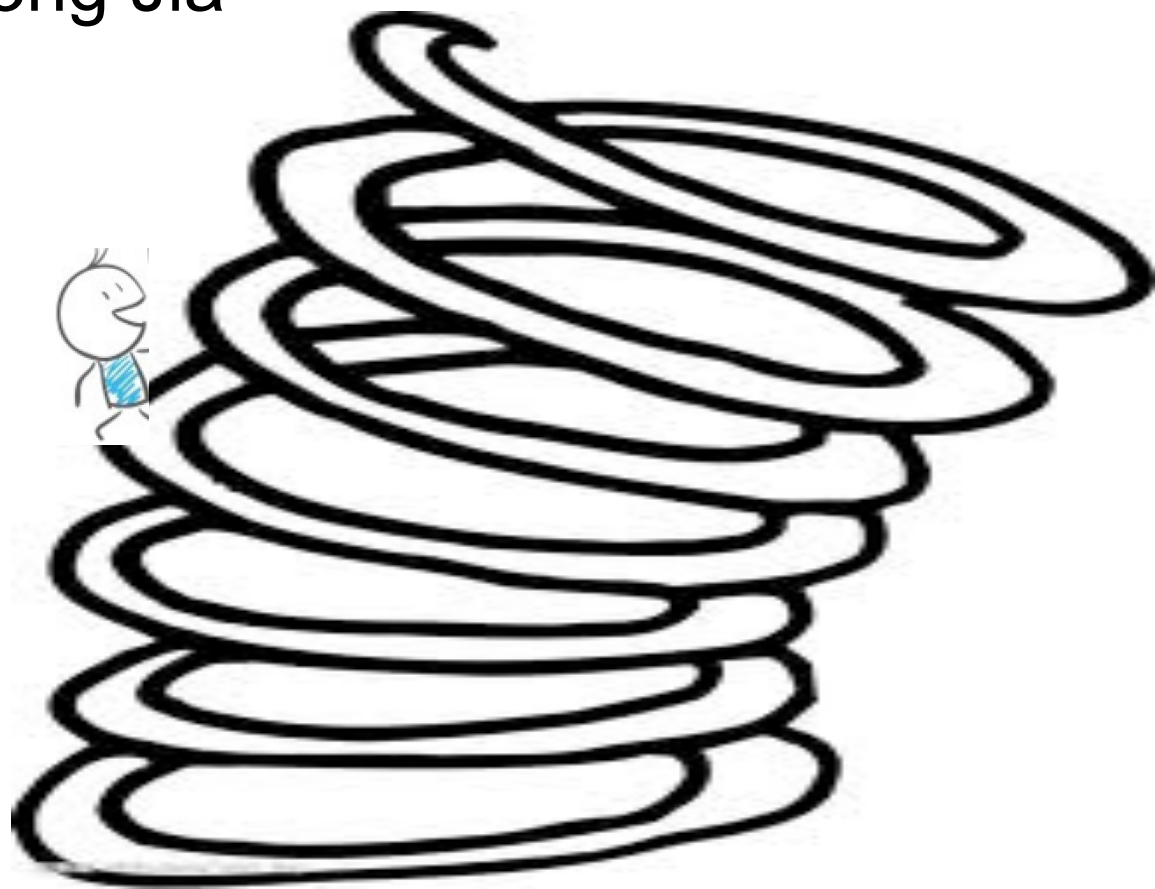


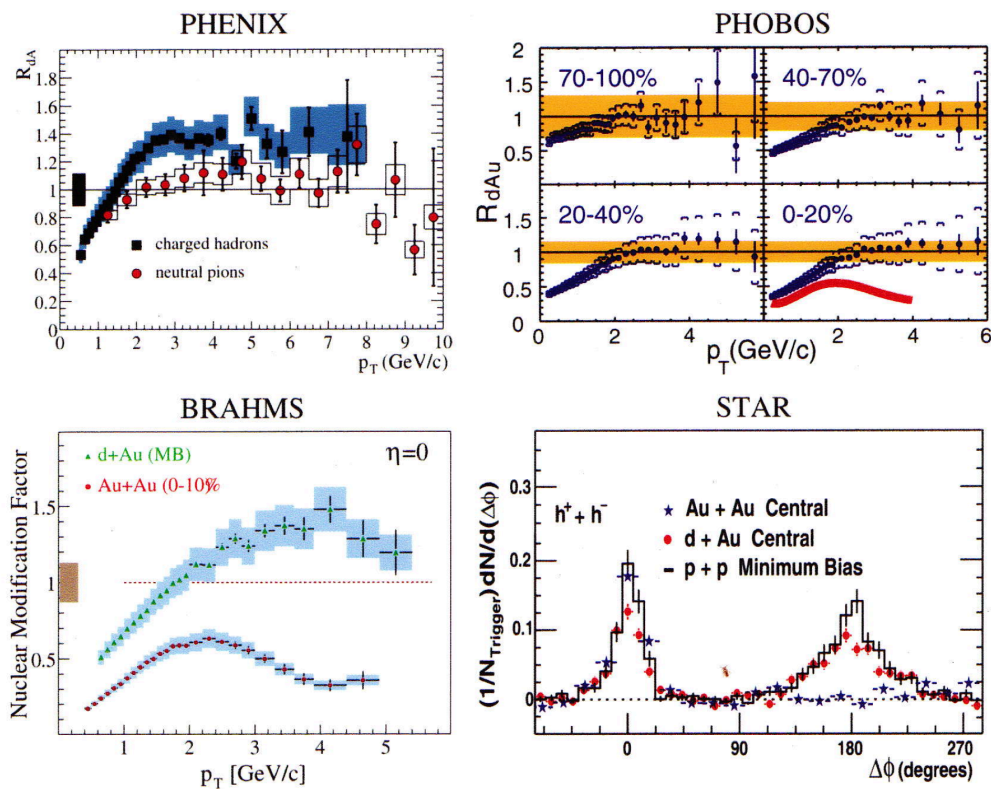
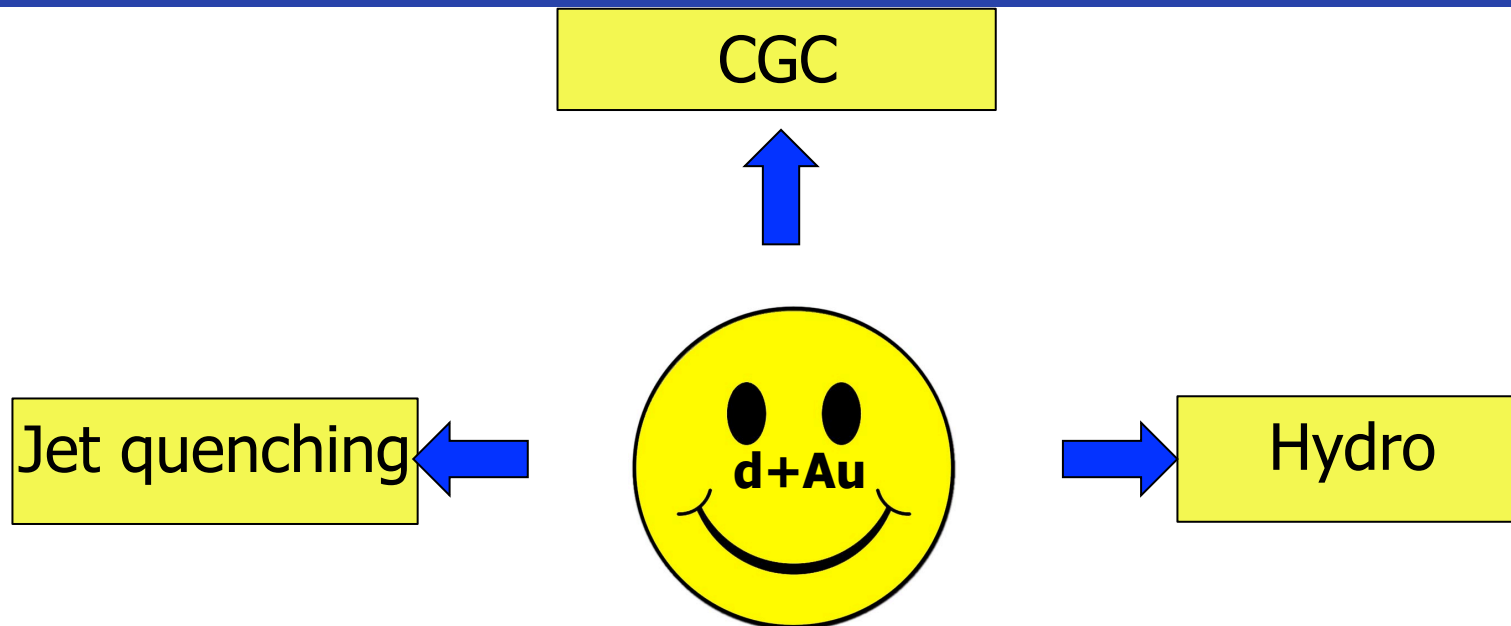


