

# **Elliptic flow at high $p_T$ from parton coalescence**

Dénes Molnár

Ohio State University

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# Outline

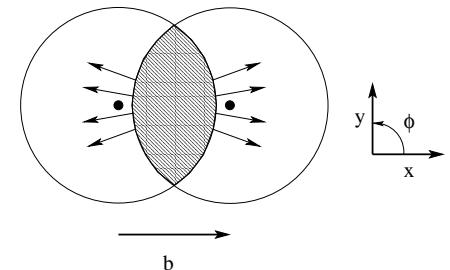
- **Elliptic flow puzzle** - data vs. theory, large parton opacities?
- **Parton coalescence** - why/how it helps resolve opacity problem
- **Implications** - elliptic flow ordering at high  $p_\perp$ , baryon/meson ratios
- **Conclusions, next steps**

**References:** - [nucl-th/0302014](#)  
- NPA 697, 495 ('02) [[nucl-th/0104073](#)]

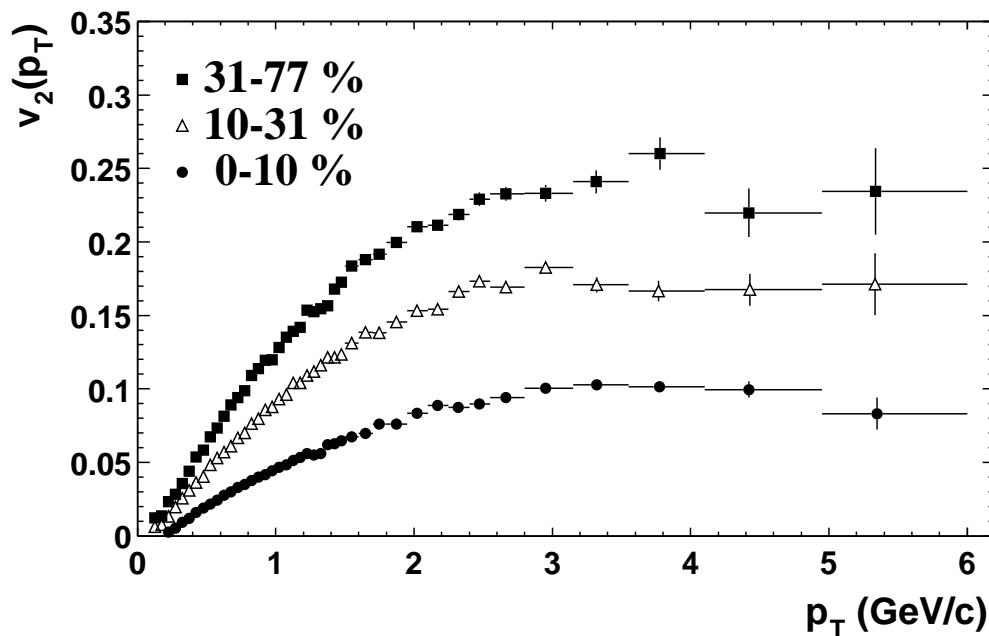
# Saturation of elliptic flow at RHIC

- coordinate-space  $\rightarrow$  momentum-space anisotropy

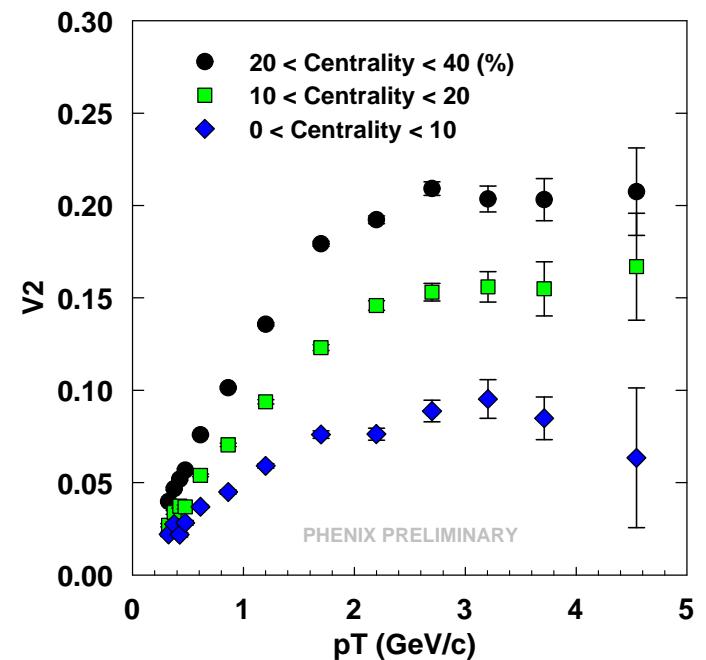
$$\frac{dN}{d\phi dX} \equiv \frac{1}{2\pi} \frac{dN}{dX} [1 + 2 \sum_{n=1} v_n(X) \cos(n\phi)]$$



STAR, PRL 90, 032301 ('03):



PHENIX, nucl-ex/0210007:

