

Measurement of Direct Photons at High p_T

Methods and Results

Jet Physics In Heavy Ion Collisions at the LHC
Trento
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Outline

- **What?**
- **Why?**
- **How?**



What are Direct Photons?

- **Pragmatic definition:**
 - ✗ Anything but decay photons

$$\text{inclusive photons} = \text{decay photons} + \text{direct photons}$$

- **Difficult measurement:**

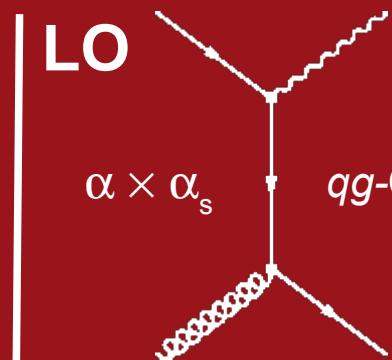
$$\left. \begin{array}{l} \pi^0 \rightarrow \gamma + \gamma \\ \eta \rightarrow \gamma + \gamma \end{array} \right\} \text{large background!}$$



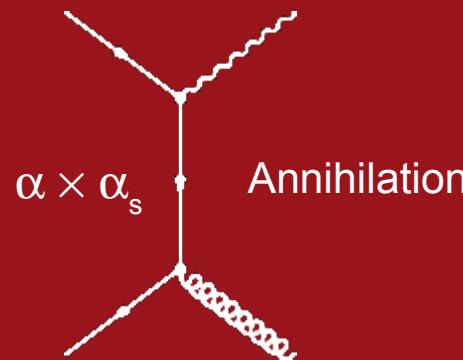
Why Direct Photons?

- **Production in p+p**

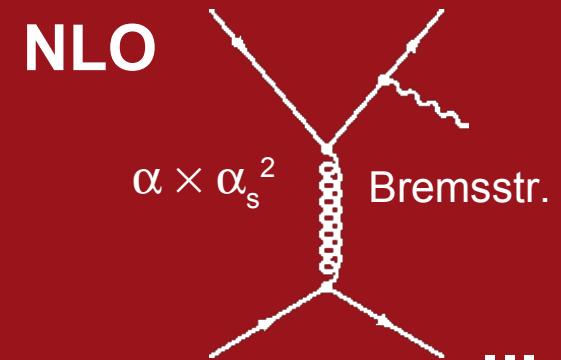
- × Hard (with large Q^2) parton-parton collisions e.g.:



- × Photon+Jet



- Annihilation



- Bremsstr.

- × Precision test of pQCD

$$\frac{d^2\sigma}{dp_T dy} = \int \text{PDF} \times \text{pQCD} \times \delta$$

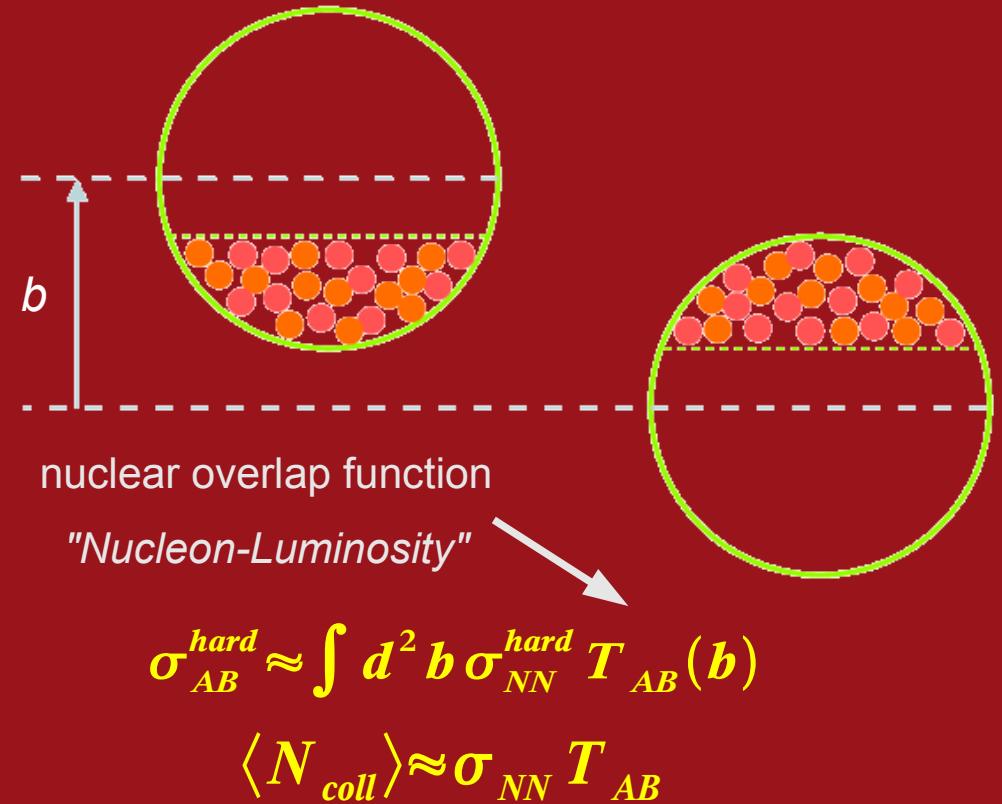
- × Constrains gluon distribution and polarization
 - × Choice of renormalization, factorization and fragmentation scales arbitrary (usually of the order of p_T)

Going from p+p to A+A



Hard Photons in A+A

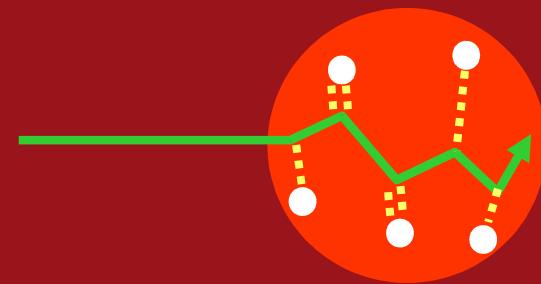
- Increased number of scattering centers





Hard Photons in A+A

- **Increased number of scattering centers**
- **Nuclear effects**
 - ✗ “Shadowing” of PDFs
 - ✗ Cronin Effect, multiple soft scattering
- **Still at parton level, but “early” reaction phase**

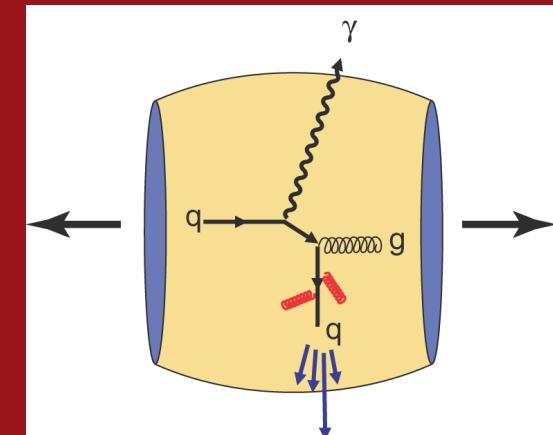


$$\frac{d^2\sigma}{dp_T dy} = \int \text{PDF} \times \text{pQCD} \times \delta$$



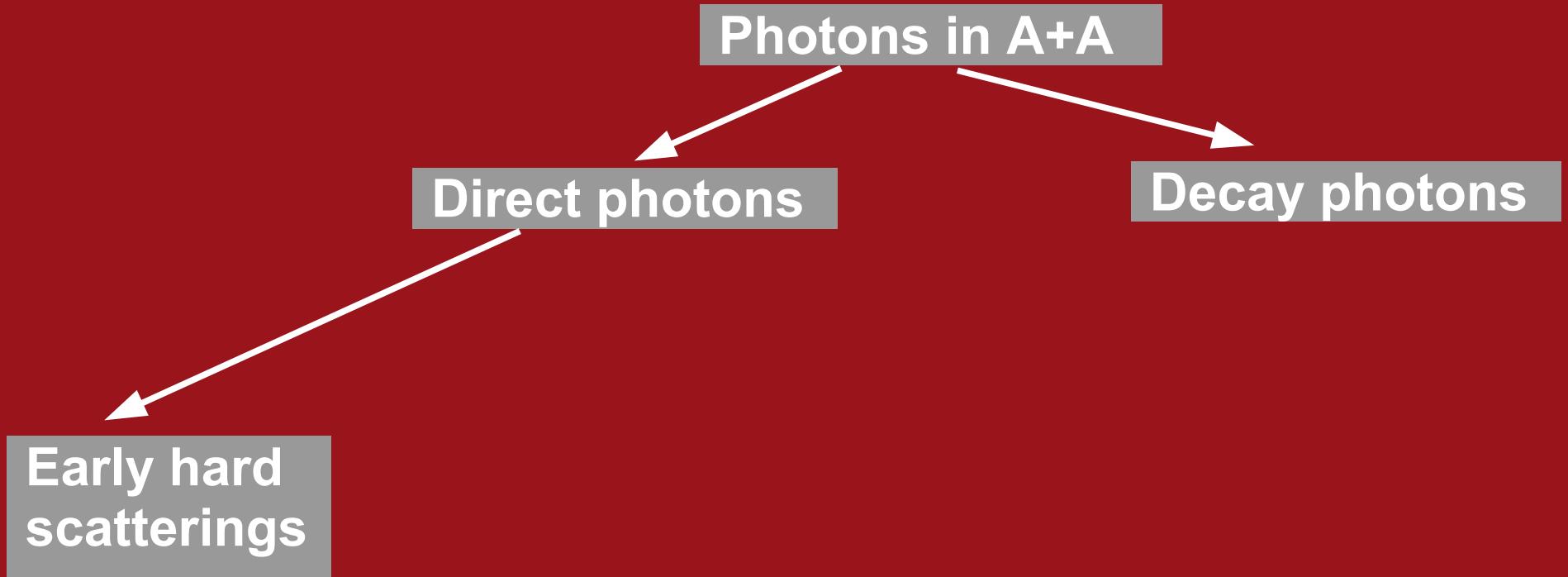
Hard Photons in A+A

- **Increased number of scattering centers**
- **Nuclear effects**
 - ✗ “Shadowing” of PDFs
 - ✗ Cronin Effect, multiple soft scattering
- **Still at parton level, but “early” reaction phase**
- **Hot and dense medium**
 - ✗ Probed by partons
 - ✗ Photons unaffected by strong interaction
 - ✗ Photons provide **in situ** control