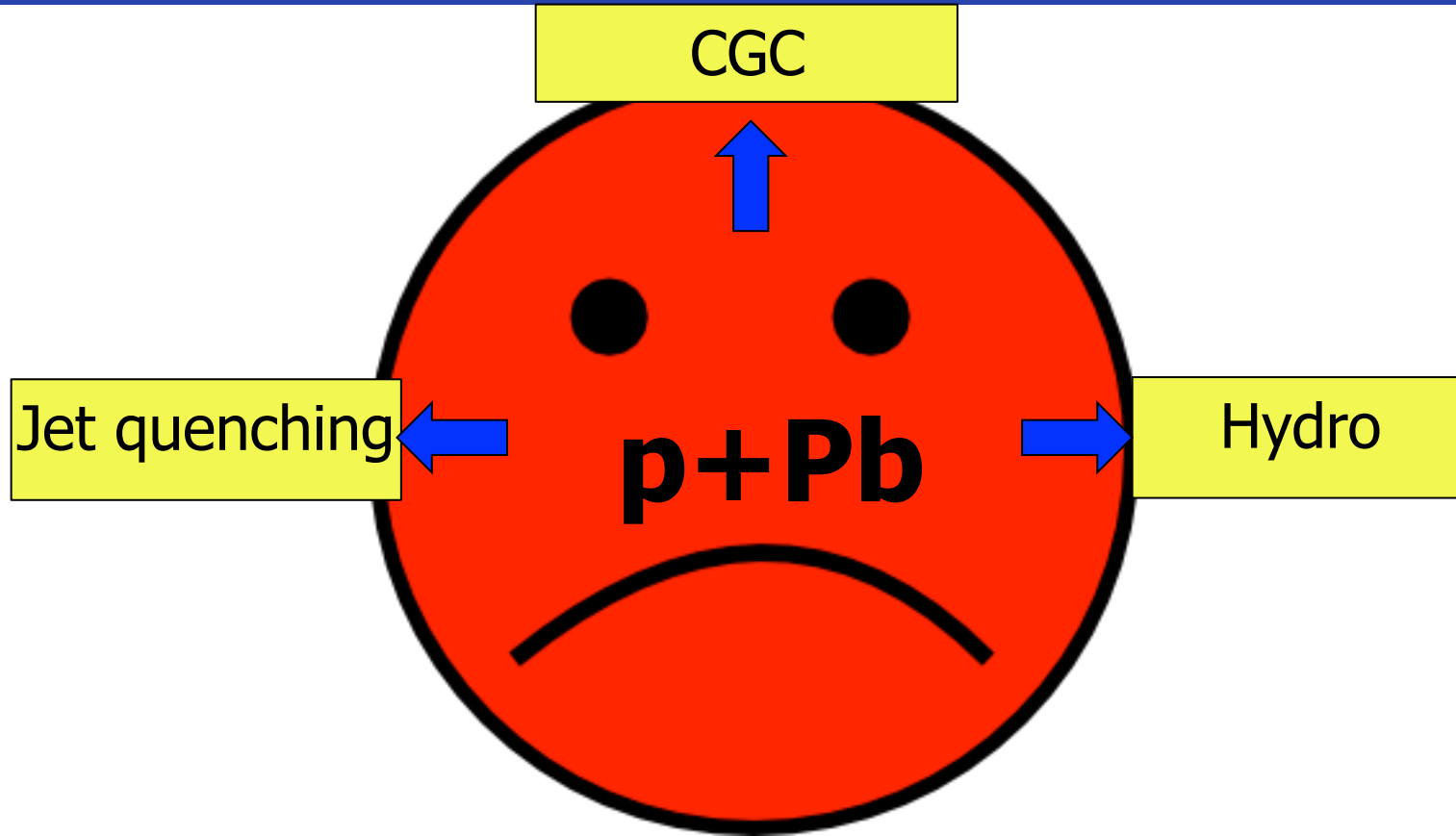
Some personal opinions

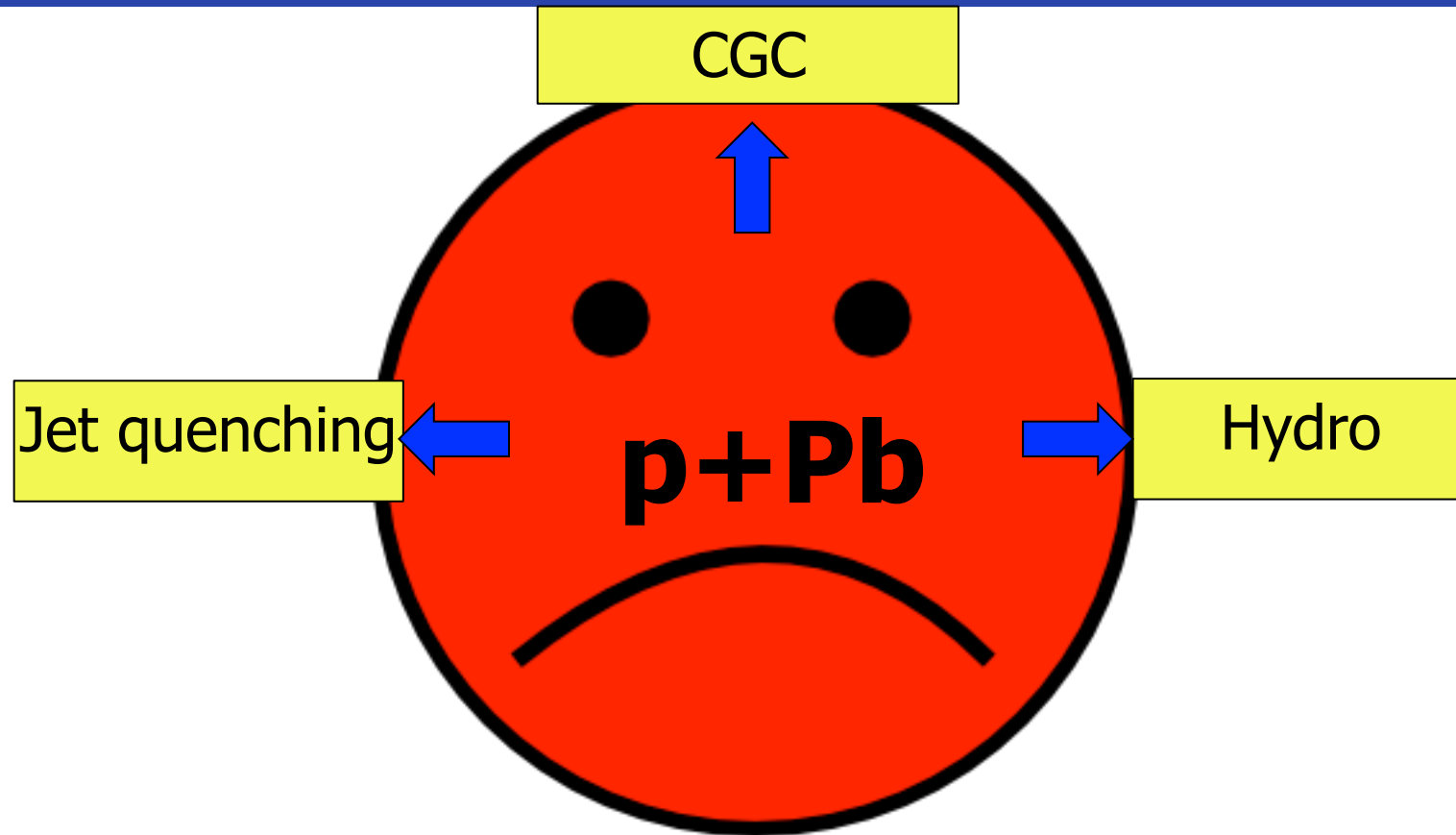
Jiangyong Jia



State of affair 2003



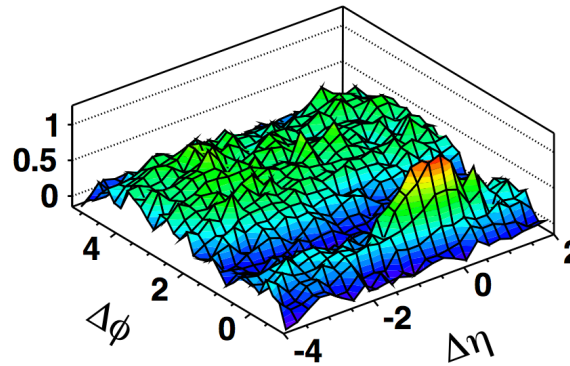
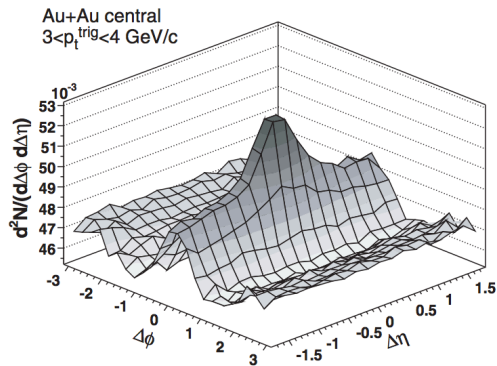




Miklos: My personal perspective is that instead of converging on a solid basis of null controls, we reached a **maximal entropy state both theoretically and experimentally**

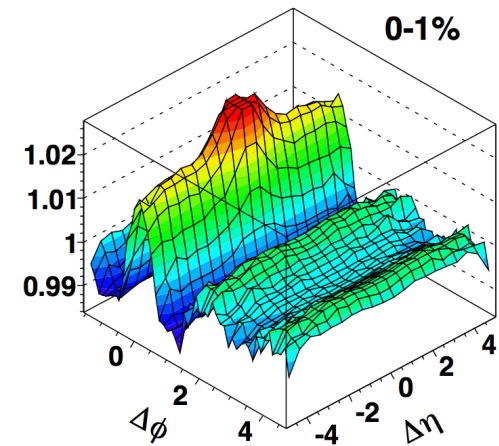
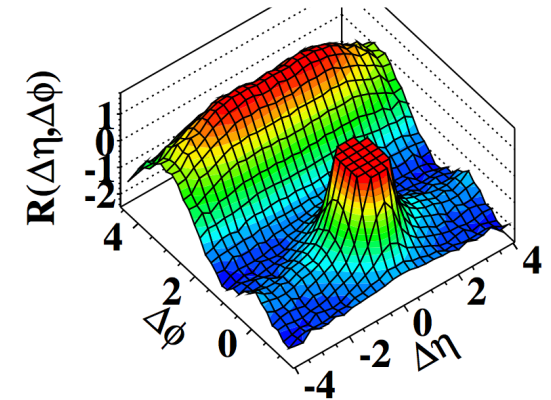
- Theory : Indeed...
- Experiment : undigested information \neq more entropy

What is the effective picture/theory of QCD in high-density system??

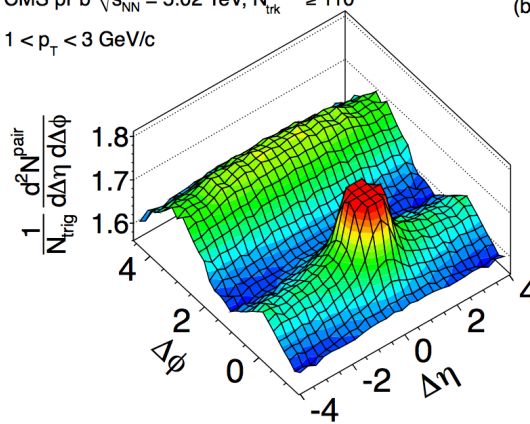


(b) Au+Au 0%-30% (PHOBOS)

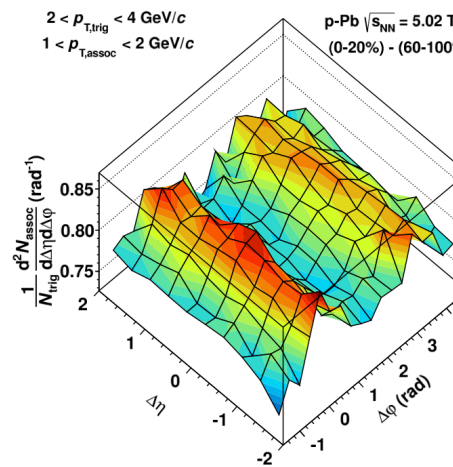
(d) CMS $N \geq 110$, $1.0 \text{ GeV}/c < p_T < 3.0 \text{ GeV}/c$



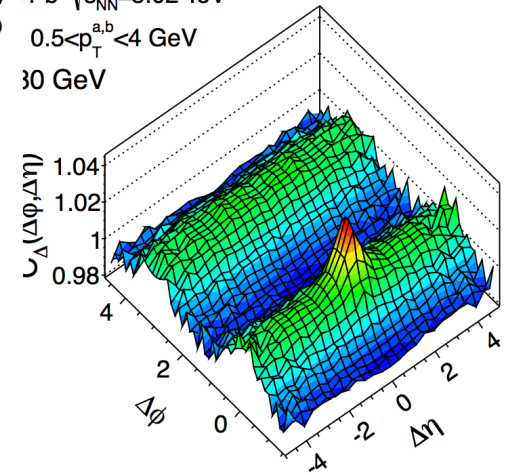
CMS pPb $\sqrt{s_{NN}} = 5.02 \text{ TeV}$, $N_{\text{trk}}^{\text{offline}} \geq 110$
 $1 < p_T < 3 \text{ GeV}/c$



(b)



$\rho\text{-Pb } \sqrt{s_{NN}} = 5.02 \text{ TeV}$
 (0-20%) - (60-100%)
 $0.5 < p_{T, \text{trig}}^{a,b} < 4 \text{ GeV}$
 30 GeV

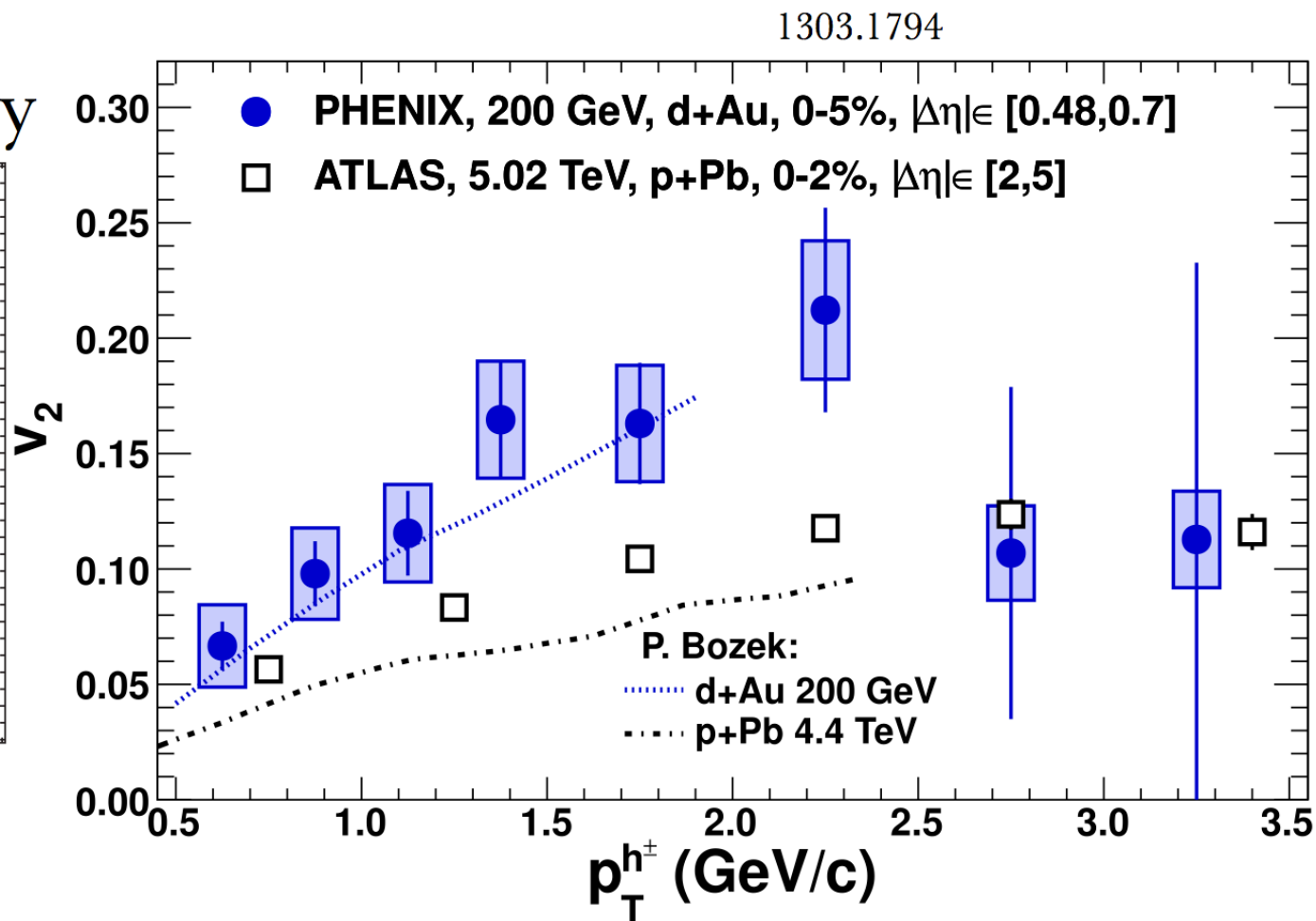
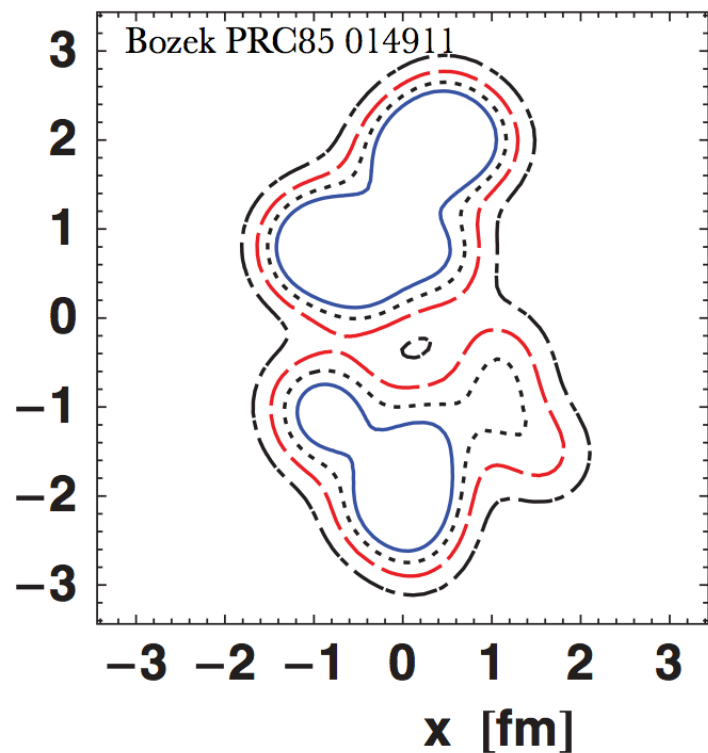