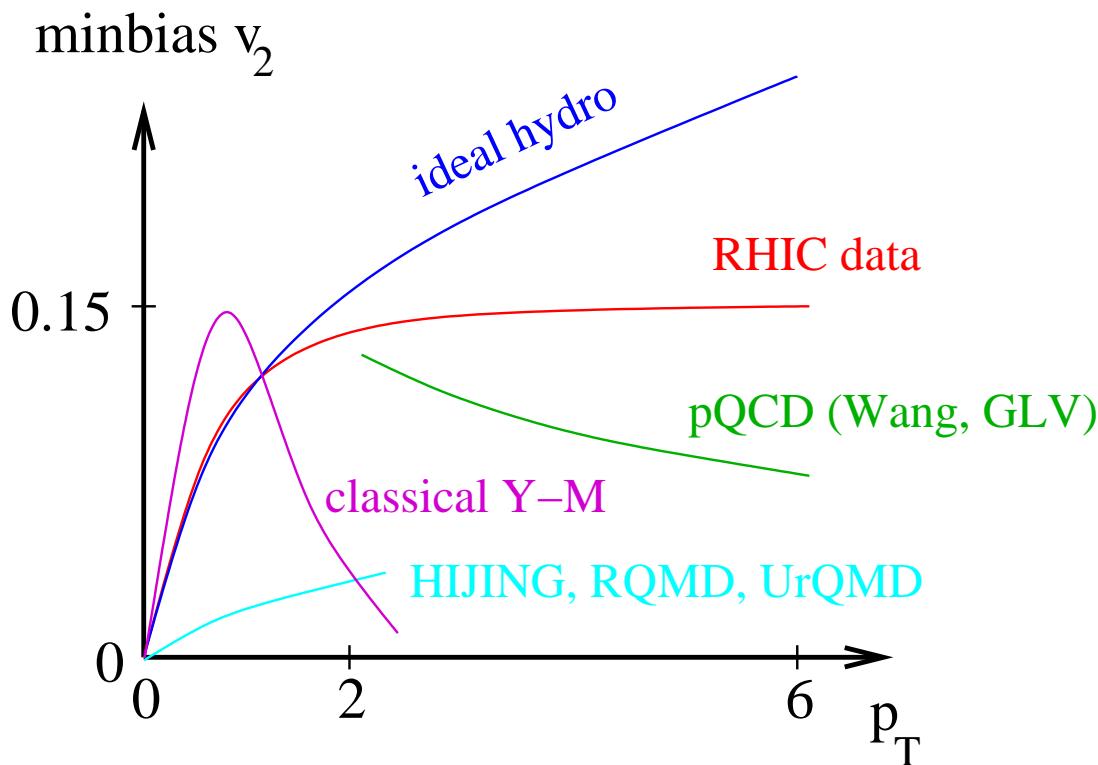


- $v_2 \approx 0.15 \Rightarrow$  large **2 : 1 asymmetry**, which **saturates** for  $p_\perp > 2$  GeV
- same pattern for **all centralities, all particle species**

# Puzzle for theory

## Various theoretical expectations:

[Heinz, Kolb, Huovinen et al; Gyulassy, Vitev, Wang et al; Sorge et al; Bleicher, Stöcker et al; Krashnitz, Venugopalan et al]



- cannot make  $v_2(p_\perp)$  flat



explore what it takes to  
make it flat

# Try covariant parton transport theory

Pang, Zhang, Gyulassy, D.M., Vance, Csizmadia, Pratt, Cheng , ...

## Simplest Lorentz-cov. nonequil. theory (next step beyond hydrodynamics)

- dynamics governed by the mean free path:  $\lambda(s, x) = 1/\sigma(s)n(x)$ 
  - interpolates between ideal hydro  $\lambda = 0$  and free streaming  $\lambda = \infty$
- natural decoupling,  $\lambda(t \rightarrow \infty) \rightarrow \infty \leftrightarrow$  unlike Cooper-Frye in hydro

### Nonlinear transport equation, in classical limit:

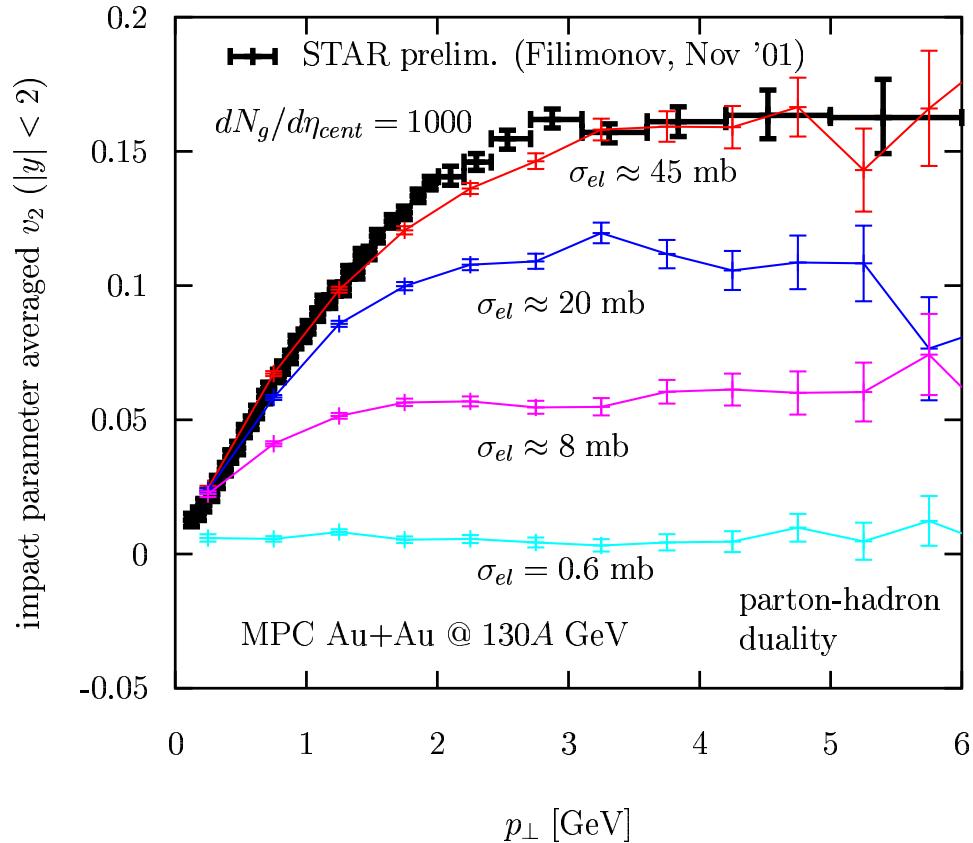
$$p^\mu \partial_\mu f_i(x, \vec{p}) = \overbrace{S_i(x, \vec{p})}^{\text{source}} + \overbrace{C_i^{\text{el.}}[f](x, \vec{p})}^{2 \rightarrow 2 (\text{ZPC, GCP, ...})} + \overbrace{C_i^{\text{inel.}}[f](x, \vec{p})}^{2 \leftrightarrow 3 (\text{MPC})} + \dots$$

