV$  bin in North arm with pp data



Figure 47: Inclusive and background  $A_N$  got from standal one code with  $0 < p_T < 2 GeV$  bin in South arm with pp data



Figure 48: Inclusive and background  $A_N$  got from standal one code with  $2 < p_T < 10 GeV$  bin in South arm with pp data



Figure 49: Inclusive and background  $A_N$  got from standal one code with  $0 < p_T < 2 GeV$  with  $p{\rm Au}$  data



Figure 50: Inclusive and background  $A_N$  got from standal one code with  $2 < p_T < 10 GeV$  with  $p{\rm Au}$  data



Figure 51: Inclusive and background  $A_N$  got from standal one code with one  $x_F$  bin with  $p{\rm Au}$  data

which is caused by detector acceptance or/and trigger efficiency change within the whole data taking. Figure 52 shows the Fill-by-Fill result. This result is compared with result got from section 7.7.2. The largest difference observed between this two methods is the inclusive  $A_N$  in North arm which varies about  $0.15\sigma$  difference. Other than that, the difference is all less than 5%. So we may conclude that result with combined data for this analysis is consistent with Fill-by-Fill method.



Figure 52: Fill-by-fill Inclusive and background  $A_N$  from Maximum Likelihood method with pAu data

### 6.6 Cross check for *p*Au data from other collaborators

Another cross check also has been done with Sanghoon and Marie from LANL. I appreciate their time and work on this cross check. A event-by-event check has been performed before comparing the inclusive  $A_N$ . In this check, several quantities have been picked for comparison such as x, y, z components of dimuon momentum, azimuthal angle of prompt dimuon and also the spin pattern. And we got perfect match on this part. After that, Sanghoon and I produced inclusive  $A_N$  using same picoDST and good run list but different sets of dimuon cuts. Marie was using a different good run list and dimuon cut. The purpose of this cross check is to see whether there is a coding issue. Rather than that, it also check whether we introduced some bias when applying the cut. Figure 53 shows the inclusive  $A_N$  for north arm with lower  $p_T$  bin. My result is perfectly match with the result produced by Sanghoon. And Marie's result is also consistent with mine. Considering that she was using a different cut sets, the fluctuation shown in the figure is expected. With different cut sets, the inclusive  $A_N$  is consistent with each other.



Figure 53: Compare inclusive  $A_N$  from different cut set with Sanghoon and Marie using pAu data

# 7 Discrepancy between preliminary and current result

# 7.1 Discrepancy due to different taxi production

For preliminary result, we were using production 105. Currently, we are using production 107. The difference between these two productions is the alignment of FVTX. The changing of alignment of FVTX will result in the event vertex shift which will affect the refitting in the dimuon reconstruction process. For the MuTr tracks that match with FVTX tracklets, the mass and momentum will change about 1% due to the alignment. The change of mass and momentum will shift the final result by about 0.2 sigma as we can see in figure 54.



Figure 54: Compare inclusive  $A_N$  from different production and cut with pAu data. The x-axis is

### 7.2 Discrepancy due to different single muon $dca_r$ cut

Single muon  $dca_r$  is filled into picoDST with the strategy in following: if the track of single muon from Mutr match with the tracklet from FVTX, fill Mutr  $dca_r$  with FVTX  $dca_r$  into picoDST. Otherwise, fill single muon container with

Mutr  $dca_r$ . Previous  $dca_r$  cut at 5 is applied on both FVTX and MuTr  $dca_r$ . Now all the  $dca_r$  is calculated with the Mutr  $dca_r$  definition. The  $dca_r$  cut is applied at 10 in order to keep as many statistics as possible and also minimize the hadronic in background mass region. Figure 55 shows Mutr  $dca_r$  distribution in north and south arm with pAu data.



Figure 55: Top: Single muon  $dca_r$  distribution from FVTX. Bottom: Single muon  $dca_r$  distribution from Mutr.

# 8 Further study for $A_N$ in first $p_T$ bin with pAu data

As it has been shown in section 5, we observed a negative 2.5-sigma level  $A_N$  in first  $p_T$  bin with pAu data. In order to find the possible reason for causing it, we checked the  $A_N$  with different subsystem activities, such as number of FVTXTracklets and BBC centrality(BBC charge).

Studying on different subsystem activities means more binning will be made for the first  $p_T$  bin. In other words, the statistics for low side band will be too low to carry a good analysis for background  $A_N$ . However, inclusive  $A_N$  would be good enough for this study since dimuons are dominant(90%) in 2-sigma dimuon mass window.

# 8.1 A<sub>N</sub> with number of FVTXTracklets

For each dimuon that passed the dimuon event cuts, the corresponding number of FVTXTracklets information will be calculated with the data collected by FVTX. A total number of FVTXTracklets is already in picoDST. The FVTXTracklets which is coming from dimuons or with less than two hits in FVTX or FVTX  $dca_r$ ; 1.0 will be excluded from total number of FVTXTracklets. Figure 56 shows the number of FVTXTracklets distribution. Basing on the distribution, four bins has been made for number of FVTXTracklets. Each bin has roughly equal statistics.



