



Forward Physics Power Corrections and Correlations



Santa Fe Muon Workshop June 13 - June 15, 2005, Santa Fe, NM

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Understanding shadowing:

- Resumming coherent QCD power corrections
- Modifications to F_L and F_T (F_1 , F_2 and F_3)
- Relations to lowest order and leading twist
- ► p+A reactions at RHIC:
 - Understanding initial and final state multiple scattering
 - Dynamical gluon "shadowing" yields and correlations
 - E-loss in cold nuclear matter

Open charm production and correlations:

- Partonic subprocesses and cross sections
- Dynamical gluon "shadowing" particle yields and correlations
- Partial Summaries:





Collinear factorization approach: can be systematically expanded to include nuclear corrections

Other phenomenologies: data = model, not proven, anyone heard of NLO correction to a dipole or k_T model ...



Twist: from Opertaor Product Expansion (OPE)

Non-perturbative matrix elements:

Twist 2, 4, 6, ...

T = Dimension - Spin

Higher twist (elastic) corrections: dynamical shadowing



Inclusive Deeply Inelastic Lepton-Hadron Scattering





Variables:
$$q = k - k', v = E - E',$$

 $y = (E - E')/E, Q^2 = -q^2, x = Q^2/(2p \cdot q)$

$$\frac{d\sigma_{lh}}{dxdy} = \frac{4\pi\alpha_{em}}{Q^2} \frac{1}{xy} \left[\frac{y^2}{2} 2xF_1(x,Q^2) + \left(1 - y - \frac{m_N xy}{2E}\right)F_2(x,Q^2) \right]$$

$$F_1(x,Q^2), \ F_2(x,Q^2) \quad \text{- the DIS structure functions}$$

Convenient to calculate in a basis of polarization states of \mathbf{g}^*

$$F_{T}(x,Q^{2}) = F_{1}(x,Q^{2}),$$

$$F_{L}(x,Q^{2}) = \frac{F_{2}(x,Q^{2})}{2x} - F_{1}(x,Q^{2})$$
if $\frac{4x^{2}m_{N}^{2}}{Q^{2}} \ll 1$

QCD kicks in with the parton model / factorization

$$F_{T}(x,Q^{2}) = \frac{1}{2} \sum_{f} Q_{f}^{2} \int d\lambda_{0} e^{ix\lambda} \left\langle p \left| \overline{\Psi}(0) \frac{\gamma^{+}}{2p^{+}} \Psi(\lambda_{0}) \right| p \right\rangle$$
$$= \frac{1}{2} \sum_{f} Q_{f}^{2} \phi_{f}(x,Q^{2}) + \mathcal{O}(\alpha_{s})$$
$$F_{L}(x,Q^{2}) = 0 + \mathcal{O}(\alpha_{s})$$
Lowest Order and
Leading Twist relation

Used to determine the parton distribution functions (PDFs)

Both simple and dangerous

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Lepton+Nucleus from Theory







The Idea Behind the Calculation



• Lightcone gauge: $A \cdot n = A^+ = 0$ • Breit frame: $\overline{n} = [1, 0, 0_{\perp}], n = [0, 1, 0_{\perp}]$ $q = -xp^+\overline{n} + \frac{Q^2}{2xp^+}n, p = \overline{n}p^+, xp + q = \frac{Q^2}{2xp^+}n$



Perturbative





Numerical A- and x_B-Dependence



Purely quantum exp $\left[+ \frac{\xi^2 (A^{1/3} - 1)}{Q^2} x \frac{d}{dx} \right] F_2(x)$ effect $F_T^A(x, Q^2) \approx A F_T^{(LT)} \left(x + \frac{x\xi^2 (A^{1/3} - 1)}{Q^2}, Q^2 \right)$

The scale of higher twist per nucleon is small $\xi^2 \simeq 0.1 \ GeV^2$

• Favorable comparison for the x- and A-dependence NA37 (NMC) and E665 data

• For $Q^2 \rightarrow 0$ we impose $Q^2 = m_N^2$. Finite resolution: same for all models (r_{max})