solvable numerically → only a handful of covariant algorithms: ZPC, MPC, ...

### Real dynamical parameter: transport opacity [see NPA 697, 495 ('02)]

$$\chi \equiv \langle n_{\text{coll}} \rangle \sigma_{\text{tr}} / \sigma_{\text{el}} \propto \sigma_{\text{tr}} \times dN/d\eta$$

# $v_2(p_T)$ at RHIC from parton transport



$$v_2 \equiv \langle \cos 2(\phi - \phi_0) \rangle$$

minijet initial conditions  
 $1g \rightarrow 1\pi$  hadronization

- **saturation pattern can be reproduced with elastic  $2 \rightarrow 2$  interactions, requires large transport opacities**  $\chi_0 \approx 45 \Leftrightarrow \sigma_{el} \times dN_g/d\eta \approx 45000 \text{ mb}$ 
  - pion HBT data ( $R_O, R_L$ ) also suggest large opacities [nucl-th/0211017]

# Off by factor 15 - checkmate?

Need  $\sigma_{el} \times dN_g/d\eta \approx 45000 \text{ mb} \gg$  optimistic pQCD estimates  $3 \text{ mb} \times 1000$   
(EKRT)

- can cross sections be larger? - only few times
  - large  $Q^2$ : no room, pQCD works (verified against  $pp, p\bar{p}$ )
  - small  $Q^2$ : some uncertainties - e.g., in Debye screening mass  $\mu$   
but soft scatterings do little for transport (though  $\sigma_{tot} \propto 1/\mu^2$ )
  - multiple scatterings: only incoherent  $2 \rightarrow 2$  implemented
    - overestimate: missing interference effects (LPM)
    - underestimate: missing inelastic channels, e.g.,  $2 \leftrightarrow 3$   
likely to give a factor two only [NPA 661 ('99) 236]
- what about the parton density?
  - large  $p_T$ : initial jet production is fixed by pQCD
  - low  $p_T$ : large uncertainties - could assume  $dN/d\eta \sim 15000$   
but  $dN_{had}/d\eta \approx 1000$  only  $\Rightarrow$  novel “many  $\rightarrow 1$ ” hadronization?

# Solution: parton coalescence

(Voloshin, D.M., nucl-th/0302014)

- **Coalescence:**  $q\bar{q} \rightarrow \text{meson}$ ,  $qqq \rightarrow \text{baryon}$

$$\frac{dN_h}{p_\perp dp_\perp d\Phi}(p_\perp) = C_h \left[ \frac{dN_p}{p_\perp dp_\perp d\Phi}(p_\perp/n) \right]^n, \quad (n = 2, 3)$$

- valid if coalescence is rare, i.e., phase space densities are not large
- otherwise linear relation