Figure 56: FVTX Tracklets distribution for the dimuons that pass the dimuon event cuts with pAu data

Figure 57 shows the inclusive  $\mathcal{A}_N$  in each number of FVTXT racklets bin.



Figure 57: Inclusive  $A_N$  vs. nFVTXTracklets. The first point(star point) is the combined inclusive  $A_N$  for first  $p_T$  bin got in section 6.

# 8.2 $A_N$ with BBC centrality(charge)

Similar with number of FVTXTracklets, BBC centrality distribution is got for the dimuons that pass the dimuon event cuts. Figure 58 is BBC centrality distribution. Basing on the distribution, four bins has been made for BBC centrality. Each bin has roughly equal statistics.

Figure 59 is inclusive  $A_N$  in each BBC centrality(charge) bin. Considering that higher BBC centrality is corresponding to lower BBC charge, the BBC



Figure 58: BBC centrality distribution for the dimuons that pass the dimuon event cuts with pAu data

centrality binning in the figure is in the descending order.



Figure 59: Inclusive  $A_N$  vs. BBC centrality. The first point(star point) is the combined inclusive  $A_N$  for first  $p_T$  bin got in section 6.

## 8.3 $A_N$ in three and four $p_T$ bins

In order to check whether there exist a  $p_T$  dependent  $A_N$ , it would be helpful to make the number of  $p_T$  bin three and four rather than just two. Figure 60 and figure 61 show the inclusive  $A_N$  in three and four  $p_T$  bins. In the case of three  $p_T$  bins, the binning is [0GeV,1.2GeV],[1.2GeV,2GeV] and [2GeV,10GeV]. While in the case of four  $p_T$  bins, the binning is [0GeV,1.GeV], [1.GeV,1.8GeV],

### [1.8GeV,2.8GeV]and [2.8GeV,10GeV].

Since pAu data is very limited, the inclusive  $A_N$  with further binning in nFVTXTracklets and centrality is consistent with each other with relatively big statistical uncertainty. We cannot find out very strong evidences to show that  $A_N$  is dependent on nFVTXTracklets or/and centrality.



Figure 60: Inclusive  $A_N$  with three  $p_T$  bins.



Figure 61: Inclusive  $A_N$  with four  $p_T$  bins.

# 9 Systematic Uncertainty Study

In this section the results of a number of systematic studies are presented where the stability of the result is being probed.

## 9.1 Bunch shuffling result for transverse single spin $A_N$

Shuffling the assigned spin direction for each bunch is a method to check for bunch related false asymmetries. Those can occur if the acceptance or efficiency of the trigger or the detector depend on the bunch structure or the timing. By definition the average asymmetries with randomized spins are zero, but the distribution of asymmetries from many randomized samples would be wider than expected. Bunch shuffling is not sensitive to any physics related asymmetry, i.e., an asymmetry of the MiniBias trigger physics itself, background asymmetries or trigger biases. Of course, bunch shuffling is only sensitive to effects of a similar magnitude as the statistical error of the asymmetry.

The systematic bias has been checked with bunch shuffling. The procedure is:

- 1. randomly reassign the polarization direction for each bunch crossing,
- 2. recalculate the asymmetry,
- 3. repeat many times (in our case is 10000) to produce a shuffled asymmetry distribution centered around zero,
- 4. compare width of shuffled distribution to statistical error on the physics asymmetry

Figure 62 and 63 show the bunch shuffling result for pp in two  $p_T$  and figure 64 and 65 show the bunch shuffling result for p(Au). Those plots show that the peak of the Gaussian distribution is around zero and  $\sigma$  is around one.



Figure 62: 10000 times bunch shuffling  $p_T$  dependent inclusive asymmetries calculated by standalone code on blue beam with pp data

# 9.2 Systematic uncertainty from different invariant mass fitting

The other source of systematic uncertainty comes from background fraction got from different fitting methods. The dimuon invariant mass is fitted by one



Figure 63: 10000 times bunch shuffling  $p_T$  dependent background asymmetries calculated by standalone code on blue beam with pp data



Figure 64: 10000 times bunch shuffling  $p_T$  dependent inclusive asymmetries calculated by standalone code on blue beam with pAu data



Figure 65: 10000 times bunch shuffling  $p_T$  dependent background asymmetries calculated by standalone code on blue beam with pAu data

Crystal Ball function for  $J/\psi$  peak, one Gaussian function for  $\psi'$  peak and a third-order polynomial for the background.

The fitting result with pp data is shown in figure 66 to 68 and figure 69 to 74 show the fitting result with pAl and pAu data respectively.