PROJECT

THE RIDGE AT RHIC & THE LHC

leveraging RHIC/LHC differences

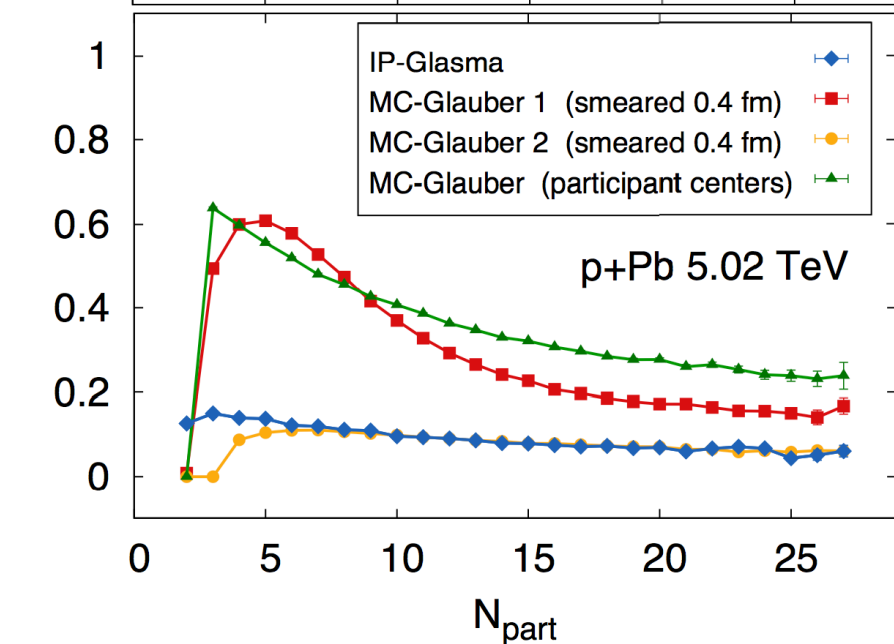
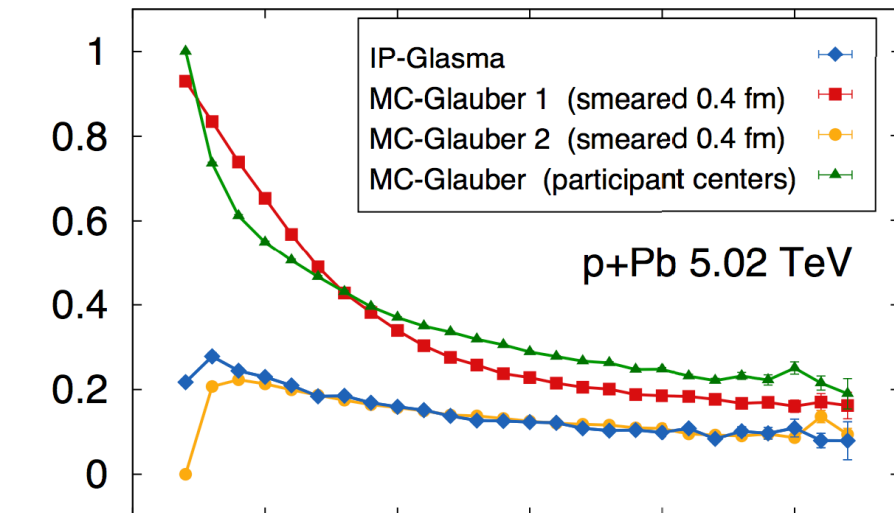
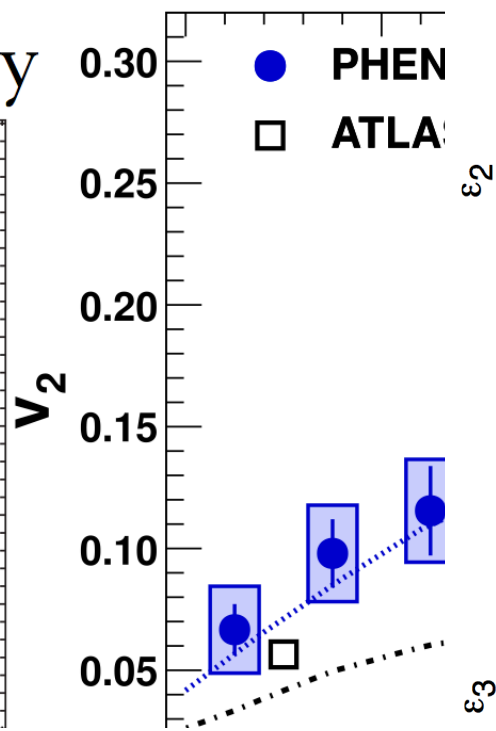
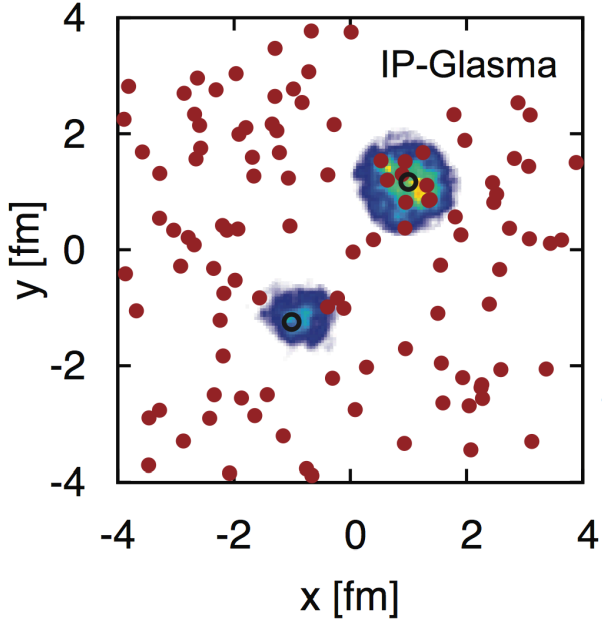
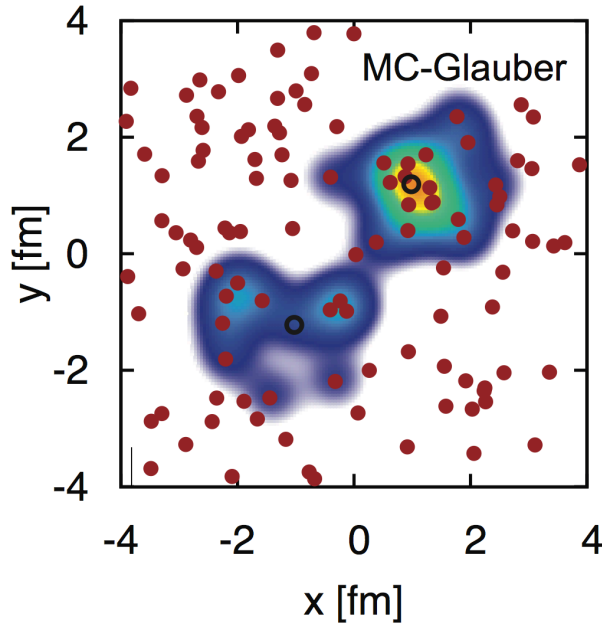
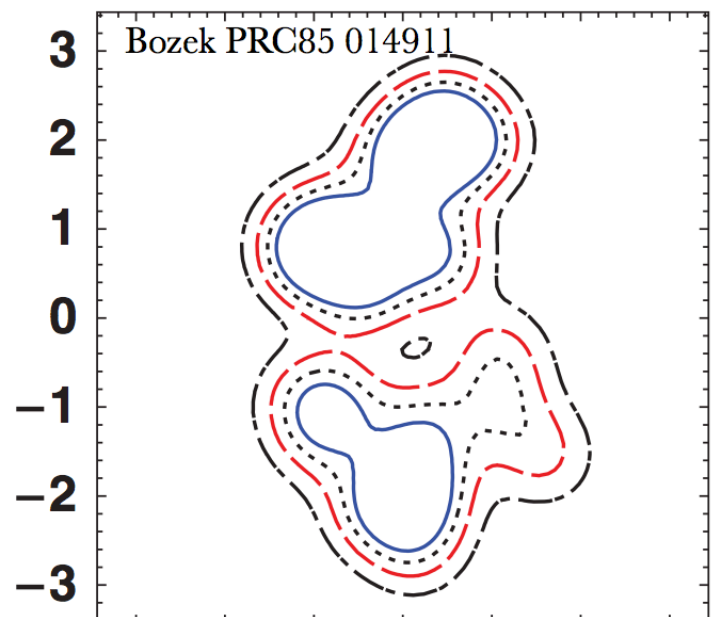
initial entropy density



- changing both the collision energy and the shape of the initial system as compared to the ridge seen in pPb