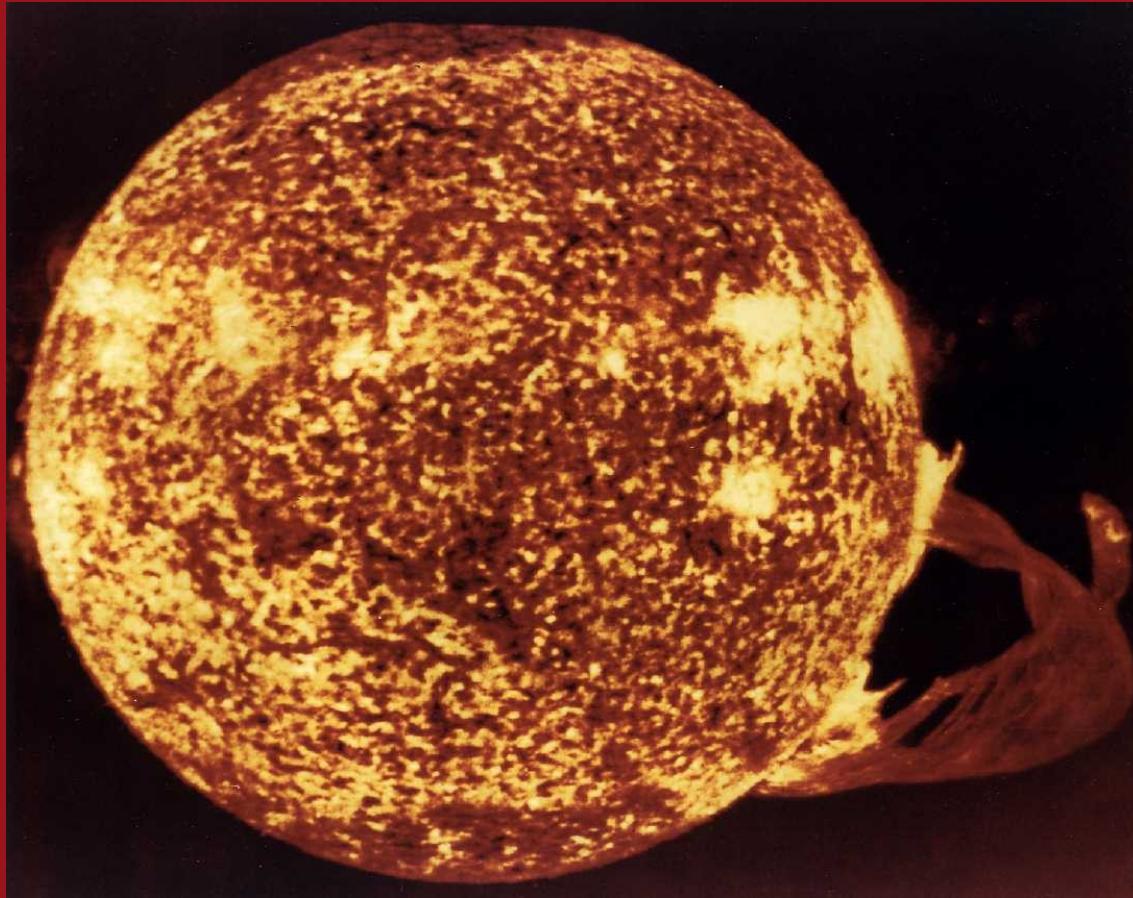


Photon Sources in A+A



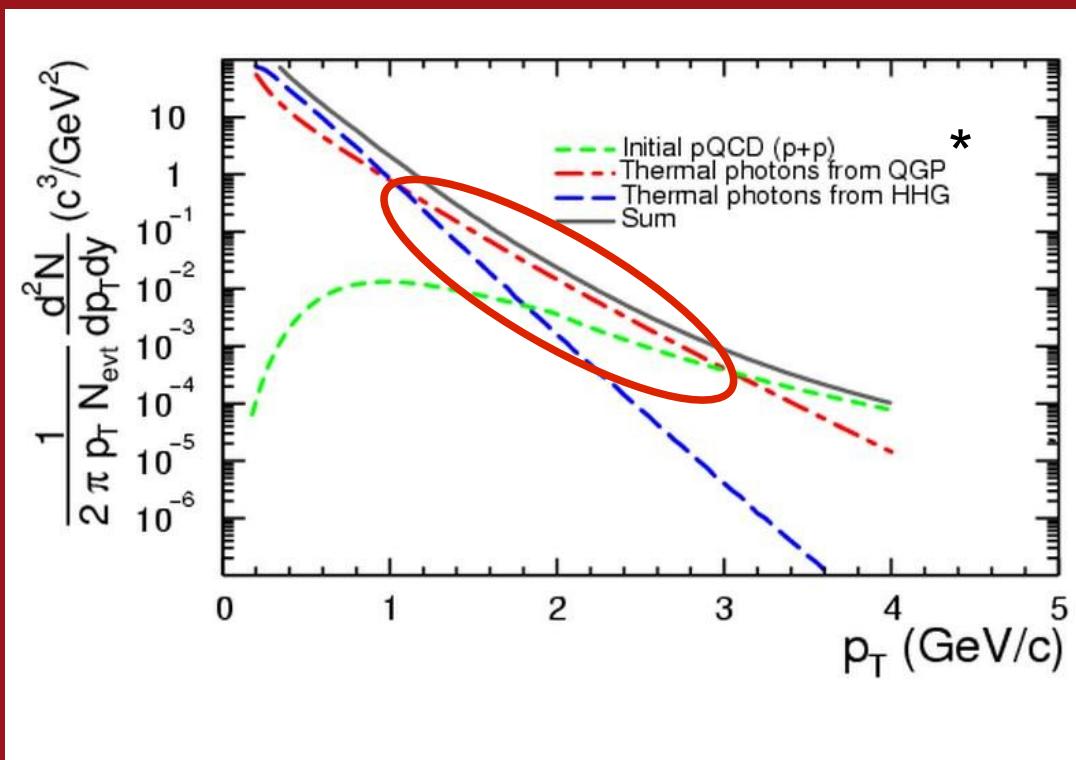
Also called
prompt photons

There is more information from photons in HIC...





Thermal Photons in A+A



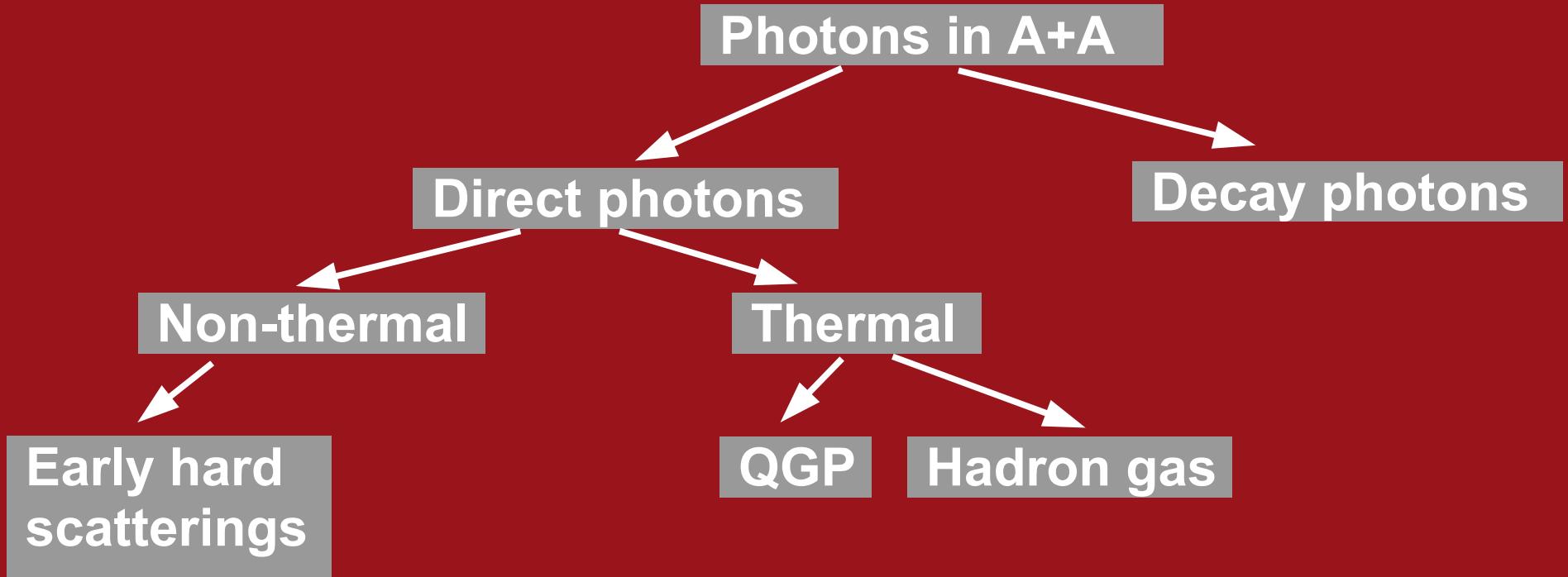
- **Thermal photons**
 - × From QGP and HHG
 - × Measure for initial temperature of the system (here $T_i = 370$ MeV)
 - × Additional signature for QGP

*Turbide, Rapp, Gale:

Phys. Rev. C 69:014903, 2004

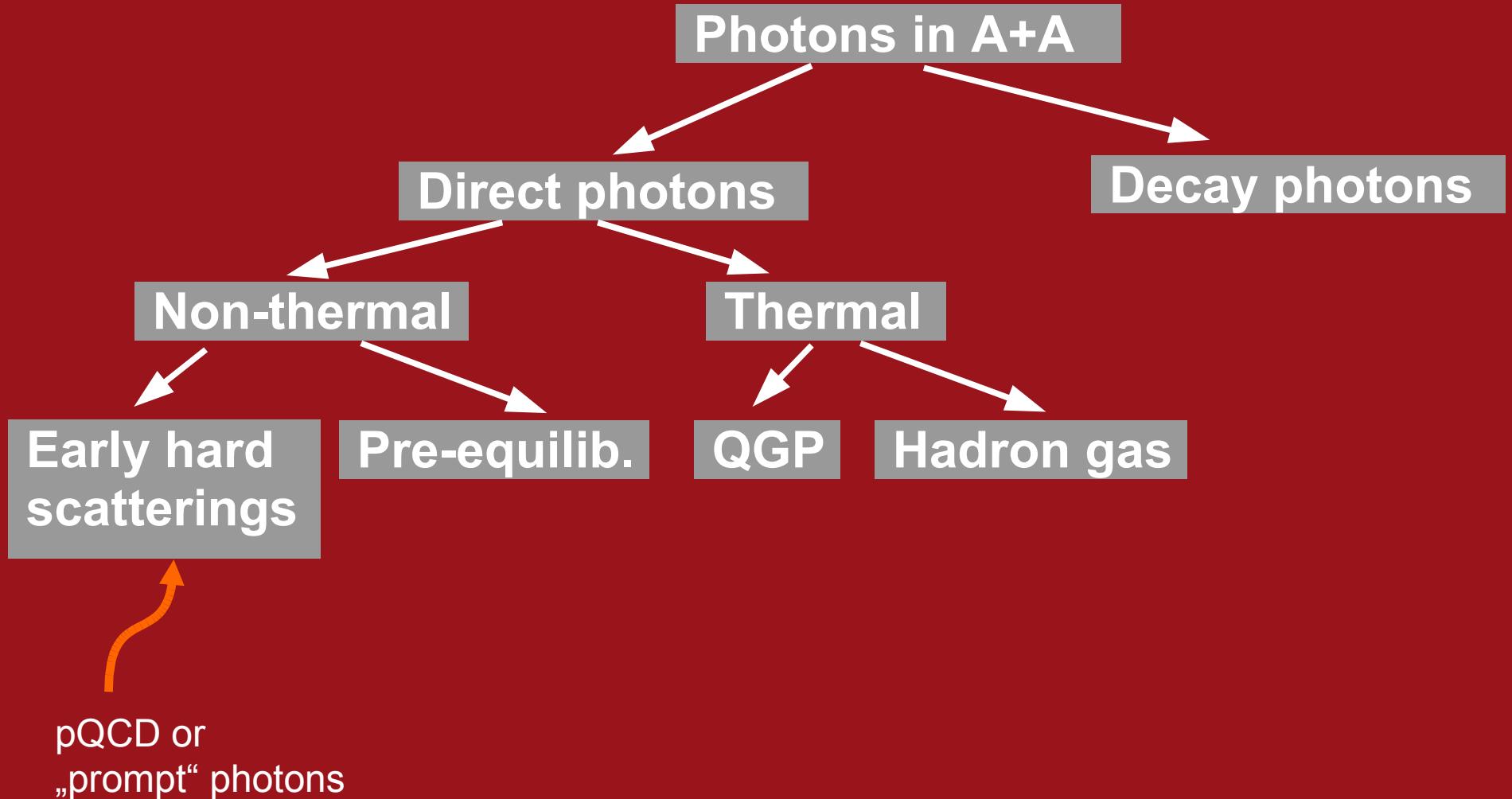


Photon Sources in A+A



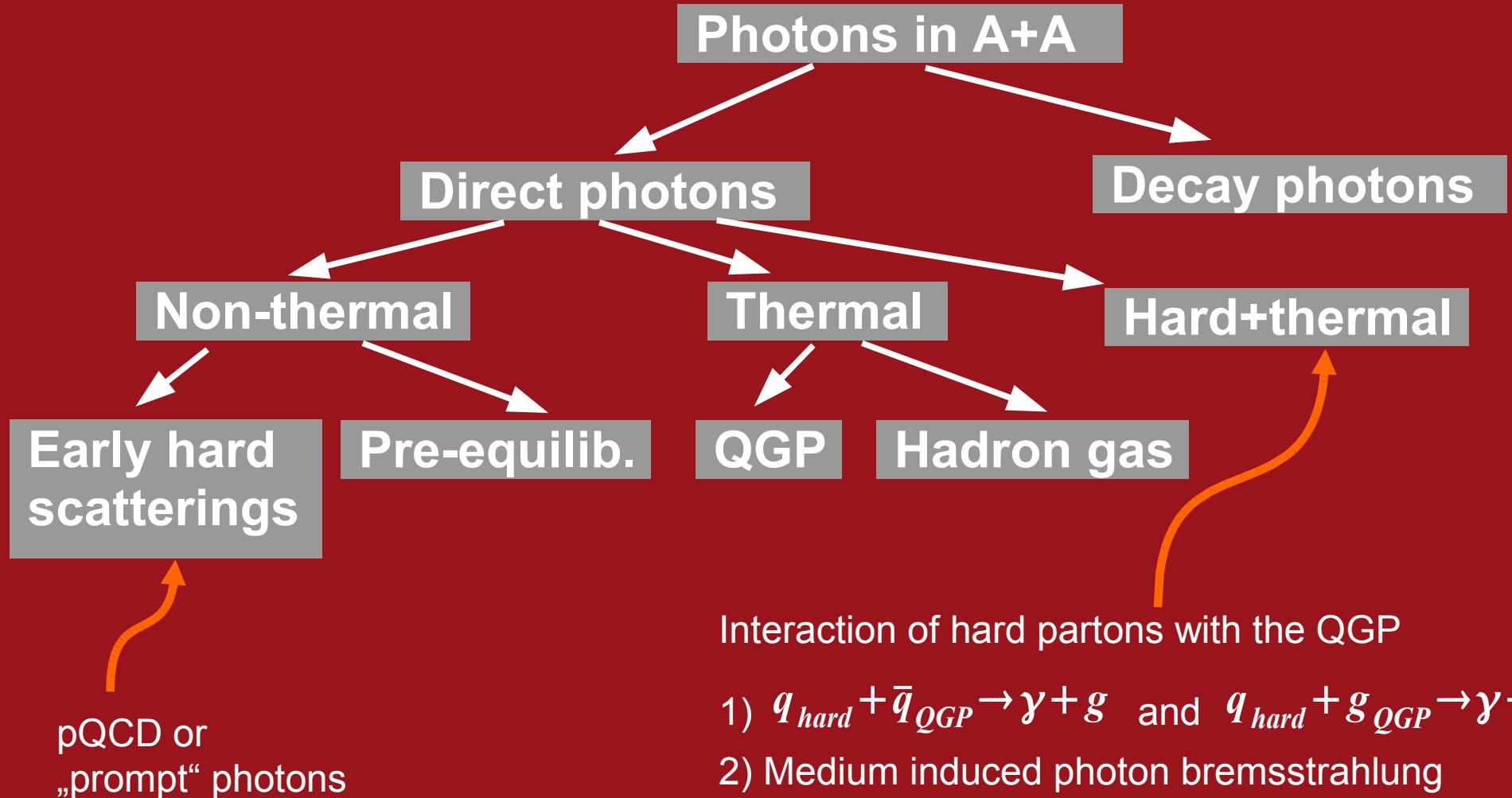


Photon Sources in A+A



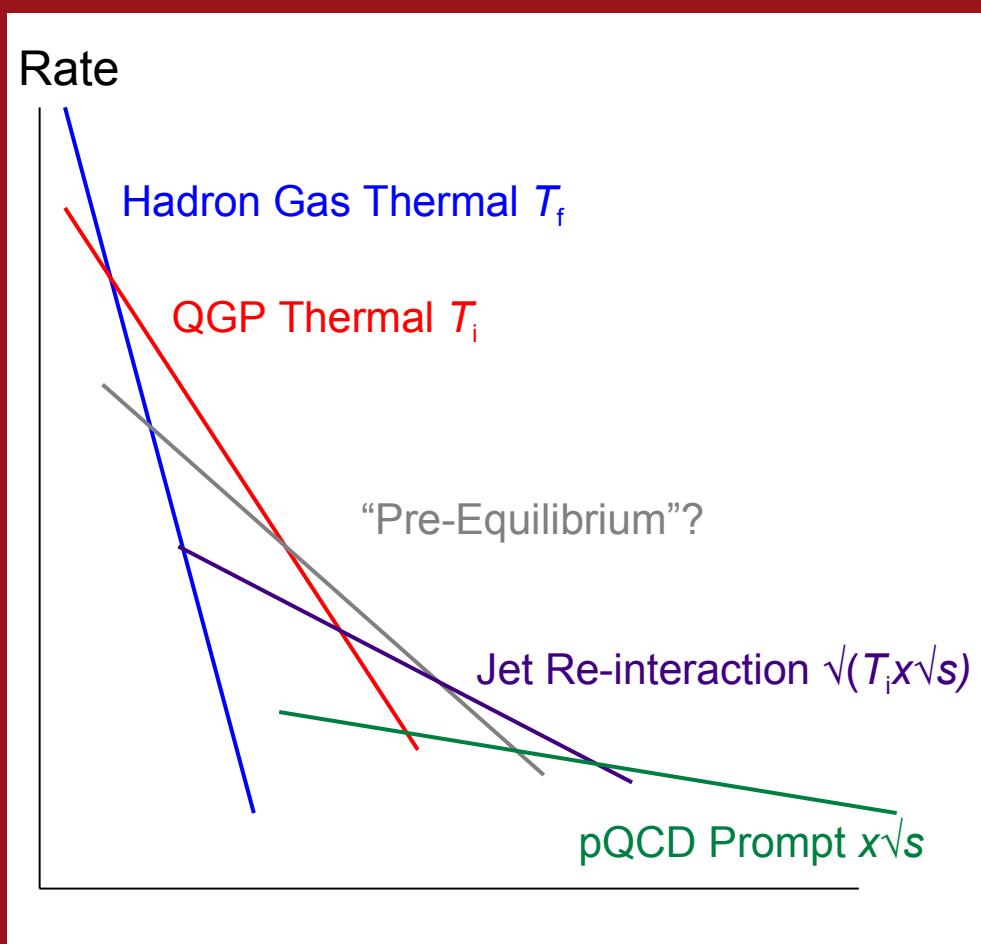


Photon Sources in A+A





Summary



**The promise and the peril:
Photon signal is very ambiguous!**

- **Direct photons in p+p**
 - ✗ Precision test of pQCD
 - ✗ Do not suffer from fragmentation
 - ✗ Direct (LO) access to gluon polarization
- **Direct photons in A+A**
 - ✗ Carry information of all stages of the reaction
 - ✗ In situ control of hard scattering at high p_T
 - ✗ Thermal radiation from QGP and HHG at low p_T
 - ✗ Additional photons:
 - Pre-equilibrium
 - Jet – plasma interactions



How to measure Direct Photons

- **Inclusive Photons**

$$N_{all}^{\gamma} = N_{direct}^{\gamma} + N_{decay}^{\gamma}$$

- **Challenge to separate signal from decay background**

- ✗ Mainly $\pi^0 \rightarrow \gamma\gamma$

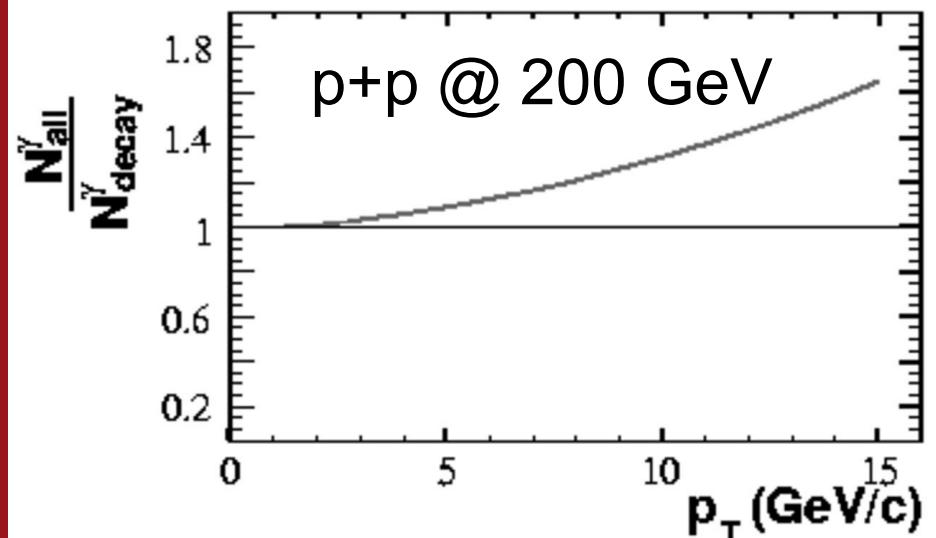
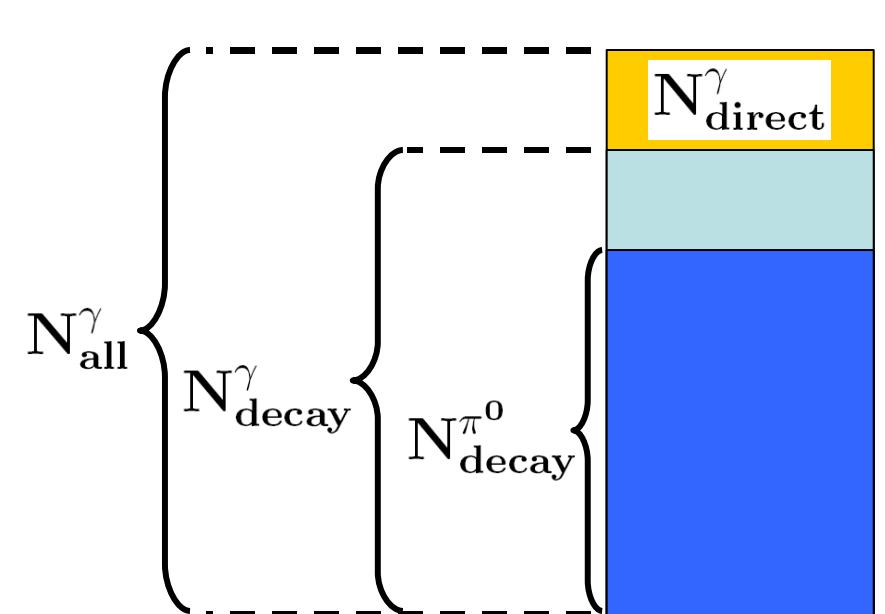
- **Direct separation**

- ✗ event-by-event isolation cuts

- **Statistical separation**

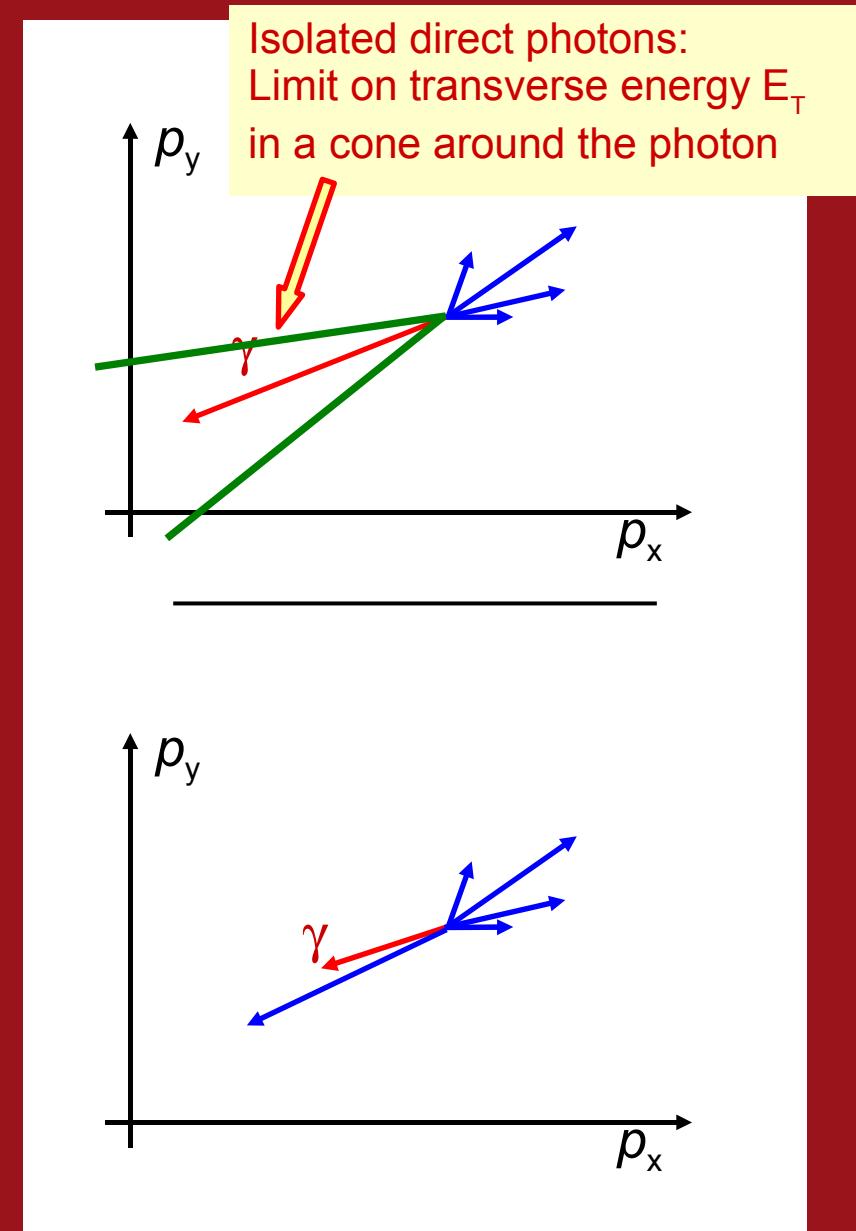
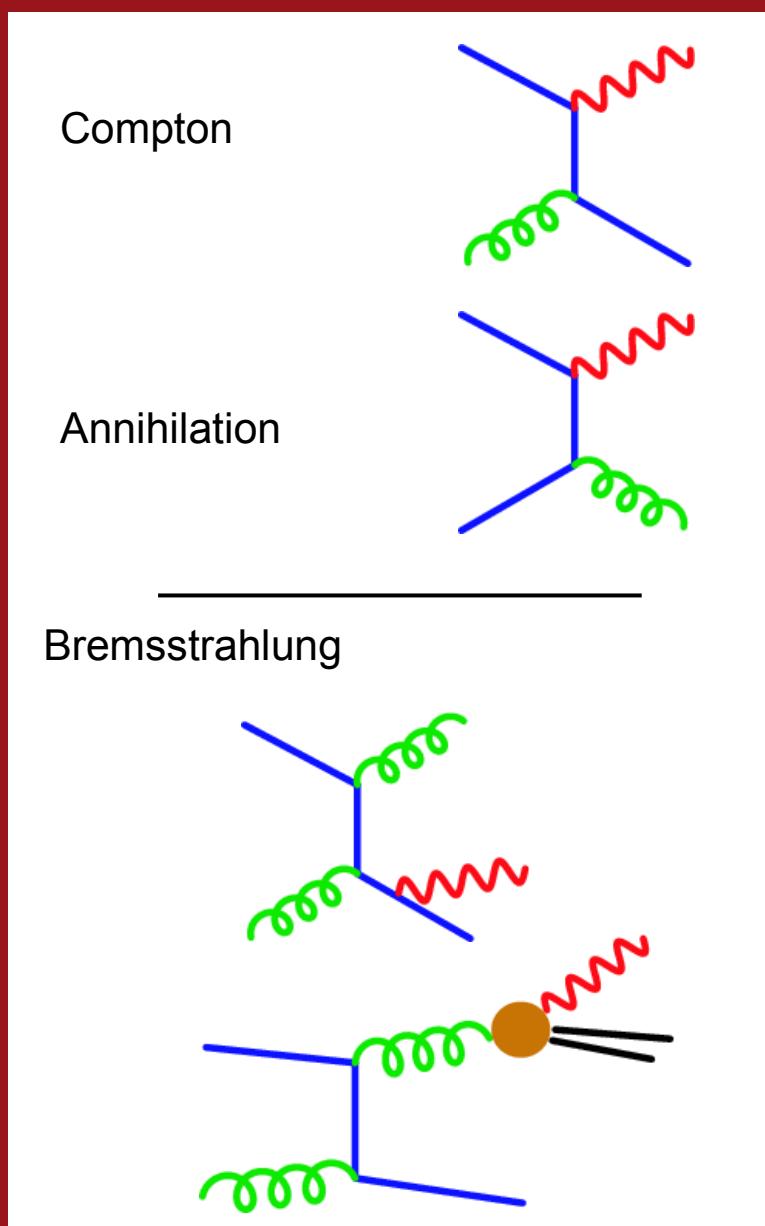
- ✗ Compare measured inclusive γ to expected decay γ

$$N_{direct}^{\gamma} = N_{all}^{\gamma} - N_{decay}^{\gamma}$$





Isolation Cuts





Example of Isolation Cuts

- Cone radius: $R = \sqrt{\Delta\eta^2 + \Delta\phi^2}$
- Fermilab experiments ($p + \bar{p}$ at $\sqrt{s} = 1.8$ TeV):
 - × CDF: $E_T < 5$ GeV for $R < 0.65$
 - × D0: $E_T(R \leq 0.4) - E_T(R \leq 0.2) < 2$ GeV

For a meaningful comparison with NLO pQCD, the experimental isolation cut needs to be translated into a theoretical cut.