Figure 66: CB+Gaussian+Pol3 fitting in North and South arm with pp data



Figure 67: CB+Gaussian+Pol3 fitting in North and South arm for different  $p_T$  bins with pp data



Figure 68: CB+Gaussian+Pol3 fitting in North and South arm for different  $x_F$  bins with pp data



Figure 69: CB+Gaussian+Pol3 fitting in North and South arm with pAu data



Figure 70: CB+Gaussian+Pol3 fitting in North and South arm for different  $p_T$  bins with  $p{\rm Au}$  data



Figure 71: CB+Gaussian+Pol3 fitting in North and South arm for different  $x_F$  bins with  $p{\rm Au}$  data



Figure 72: CB+Gaussian+Pol3 fitting in North and South arm with pAl data



Figure 73: CB+Gaussian+Pol3 fitting in North and South arm for different  $p_T$  bins with pAl data



Figure 74: CB+Gaussian+Pol3 fitting in North and South arm for different  $x_F$  bins with pAl data

A set of background fraction is got using this new fitting function with pp, pAl and pAu data. Table 17, 18 and 19 list the background fraction for each bin. The differences between two different fitting methods in each bin are treated as systematic uncertainty of background fraction and it propagates to the systematic uncertainty of  $A_N^{J/\psi}$  using equation:

$$\delta_{sys} A_N^{J/\psi} = \frac{\partial A_N^{J/\psi}}{\partial f} \dot{\delta f} = \frac{A_N^{Incl.} - A_N^{bgr}}{(1-f)^2} \dot{\delta f}$$
(13)

$p_T$	$f_{Bgr} \pm \delta f_{Bgr}(Stat.)(\%)$ North	$f_{Bgr} \pm \delta f_{Bgr}(Stat.)(\%)$ South
$p_T \in 0-2$	11.6	10.7
$p_T \in 2 - 10$	9.0	8.2
$x_F \in 0.05 - 0.11$	12.8	11.4
$x_F \in 0.11 - 0.30$	6.4	5.7

Table 17: Background Fraction with CB + Gaussian + 3Pol for pp data

$p_T$	$f_{Bgr} \pm \delta f_{Bgr}(Stat.)(\%)$ North	$f_{Bgr} \pm \delta f_{Bgr}(Stat.)(\%)$ South
$p_T \in 0-2$	12.7	18.7
$p_T \in 2 - 10$	10.9	10.5
$x_F \in 0.05 - 0.11$	13.5	18.1
$x_F \in 0.11 - 0.30$	7.2	8.9

Table 18: Background Fraction with CB + Gaussian + 3Pol for pAu data

$p_T$	$f_{Bgr} \pm \delta f_{Bgr}(Stat.)(\%)$ North	$f_{Bgr} \pm \delta f_{Bgr}(Stat.)(\%)$ South
$p_T \in 0-2$	11.9	13.8
$p_T \in 2 - 10$	7.1	8.9
$x_F \in 0.05 - 0.11$	13.4	14.3
$x_F \in 0.11 - 0.30$	3.5	7.2

Table 19: Background Fraction with CB + Gaussian + 3Pol for pAl data

# 9.3 Systematic Uncertainty from $A_N^{bgr}$ in different mass window

As it has been described in previous section,  $A_N^{bgr}$  is estimated using the low side band dimuon mass range which is from 1.5GeV to 2.4GeV. Two different mass windows are used for estimating  $A_N^{bgr}$ : 1.3GeV - 1.9GeV and 1.9GeV - 2.5GeV. We use  $A_N^{bgr}$  from 1.9GeV - 2.5GeV mass window to calculate the systematic uncertainty in this analysis. Figure 75 to 77 show the  $A_N^{bgr}$  in  $p_T$  bins got from different low side band mass range. The differences of  $A_N^{J/\psi}$  got from those  $A_N^{bgr}$ are treated as one of the systematic uncertainty sources.



Figure 75:  $A_N^{bgr}$  in  $p_T$  bins on Blue beam with different low side mass windows with pp data



Figure 76:  $A_N^{bgr}$  in  $p_T$  bins on Yellow beam with different low side mass windows with pp data



Figure 77:  $A_N^{bgr}$  in  $p_T$  bins with different low side mass windows with pAu data

#### 9.4 Combining Systematic Uncertainty from different sources

So far, three sources of systematic uncertainty are discussed in previous section. Source one is the systematic uncertainty coming from using different analysis method as we described in section 7. The other systematic uncertainty source is related with background fraction with different fitting methods. The last one is from  $A_N^{bgr}$  estimated with different mass windows. These sources are independent with each other. Therefore, they can be combined together by using function:

$$\delta_{sys.}A_N = \sqrt{\delta_{sys.(ML)}^2 A_N + \delta_{sys.(fit)}^2 A_N + \delta_{sys.(bgr)}^2 A_N} \tag{14}$$

# 10 Summary And Final Result

The transverse single spin asymmetries  $A_N$  in prompt muons productions (mostly from open heavy flavor decays) are measured as a function of  $x_F$  (one bin) and  $p_T$  (two bins) by using Run15 data.