leveraging RHIC/LHC differences

initial entropy density

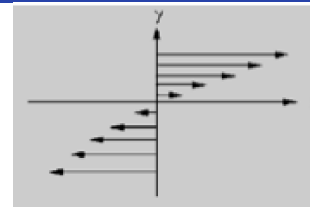


the shape of the initial system

Bzdak et.al. 1304.3403

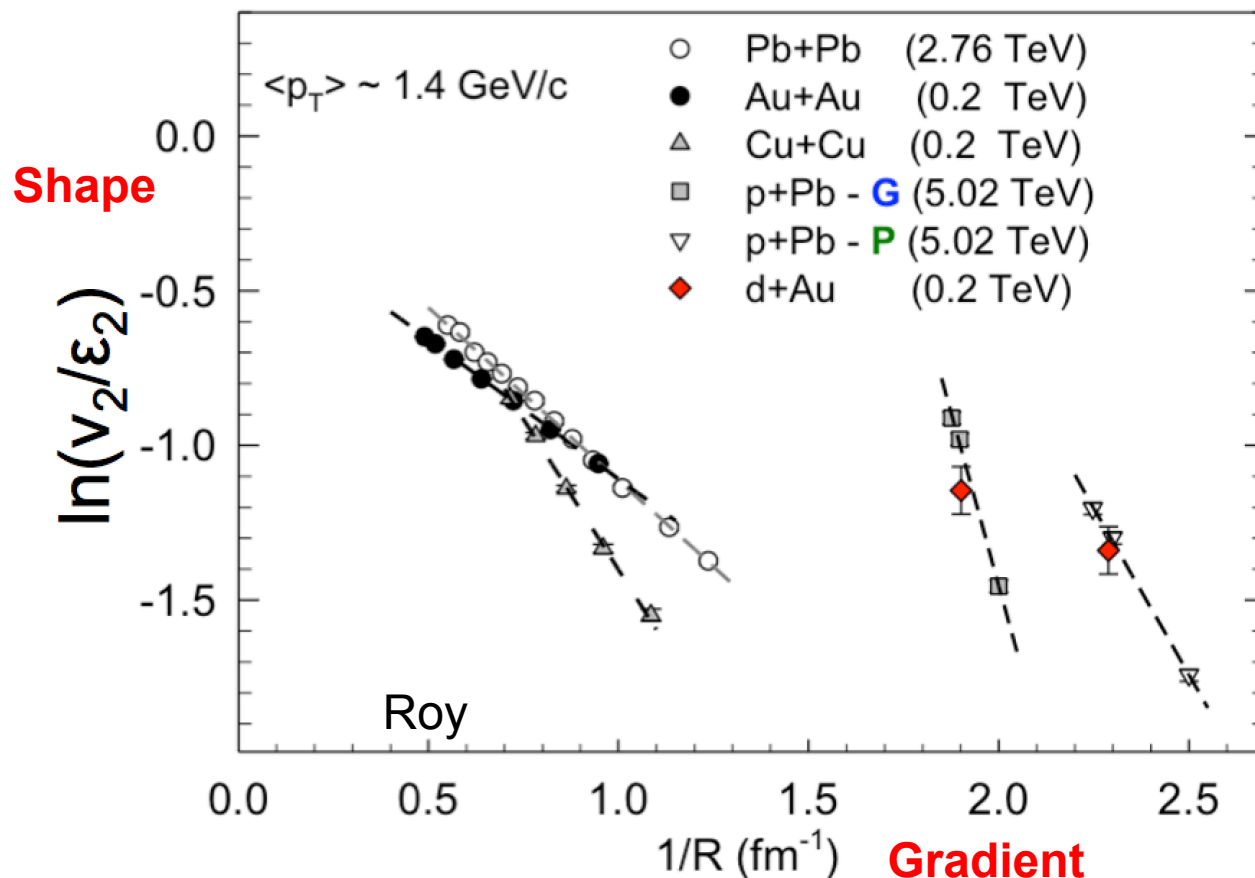
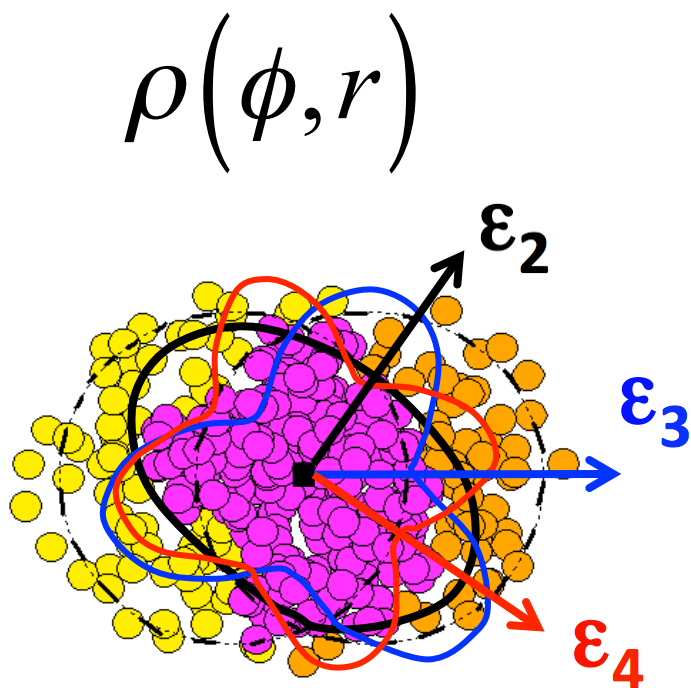
Hydrodynamics in small system?

- Flow depends on shape and size/gradient



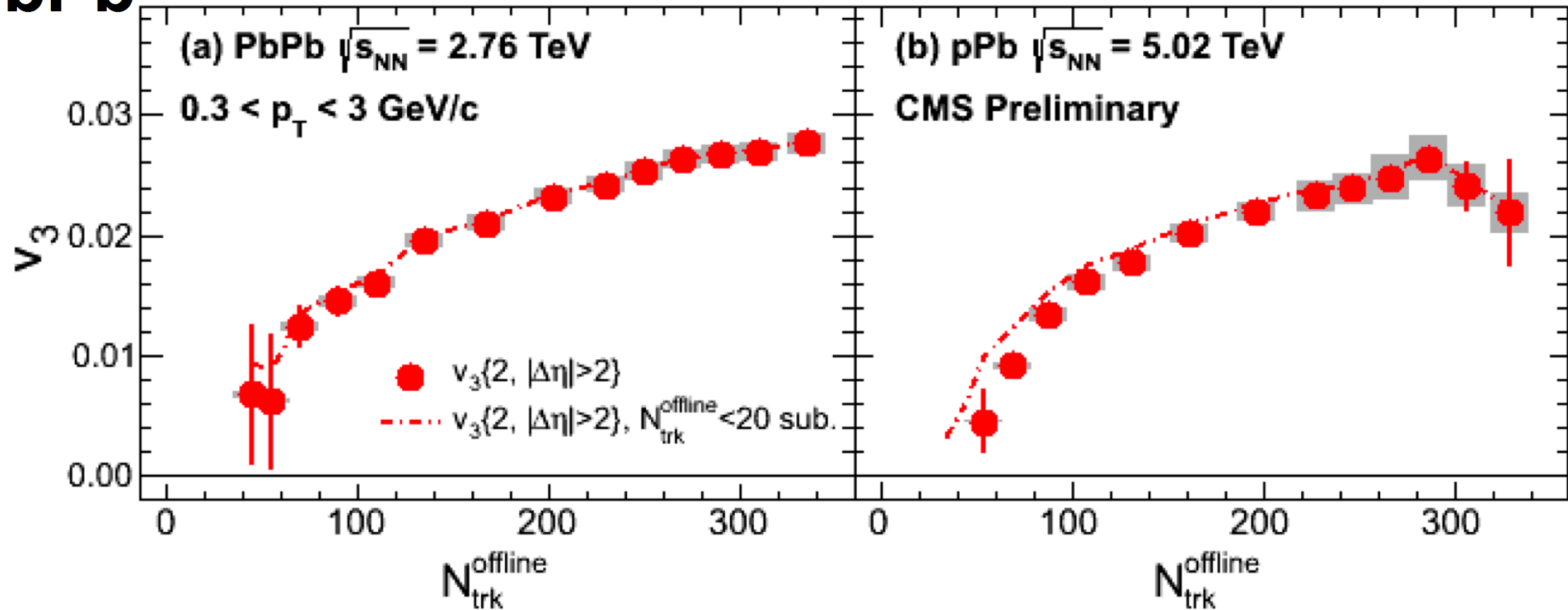
$$\frac{F_x}{A} = -\eta \frac{\partial v_x}{\partial y}$$

- HM pp and pA have larger density (η/s) but much larger gradient!



v_3 in pPb and PbPb

PbPb



pPb

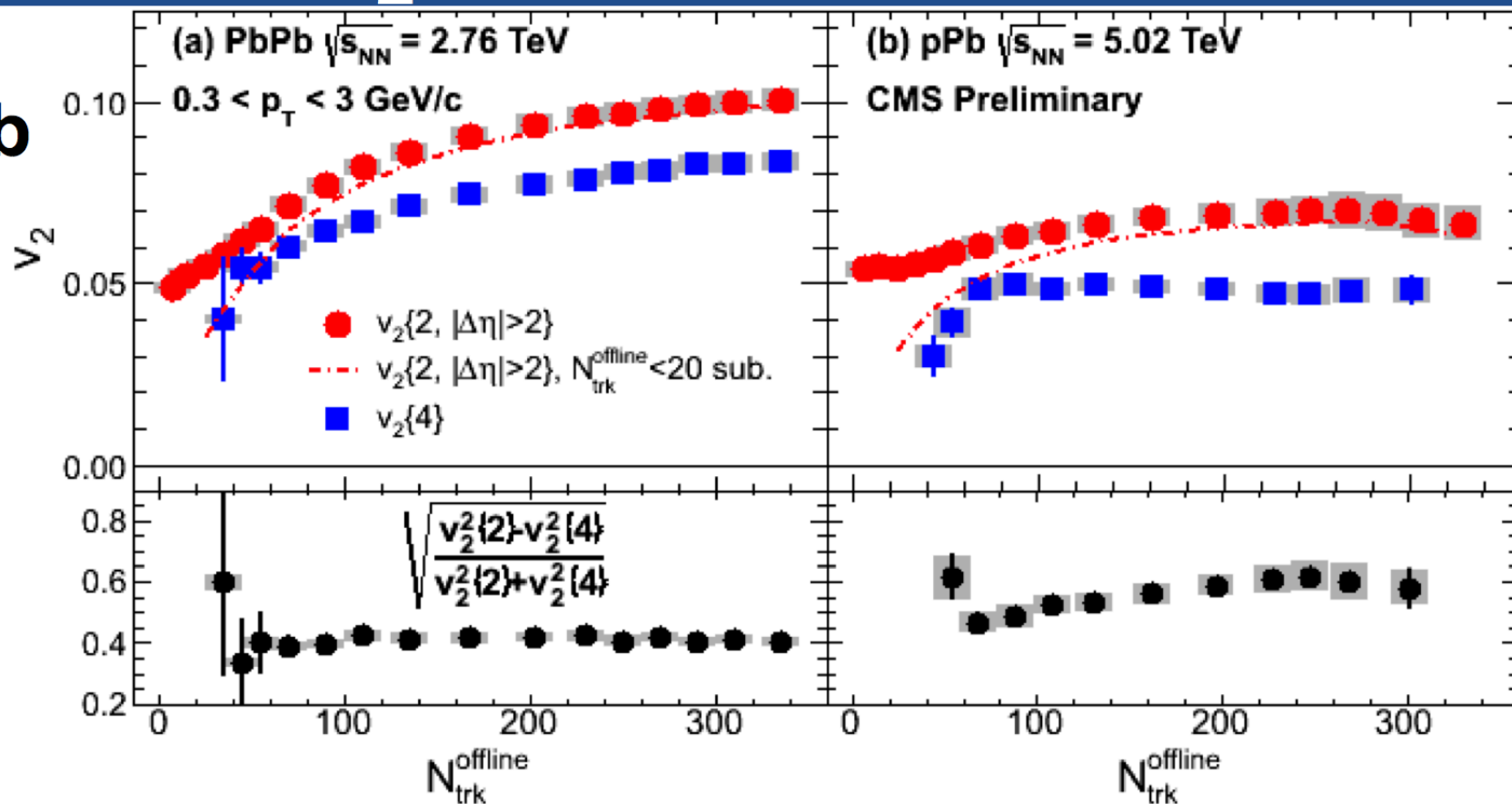
v_3 shows similar shape in pPb and PbPb; magnitude comparable

“Peripheral subtraction” makes essentially no difference

v_2 in pPb and PbPb

PbPb

pPb



“Fluctuations” larger in pPb,
 with moderate multiplicity
 dependence

$$v_2\{2\} = \sqrt{\langle v_2 \rangle^2 + \sigma_{v_2}^2}$$

$$v_2\{4\} = \sqrt{\langle v_2 \rangle^2 - \sigma_{v_2}^2}$$

$$\frac{\sigma_{v_2}}{v_2} = \sqrt{\frac{v_2^2\{2\} - v_2^2\{4\}}{v_2^2\{2\} + v_2^2\{4\}}}$$

Flow fluctuation & v_n {4}

- Bessel-Gaussian

$$p(\vec{v}_n) \propto \exp\left(\frac{-(\vec{v}_n - \vec{\bar{v}}_n)^2}{2\delta_n^2}\right)$$

$$p(v_n) \propto v_n \exp\left(\frac{-(v_n^2 + (\bar{v}_n)^2)}{2\delta_n^2}\right) I_0\left(\frac{v_n \bar{v}_n}{\delta_n^2}\right) \quad I_0(x) \approx e^{\frac{x^2}{4}} \left[1 - \frac{x^4}{64}\right]$$

For pure fluctuations $\bar{v}_n = 0 \Rightarrow p(v_n) \propto v_n \exp\left(\frac{-(v_n^2)}{2\delta_n^2}\right)$

- When $\alpha = \frac{\delta_n}{\bar{v}_n} \gg 1$ distribution is very close to pure Gaussian with a redefinition of δ

$$\begin{pmatrix} \delta_n^2 \\ \bar{v}_n \end{pmatrix} \rightarrow \begin{pmatrix} \delta_n^{2'} = \delta_n^2 + (\bar{v}_n)^2 / 2 \\ \bar{v}_n' = 0 \end{pmatrix}$$

Valid when

$$\frac{v_n \bar{v}_n}{\delta_n^2} \ll 64^{1/4} = 2.8 \text{ or } v_n \ll 2.8 \delta_n \alpha$$

