

The nonperturbative Contribution to TMD Cross sections in SIDIS

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Background and motivation

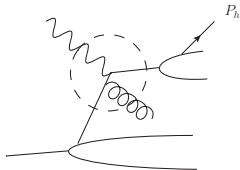
- Polarized and unpolarized cross sections in TMD factorization
- Large and small transverse momentum

Recent progress and next steps

- Phenomenology
- Issues

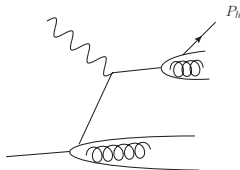
TMD physics at different q_T

$$q_T \gtrsim Q$$



Pert. approx.
Coll. Factorization

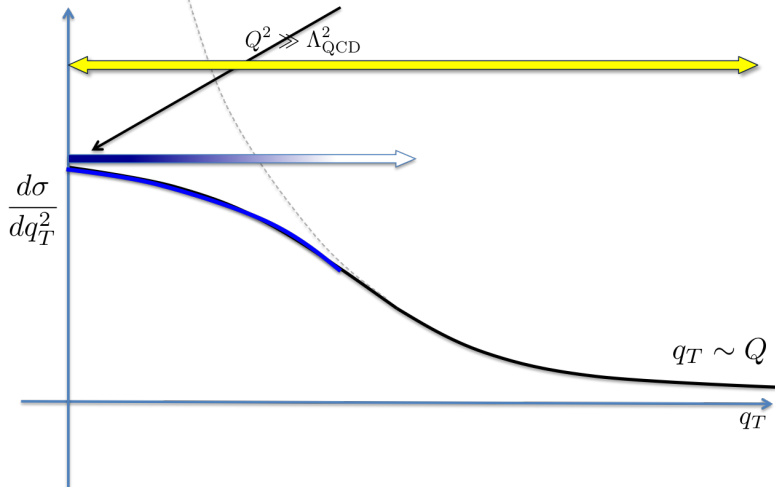
$$q_T \sim \Lambda_{\text{QCD}}$$



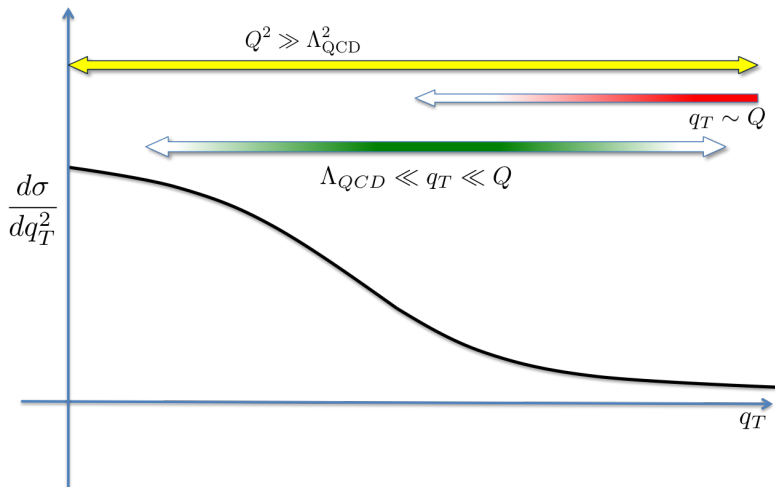
Small q_T approx.
TMD Factorization

(Small) Transverse Momentum:

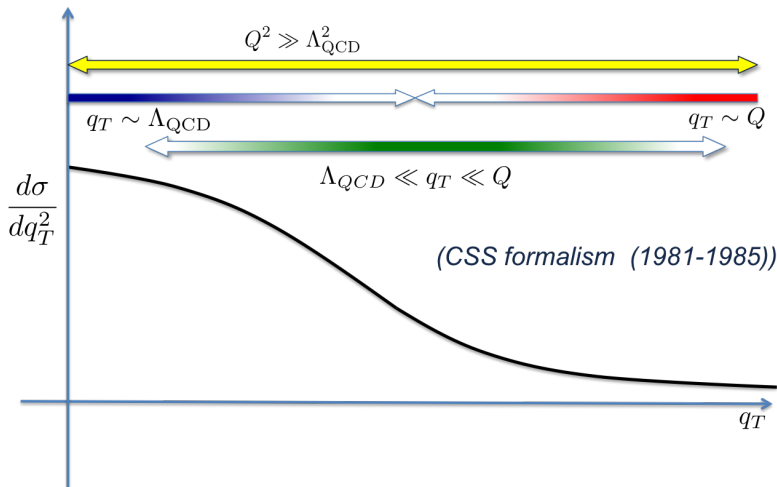
Intrinsic NP Transverse Motion



(Large) Transverse Momentum:



Unified: Transverse Momentum:



Structure of TMD cross sections

$$\begin{aligned}\Gamma &= \mathbf{T}_{\text{TMD}}\Gamma + [\Gamma - \mathbf{T}_{\text{TMD}}\Gamma] \\ &\approx \underbrace{\mathbf{T}_{\text{TMD}}\Gamma}_{\mathbf{W}} + \underbrace{\mathbf{T}_{\text{coll}}[\Gamma - \mathbf{T}_{\text{TMD}}\Gamma]}_{\mathbf{Y}}\end{aligned}$$

Γ = Cross section

$\mathbf{T}_{\text{TMD}}$ = Small q_T approximant

$\mathbf{T}_{\text{coll}}$ = Large q_T approximant corrections

Structure of TMD cross sections

Cross section

$$\begin{aligned}\Gamma &= \mathbf{T}_{\text{TMD}}\Gamma + [\Gamma - \mathbf{T}_{\text{TMD}}\Gamma] \\ &\approx \underbrace{\mathbf{T}_{\text{TMD}}\Gamma}_{\text{W}} + \underbrace{\mathbf{T}_{\text{coll}}[\Gamma - \mathbf{T}_{\text{TMD}}\Gamma]}_{\text{Y}}\end{aligned}$$

$$\text{W: } q_T \ll Q$$

$$\text{Y: } q_T \sim Q$$

$$\text{W+Y:}$$

$$\Lambda_{QCD} < q_T \lesssim Q$$

Why study the $\text{W} \rightarrow$ Nucleon structure

- TMD PDFs (flavor dependence)
- Spin dependent effects
- Non-perturbative evolution
- Contains perturbative contribution

Role of Y term

- Calculable in pQCD
- Needed to identify non-perturbative effects

Interplay between $\mathbf{W}$ and $\mathbf{Y}$

Cross section

$$\begin{aligned}\Gamma &= \mathbf{T}_{\text{TMD}}\Gamma + [\Gamma - \mathbf{T}_{\text{TMD}}\Gamma] \\ &\approx \underbrace{\mathbf{T}_{\text{TMD}}\Gamma}_{\mathbf{W}} + \underbrace{\mathbf{T}_{\text{coll}}[\Gamma - \mathbf{T}_{\text{TMD}}\Gamma]}_{\mathbf{Y}}\end{aligned}$$

Region of $q_T \ll Q$

- TMD approx. dominates $\rightarrow \Gamma \approx \mathbf{T}_{\text{TMD}}\Gamma$
- $\mathbf{Y}$ term small

Region of $q_T \sim Q$

- Collinear approx. dominates $\rightarrow \Gamma \approx \mathbf{T}_{\text{coll}}\Gamma$
- Consistency demands $\rightarrow \mathbf{T}_{\text{TMD}}\Gamma - \mathbf{T}_{\text{coll}}\mathbf{T}_{\text{TMD}}\Gamma \sim \text{Small}$

Complementary

- One has universal properties: hadron structure and fragmentation
- Other is directly computable, can give high precision

Pert. calculations need non-perturbative input (e.g., W boson mass extraction)

Non-perturbative extractions need isolation of pert./non-pert parts.