J.W.Qiu, I.V., Phys.Rev.Lett. 93 (2004)





Q²-dependence and F_L(x,Q²) from Power Corrections





J.W.Qiu, I.V., Phys.Rev.Lett.93 (2004)

Two more tests:

NMC data shows evidence for a power law in $1/Q^2$ behavior in $F_2(Sn)/F_2(C)$

$$\mathbf{R}(x,Q^2) = \frac{\boldsymbol{\sigma}_L}{\boldsymbol{\sigma}_T} = \frac{\boldsymbol{F}_L(x,Q^2)}{\boldsymbol{F}_1(x,Q^2)}$$

$$F_L^A(x,Q^2) \approx A F_L^{(LT)}(x,Q^2) + \frac{4\xi^2}{Q^2} F_T^A(x,Q^2)$$

• The Leading Twist (LT) $R(x,Q^2)$ is not sensitive to modifications of the nPDFs



How to Check the Origin of Shadowing



Experimental data

TABLE I:	Nuclear data inc	cluded in the fit.	
Measurement	Collaboration	Refs.	# data
F_2^{He}/F_2^D	NMC	[13]	18
	SLAC-E139	[14]	18
F_2^{Be}/F_2^D	SLAC-E139	[14]	17
F_2^C/F_2^D	NMC	[13]	18
,	SLAC-E139	[14]	7
F_2^{Al}/F_2^D	SLAC-E139	[14]	17
F_2^{Ca}/F_2^D	NMC	[13]	18
,	SLAC-E139	[14]	7
F_{2}^{Fe}/F_{2}^{D}	SLAC-E139	[14]	23
F_2^{Ag}/F_2^D	SLAC-E139	[14]	7
$F_2^{Au'}/F_2^D$	SLAC-E139	[14]	18
F_2^{Be}/F_2^C	NMC	[15]	15
F_2^{Al}/F_2^C	NMC	[15]	15
F_2^{Ca}/F_2^C	NMC	[15]	15
F_2^{Fe}/F_2^C	NMC	[15]	15
F_{2}^{Pb}/F_{2}^{C}	NMC	[15]	15
F_2^{Sn}/F_2^C	NMC	[16]	145
$\sigma_{DY}^C / \sigma_{DY}^D$	E772	[17]	9
$\sigma_{DY}^{Ca} / \sigma_{DY}^{D}$	E772	[17]	9
$\sigma_{DY}^{Fe}/\sigma_{DY}^{D}$	E772	[17]	9
$\sigma_{DY}^W/\sigma_{DY}^D$	E772	[17]	9
Total			420



Very small (negligible) gluon shadowing

• **Paradox:** for initial state shadowing models $C_A/C_F = 2.25$

• Natural: for final state resummed power corrections

- Only NLO analysis is directly sensitive to gluon distributions in the nucleus
- So far only one such analysis with extremely interesting results





- Modifications to v + A Scattering
- No theory for the shadowing in $\nu + A$
- 3σ deviation from the Standard Model (Now 1.8 σ)

 $\sin^2 \theta_W(SM) = 0.2227 \pm 0.0004$ $\sin^2 \theta_W(NuTeV) = 0.2277 \pm 0.0013 \pm 0.0009 \pm \dots$

NuTeV experiment

G.P.Zeller et al., Phys.Rev.Lett 88 (2002)

(exchange W^{\pm}, Z^0)



• MINOS up and running - a case for MINERvA

Cross sections matter

$$\frac{d\sigma^{v,\overline{v}}_{cc}}{dxdy} \propto \frac{1}{\left(\sin^2\theta_W\right)^2} \left[\frac{y^2}{2} 2x F_1^{W^{\pm}}(x,Q^2) + \left(1 - y - \frac{m_N xy}{2E}\right) F_2^{W^{\pm}}(x,Q^2) \pm \left(y - \frac{y^2}{2}\right) x F_3^{W^{\pm}}(x,Q^2)\right]$$
Axial and vector part (weak current) Similarly for the neutral current