Flow fluctuation & v_n {4}

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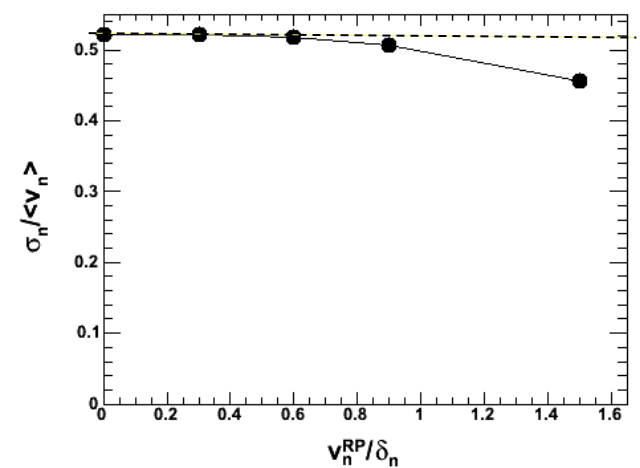
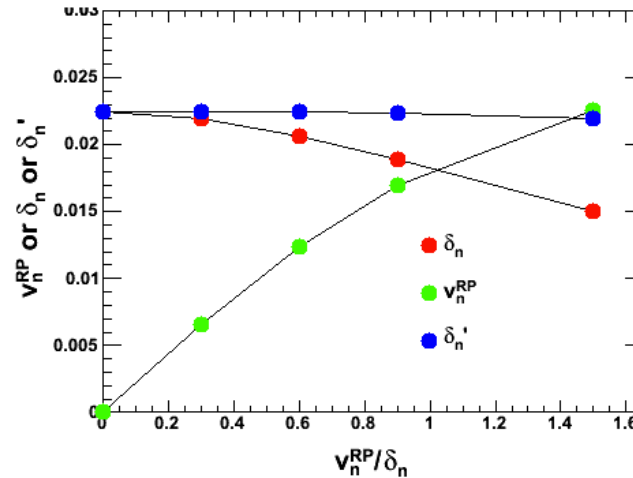
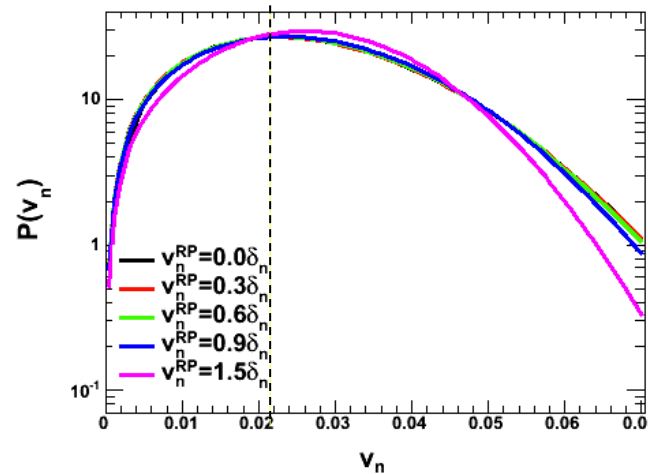
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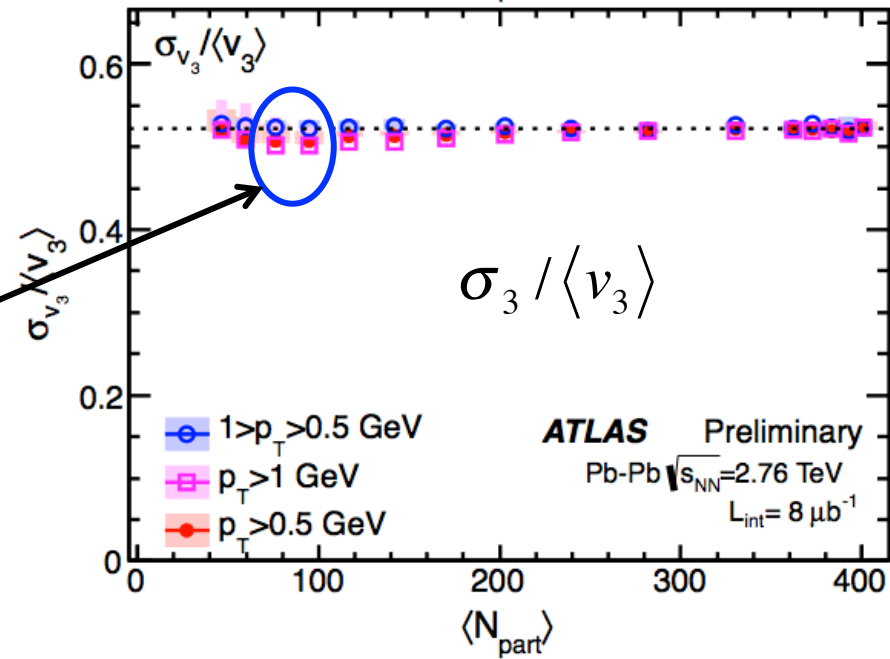
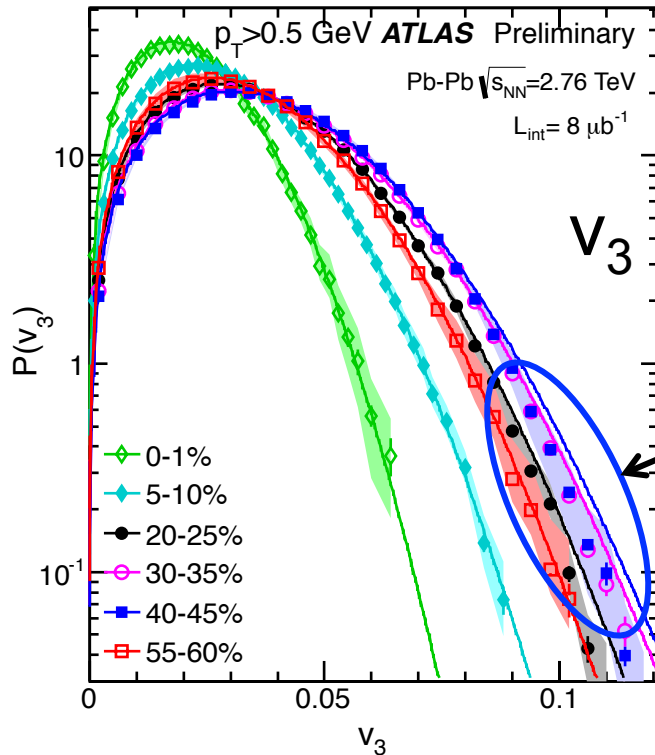
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Flow fluctuation & $v_n\{4\}$



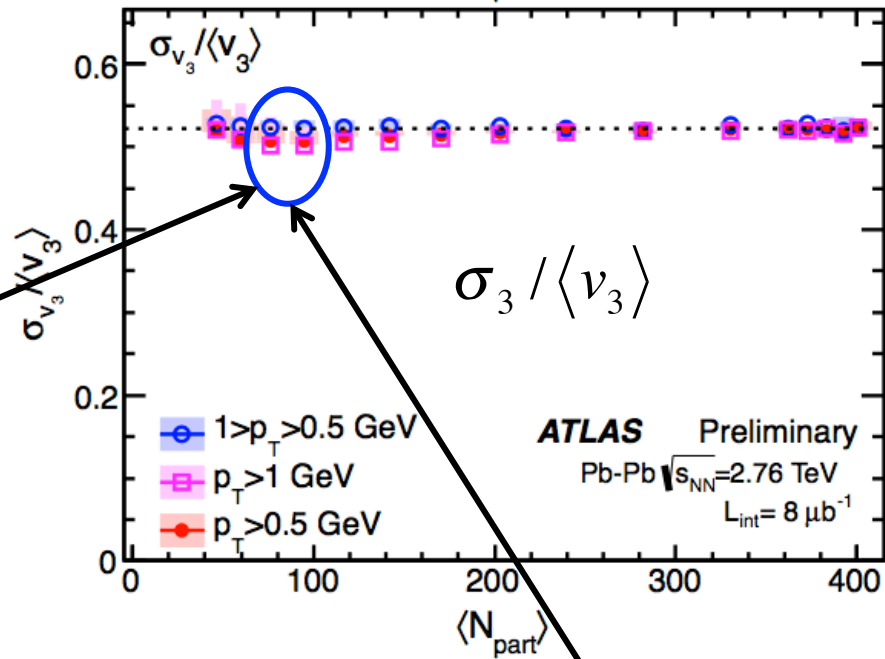
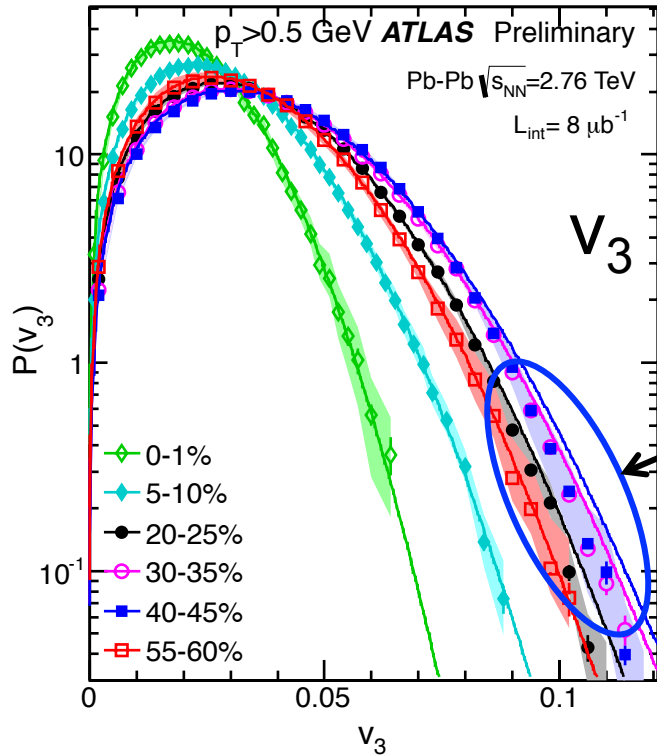
- Even a small deviation will give a large v_n^{RP} or large $v_n\{4\}$

$$v_n\{4\} = \left[2\langle v_n^2 \rangle^2 - \langle v_n^4 \rangle \right]^{1/4}$$



a 4% difference gives a $v_n\{4\}$
value of about 45% of $v_n\{2\}$

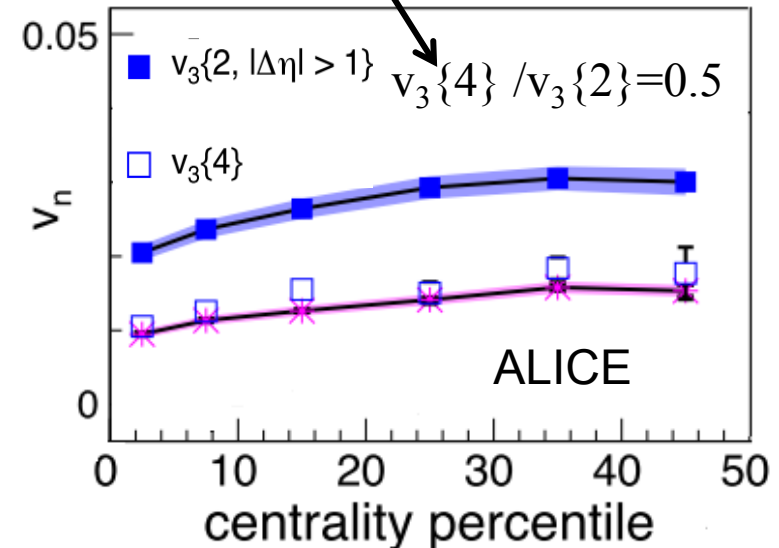
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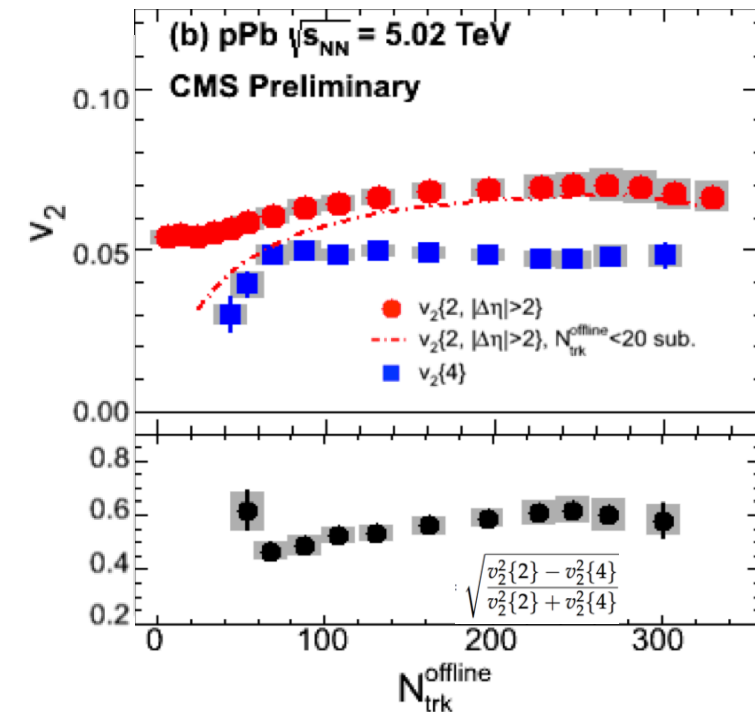
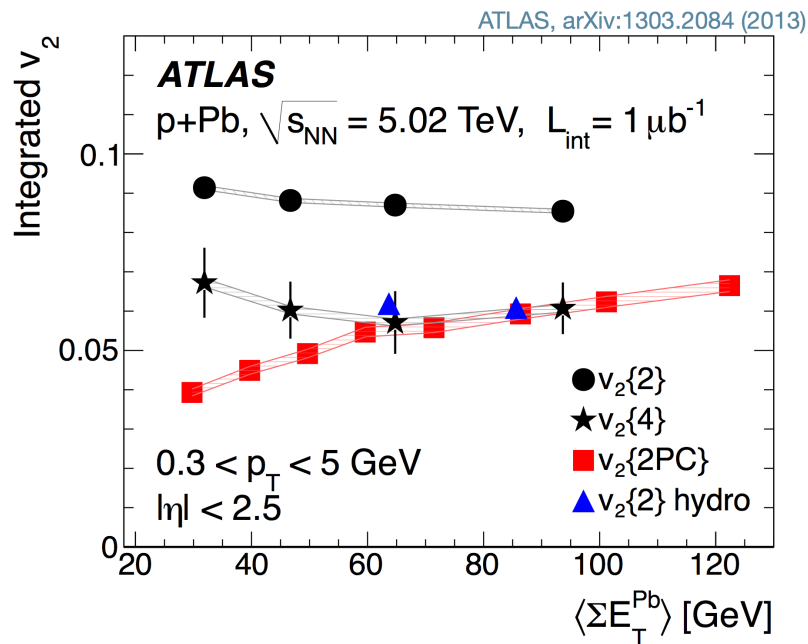