This is not trivial.



Subtraction Method

- Determine inclusive photon spectrum
 - ✗ Calorimeter
 - ✗ Tracking of conversion photons
- Extract significance of direct photon signal
 - ✗ Cocktail Method
 - ✗ HBT correlation strength
 - ✗ Internal conversions

$$\begin{aligned}\gamma_{direct} &= \gamma_{inclusive} - \gamma_{decay} \\ &= \left(1 - \frac{\gamma_{decay}}{\gamma_{inclusive}}\right) \gamma_{inclusive} \\ &= (1 - 1/R) \gamma_{inclusive}\end{aligned}$$

e.g with $R = \frac{(\gamma_{inclusive}/\pi^0)_{meas}}{(\gamma_{decay}/\pi^0)_{calc}}$

R contains the statistical and systematic significance of the direct photon signal



Measurements in p+p

- First measurement in the late 1970s

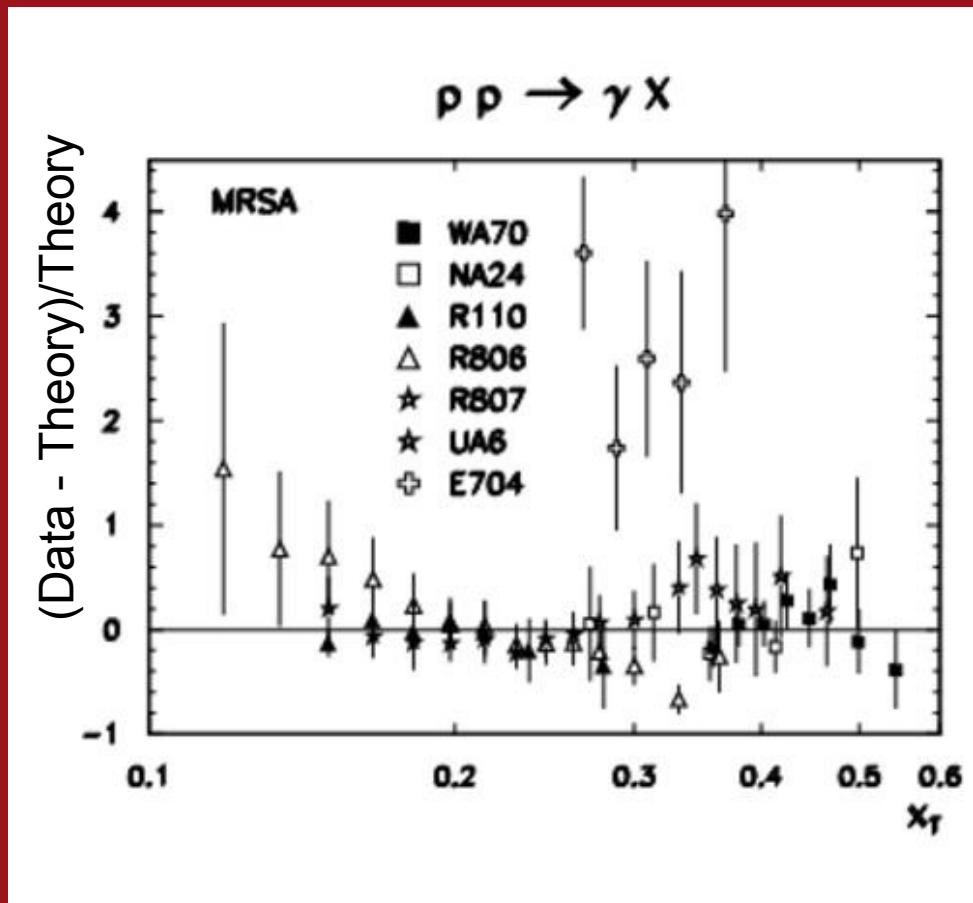
✗ Today: $\sqrt{s_{\text{NN}}} = 19.3 - 1800 \text{ GeV}$

- Momentum fraction of probed parton relevant

$$x \approx x_T = \frac{2p_T}{\sqrt{s}}$$

- Open issues/uncertainties

- ✗ Analysis cuts
- ✗ Arbitrary choice of scales
- ✗ Additional intrinsic k_T needed?
- ✗ Gluon PDF poorly known
- ✗ FF($g/q \rightarrow \gamma$)



W. Vogelsang J. Phys. G23 (1997)



Direct Photon Measurement in A+A

- Challenging
 - ✗ Large decay background
 - ✗ High multiplicities
- Two measurements:
 - ✗ WA98:
 - Pb+Pb @ $\sqrt{s_{NN}} = 17.2 \text{ GeV}$
 - PRL **85** (2000) 3595
 - ✗ PHENIX:
 - Au+Au @ $\sqrt{s_{NN}} = 200 \text{ GeV}$
 - PRL **94** (2005) 232301



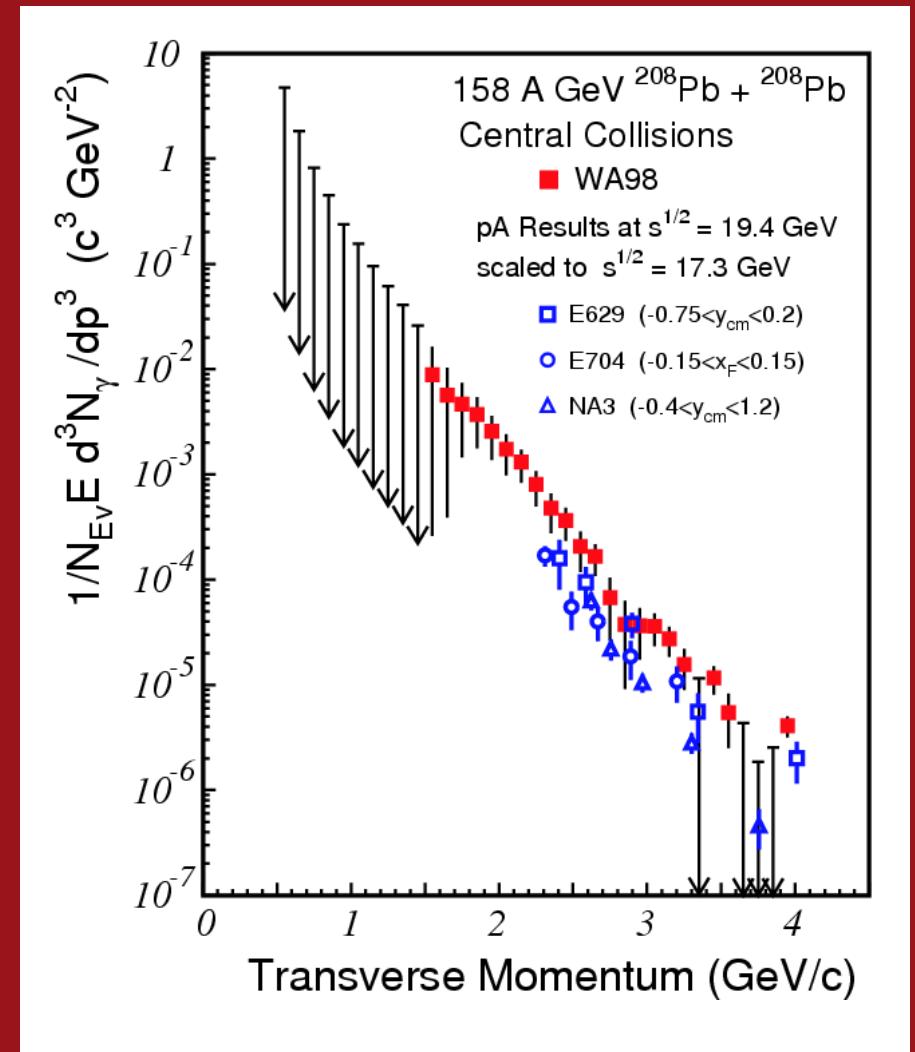
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- Similar Methods
 - ✗ Subtraction
$$\frac{d^2 N}{dp_T dy_{direct}} = \left(1 - \frac{\gamma_{bkgd}}{\gamma_{meas}} \right) \frac{d^2 N}{dp_T dy_{incl}}$$
 - ✗ Compare inclusive Photons to expectation from decay photons (Cocktail)
$$R = \frac{\gamma_{meas}}{\gamma_{bkgd}} = \frac{(\gamma/\pi^0)_{meas}}{(\gamma/\pi^0)_{bkgd}}$$



Direct Photon Measurement in A+A

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Details of the first Direct Photon Measurement at RHIC (Cocktail Subtraction)

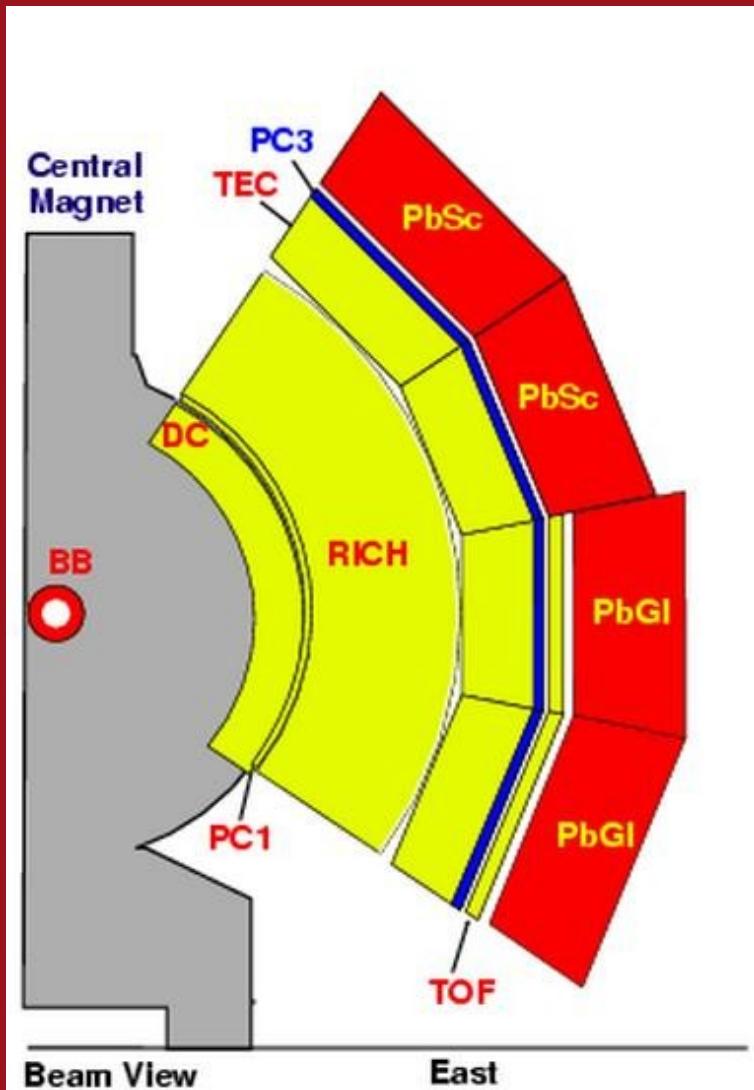


Measurement of Direct Photons with Cocktail Method

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Subtract decay background from inclusive photon spectrum



Direct Photon Measurement



- **Photon candidates**
 - ✗ 6 Sectors PbSc sandwich
 - ✗ 2 Sectors PbGI Cherenkov
- **Charged particles with PC3**