Results: $F_2(x,Q^2)$ and $xF_3(x,Q^2)$





$$F_{1,3}^{(\nu W^{+})}(x_{B},Q^{2}) = \{2\} A \left(\sum_{D,U} |V_{DU}|^{2} \phi_{D}(x_{B} + x_{\xi^{2}} + x_{M_{U}}) \pm \sum_{\overline{U},\overline{D}} |V_{\overline{U}\overline{D}}|^{2} \phi_{\overline{U}}(x_{B} + x_{\xi^{2}} + x_{M_{U}}) + \sum_{\overline{U},\overline{D}} |V_{U}|^{2} \phi_{\overline{U}}(x_{B} + x_{\xi^{2}} + x_{M_{U}}) + \sum_{\overline{U},\overline{U},\overline{D}} |V_{U}|^{2} \phi_{\overline{U}}(x_{B} + x_{\xi^{2}} + x_{M_{U}}) + \sum_{\overline{U},\overline{U},\overline{U}} |V_{U}|^$$

• Physics: generation of a dynamical parton mass in the nuclear field

$$x_B \to x_B \left(1 + \frac{\xi^2 (A^{1/3} - 1)}{Q^2} + \frac{M^2}{Q^2} \right) = x_B \left(1 + \frac{m_{dyn}^2 + M^2}{Q^2} \right)$$





M.Tzanov, DPF 2004 fall meeting Riverside, CA, DIS 2005 Madison, WI



- Focus on the small Q² and x < 0.1 region
- Look relative to MRST 2001 (CTEQ 5,6 have included the data in their analysis thus incorrectly including the nuclear effect in PDFs)



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Physics of the Dynamical Power Corrections





T.Goldman et al., in preparation



- Shadowing in the perturbative regime is calculable based on the uncertainty principle and energy conservation
- Soft final state interactions generate dynamical parton mass $m^2_{dyn} = \xi^2 A^{1/3}$
- If dictated by the uncertainty principle $x_B < 0.1$ the energy of the struck parton should be larger

$$x_B \rightarrow x_B \left(1 + \frac{m_{dyn}^2}{Q^2} \right)$$

• Clearly a high twist and process dependent effect (final state)

$$S_g > S_{u-sea} > S_{u-val}$$

Ivan Vitev, LANL





- Shadowing" results from the coherent final state parton scattering with several nucleons
- The effect is purely quantum. It enters as a shift of the quantum phase and suppresses the SF. The PDFs are the same a in the nucleon
- The shadowing effect exhibits higher twist (power) behavior, i.e. strong Q² dependence

Nuclear matter has refraction index for quarks and gluons





Type of scattering	Transverse momentum dependence of the nuclear effect
Elastic (incoherent)	Cronin effect: small suppression at low p_T , enhancement at moderate p_T , disappears at high p_T . Dijet acoplanarity: p_T diffusions, broadening of away-side corelations
Inelastic (radiative)	Single inclusives: suppression at all p_T , weak p_T dependence, persists at high p_T (amplified near kinematic bounds). Double inclusive: suppression of high p_T correlations, reapearance of the energy at low p_T
Coherent (elastic t-channel)	Both single and double inclusive: suppression at low p_T , disappears at high p_T , pronounced p_T dependence

TABLE I: Effect of elastic, inelastic and coherent multiple scattering on the transverse momentum dependence of single and double inclusive hadron production in the perturbative regime.



- p+A collisions do not carry direct information about PDFs (unfortunately all effects)
- Forward (backward) physics not equal small x (large x)
- 1) Initial state energy loss and broadening DY
- 2) Shadowing DIS
- 3) Final state e-loss is added in p+A



p+A Collisions



Ivan Vitev, LANL



Resum the multiple final state scattering of the parton "d" with the remnants of the nucleus