$v_2\{4\}$ in p+Pb

Just need a small deviation from Gaussian

- Small N_{part} , or Negative binomial fluctuation (Bozek)
- Fluctuation of M and v_n aren't de-coupled

$$\frac{dN}{d\phi} = M \left[1 + \sum_n 2v_n \cos n(\phi - \Phi_n) \right]$$

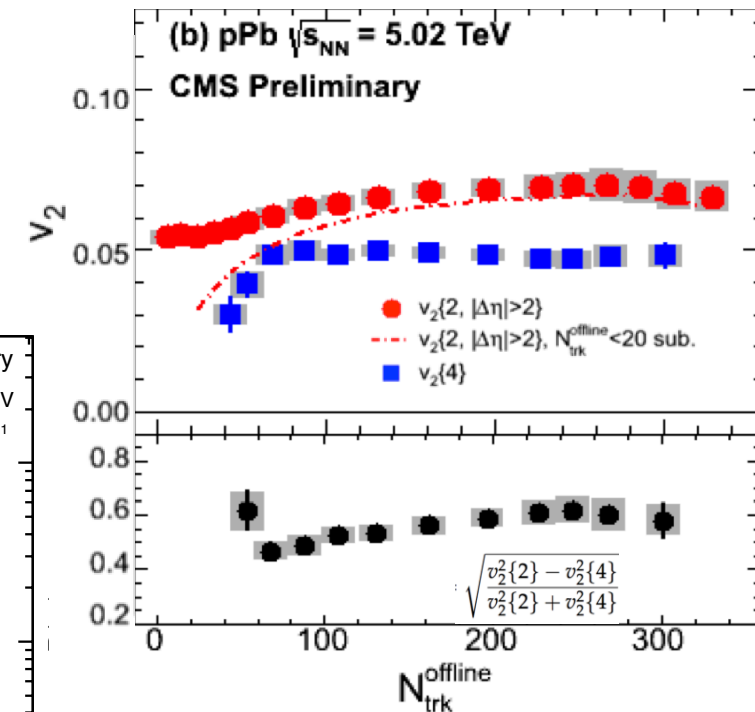
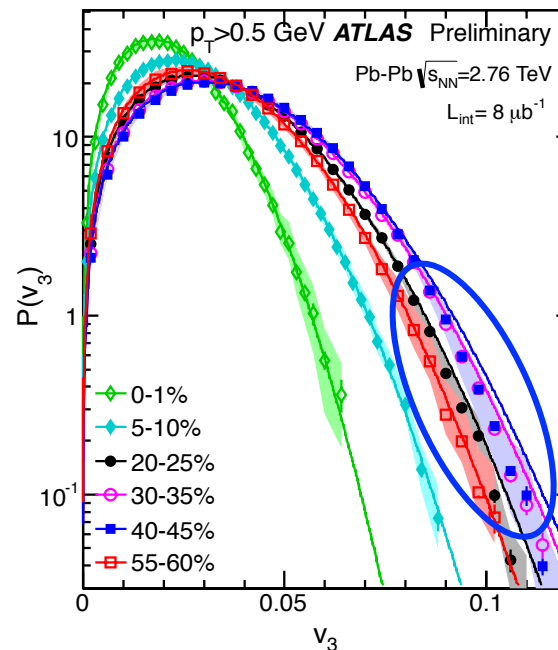
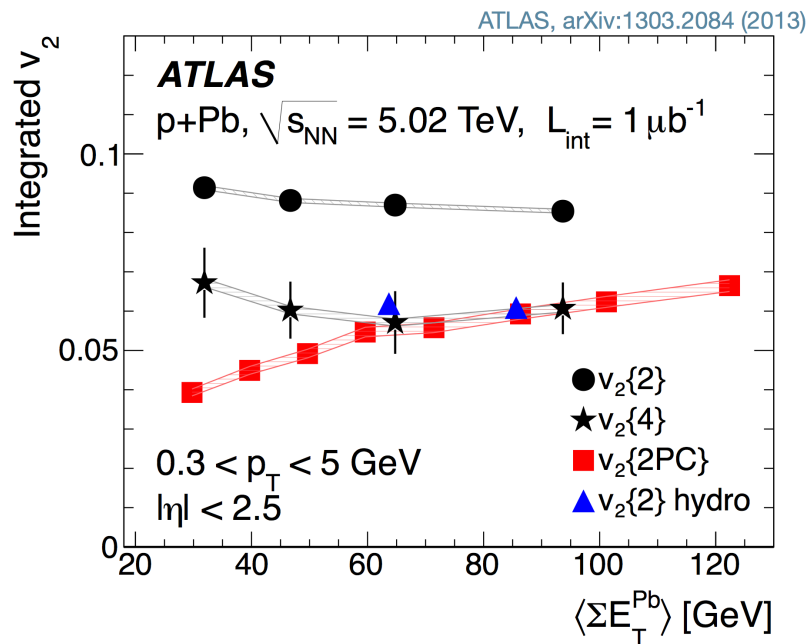


$v_2\{4\}$ in p+Pb

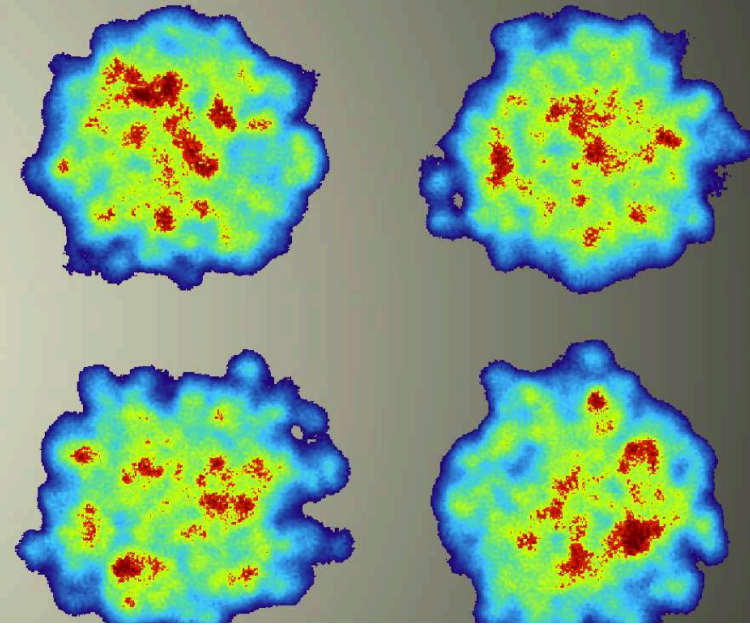
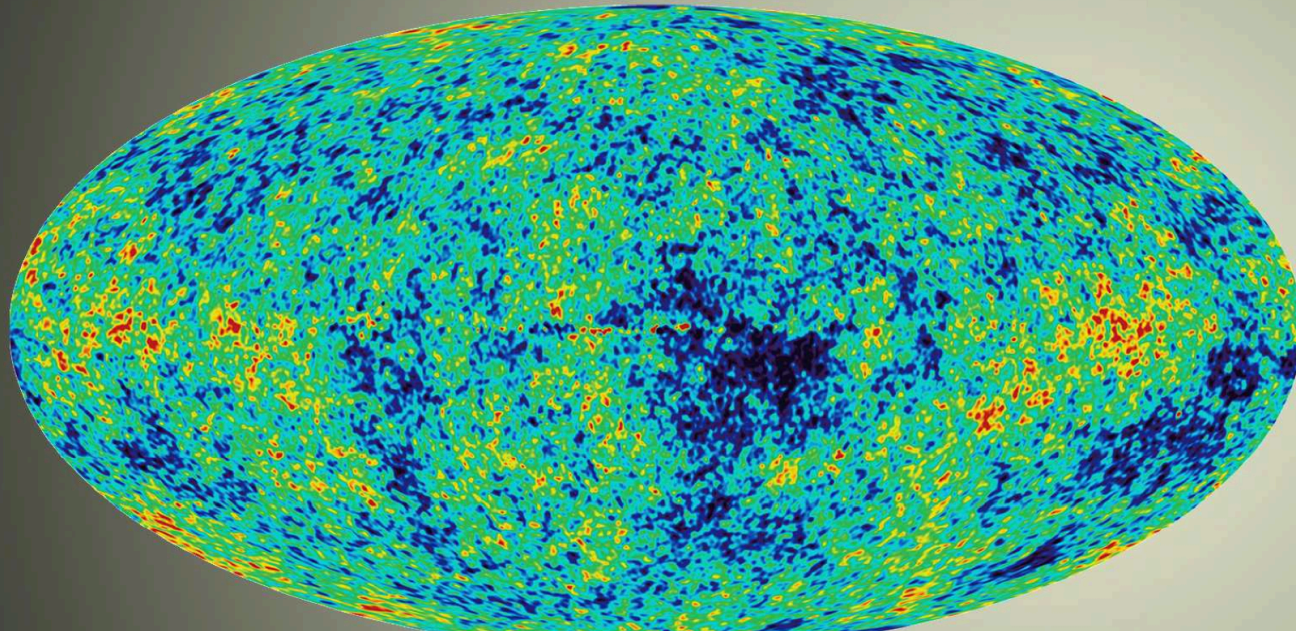
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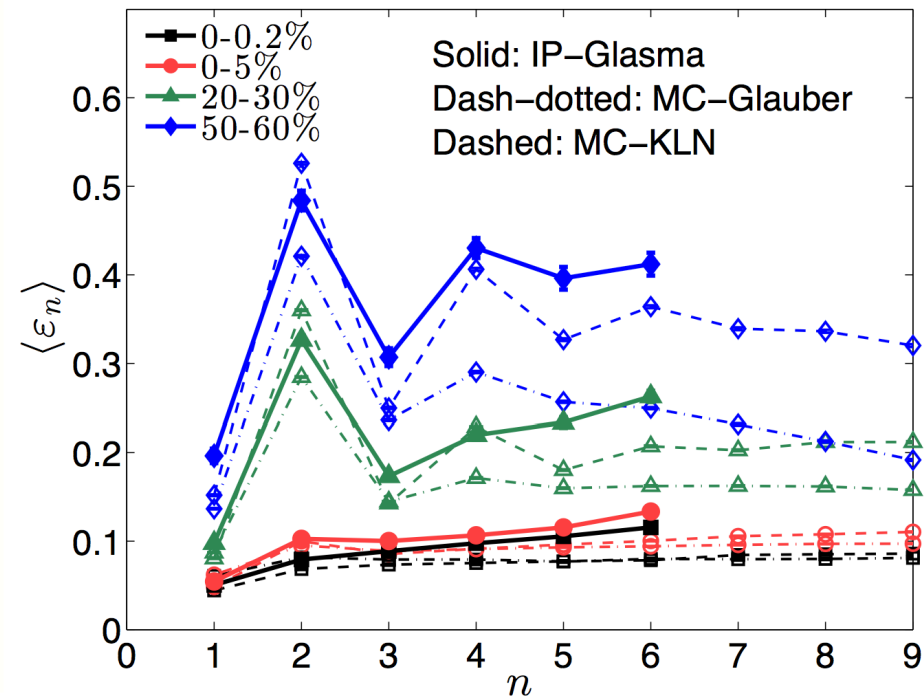
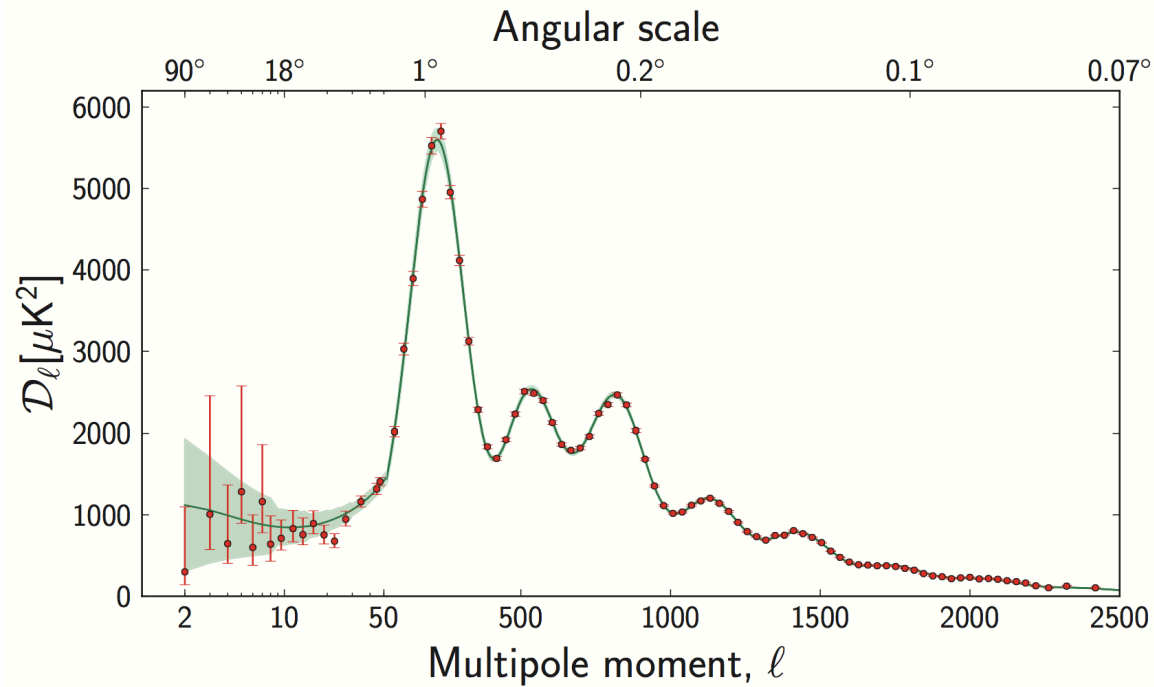


