

SUPPRESSION OF ENERGY LOSS FROM PARTIALLY IONIZED COLOR

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Y. Hidaka, S. Lin, R. Pisarski



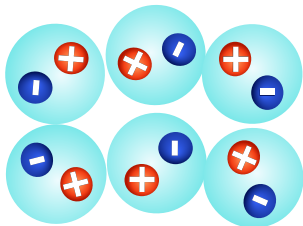
pA workshop BNL 2013

- Introduction: ionization in QED/QCD plasmas

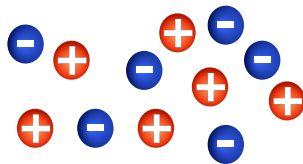
- Introduction: ionization in QED/QCD plasmas
- Collisional energy loss in partially ionized plasma

- Introduction: ionization in QED/QCD plasmas
- Collisional energy loss in partially ionized plasma
- Conclusions

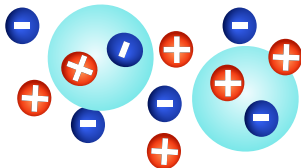
IONIZATION IN QED PLASMA



Neutral state \leadsto atoms,
electric neutrality $>$ atomic scales

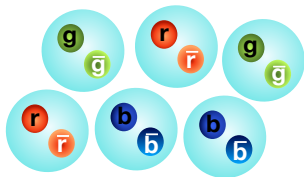


Completely ionized plasma \leadsto plasma
with freely moving electric charges

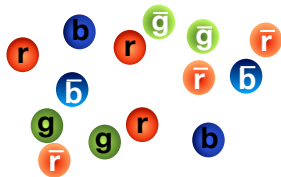


Partially ionized plasma \leadsto *partially* ionized plasma with atoms and electric charges

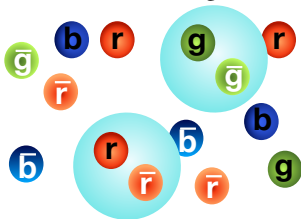
IONIZATION IN QCD PLASMA



Neutral state \leadsto confined phase,
color neutrality $>$ hadronic scale



Completely ionized plasma \leadsto
perturbative QGP with freely moving
charges



Partially ionized plasma \leadsto *partial* ionization of color: hadrons and color charges;
semi-QGP, nontrivial holonomy

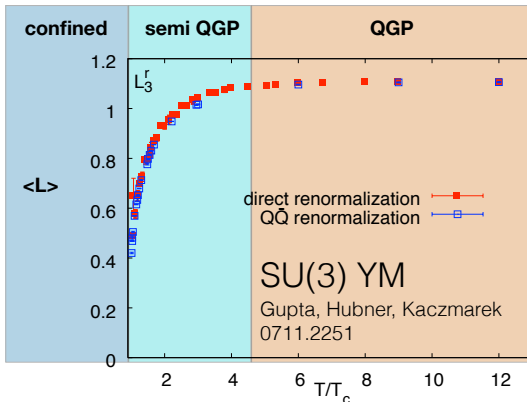
POLYAKOV LOOP AS A MEASURE OF PARTIAL IONIZATION: PURE GLUE

$$\text{Polyakov loop: } \langle L \rangle \sim e^{-F_{\text{test qk}}/T}$$

Confined: $F_{\text{test qk}} \rightarrow \infty$,
 $\langle L \rangle \rightarrow 0$

Semi QGP: $0 < \langle L \rangle < 1$
 $\langle L \rangle$ measures degree of ionization

Perturbative QGP:
 $F_{\text{test qk}}/T \rightarrow 0$, $\langle L \rangle \rightarrow 1$