TMD evolution

- Nonperturbative component
- Strongly universal, same for unpolarized and polarized TMDs

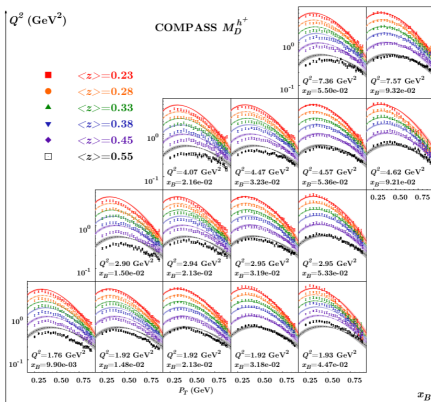
Phenomenology in SIDIS

Qualitative success with Gaussians: $\rightarrow$ Anselmino *et al.*

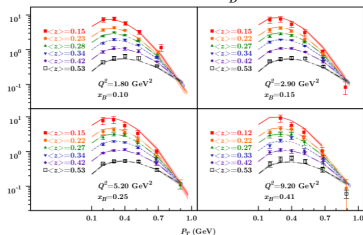
HERMES $\rightarrow$

Points: ~ 497

$$\chi^2_{\text{dof}} = 1.69$$



HERMES $M_D^{\pi^+}$



$\leftarrow$ **COMPASS**

Points: ~ 5385

$$\chi^2_{\text{dof}} = 8.54$$

$$M \propto \sum_q f_{q/p}(x_B) D_{h/q}(z_h) \frac{e^{-P_T^2/\langle P_T^2 \rangle}}{\pi \langle P_T^2 \rangle}$$

How important is TMD evolution at low Q ?

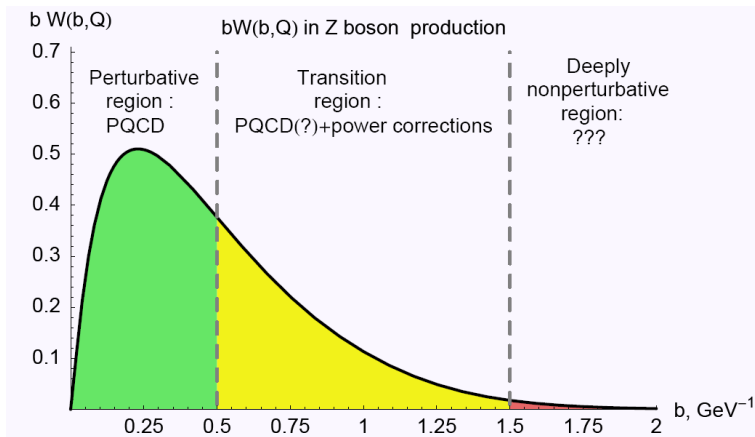
Can we consistently use a Y term in fits that include low Q ?

- Nadolsky et al, 1999. Energy flow/HERA

Do nonperturbative parts prefer Gaussian or exponential large b_T dependence? Schweitzer et al. 2012 $\rightarrow \sim e^{-mb_T}$

Treatment of W

$$W(q_T, Q) = \int \frac{d^2 \mathbf{b}_T}{(2\pi)^2} e^{i \mathbf{q}_T \cdot \mathbf{b}_T} \tilde{W}(\mathbf{b}_T, Q)$$



Parameterization of $\mathbf{W}$

In TMD factorization $\tilde{W}$ takes the form

$$\begin{aligned}\tilde{W}(b_T, Q) &= \sum_j H_{jj}(\mu_Q, Q) \tilde{F}_j(x, b_T, Q_0^2, \mu_{Q_0}) \tilde{D}_j(z, b_T, Q_0^2, \mu_{Q_0} l) \\ &\times E^P(b_*(b_T), Q) E^{NP}(b_T, Q)\end{aligned}$$

At some input scale Q_0 , the nonperturbative part of TMD PDF and FF are parameterized with a power law function in q_T space

$$F^{NP}(q_T, x, Q_0^2, \mu_{Q_0}) \rightarrow \mathcal{K}(q_T) = \frac{C}{(q_T^2 + m^2)^\nu}$$