Formula for Fully Corrected Inclusive Photon Spectra

$$\frac{1}{2\pi p_T N_{\text{in}}} \left. \frac{d^2 N_\gamma}{dp_T dy} \right|_{\text{incl}} = \frac{1}{2\pi p_T N_{\text{in}}} \cdot \frac{(1 - X_{n\bar{n}}) \cdot (1 - X_{\text{ch}})}{\varepsilon_\gamma \cdot a_\gamma \cdot c_{\text{conv}}} \cdot \frac{\Delta N_{\text{cluster}}}{\Delta p_T \Delta y},$$

fraction of neutral background (neutron, anti-neutrons)

fraction of charged clusters

efficiency

acceptance

photon conversion



Formula for Fully Corrected Inclusive Photon Spectra

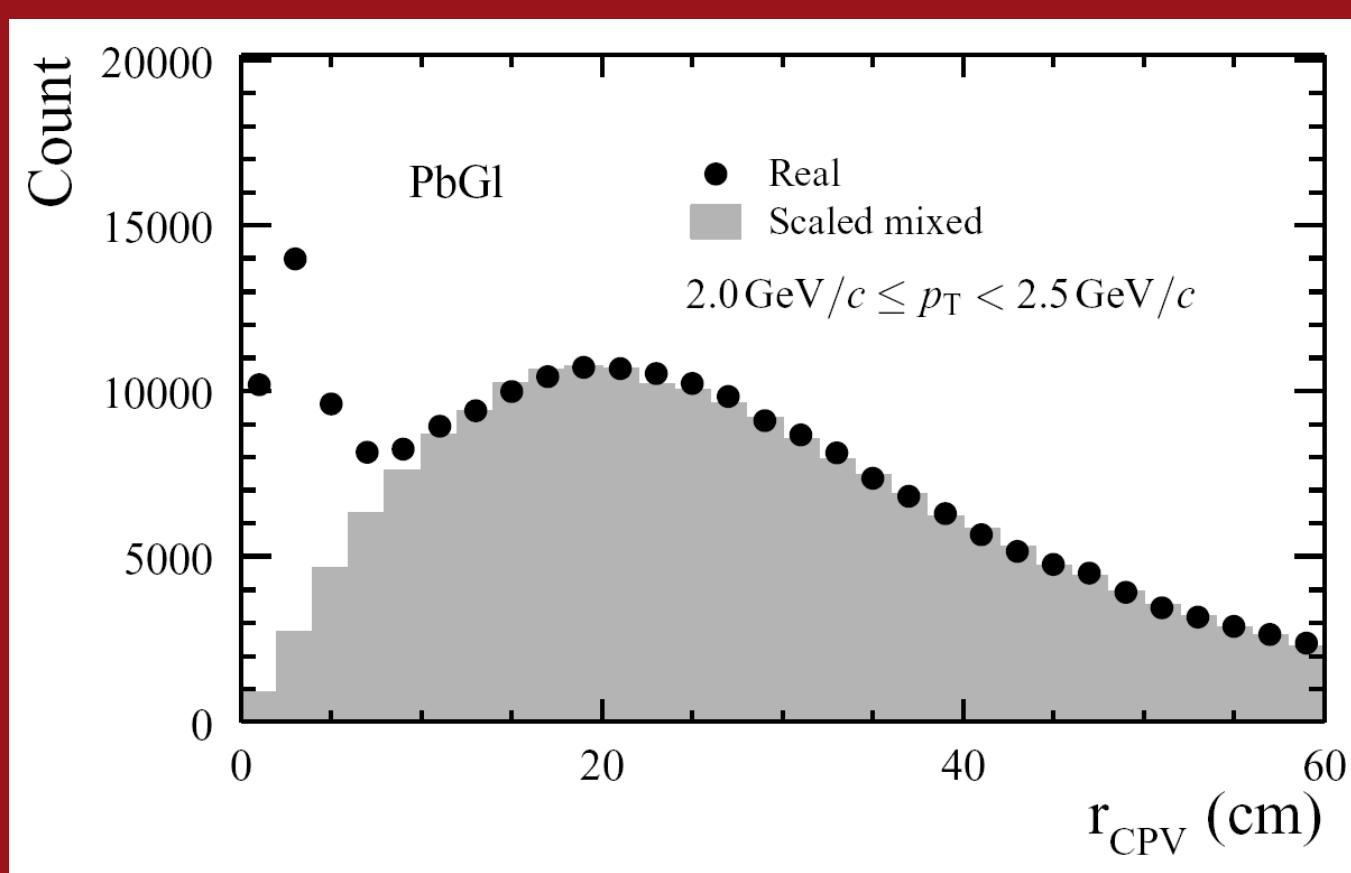
$$\frac{1}{2\pi p_{\text{T}} N_{\text{in}}} \left. \frac{d^2 N_{\gamma}}{dp_{\text{T}} dy} \right|_{\text{incl}} = \frac{1}{2\pi p_{\text{T}} N_{\text{in}}} \cdot \frac{(1 - X_{n\bar{n}}) \cdot (1 - X_{\text{ch}})}{\varepsilon_{\gamma} \cdot a_{\gamma} \cdot c_{\text{conv}}} \cdot \frac{\Delta N_{\text{cluster}}}{\Delta p_{\text{T}} \Delta y},$$

fraction of
charged clusters





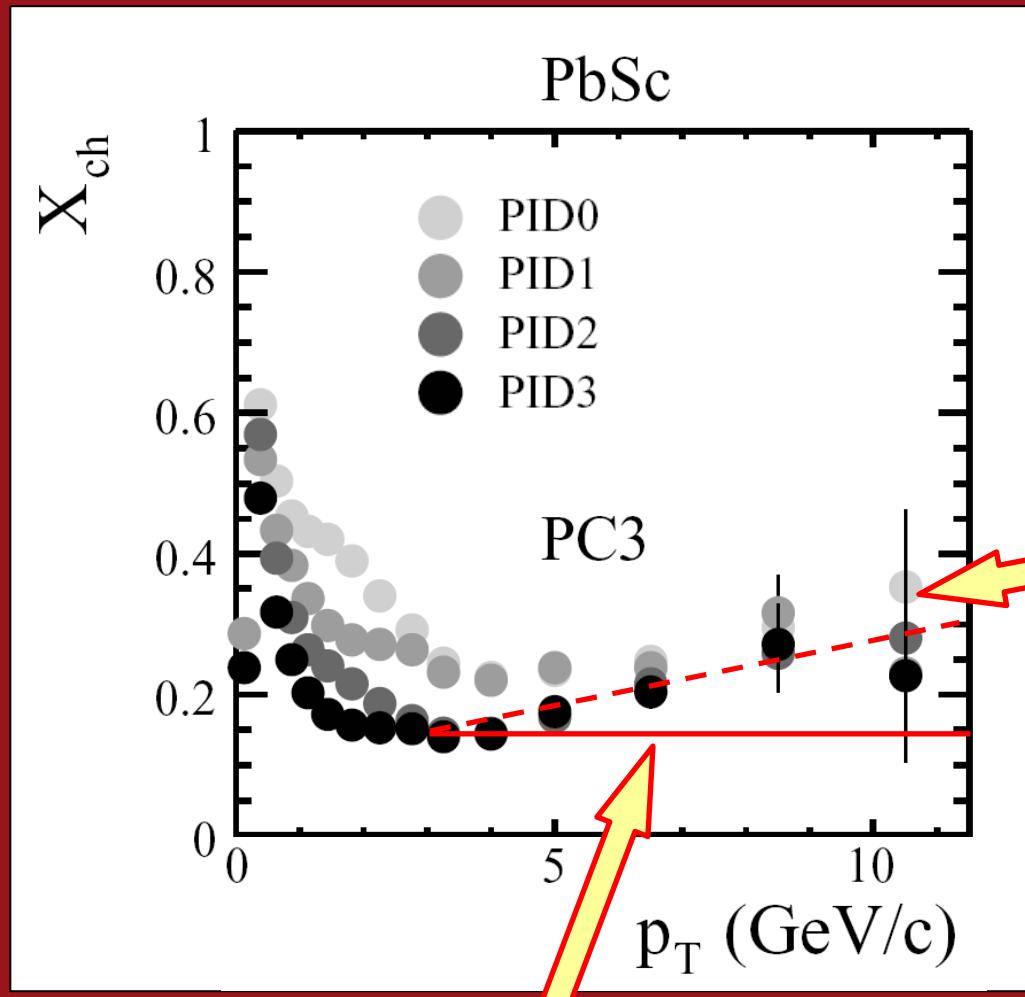
PC3 – EMCal Correlation



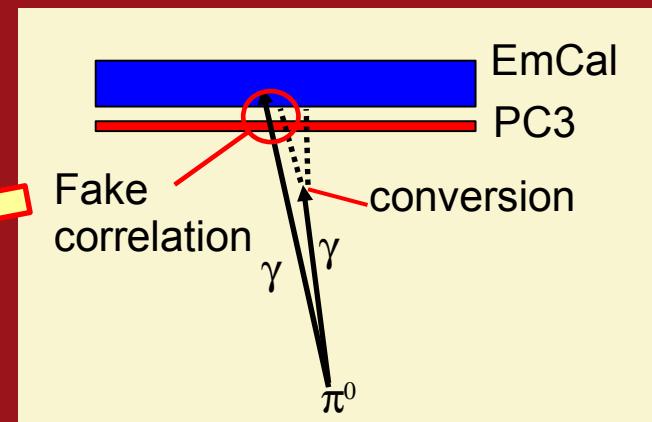
- r_{CPV} : distance to closest PC3 hit projection
- Random associations of PC3 and EMCal hits subtracted (event mixing)
- Background scaled to match real distribution at $r_{\text{CPV}} > 30$ cm



Charged Background: X_{ch}



- $X_{\text{ch}} > 0$ at high p_T largely due to photon conversion
- Artificial decay photon-PC3 correlations at high p_T :



- Verified with DC tracks
 - ✗ Closer to beam pipe
 - ✗ Less conversions
- MUST not be corrected: bias towards decay photons



Formula for Fully Corrected Inclusive Photon Spectra

fraction of
neutral background
(neutron, anti-neutrons)

$$\frac{1}{2\pi p_{\text{T}} N_{\text{in}}} \frac{d^2 N_{\gamma}}{dp_{\text{T}} dy} \Big|_{\text{incl}} = \frac{1}{2\pi p_{\text{T}} N_{\text{in}}} \cdot \frac{(1 - X_{n\bar{n}}) \cdot (1 - X_{\text{ch}})}{\varepsilon_{\gamma} \cdot a_{\gamma} \cdot c_{\text{conv}}} \cdot \frac{\Delta N_{\text{cluster}}}{\Delta p_{\text{T}} \Delta y},$$





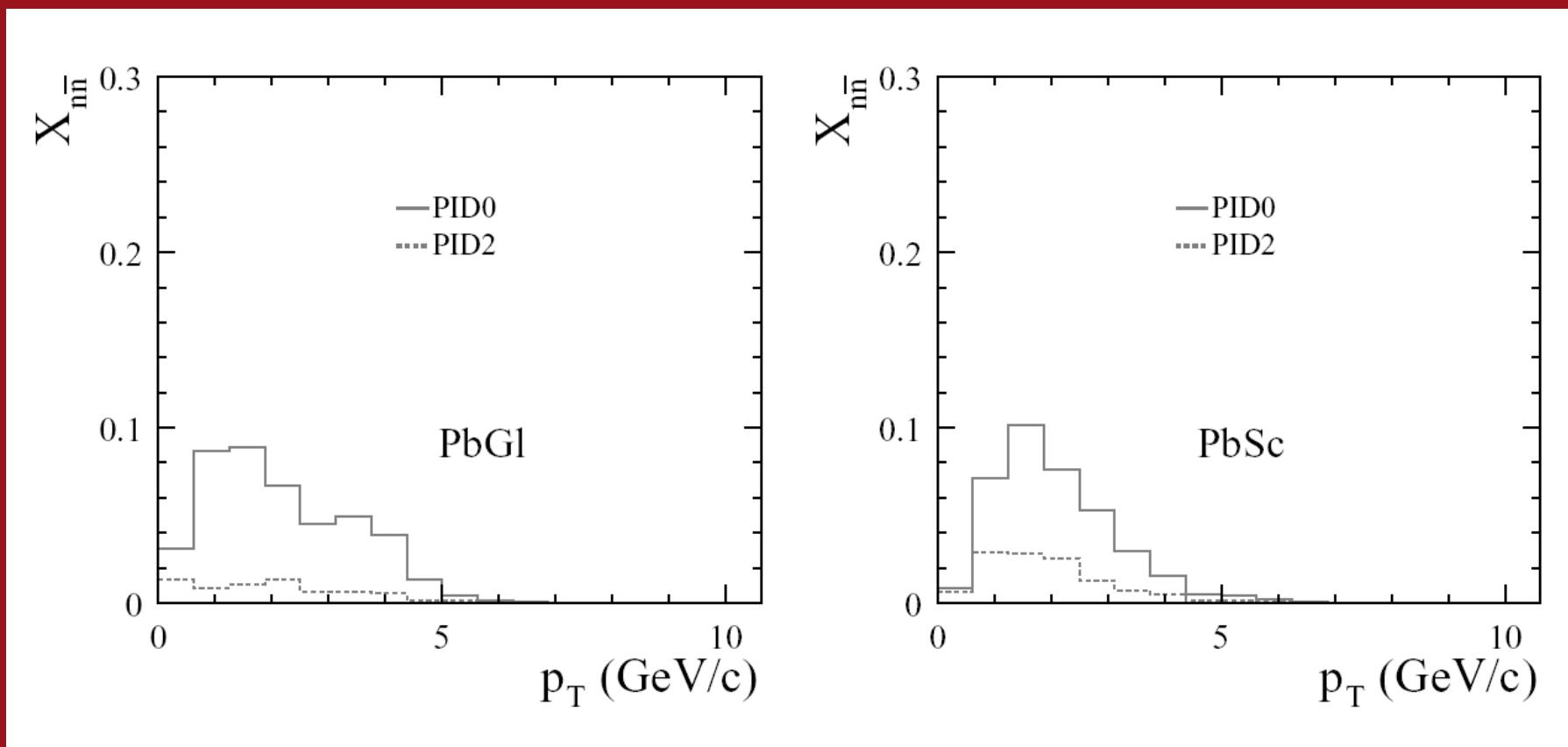
Neutral Background: X_{nn}

- **Background from neutrons and antineutrons needs to be simulated (PISA)**
- **Input neutron and anti-neutron spectra “determined” from measured proton and anti-proton spectra**

$$\begin{aligned}\left. \frac{d^2N}{dp_T dy} \right|_{\bar{n}} &= \left. \frac{d^2N}{dp_T dy} \right|_{\bar{p}}, \\ \left. \frac{d^2N}{dp_T dy} \right|_n &= \left. \frac{d^2N}{dp_T dy} \right|_{\bar{p}} + \left(\left. \frac{d^2N}{dp_T dy} \right|_p - \left. \frac{d^2N}{dp_T dy} \right|_{\bar{p}} \right) \frac{A-Z}{Z}\end{aligned}$$