- Coalescence helps because

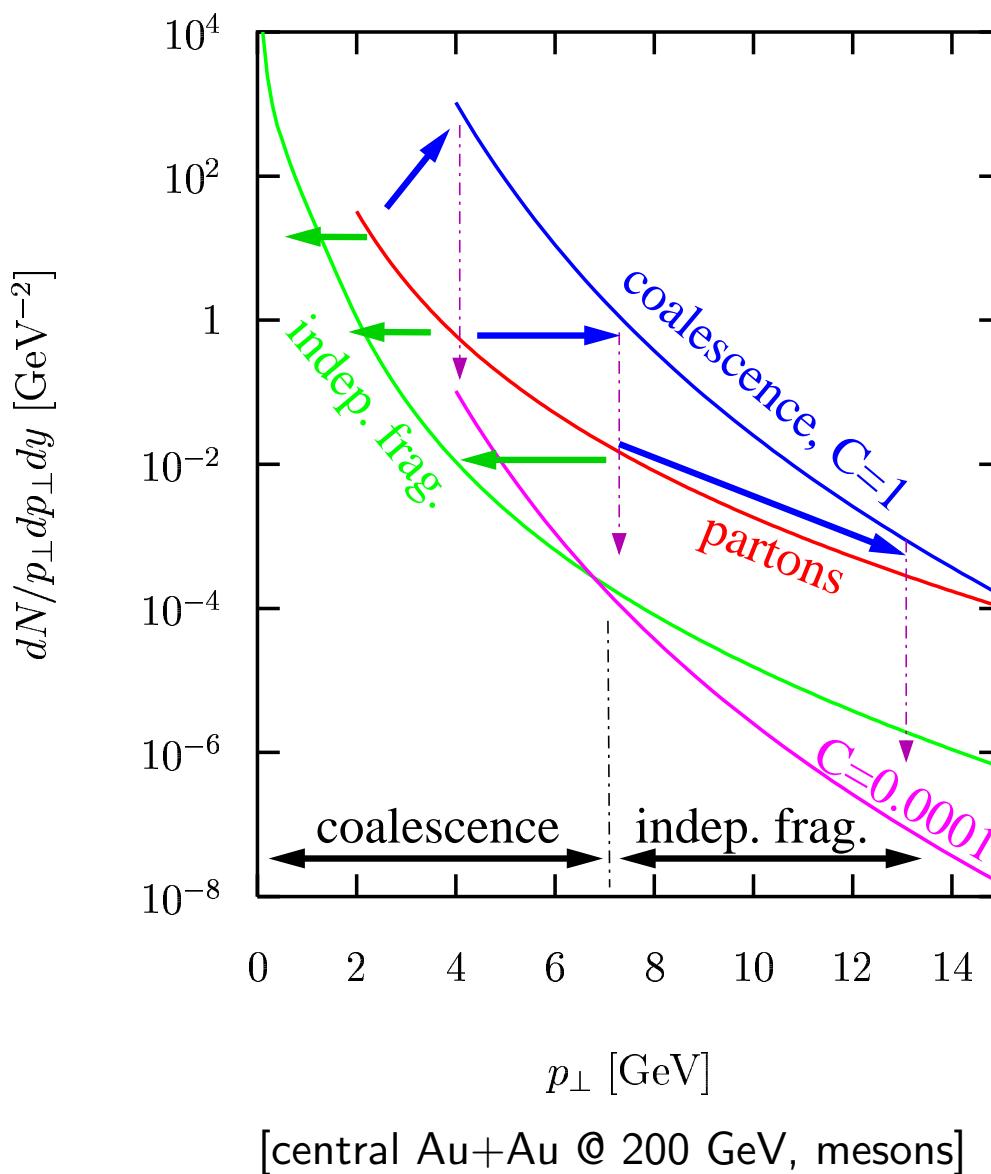
- requires larger parton densities

$$\frac{dN_p}{d\eta} = n \times \frac{dN_{had}}{d\eta} \sim 2000 - 3000$$

- enhances hadron elliptic flow  $\rightarrow$  much smaller opacities are enough

$$v_{2,had}^{max} \approx n \times v_{2,p}^{max}$$

# Coalescence vs. fragmentation



- **momenta:**

**frag:**  $p_\perp \rightarrow z p_\perp$  ( $z < 1$ )

**coal:**  $p_\perp \rightarrow n p_\perp$  ( $n = 2, 3$ )

- **parton spectrum dependence:**

**frag:** **linear**  $dN_{had} \propto dN_{part}$

**coal:** **nonlinear**  $dN_{had} \propto [dN_{part}]^n$



$p_\perp > p_\perp^{crit}$ : **fragmentation region**

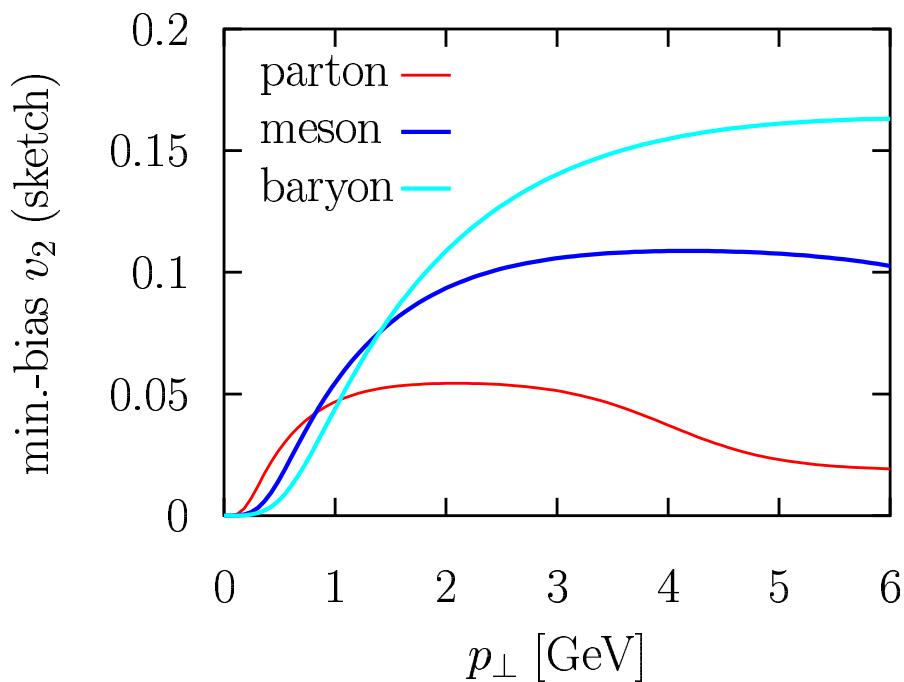
$p_\perp < p_\perp^{crit}$ : **coalescence dominates**

$p_\perp^{crit}$ : decreases with incr. centrality  
depends on  $C_h$   
**may be large**  $> 5$  GeV

# Amplification of elliptic flow

Easy to work out that  $dN_{had} = C_h [dN_{part}]^n$  implies [nucl-th/0302014]