The nonperturbative evolution factor is parameterized as

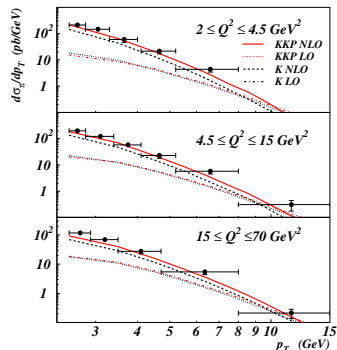
$$\begin{aligned}E^{NP}(b_T, Q) &= e^{-2g_K(b_T, b_{max}) \ln(Q/Q_0)} \\ g_K(b_T; b_{max}) &= g_0(b_{max}) \left(1 - \exp \left[-\frac{C_F \alpha_s(\mu_{b_*}) b_*^2(b_T)}{\pi g_0(b_{max}) b_{max}^2} \right] \right)\end{aligned}$$

Region of $q_T \ll Q$

- not important, the region is dominated by $\mathbf{W}$

Region of $q_T \gtrsim Q$

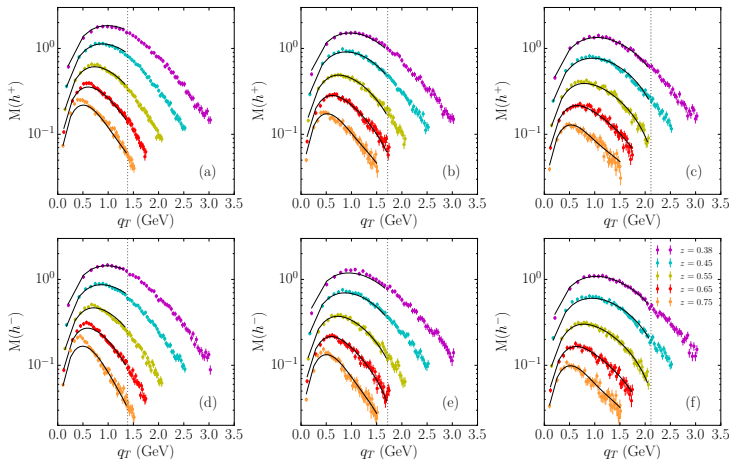
- important high order corrections needed to describe data. Due to lack of NLO perturbative terms we cut large q_T region in our study.



Perturbative cross section in SIDIS.
A. Daleo et al., *etal* (2004)

Baseline fit of COMPASS with power law (Preliminary)

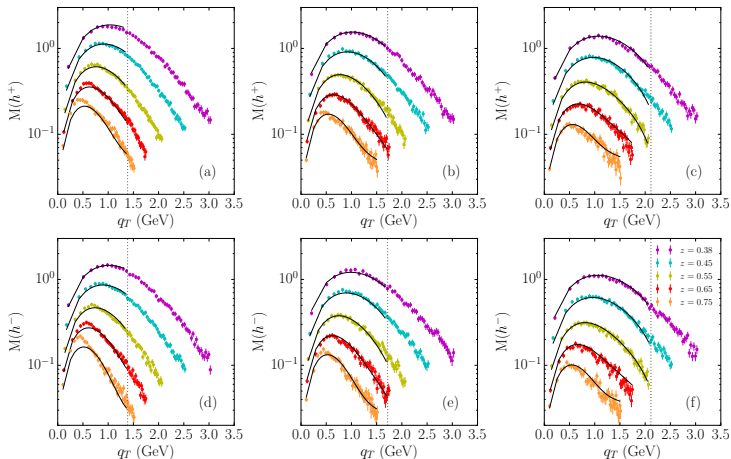
$$M(x, Q^2, z, P_T) \equiv \frac{1}{\frac{d^2\sigma^{DIS}(x, Q^2)}{dx dQ^2}} \frac{d^4\sigma(x, Q^2, z, P_T)}{dx dQ^2 dz dP_T}, P_T = zq_T$$



$$x = 0.03, Q^2 = 1.92, 2.95, 4.47 \text{ GeV}^2$$

Baseline fit of COMPASS with Gaussian (Preliminary)

$$M(x, Q^2, z, P_T) \equiv \frac{1}{\frac{d^2\sigma^{DIS}(x, Q^2)}{dx dQ^2}} \frac{d^4\sigma(x, Q^2, z, P_T)}{dx dQ^2 dz dP_T}, P_T = zq_T$$