Power spectrum

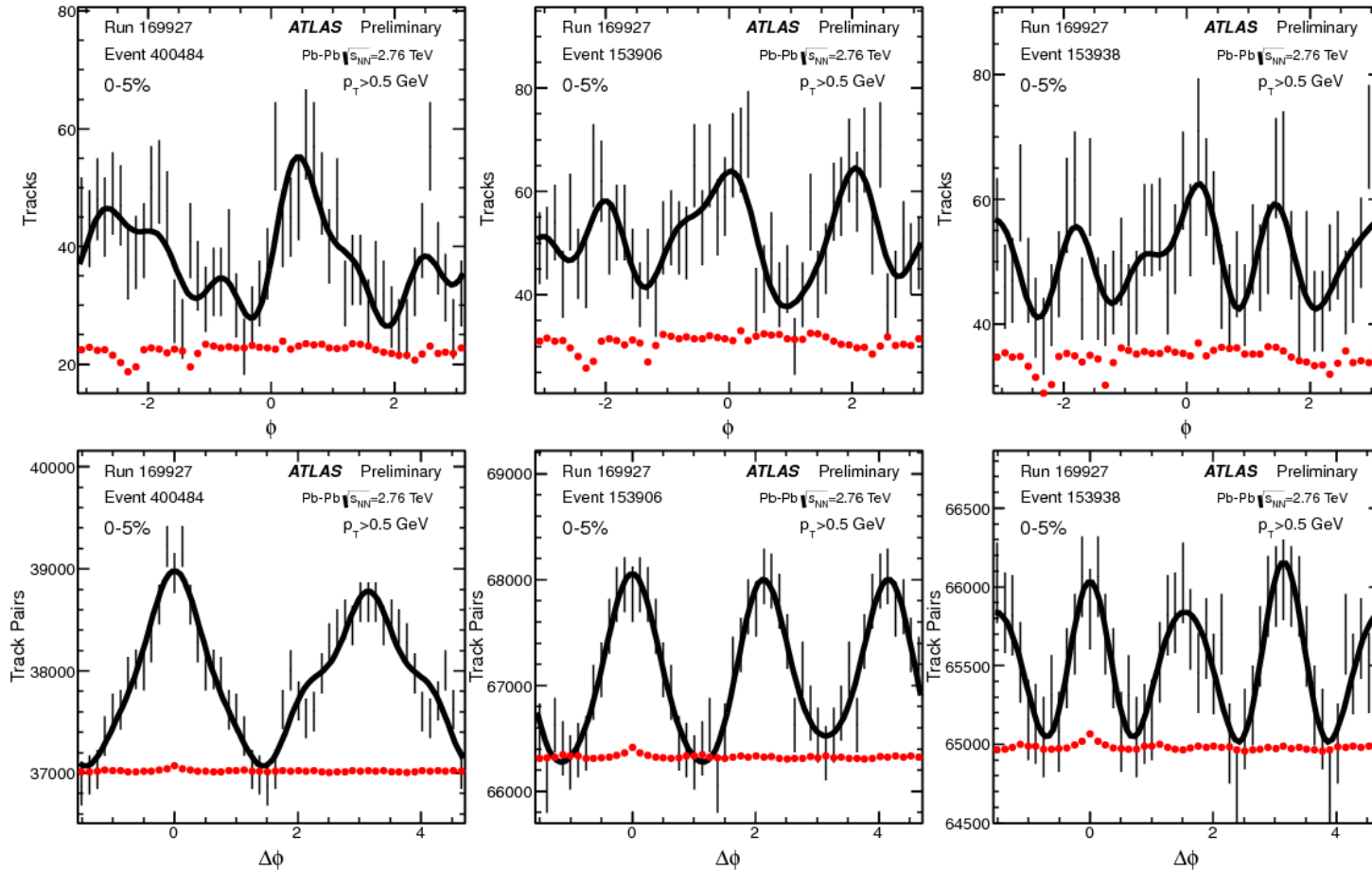


Planck 2013 CMB temperature power spectrum

Little Bang density power spectra 2013



Ripples of “little-bangs”



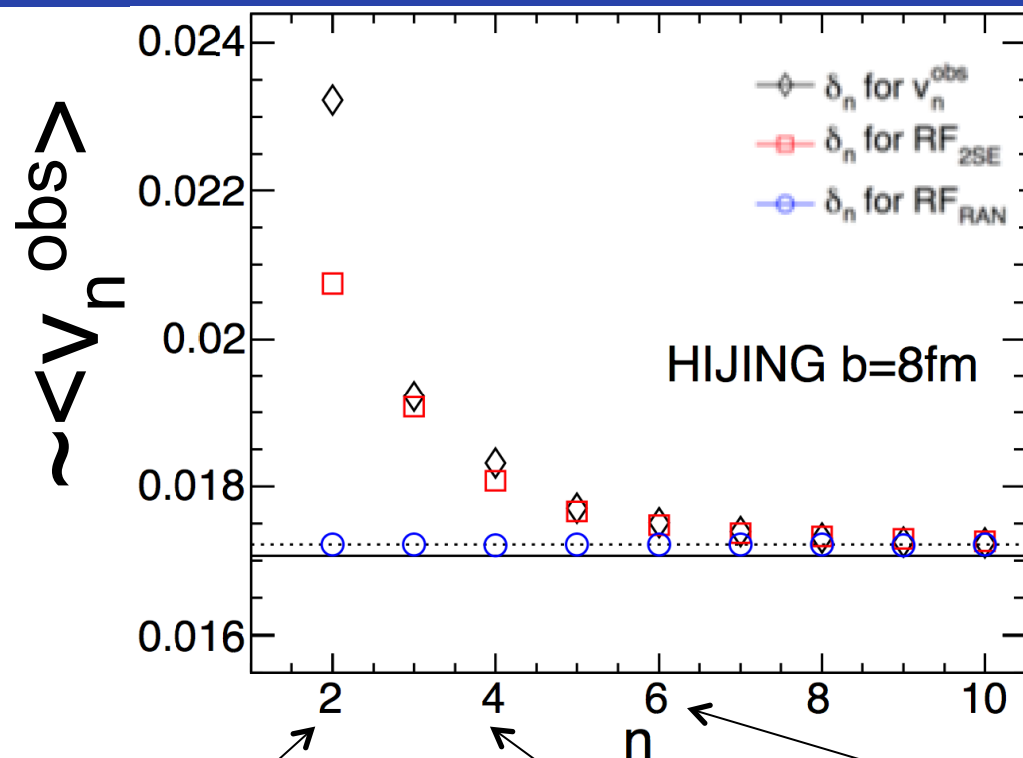
- Data-driven unfolding the key:

$$\text{Sub-event "A"} - \text{Sub-event "B"} = \left\{ \begin{array}{l} \text{Signal} \quad \quad \quad : \text{cancelled} \\ \text{Fluctuations+short-range corr.} : \sqrt{2} \text{ larger} \end{array} \right.$$

$$(\vec{v}_n^{\text{obs}})^a - (\vec{v}_n^{\text{obs}})^b = \text{nonflow} + \text{noise}$$

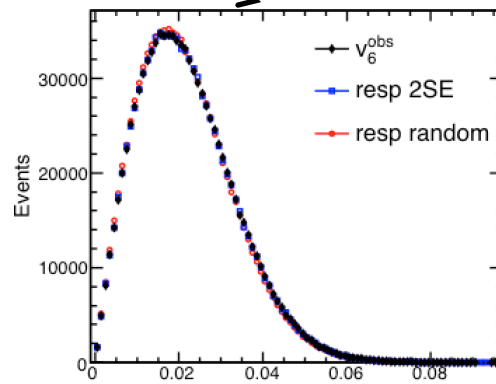
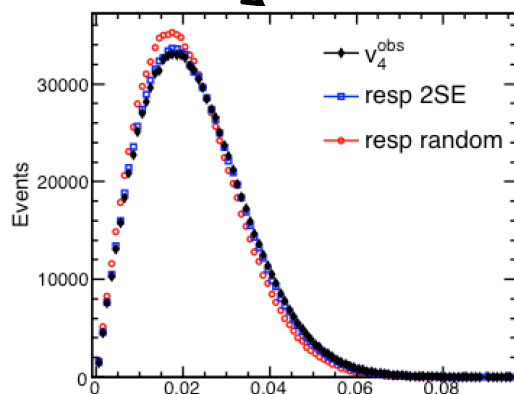
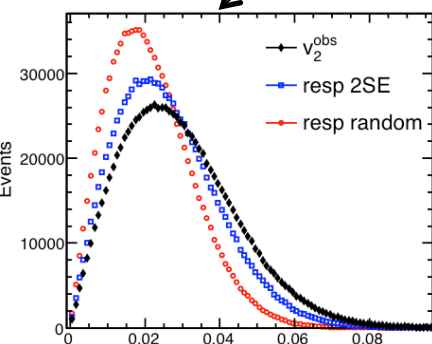
$$(\vec{v}_n^{\text{obs}})^a + (\vec{v}_n^{\text{obs}})^b = 2\vec{v}_n$$

Azimuthal power spectrum in hijing: (non-flow)

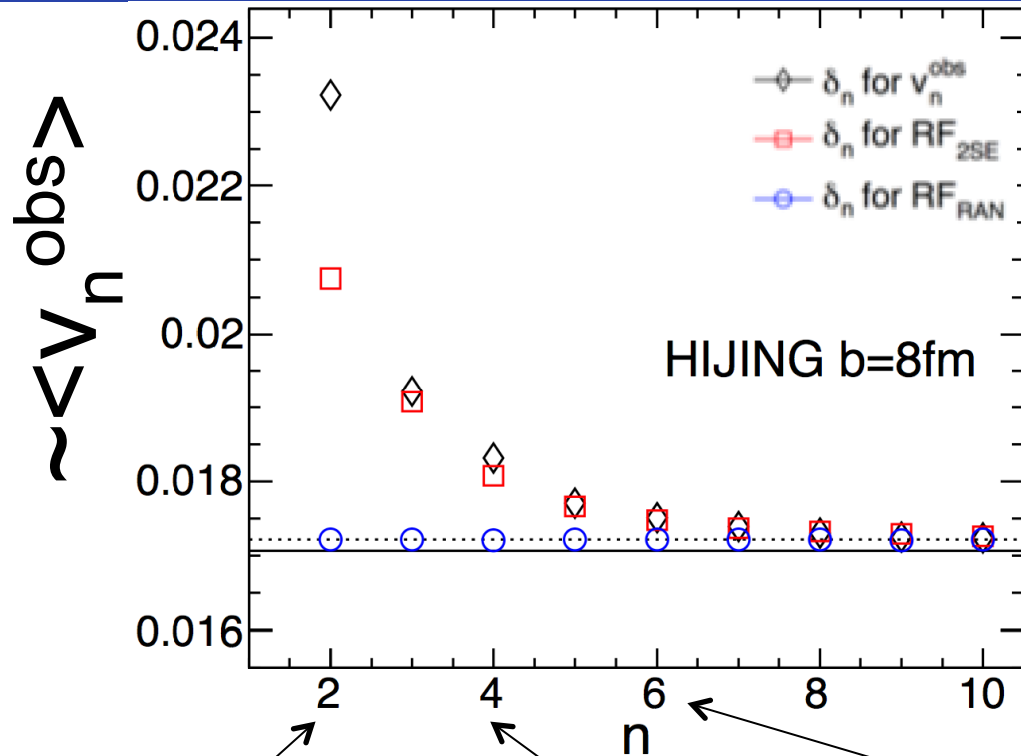


- Unfolding method allow extraction of EbE distribution of short-range and long-range correlations