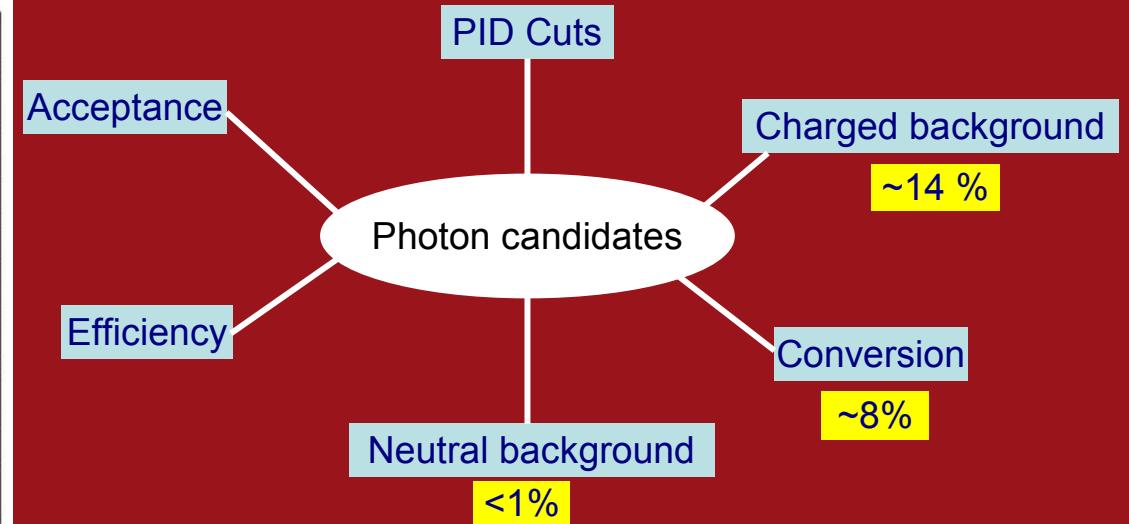
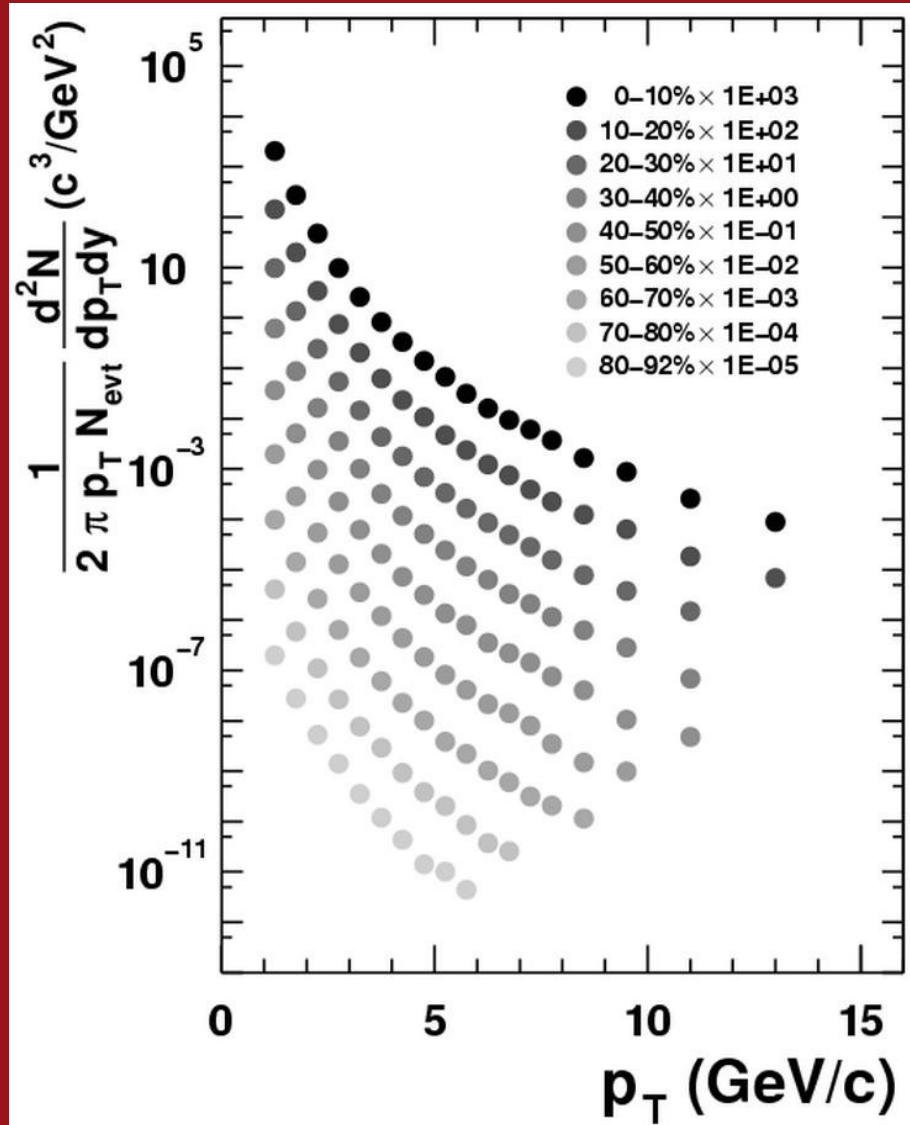
Simulation Results for X_{nn}



- Neutral background negligible after TOF and shower shape cut (PID2)



Inclusive Photons



- **Suffers from calorimeter resolution and background at low p_T**
 - ✗ Alternative approach via tracking of conversions ($\gamma \rightarrow e^+e^-$)
 - ✗ See talk by S. Bathe



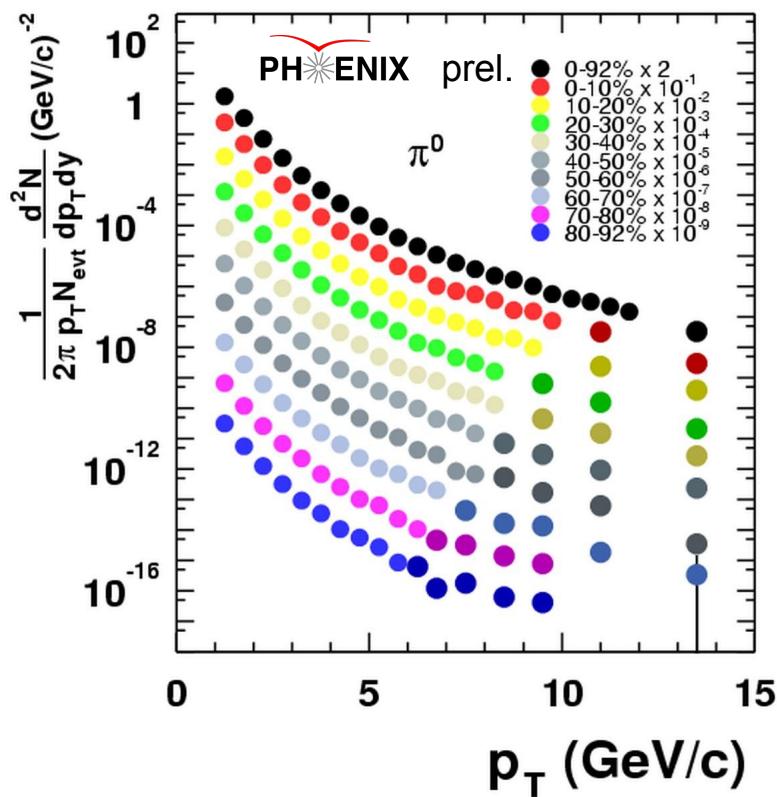
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π^0 and η @ PHENIX

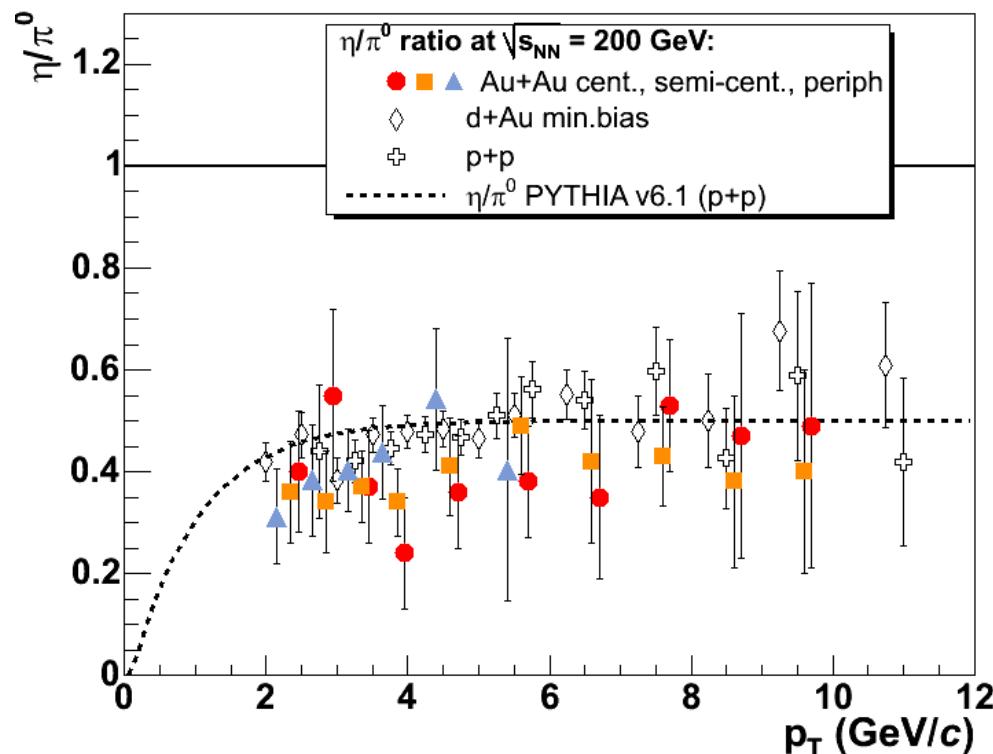
PRL 91,072301 (2003) + high p_T triggered data



- **Reconstructed via 2γ decay**
- **Same suppression pattern**
 - ✗ PRL 96 202301 (2006)
 - ✗ Factor 5 in central Au+Au
 - ✗ Reduced decay background for direct γ measurement



π^0 and η @ PHENIX



- Reconstructed via 2γ decay
- Same suppression pattern
 - ✗ PRL 96 202301 (2006)
 - ✗ Factor 5 in central Au+Au
 - ✗ Reduced decay background for direct γ measurement
- m_T -scaling works for η