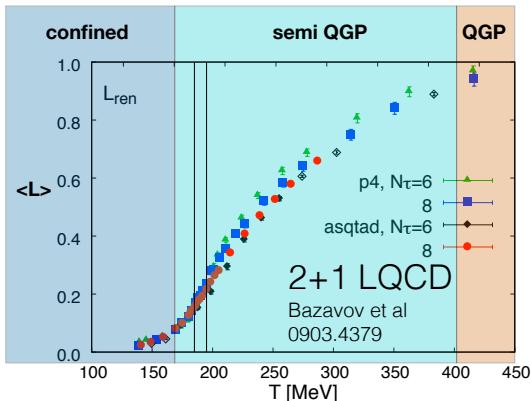
POLYAKOV LOOP AS A MEASURE OF PARTIAL IONIZATION: LQCD

$$\text{Polyakov loop: } \langle L \rangle \sim e^{-F_{\text{test qk}}/T}$$

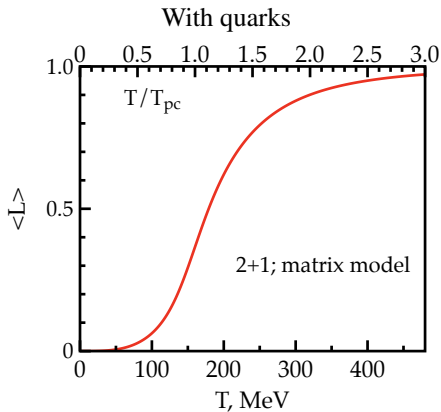
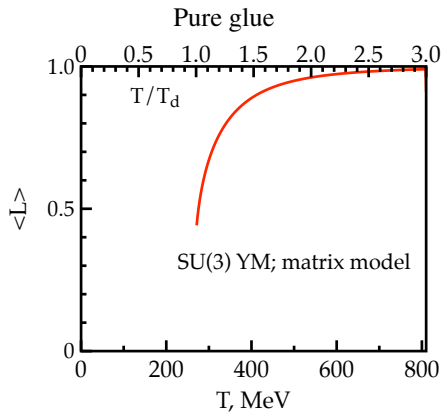
Confined: $F_{\text{test qk}} \rightarrow \infty$,
 $\langle L \rangle \rightarrow 0$

Intermediate regime: $0 < \langle L \rangle < 1$
 $\langle L \rangle$ measures degree of ionization

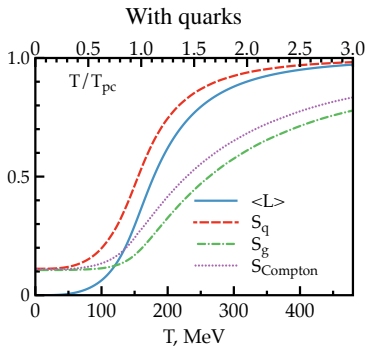
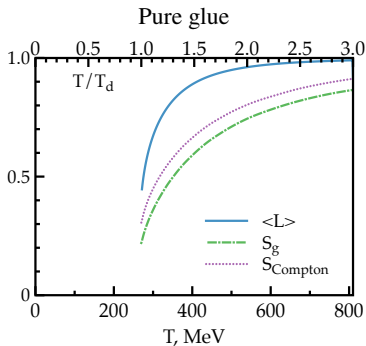
Deconfined:
 $F_{\text{test qk}}/T \rightarrow 0$, $\langle L \rangle \rightarrow 1$



POLYAKOV LOOP: MATRIX MODEL



**Punchline: transition region (“semi”-QGP):
must exhibit partial ionization of color
shear viscosity, energy loss... must depend upon the degree of ionization**



$$S_i = \frac{\text{energy loss in semi-QGP}}{\text{energy loss in perturbative QGP}}$$

S_i increases as color is ionized

- $i = q$ scattering on **light quark** (t channel)
- $i = g$ scattering on **gluons** (t channel)
- $i = \text{Compton}$ scattering on **gluons**, **Compton** scattering (u channel)

Usual argument of kinetic theory

Majumder, Muller and Wang, hep-ph/0703082

Liao and Shuryak, 0810.4116

Asakawa, Bass, and Muller, hep-ph/0603092, 1208.2426

- Viscosity $\eta \sim \rho^2 / \sigma$
 - ρ - density of color charges
 $\rho \sim 1$
 - σ - cross-section: $\sigma \sim g^4$,
 g - coupling
 - large $g \rightsquigarrow$ small η

- Energy loss $\frac{dE}{dx} \sim g^2 \rho^2$
 - large $g \rightsquigarrow$ large $\frac{dE}{dx}$

Semi-QGP

Y. Hidaka, R. Pisarski 0912.0940

R. Pisarski, V. Skokov proceedings of QM2013

- Viscosity $\eta \sim \rho^2 / \sigma$
 - ρ - density of color charges, $\rho \sim \langle L \rangle^2$
 - σ - cross-section: $\sigma \sim \langle L \rangle^2$
 - $\eta \sim \langle L \rangle^2$, small in semi-QGP

- Energy loss (large N_c)
 - $\frac{dE}{dx} \sim \langle L \rangle \cdot \frac{dE}{dx}$ on light quarks
 - $+\langle L \rangle^2 \cdot \frac{dE}{dx}$ on gluons

Details

- Matrix model
- Collisional energy loss in large N_c limit
- Collisional energy loss due to scattering on light quark, $N_c = 3$
- Collisional energy loss due to scattering on gluons, $N_c = 3$
- Outlook: radiative?!