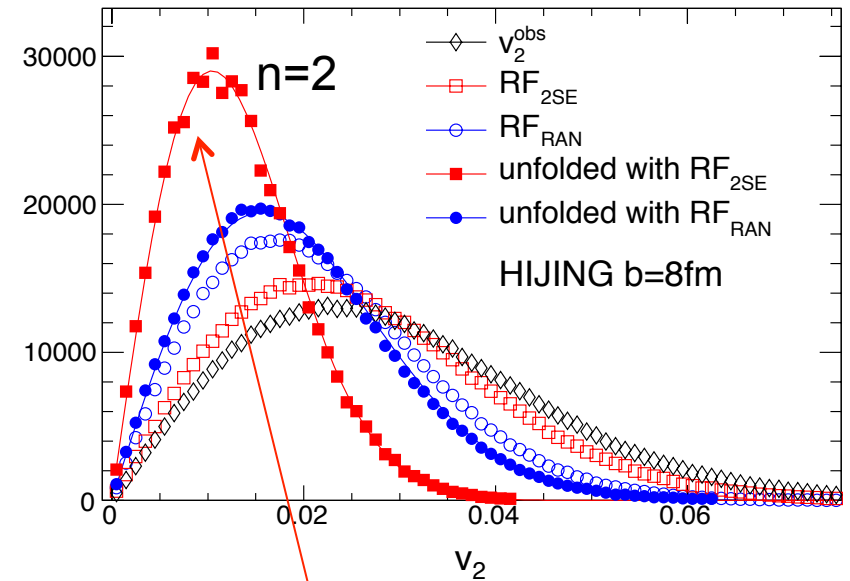
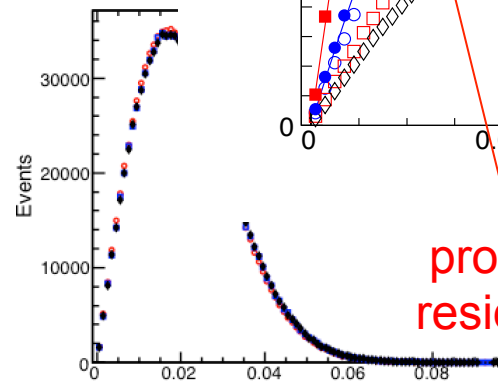
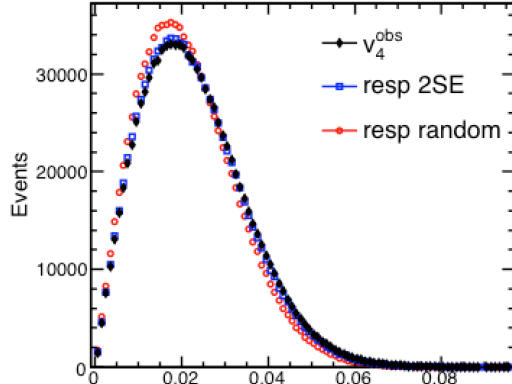
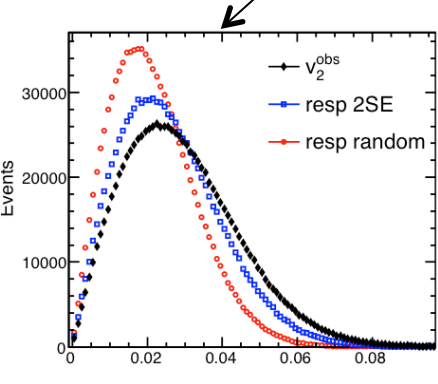
- Well-defined noise limit



Azimuthal power spectrum in hijing: (non-flow)

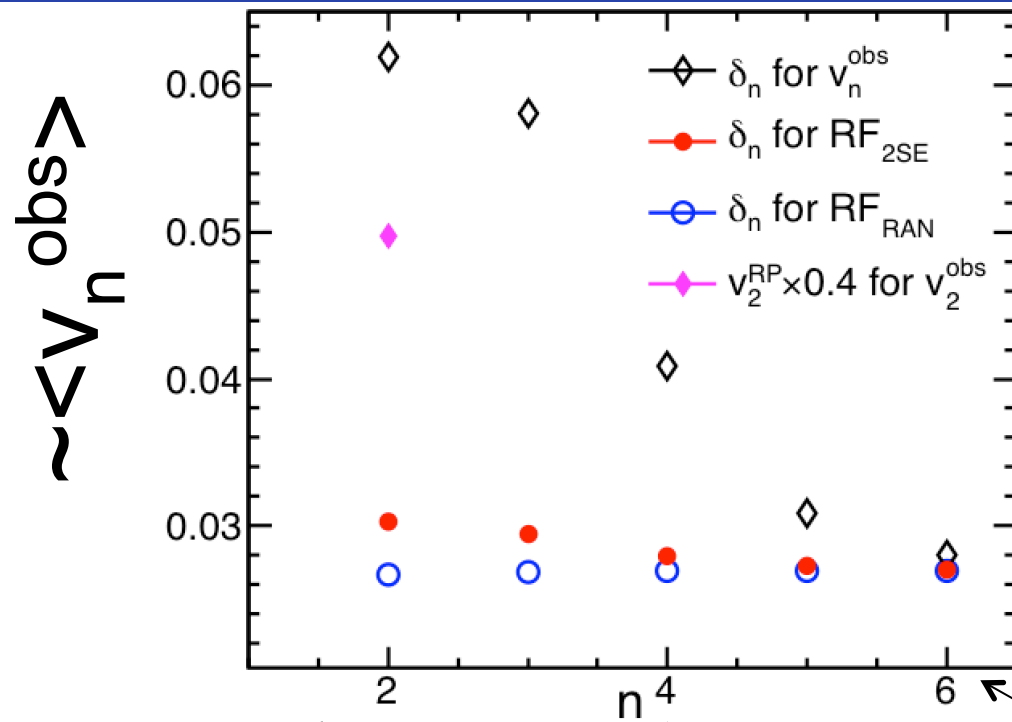


- Unfolding method allow extraction of EbE distribution of short-range and long-range correlations
- Well-defined noise limit



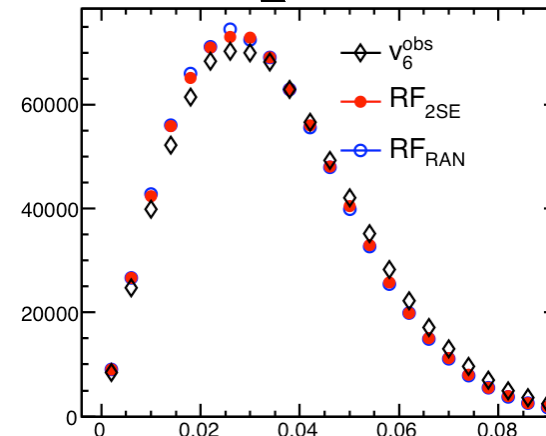
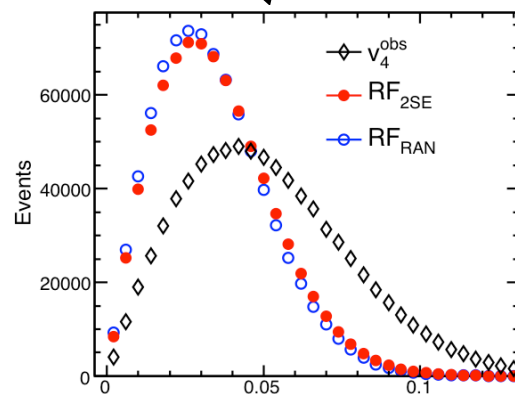
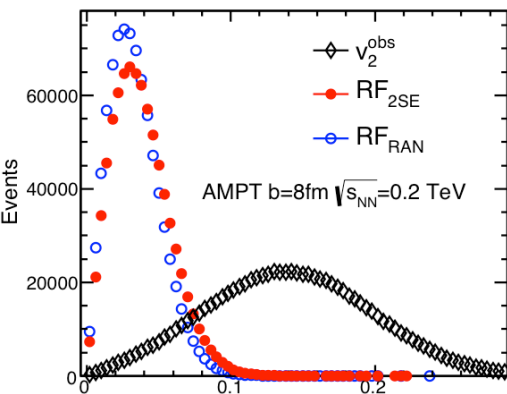
probability distribution of residual non-flow!!!

Azimuthal power spectrum in AMPT: (flow+non-flow) ²¹



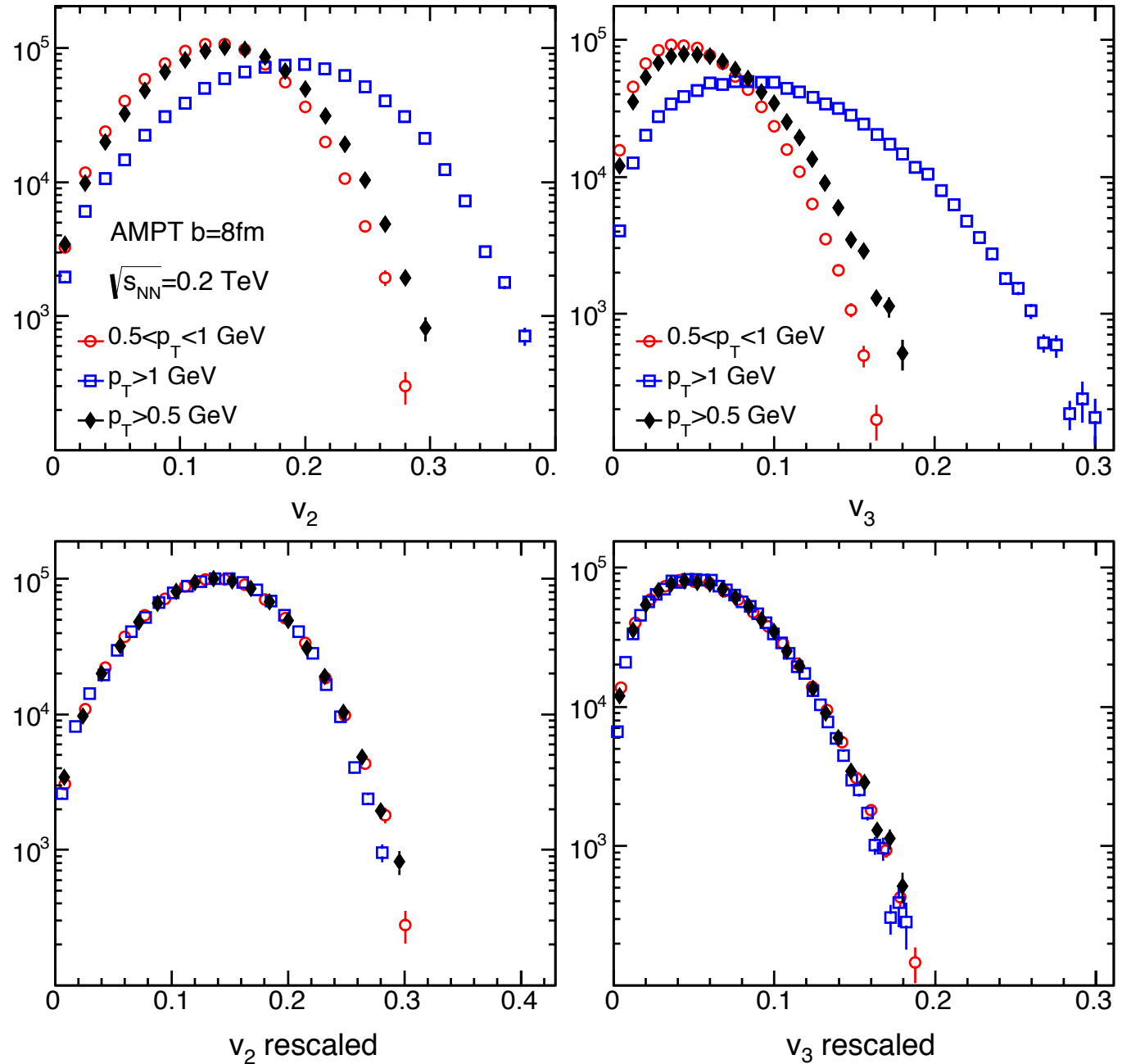
- Unfolding method allow extraction of EbE distribution of short-range and long-range correlations

- Well-defined noise limit



AMPT unfolded distributions

- Unfolded distribution scales well.



It was a memorable workshop