$$E \frac{d^3 \sigma_h}{dp^3} = C_h f(m_T)$$

- ✗ $C_\eta \sim 0.45$ for all species (p+p, d+Au, Au+Au) and centralities

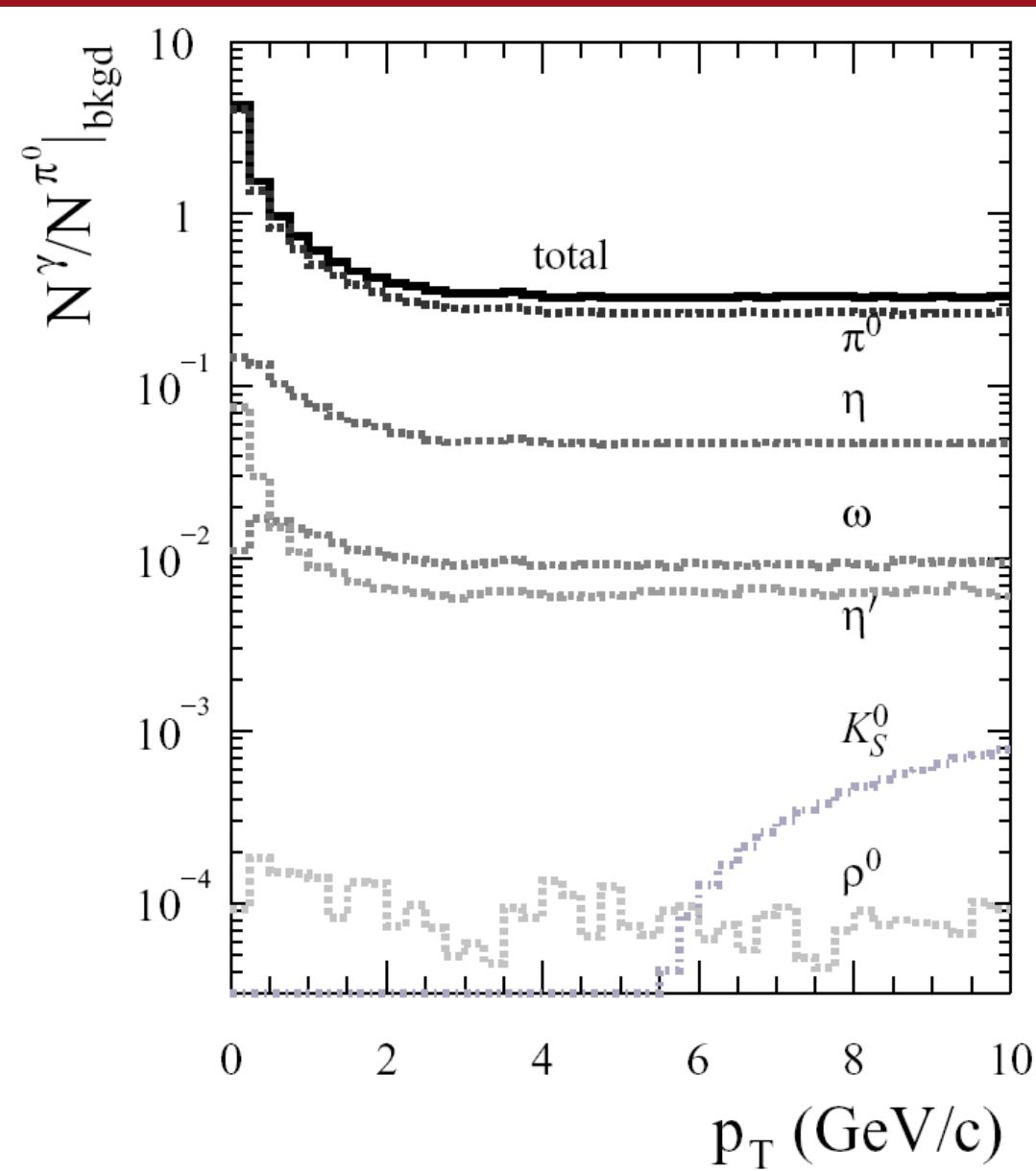


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Decay Photon Background



- Reference to compare:

$$R = \frac{\gamma_{meas}}{\gamma_{bkgd}} = \frac{(\gamma/\pi^0)_{meas}}{(\gamma/\pi^0)_{bkgd}}$$

- ~96% background γ from π^0 and η (measured)

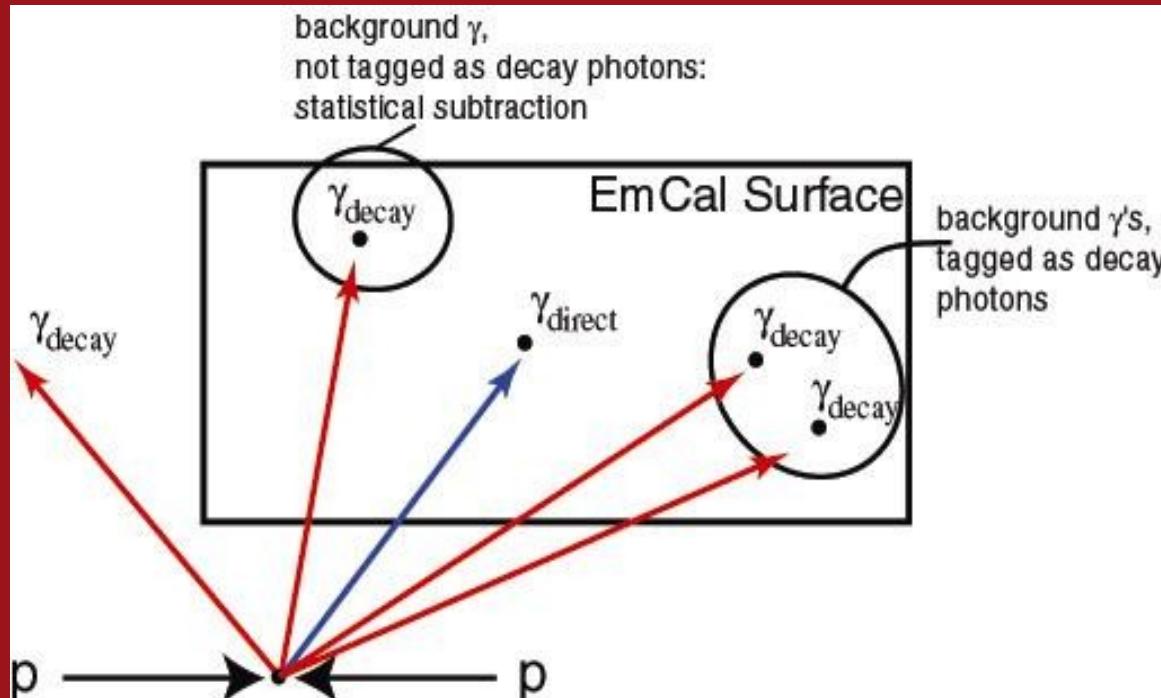
- Pocket formula:

$$\frac{1}{p_T} \frac{dN^{\pi^0}}{dp_T} \propto 1/p_T^n$$
$$\rightarrow \frac{\gamma_{\pi^0}^{decay}}{\pi^0} = \frac{2}{n-1} \approx 0.29$$



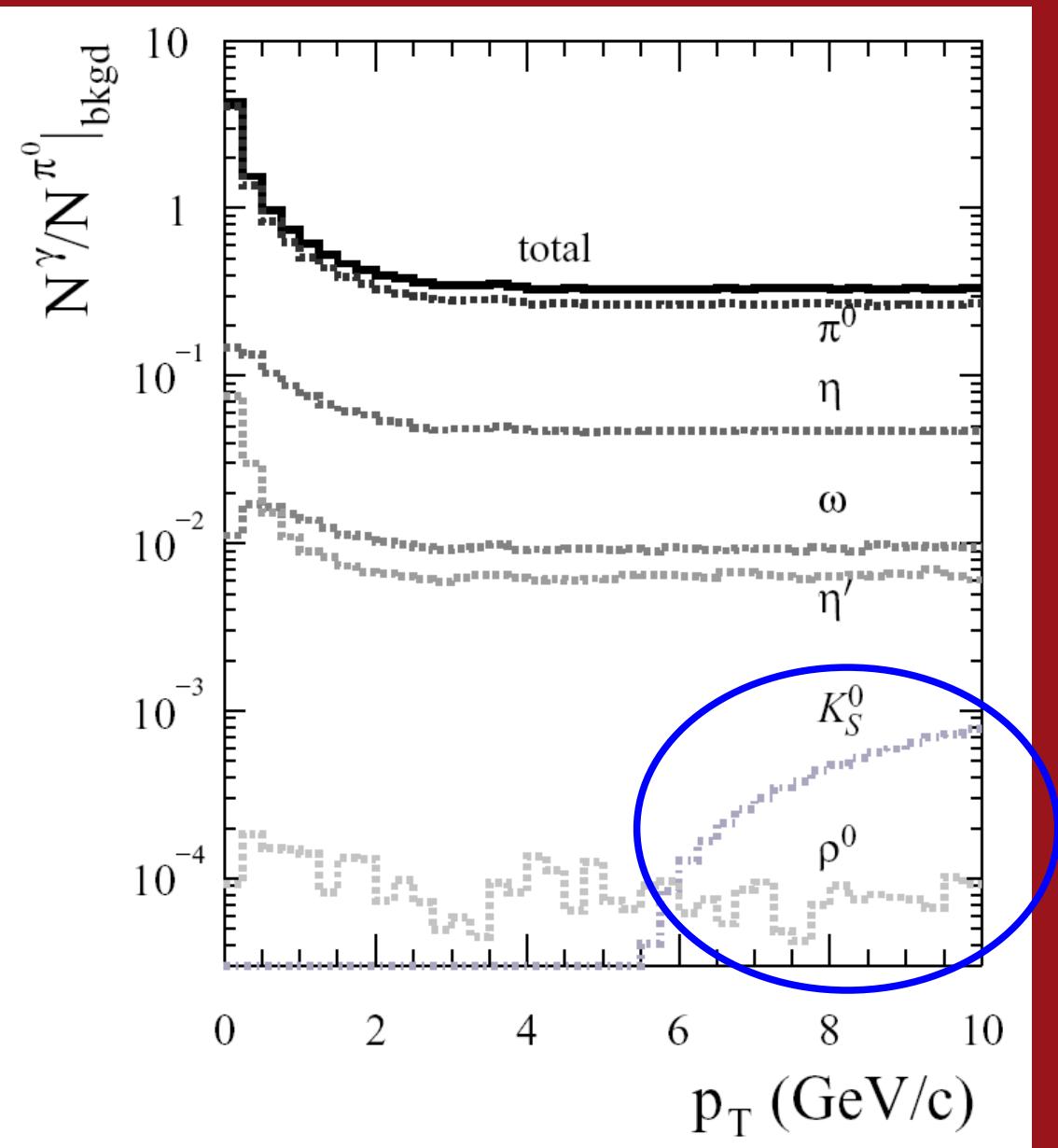
Side-Remark: π^0 and η tagging

- In low multiplicity environments the S/B ratio can be improved by accepting only those photons as direct photon candidates that don't form an inv. mass in the π^0 or η range (needs to be done in MC and real events)
- In central A+A collisions the number of random associations is too high for this approach





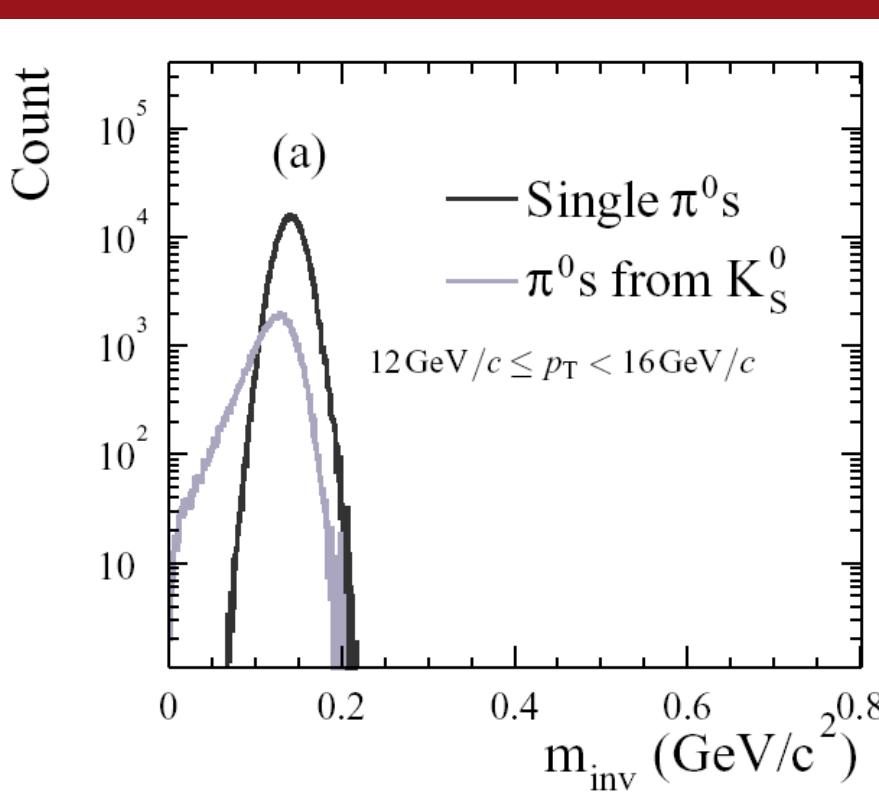
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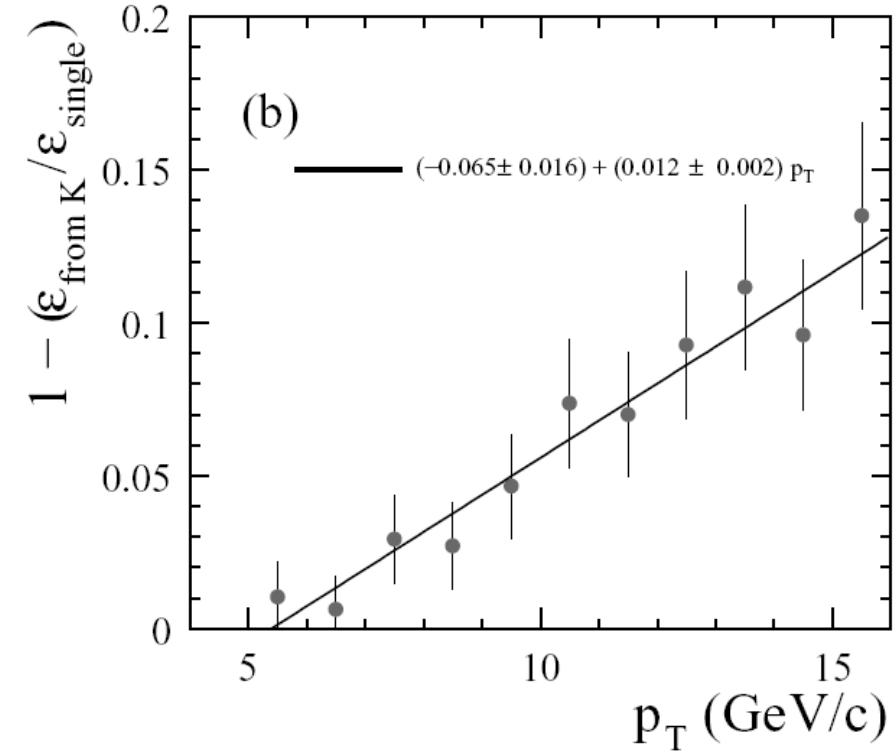
- ~96% background γ from π^0 and η (measured)
 - ✗ π^0 also includes $\eta \rightarrow (\pi^0\pi^0)$
- Other hadrons via m_T -scaled π^0 spectra
- Monte Carlo based on JETSET
 - ✗ $\pi^0 \rightarrow \gamma\gamma, e^+e^-\gamma$
 - ✗ $\eta \rightarrow \gamma\gamma, \pi^+\pi^-\gamma$
 - ✗ $\omega \rightarrow \pi^0\gamma \dots$
 - ✗ $\eta' \rightarrow \rho^0\gamma \dots$
 - ✗ $K_S^0 \rightarrow (\pi^0\pi^0)$