For pp collision, since both proton beams are porlarized, we need to combine blue beam with yellow beam for forward and backward  $A_N$  using equation 13:

$$A_{N}^{comb.} = \frac{A_{N}^{Blue} \cdot 1/(\delta_{stat.} A_{N}^{Blue})^{2} + A_{N}^{Yellow} \cdot 1/(\delta_{stat.} A_{N}^{Yellow})^{2}}{1/\delta_{stat.}^{2} A_{N}^{Blue} + 1/\delta_{stat.}^{2} A_{N}^{Yellow}}$$
(15)

The statistic uncertainty is given by:

$$\delta_{stat.}^2 A_N^{comb.} = \frac{1}{1/\delta_{stat.}^2 A_N^{Blue} +_{stat.} 1/\delta^2 A_N^{Yellow}}$$
(16)

The systematic uncertainty from background fraction is given by:

$$\delta_{sys.}A_N^{comb.} = \sqrt{\left(\frac{\partial A_N^{comb.}}{\partial A_N^{Blue}}\right)^2 \delta_{sys.}^2 \dot{A}_N^{Blue}} + \left(\frac{\partial A_N^{comb.}}{\partial A_N^{Yellow}}\right)^2 \delta_{sys.}^2 \dot{A}_N^{Yellow}} \tag{17}$$

Figure 78 and 79 show the  $A_N^{J/\psi}$  with statistic and combined systematic uncertainty and table 20, 21 and 22 list the value of  $A_N^{J/\psi}$  as well as systematic /statistical uncertainties in each bin for pp, pAl and pAu data. Figure 80 shows the comparison between Run15 and previous analysis result. The fluctuation for each point is about 1 sigma.

$$\begin{array}{c|c} & \text{North Arm} & \text{South Arm} \\ p_T & A_N^{J/\psi} \pm \delta A_N^{J/\psi}(Stat.) \pm \delta A_N^{J/\psi}(Syst.) & A_N^{J/\psi} \pm \delta A_N^{J/\psi}(Stat.) \pm \delta A_N^{J/\psi}(Syst.) \\ \hline p_T \in 0-2 & 0.004 \pm 0.011 \pm 0.003 & 0.013 \pm 0.011 \pm 0.002 \\ p_T \in 2-10 & 0.004 \pm 0.015 \pm 0.004 & 0.032 \pm 0.016 \pm 0.003 \\ x_F \in 0.05 - 0.11 & 0.004 \pm 0.011 \pm 0.001 & 0.014 \pm 0.011 \pm 0.003 \\ x_F \in 0.11 - 0.30 & 0.001 \pm 0.015 \pm 0.004 & 0.030 \pm 0.015 \pm 0.003 \\ \end{array}$$

Table 20:  $A_N^{J/\psi}$  with systematic uncertainty in different  $p_T$  bins with pp data



Figure 78: Forward and Backward  $A_N^{J/\psi}$  in different  $p_T$  bins with  $pp,\,p{\rm Al}$  and  $p{\rm Au}$  data



Figure 79:  $A_N^{J/\psi}$  in all  $x_F$  with pp, pAl and pAu data

Table 21:  $A_N^{J/\psi}$  with systematic uncertainty in different  $p_T$  bins with pAl data

$$\begin{array}{ccc} & \text{North Arm} & \text{South Arm} \\ p_T & A_N^{J/\psi} \pm \delta A_N^{J/\psi}(Stat.) \pm \delta A_N^{J/\psi}(Syst.) & A_N^{J/\psi} \pm \delta A_N^{J/\psi}(Stat.) \pm \delta A_N^{J/\psi}(Syst.) \\ p_T \in 0-2 & -0.067 \pm 0.025 \pm 0.004 & -0.074 \pm 0.029 \pm 0.014 \\ p_T \in 2-10 & 0.013 \pm 0.031 \pm 0.005 & 0.012 \pm 0.033 \pm 0.008 \\ x_F \in 0.05 - 0.11 & -0.027 \pm 0.027 \pm 0.006 & -0.058 \pm 0.027 \pm 0.008 \\ x_F \in 0.11 - 0.30 & -0.045 \pm 0.029 \pm 0.005 & -0.019 \pm 0.037 \pm 0.011 \end{array}$$

Table 22:  $A_N^{J/\psi}$  with systematic uncertainty in different  $p_T$  bins with pAu data



Figure 80:  $A_N^{J/\psi}$  in all  $x_F$  comparison with previous result with pp data. The fluctuation for each data point is around 1-sigma.