Starting point: LO pQCD



- Interested in the maximum coherent rescattering of the small \mathbf{x}_{b} parton in the nucleus
- Other interactions are less coherent (elastic) and sppressed at forward rapidity by a large scale 1/u, 1/s

$$\begin{split} \frac{d\sigma_{NN}^{h_1}}{dy_1 d^2 p_{T1}} &= K \sum_{abcd} \int_{z_1 \min}^1 dz_1 \frac{D_{h_1/c}(z_1)}{z_1^2} \int_{x_a \min}^1 x_a \frac{\phi(x_a)}{x_a} \frac{1}{x_a S + U/z_1} \frac{\alpha_s^2}{S} \int_{0}^1 x_b \delta(x_b - \overline{x}_b) F(x_b) \\ \frac{d\sigma_{NN}^{h_b h_2}}{dy_1 dy_2 d^2 p_{T1} d^2 p_{T2}} &= \frac{\delta(\Delta \varphi - \pi)}{p_{T1} p_{T2}} \sum_{abcd} \int_{z_1 \min}^1 dz_1 \frac{D_{h_1/c}(z_1)}{z_1} D_{h_2/d}(z_2) \frac{\phi(\overline{x}_a)}{\overline{x}_a} \frac{\alpha_s^2}{S^2} \int_{0}^1 x_b \delta(x_b - \overline{x}_b) F(x_b) \\ \phi(x_b) - \text{standard parton distribution} \\ functions \\ \text{Isolate all the } \mathbf{x}_b \text{ dependence of the integrand:} \quad F(x_b) = \frac{\phi(x_b)}{x_b} \left| \overline{M}^{-2}_{ab \to cd} \right| \end{split}$$



Numerical Results





- Similar power corrections modification to single and double inclusive hadron production
 - increases with rapidity and centrality
 - disappears at high p_T in accord with the QCD factorization theorems



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Forward Correlations



TAR Preliminary: L.Bland, [STAR Colaboration]

Los Alamos



• There isn't mono jettiness or g-fusion

• I think that the p+A analysis has under and over estimated the away-side area

• There may be room for some suppression due to power corrections





J.W.Qiu, I.V., hep-ph/0405068

Comparison to the data:

I.Arsene et al., Phys.Rev.Lett. 93 (2004)

$$F(x_b) \rightarrow F\left(x_b + x_b C_d \frac{\xi^2}{-t} (A^{1/3} - 1)\right)$$
$$F(x_b) = \frac{\phi(x_b)}{x_b} \left| \overline{M} \right|_{ab \to cd}^2$$

Suppression increases with rapidity and centrality

Suppression disappears at high p_T

Data supports this type of power behavior

However, there may be room for additional suppression - may be 50 % more, may be a factor of 2

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p+A Yields





Before jumping to conclusions investigate existing data

NA35 collaboration: d+Au (interestingly enough) data - $\sqrt{s_{NN}} = 19.4 \ GeV$ Same rapidity asymmetry as at $\sqrt{s_{NN}} = 200 \ GeV$



- Leading twist shadowing: (phenomenology) clearly insufficient (in fact antishadowing)
- Power corrections (theory): clearly insufficient (~13%)

Leaves additional effects: enegy loss

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One Implementation of Energy Loss



Bertsch-Gunion bremsstrahlung:

$$\frac{dn_G}{dy} = \frac{3\alpha_s}{\pi} \ln\left(\frac{m_\rho^2}{\Lambda_{QCD}^2}\right)$$

Implemented as "Sudakov Form Factors":

$$S(x_F) = (1 - x_F)^{dn_G/dy}$$

This is one way of implementing energy loss (large rapidity gap events, amplification near kinematic bounds)

B. Kopeliovich *et al.*, hep-ph/0501260

Where energy loss arguably plays a role







- p+A is not substitute for DIS. Don't learn much about PDFs. Learn about multiple parton interactions
- Calculated the upper limit of the suppression in p+A reactions from shadowing.
- The results are compatible with the data but the current statistics and systematics are large
- At large x_F energy loss can play a significant role. There is low energy p+A to be analized. Low energy RHIC run.