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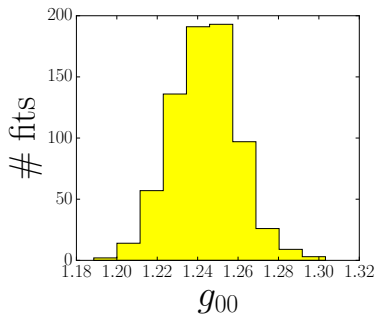
Baseline fit of COMPASS (Preliminary)

Power law fit

g_0	χ^2_{dof}	# pts
1.24	0.995	1042

Gaussian fit

g_0	χ^2_{dof}	# pts
1.19	1.364	1042



- g_0 parameter for NP evolution
- Stability is good evidence for strong universality

Matching at large q_T

$$\begin{aligned}\Gamma &= \mathbf{T}_{\text{TMD}}\Gamma + [\Gamma - \mathbf{T}_{\text{TMD}}\Gamma] \\ &\approx \underbrace{\mathbf{T}_{\text{TMD}}\Gamma}_W + \underbrace{\mathbf{T}_{\text{coll}}[\Gamma - \mathbf{T}_{\text{TMD}}\Gamma]}_Y\end{aligned}$$

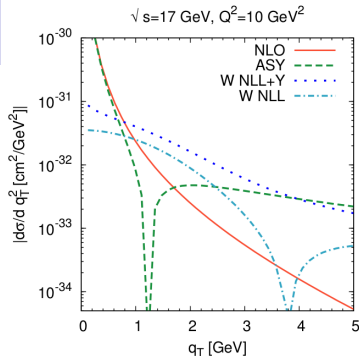
At large Q

- $W = \mathbf{T}_{\text{TMD}}\Gamma$ is mostly perturbative
- broader region where W overlaps with its perturbative approximation
- matching is almost automatic

The difficulty at small Q

- W dominated by NP contributions
- Smooth transition occurs between the NP, and a perturbative part.
- Parameterize W itself : difficult, under study,

$$\text{e.g. } \int dq_T \frac{d\sigma}{dQ^2 dq_T dx dz} = \frac{d\sigma}{dQ^2 dx dz}$$



M. Boglione,

J. Gonzalez. H. *et al* (2014)

Summary

- ✓ Can we do fits including Y term?
- ✓ Strong universal NP evolution
- ✓ Large b_T behavior $\sim e^{-mb_T}$

Next

- $q_T > Q$?
- $O(\alpha_S^2)$ Y term

Backup slides

Parameterize the nonperturbative contribution

Use variable b_* to freeze perturbative contribution at large b_T

$$b_*(b_T) = \begin{cases} b_T & b_T \ll b_{max} \\ b_{max} & b_* \gg b_{max} \end{cases}$$

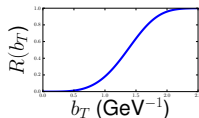
Normally, $\tilde{W}$ is parameterized as

$$\tilde{W}(b_T, Q) = \tilde{W}(b_*(b_T), Q) \tilde{W}_{NP}(b_T, Q)$$

Our parameterization is

$$\tilde{G}(b_T, Q) = \tilde{G}^{NP}(b_T, Q) R(b_T) + \tilde{G}(b_*(b_T), Q) (1 - R(b_T))$$

where G stands for TMD PDF or FF
and R is a switching function $\rightarrow$



Baseline fit of COMPASS (Preliminary)

$$\Gamma \approx \underbrace{\mathbf{T}_{\text{TMD}}\Gamma}_{\mathbf{W}} + \underbrace{\mathbf{T}_{\text{coll}}[\Gamma - \mathbf{T}_{\text{TMD}}\Gamma]}_{\mathbf{Y}}$$