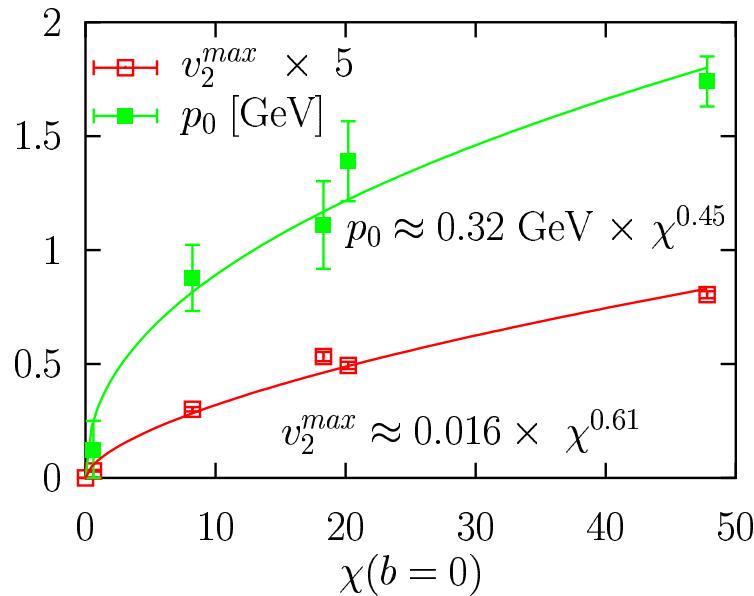
$$\begin{aligned} v_{k,M}(p_\perp) &\approx v_{k,a}(p_\perp/2) + v_{k,\bar{a}}(p_\perp/2) \\ v_{k,B}(p_\perp) &\approx v_{k,a}(p_\perp/3) + v_{k,b}(p_\perp/3) + v_{k,c}(p_\perp/3), \quad (k = 1, 2, \dots) \end{aligned}$$



- behavior depends on  $v_{k,p}(p_\perp)$ :
  - faster than linear:  $v_{k,p} > v_{k,M} > v_{k,B}$
  - weaker than linear:  $v_{k,p} < v_{k,M} < v_{k,B}$
  - ENHANCEMENT
  - flat:  $v_{k,B} \approx 3v_{k,p}$ ;  $v_{k,M} \approx 2v_{k,B}$
- baryons saturate at higher value and at higher  $p_\perp$  than mesons
- any drop in parton  $v_2$  is pushed out to higher  $p_\perp$  for hadrons

# Putting the pieces together

- larger parton density → **factor 2 – 3 in opacity**  $[\chi \propto \sigma_{el} \times dN/d\eta]$
- amplification of elliptic flow →  $2 - 3 \times$  in  $v_2$  → **3 – 6× in opacity**



**WHY?** - parton transport solutions show  
 $v_2$  depends nonlinearly on opacity

$$v_2^{parton}(p_\perp, \chi) \approx v_2^{max}(\chi) \tanh(p_\perp/p_0(\chi))$$

where  $\frac{v_2^{max}(\chi) \propto \chi^{0.61}}{[NPA 697, 495 ('02)]}$

- nonflow correlations in first  $v_2$  data → extra 25% opacity reduction
- ⇒ **total 7.5 – 23× reduction in opacity** → back to reality (needed 15)

note: lower value assumes purely mesons, upper one purely baryons

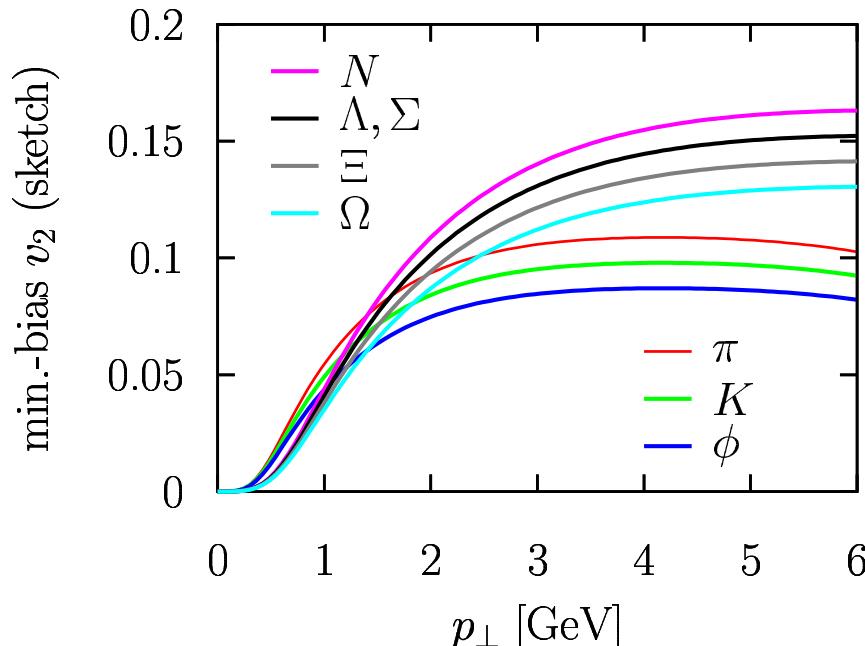
# Elliptic flow ordering at high $p_\perp$

In the saturation region:  $v_{2,B} \approx v_{2,a} + v_{2,b} + v_{2,c}$ ;  $v_{2,M} \approx v_{2,a} + v_{2,\bar{a}}$

$\Rightarrow$  if all  $v_{2,p}$  are same: baryons have  $\approx 50\%$  larger flow than mesons

however: - high  $p_\perp$ : quark energy loss depends on quark mass  
 - low  $p_\perp$ : hydrodynamic flow depends on mass