Many of the interesting features that follow are related to the $cg \to cg$ $cq(\overline{q}) \to cq(\overline{q})$ scattering

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Research of Literature



L. Odoricio, Nucl.Phys.B 209 (1982)

We present a calculation of the contribution of flavour excitation diagrams to the hadronic production of open charm. The main new ingredients in the calculation are: (i) a proper treatment of the QCD evolution of the input charm sea distribution, with constraints from the existing charm structure function data; (ii) use of the available charm transverse momentum data to fix the cutoff which regulates divergence in the diagrams. We are then able to make a stable the calculation of the resulting charm cross section. The flavour excitation contribution turns out to be an order of magnitude larger than for fusion. As a result the observed magnitudes of the charm cross section at accelerator and ISR energies are satisfactorily reproduced, thus eliminating a long standing difficulty of the perturbative QCD approach to open charm production. Furthermore, we calculate the longitudinal and transverse spectra of charmed hadrons using a simple recombination model. We show that the existing ISR data on the are well, and naturally, reproduced by this production of fast approach. Qualitative predictions for bottom production are also d i S u d С S S e

Flavor excitation = charm quark pdfs





D⁰ and **D**⁺ at the Tevatron

$$\frac{d\sigma_{NN}^{D_1}}{dy_1 d^2 p_{T_1}} = K_{NLO} \sum_{abcd} \int_{x_{1,2} \le 1} dy_2 \int_{x_{1,2} \le 1} dz_1$$
$$\times \frac{1}{z_1^2} D_{D_1/c}(z_1) \frac{\phi_{a/N}(x_a)\phi_{b/N}(x_b)}{x_a x_b} \frac{\alpha_s^2}{S^2} |\overline{M}_{ab \to cd}|^2$$

• Fragmentation functions: From heavy quark effective field theory (Vector and Pseudoscalar)

E.Braaten et al., Phys.Rev.D 51 (1995)

• Branching ratios taken into account $D^{0^*} \rightarrow D^0 (BR \ 100\%) \quad \cdots$

Very reasonable K-factor: $K_{NLO} = 1.7$ Slightly stiffer power law



Data from:

D.Acosta et al., Phys.Rev.Lett. 91 (2003)







Comparable results to:

M.Cacciari, P.Nason and R.Vogt, hep-ph/0502203

Case for a new experimental capability to detect directly heavy quarks

Preliminary STAR: power law spectrum seems noticeably stiffer

Remember - at the Tevatron the same calculation was slightly stiffer

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Contribution of Partonic Subprocesses

10



Define partial cross sections

$$R^{\sigma}(p_{T_{1}}) = \frac{d\sigma^{D_{1}}_{ab \to cd}}{dy_{1}d^{2}p_{T_{1}}} \left/ \frac{d\sigma^{D_{1}}_{tot}}{dy_{1}d^{2}p_{T_{1}}} \right.$$

Gluon fussion is not the dominant mechanism for open charm production

Clearly one expects 2 things:

- Dynamical shadowing comparable to light pions
- Trigger dependent hadrochemistry

How to test this? - di-hadron correlations

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$$\begin{array}{c} 10 \\ y = 0 \\ 0.1 \\ 0.01 \\ 0.001 \\ y = 1.25 \\ 0.001 \\ y = 1.25 \\ 0.001 \\$$

- (1) $cg \rightarrow cg$, (2) $cq(\overline{q}) \rightarrow cq(\overline{q})$
- (3) $gg \to c\overline{c}$, (4) $q\overline{q} \to c\overline{c}$
- (5) $c\overline{c} \rightarrow c\overline{c}$



D Triggered Correlations

$$\frac{d\sigma_{NN}^{D_1h_2}}{dy_1 dy_2 dp_{T_1} dp_{T_2}} = K_{NLO} \sum_{abcd} 2\pi \int_{x_1 \le 1, x_2 \le 1, z_2 \le 1} dz_1 \\ \times \frac{1}{z_1} D_{D_1/c}(z_1) D_{h_2/d}(z_2) \frac{\phi_{a/N}(x_a)\phi_{b/N}(x_b)}{x_a x_b} \\ \times \frac{\alpha_s^2}{S^2} |\overline{M}_{ab \to cd}|^2 .$$

- \bullet Very strong dependence of particle species in the away side jet on p_{T2}
- Non-monotonic behavior on the away side yields: anti D at $p_{T2} = p_{T1}$