NON-ZERO POLYAKOV LOOP \rightsquigarrow NON-TRIVIAL HOLONOMY

- Polyakov loop $L = \text{Tr } \mathcal{P} \exp \left(ig \int_0^{1/T} \mathbf{A}_0 d\tau \right)$
- Ansatz for $[A_0]_{ab} = \delta_{ab} \frac{Q^a}{g}$, for the sake of simplicity $Q^a = 2\pi T \cdot q^a$
- Tracelessness $\text{tr } \mathbf{A}_0 = 0 \rightsquigarrow \sum_a Q^a = \sum_a q^a = 0$
- Classical approximation: zero action for \mathbf{A}_0
- One loop about \mathbf{A}_0 : Gross, Pisraski, Yaffe '81:

$$U_{\text{pert}} = -2\pi^2 T^4 \left[\frac{N^2 - 1}{45} - \frac{1}{3} \sum_{a,b} (q_a - q_b)^2 (1 - |q_a - q_b|)^2 \right]$$

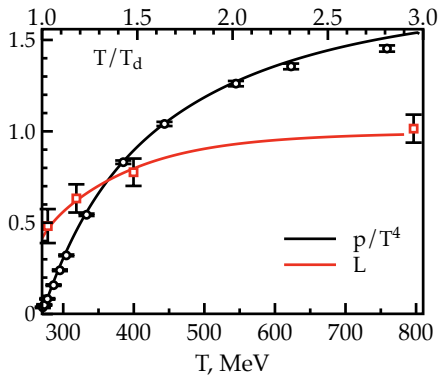
Gives only trivial \mathbf{A}_0

- Non-perturbative contribution are modeled by (R. Pisarski et al)

$$U_{\text{non-pert}} = T^2 T_d^2 \left[c_1 \sum_{a,b} |q_a - q_b| (1 - |q_a - q_b|) + c_2 \sum_{a,b} (q_a - q_b)^2 (1 - |q_a - q_b|)^2 + c_3 \right]$$

- c_i are fixed to get transition at $T = T_d$, and describe lattice data
- three colors: $q_1 = -q_2 = q$, $q_3 = 0$. Confining at $q = 1/3$ and perturbative $q = 0$.

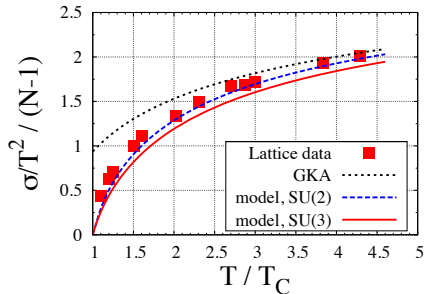
Pressure for pure glue



t'Hooft loop

(interface between different $Z(N)$ sectors)

Dumitru et al, 1011.3820



$$V \rightarrow V + \frac{1}{g^2} \sum_a^N \left(\frac{\partial Q_a}{\partial z} \right)^2$$

Quark and gluon propagator in a background A_0 field: Hidaka, Pisarski 0906.1751

- Distribution function for gluons

$$n_{a,b}^g(p, Q) = \left[\exp\left(\frac{E - i(Q_a - Q_b)}{T}\right) - 1 \right]^{-1}$$

- Distribution function for quarks

$$n_a^q(p, Q) = \left[\exp\left(\frac{E - iQ_a}{T}\right) + 1 \right]^{-1}$$

Limits:

- Trivial holonomy or perturbative QGP, $Q = 0$

$$n^g(p, Q = 0) = \left[\exp\left(\frac{E}{T}\right) - 1 \right]^{-1}$$

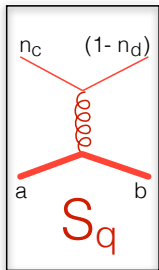
$$n^q(p, Q = 0) = \left[\exp\left(\frac{E}{T}\right) + 1 \right]^{-1}$$