$\Rightarrow$   $v_{2,s} < v_{2,light}$ : leads to richer  $v_2$  ordering at high  $p_\perp$



- $p > \Lambda \approx \Sigma > \pi > K > \phi$
- $\Lambda, \Sigma > \Xi > K$
- $\Xi > \Omega > \phi$

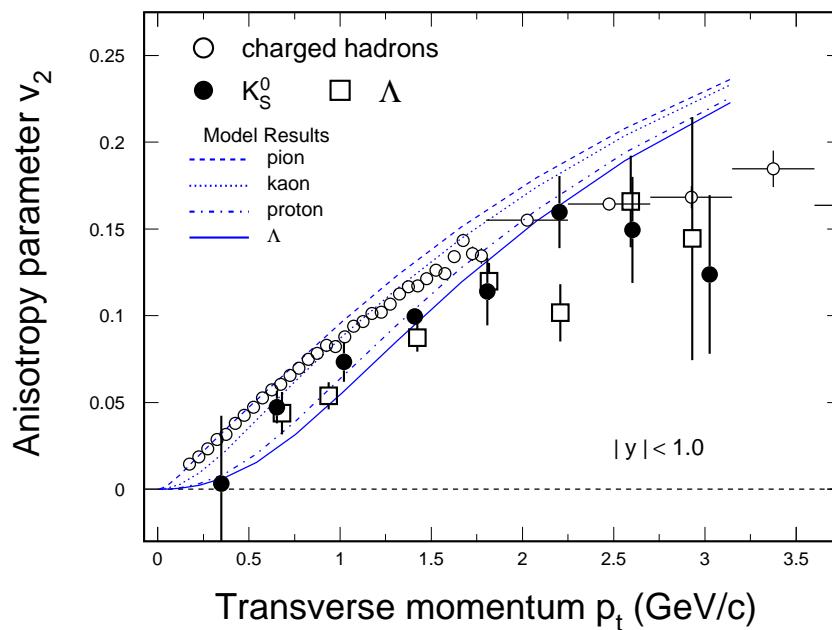
very different from that of Lin & Ko  
 $p = \pi > \Lambda, \Sigma > K > \Xi > \Omega = \phi$

reason: they assume coalescence of a high- $p_\perp$  quark and low- $p_\perp$  quark(s) - for the latter  $v_2 \approx 0$  [PRL 89, 202302 ('02)]

# Experimental evidence

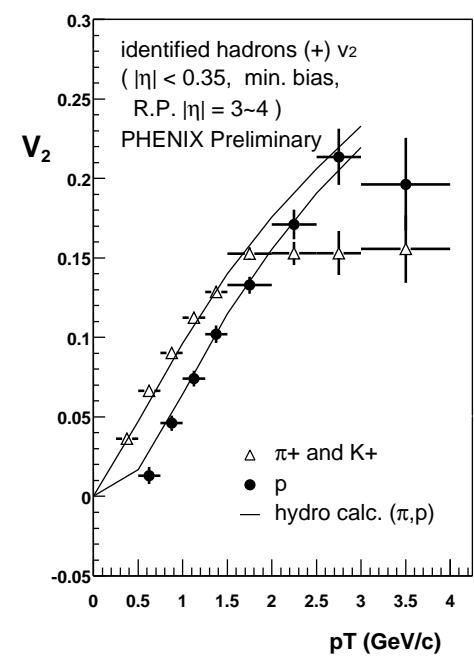
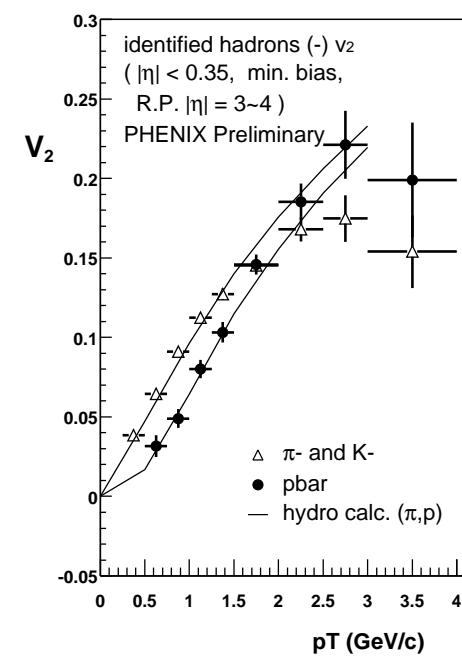
Sorensen [STAR], JPG 28 ('02) 2089:

$$\Lambda > K_{0,S}$$



Esumi [PHENIX], nucl-ex/0210012:

$$p > \pi + K$$



by now better statistics (INT WS., Dec '02)  
showing clearly  $\Lambda > K_{0,S}$

also, indication of  $p > \pi, K$  (not shown)