Real possibility for RHIC experiments to discover D meson triggered correlations

Constrain D meson production, c quark fragmentation



T.Goldman et al., in preparation



Dynamical Shadowing to Inclusive D⁰+D⁺





Increases with centrality:

(dynamical shadowing has little to do with A but with the local path length through nuclear matter) Increases with rapidity:

(slightly)

Disappears at high p_T:

(power correction type, coherent elastic)



Quite similar to light pions (even slightly larger)

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(D⁰+D⁺) - (D⁰+D⁻) Triggered Correlations



Similar results for the D meson triggered correlations

$$\hat{t} = (x_a P_a - p_c / z_1)^2$$

• We know for a fact that the c quark rescatters (as in DIS)

$$\xi^2 (A^{1/3} - 1) / (-\hat{t})$$

• In light hadrons $C_{A}/C_{E}\xi^{2}(A^{1/3}-1)/(-\hat{t})$

Naively expected that the partonic ^o composition will matter but apparently what dominates is:

 $Z_{light hadons} < Z_{cl}$

$$< z_{charm\ mesons}$$

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Experimentally probably biased to $p_{T1} = p_{T2}$





- A large contribution to the open cham (single) hard cross section comes from scattering on quarks and gluons
- Non-trivial hadron composition of D triggered correlations should be experimentally tested
- The power corrections a similar to the light hadrons but the reason is different - the large z₁, z₂ even if it is q rather than g rescattering
- We have calculated the upper high twist shadowing limit - a baseline for the energy loss







• Even if one neglects $\phi_c(x,Q^2)$, $\phi_{\overline{c}}(x,Q^2)$ mass effects show up due to the charge exchange



J.W.Qiu, I.V., Phys.Lett.B 587 (2004)

• Along the way we will develop techniques that may be useful in the discussion of charm production at RHIC

|V| - the CKM matrix elements U = (u, c, t), D = (d, s, b)

$$F_{L}^{(\nu W^{+})}(x_{B},Q^{2}) = \sum_{D,U} |V_{DU}|^{2} \frac{M_{U}^{2}}{Q^{2}} \phi_{D}(x_{B} + x_{M_{U}}) + \sum_{\bar{U},\bar{D}} |V_{\bar{U}\bar{D}}|^{2} \frac{M_{\bar{D}}^{2}}{Q^{2}} \phi_{\bar{U}}(x_{B} + x_{M_{\bar{D}}})$$

$$F_{L}^{(\bar{\nu}W^{-})}(x_{B},Q^{2}) = \sum_{U,D} |V_{UD}|^{2} \frac{M_{D}^{2}}{Q^{2}} \phi_{U}(x_{B} + x_{M_{D}}) + \sum_{\bar{D},\bar{U}} |V_{\bar{D}\bar{U}}|^{2} \frac{M_{\bar{U}}^{2}}{Q^{2}} \phi_{\bar{D}}(x_{B} + x_{M_{\bar{U}}})$$

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Mass and Nuclear Enhanced Power Corrections





Special propagator structure:

$$(\gamma \cdot \tilde{p} + M) \gamma_{\perp} (\gamma \cdot \tilde{p} + M) = 0$$
$$(\gamma \cdot p) \gamma_{\perp} (\gamma \cdot p) = 0$$

- Equations of motion nuclear enhanced power corrections and mass corrections commute
- Demonstrated that the corrections can be resummed
- Physics interpretation generation of a dynamical parton mass in the nuclear chromomagnetic field

$$x_B \rightarrow x_B \left(1 + \frac{\xi^2 (A^{1/3} - 1)}{Q^2} + \frac{M^2}{Q^2} \right) = x_B \left(1 + \frac{m_{dyn}^2 + M^2}{Q^2} \right)$$

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- Resummed power corrections are the first consistent way to address valence/sea quark shadowing
- Neutrino-nucleus reactions help discover the physical meaning of higher twist - generation of dynamical parton mass
- For light quarks we have dynamical chiral symmetry breaking (similar to electrons in B field)
- Goes in the direction of reducing the discrepancy between the NuTeV experiment and the SM
- The qualitative power law behavior at small x is seen by NuTeV / CCFR. Expect comparison