- Confining limit, large N :

$$n^q = 0$$

$$n^g = 0$$

LARGE N LIMIT FOR SCATTERING OFF LIGHT QUARK: BIRDTRACKS



$$\left(\begin{array}{c} \uparrow \downarrow \\ \text{---} \text{---} \\ a \quad b \end{array} - \frac{1}{N} \begin{array}{c} \curvearrowright \\ \text{---} \text{---} \\ a \quad b \end{array} \right) \left(\begin{array}{c} \uparrow \downarrow \\ \text{---} \text{---} \\ c \quad d \end{array} - \frac{1}{N} \begin{array}{c} \curvearrowleft \\ \text{---} \text{---} \\ c \quad d \end{array} \right) =$$

$$\begin{array}{c} \begin{array}{c} c \quad d \\ \text{---} \text{---} \\ a \quad b \end{array} \quad \begin{array}{c} c \quad d \\ \text{---} \text{---} \\ a \quad b \end{array} \quad \begin{array}{c} c \quad d \\ \text{---} \text{---} \\ a \quad b \end{array} \quad \begin{array}{c} c \quad d \\ \text{---} \text{---} \\ a \quad b \end{array} \\ -1/N \quad -1/N \quad + 1/N^2 \quad \bigcirc_N = \end{array}$$

$$\begin{array}{c} \begin{array}{c} c \quad d \\ \text{---} \text{---} \\ a \quad b \end{array} \quad \begin{array}{c} c \quad d \\ \text{---} \text{---} \\ a \quad b \end{array} \quad \begin{array}{c} -a \quad -b \\ \text{---} \text{---} \\ a \quad b \end{array} \\ -1/N \quad \xrightarrow{\text{large } N} \end{array}$$

$$\sim \sum_{ab} n_a (1 - n_b)$$

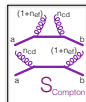
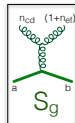
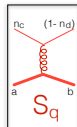
$$\begin{aligned} \frac{dE}{dx} &\propto \sum_{a,b}^N \int [dk][dk'][dp'] f(p, k, k', p') n(E_k + iQ_a) [1 - n(E_{k'} + iQ_b)] \\ &\quad \sum_a n(E_k + iQ_a) = \sum_a [\exp(\beta E_k + i\beta Q_a) + 1]^{-1} \\ &= \sum_{n=1}^{\infty} (-1)^n \exp(-\beta E_k) \sum_a \exp(in\beta Q_a) = \sum_{n=1}^{\infty} (-1)^n \exp(-\beta E_k) \text{tr } L^n \end{aligned}$$

for small $\text{tr } L$ scattering off **light quarks**

$$\frac{dE}{dx} \propto \text{tr } L \cdot \left(\frac{dE}{dx} \right)_{\text{pert.}}$$

Similar argument for scattering off **gluons** gives

$$\frac{dE}{dx} \propto (\text{tr } L)^2 \cdot \left(\frac{dE}{dx} \right)_{\text{pert.}}$$



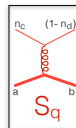
As in pQCD, but taking into account modification of distribution function in final/initial state.

N=3: SCATTERING OFF LIGHT QUARKS

$$S_i = \left(\frac{dE}{dx} \right)_{i|} \bigg/ \left(\frac{dE}{dx} \right)_{i,\text{pert.}}$$

- Scattering off light quark

$$S_q = \frac{12}{\pi^2(N^2 - 1)} \sum_{l=1}^{\infty} \sum_{m=0}^{l-1} (-1)^{l+1} \frac{l-2m}{l^3} \left(\text{tr } L^{l-m} \text{tr } L^m - \frac{1}{N} \text{tr } L^l \right)$$



- Perturbative limit $Q \rightarrow 0$, so $\forall i \text{ tr } L^i \rightarrow 1$:

$$S_q(Q=0) = \frac{12}{\pi^2(N^2 - 1)} \sum_{l=1}^{\infty} \sum_{m=0}^{l-1} (-1)^{l+1} \frac{l-2m}{l^3} (N^2 - 1) = 1$$

- Confining limit $q \rightarrow 1/3$, so $\forall i = kN$, where k is integer, $\text{tr } L^i \rightarrow N$, otherwise $\text{tr } L^{j \neq kN} \rightarrow 0$:

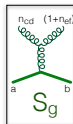
$$\begin{aligned} S_q(q=1/3) &= \frac{12}{\pi^2(N^2 - 1)} \sum_{k=1}^{\infty} \sum_{m=0}^{Nk-1} (-1)^{kN+1} \delta_{mjN} \frac{kN - 2m}{k^3 N^3} (N^2 - 1) \\ &= \frac{1}{N^2} \text{ for odd } N, \quad \frac{2}{N^2} \text{ otherwise} \end{aligned}$$

N=3: SCATTERING OFF GLUONS

$$S_i = \left(\frac{dE}{dx} \right)_{i|} \bigg/ \left(\frac{dE}{dx} \right)_{i,\text{pert.}}$$

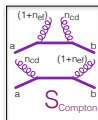
- Scattering off gluons (t channel)

$$S_g = \frac{6}{\pi^2(N^2 - 1)} \sum_{l=1}^{\infty} \sum_{m=0}^{l-1} \frac{l-2m}{l^3} \left(\text{tr } L^{l-m} \cdot \text{tr } L^l \cdot \text{tr } L^m - \text{tr } L^{2l} \right)$$

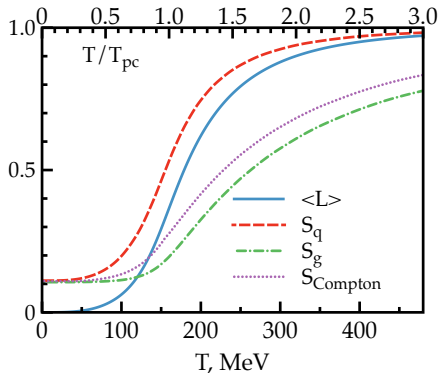


- Compton scattering off gluons (u channel), only Polyakov loop terms

$$S_{\text{Compton}} = \dots \left(\text{tr } L^l \text{tr } L^{l-m} \text{tr } L^m \right. \\ \left. - \frac{2}{N} \text{tr } L^m \text{tr } L^{2l-m} - \frac{2}{N} \text{tr } L^{l-m} \text{tr } L^{l+m} + \frac{4}{N} \text{tr } L^{2l} \right) \\ + \frac{1}{N^2} \left(\text{tr } L^m \right)^2 \text{tr } L^{2(l-m)} + \frac{1}{N^2} \left(\text{tr } L^{l-m} \right)^2 \text{tr } L^{2m} - \frac{4}{N^2} \text{tr } L^{2(l-m)} \text{tr } L^{2m} \\ + \frac{1}{N^3} \left(\text{tr } L^{2m} \right)^2 \text{tr } L^{2(l-m)}$$

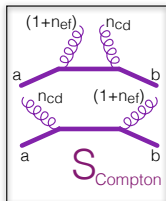
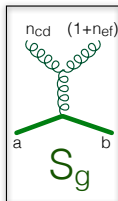
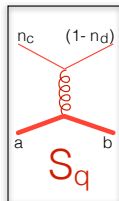


NUMERICAL RESULTS

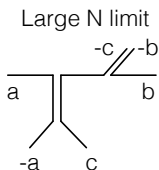
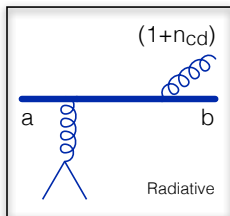


$$S_i = \left(\frac{dE}{dx} \right)_i \bigg/ \left(\frac{dE}{dx} \right)_{i,\text{pert.}}$$

- Different processes are suppressed differently
- Processes with gluons are suppressed stronger than those with quarks
- $\forall i; S_i \rightarrow 1/N^2$ at low temperatures



RADIATIVE ENERGY LOSS: PRELIMINARY LARGE N RESULT



Suppressed by

$$n_{-a}(1 - n_c)(1 + n_{-c,-b}) \sim \text{tr } L$$

- LQCD: shallow dependence of $\langle L \rangle$ on T
- This suggest that **semi-QGP** region (region with partial ionization of color) is broad and has to be taken into account when computing energy loss viscosity and etc
- Collisional energy loss is suppressed in semi-QGP either linearly (for scattering off light quarks) or quadratically (for scattering off gluons) by Polyakov loop
- Radiative energy loss is harder to compute, but, at least, in large N limit it also gets suppressed at least quadratically by Polyakov loop

Thank you!