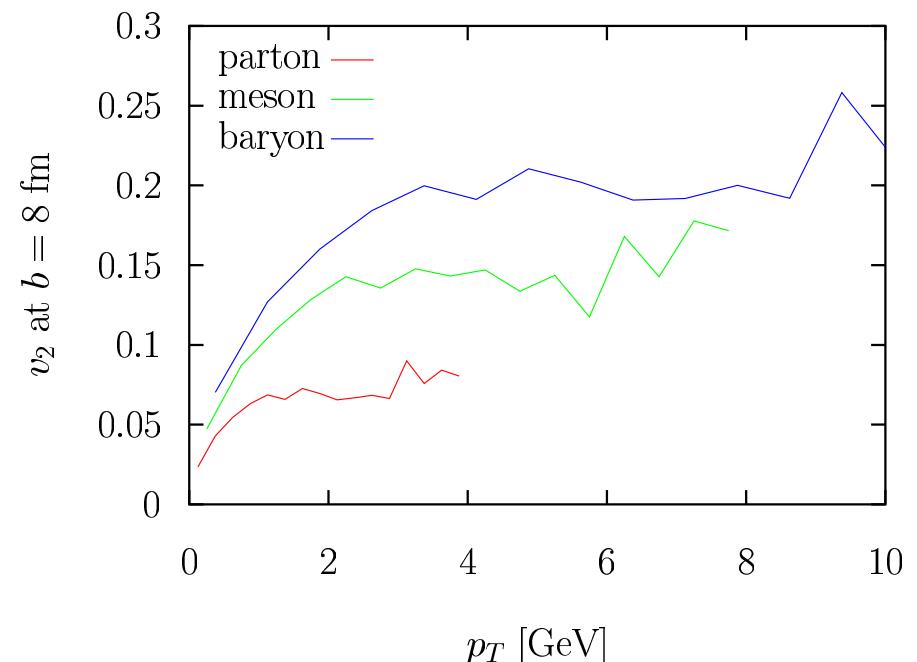
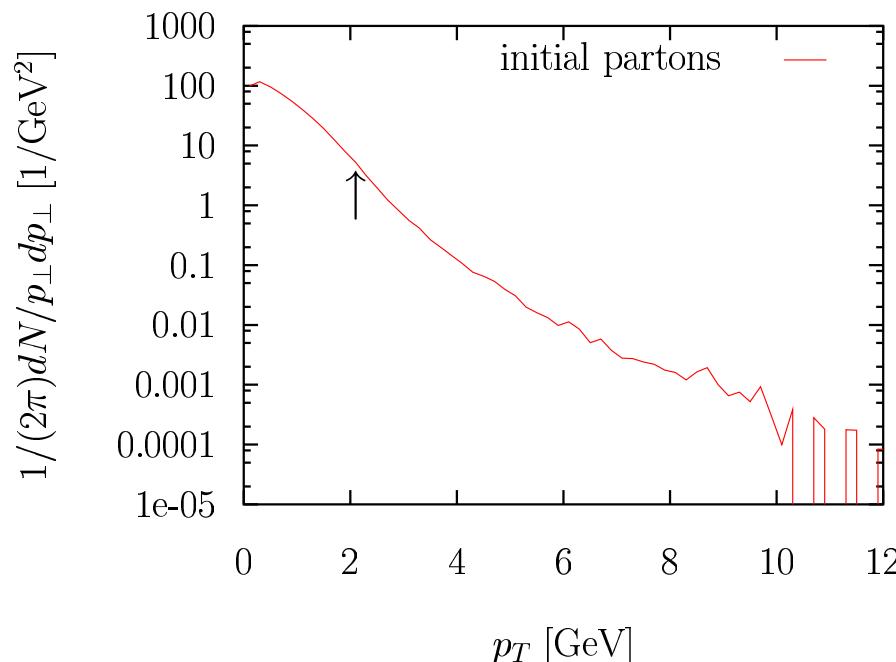
- confirms expectations qualitatively - quant. comparison soon possible

# Flow ordering from parton transport

PRELIMINARY

goal: quantitative results for Au+Au @ 200 GeV, at first only  $b = 8$  fm

- cross sections: 3mb for  $gg \rightarrow gg$ ;  $qg \rightarrow qg$ ,  $qq \rightarrow qq$  reduced by  $4/9$ ,  $(4/9)^2$
- parton spectra:
  - $p_\perp > 2$  GeV: use LO pQCD (GRV98LO, BKK95, K=2,  $Q^2 = p_\perp^2$ )
  - $p_\perp < 2$  GeV: continue spectra smoothly s.t.  $dN/d\eta(b=0) = 2000$



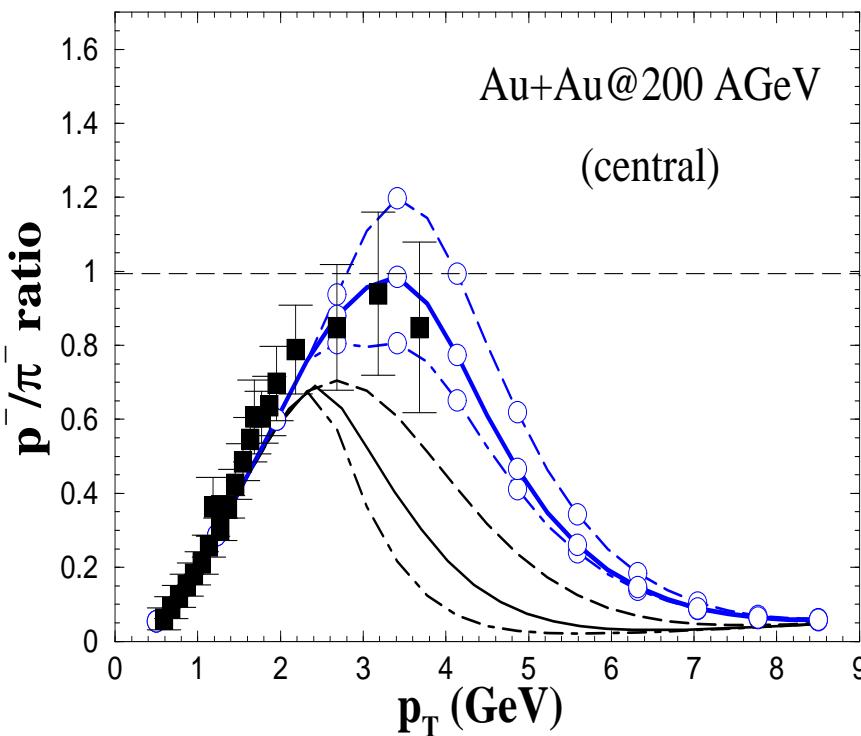
- confirms simple estimates → full scale study with MPC in progress

# Other observables

**Idea:** coalescence  $p_\perp \rightarrow np_\perp$  pushes the low- $p_\perp$ , close to thermal region in spectra out further for baryons than for mesons

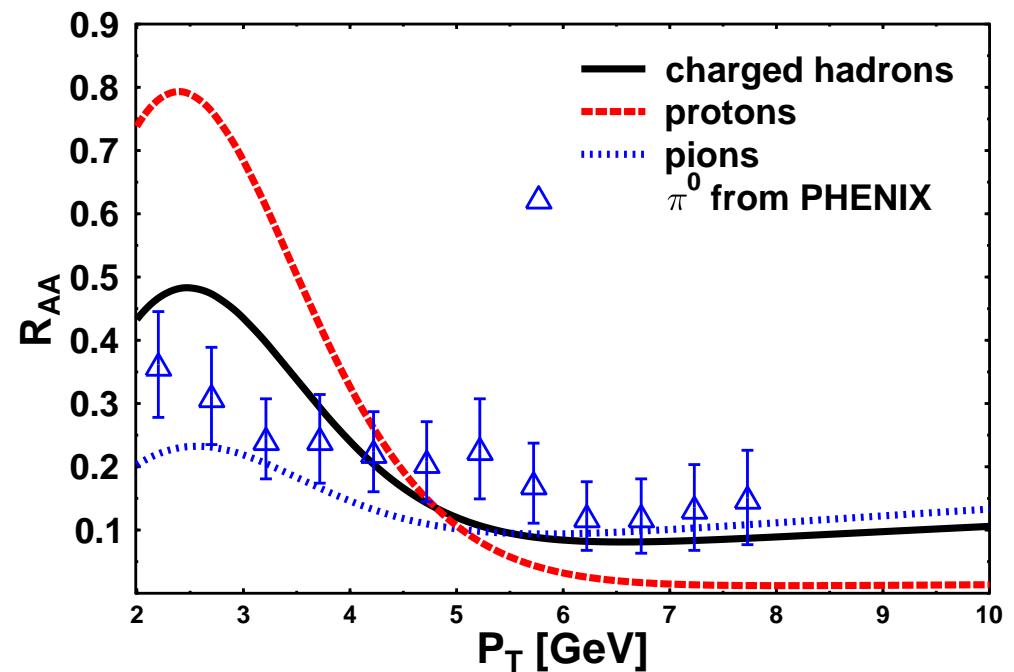
→ different from pQCD fragmentation even at  $p_\perp \sim$  several GeV

$p/\pi$  ratio



[Greco, Ko, Lévai, nucl-th/0301093]

$R_{AA}$  for hadrons



[Fries, Müller, Nonaka, Bass, nucl-th/0301087]

# Coalescence factor

Much of the theory is based on deuteron formation “ $pn \rightarrow d$ ”

- consider momentum space:

- **this talk:** equal parton momenta, e.g.,  $(p_\perp/2, p_\perp/2) \rightarrow p_\perp$   
assumes negligible momentum spread  $\Delta p \approx 0$

- **in principle:** momentum spread is allowed  
 $\Delta p$  distribution depends on hadron wave fn.

Fries et al:  $dN_M(p) \sim \int d\sigma(r) \int dq |\psi_{ab}^M(q)|^2 f_a(p - q/2, r) f_b(p + q/2, r)$

Greco et al:  $dN_M(p) \sim \int dr_1 dp_1 dr_2 dp_2 f_a(r_1, p_1) f_b(r_2, p_2) f_M(x_1 - x_2, p_1 - p_2)$

- **Lin & Ko:** assume any  $\Delta p$  is equally probable  
→ coalescence controlled by shape of constituent spectra

None of the approaches consider the large hadronic binding energies, or at least exact energy-momentum conservation. [These were not an issue in the deuteron case where  $E_{binding} \ll m_N$ ]

# Summary

- the large saturating elliptic flow at observed RHIC can be explained via parton coalescence, with “conventional”, i.e., moderate initial parton densities and cross sections
- the reasons are that coalescence
  - requires  $2 - 3 \times$  larger parton densities  $dN_g/d\eta \sim 2000 - 3000$
  - also leads to a 2-to-3-fold amplification of hadron elliptic flow
- observable effects, predictions:
  - baryon  $v_2$  saturating  $\approx 50\%$  above that of mesons
  - unique elliptic flow ordering at high  $p_\perp$   
 $p > \Lambda \approx \Sigma > \pi > K > \phi, \quad \Lambda, \Sigma > \Xi > K, \quad \Xi > \Omega > \phi \quad (\text{if } v_{2,s} < v_{2,q})$
  - enhanced baryon/meson ratios at moderately large  $p_\perp$

## Open problems

- refined/extended calculations (centrality dependence, ...)
- explore effects on other observables (spectra, HBT, ...)
- detailed space-time dynamics of coalescence mechanism

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This talk is on the WWW at <http://nt3.phys.columbia.edu/people/molnard>