Background Photons from K_s^0



Probability to miss a π^0 from $K_s^0 \rightarrow \pi^0 + \pi^0$
in the π^0 reconstruction due to displaced decay vertex



$$K_s^0: c\tau_0 = 2.67 \text{ cm}$$

$$L_{Lab} = \beta\gamma c\tau_0$$

$$\beta\gamma = \frac{p}{m_0 c}$$

p	1 GeV/c	5 GeV/c	10 GeV/c
$\langle L_{Lab} \rangle$	5,37 cm	26,9 cm	53,7 cm

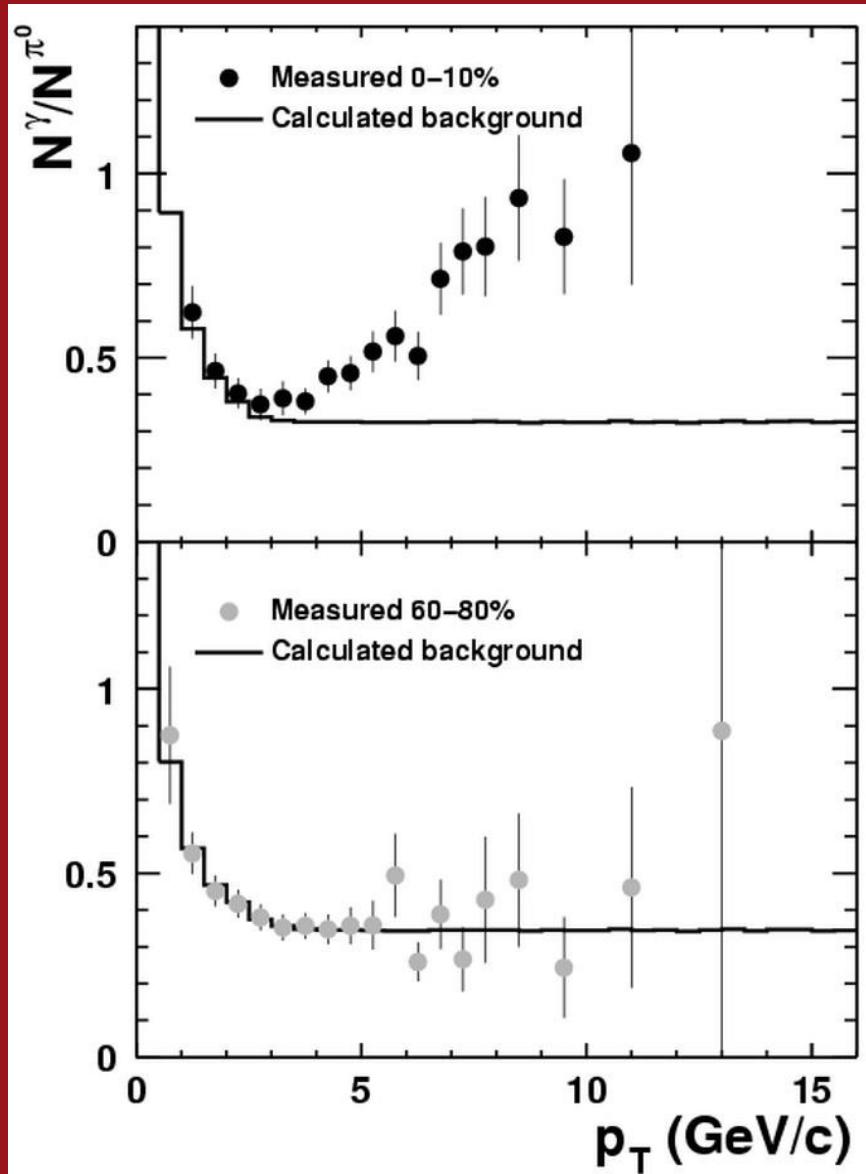


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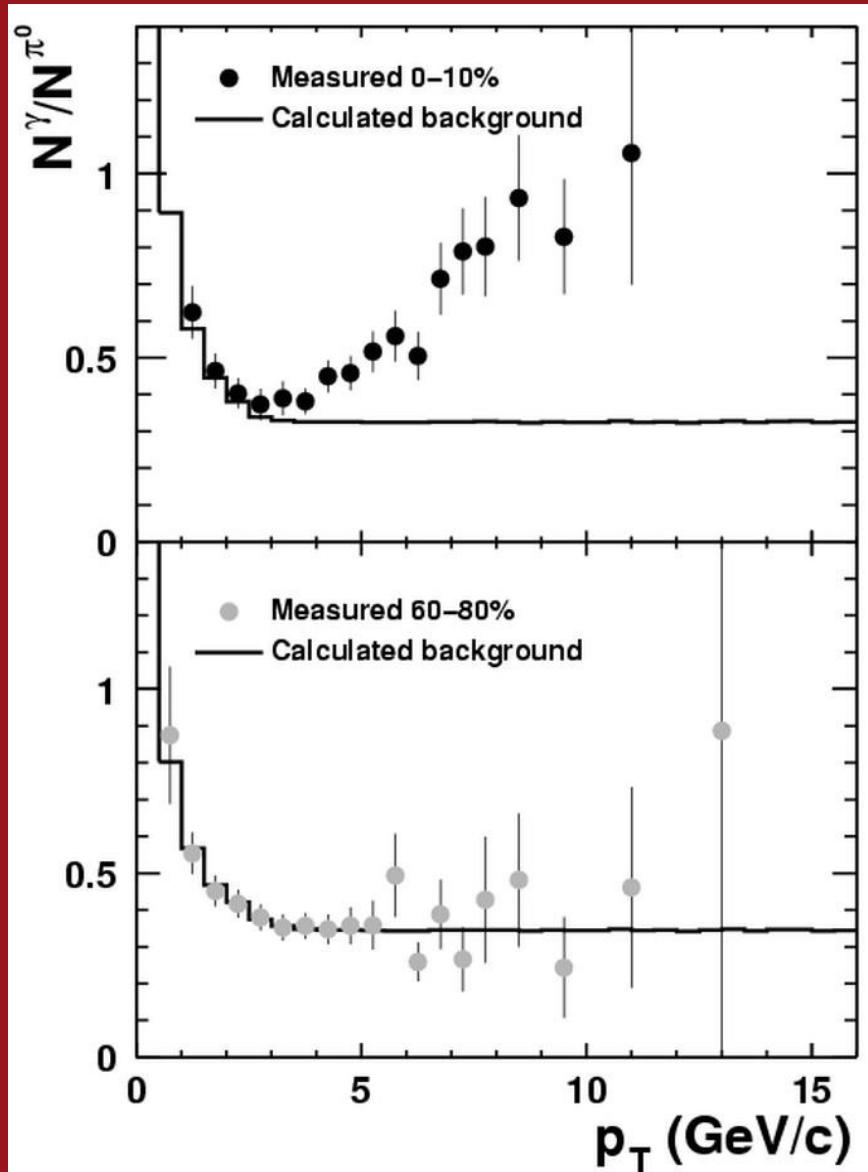


Direct Photon Signal





Direct Photon Signal



- Double ratio R gives significance of the signal

$$\frac{(\gamma/\pi^0)_{meas}}{(\gamma/\pi^0)_{decay}} = \frac{\gamma_{meas}}{\gamma_{decay}}$$

- Many systematics cancel
 - ✗ Energy scale
 - ✗ Photon efficiency and acceptance
 - ✗ Photon conversion



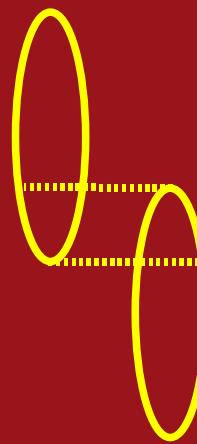
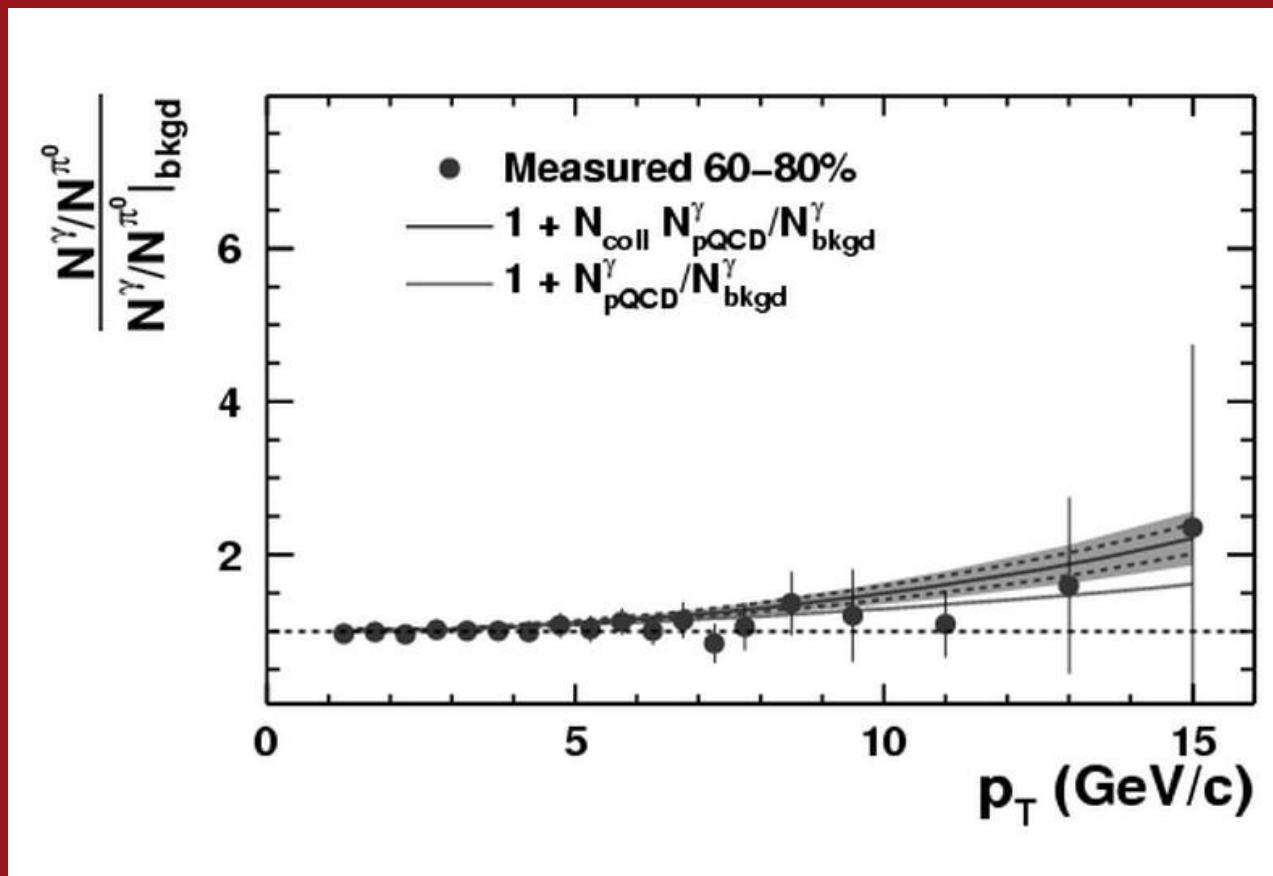
Uncertainties in PHENIX-Run2 Au+Au

π^0 error source	PbGl		PbSc	
	3.25 GeV/c	8.5 GeV/c	3.25 GeV/c	8.5 GeV/c
Yield extraction	8.7%	7%	9.8%	7.2%
Yield correction	12%	12%	12%	13.3%
Energy scale	13.8%	14.1%	10.5%	11.4%
Total systematic	20.3%	19.5%	18.8%	19%
Statistical	10.6%	32.5%	3%	13.1%
γ error source				
Non- γ correction	2.4%	2.4%	Treating photon and π^0 measurements as independent would yield a 28% systematic uncertainty for γ/π^0	
Yield correction	10.2%	12.0%		
Energy scale	15.7%	13.7%		
Total systematic	18.9%	18.4%	16.5%	16.7%
Statistical	1.2%	14.1%	0.7%	7.9%
γ/π^0 syst.	10.4%	10.4%	10.6%	10.6%
γ/π^0 stat.	10.7%	37.7%	3%	16.5%

PRL 94 (2005) 232301

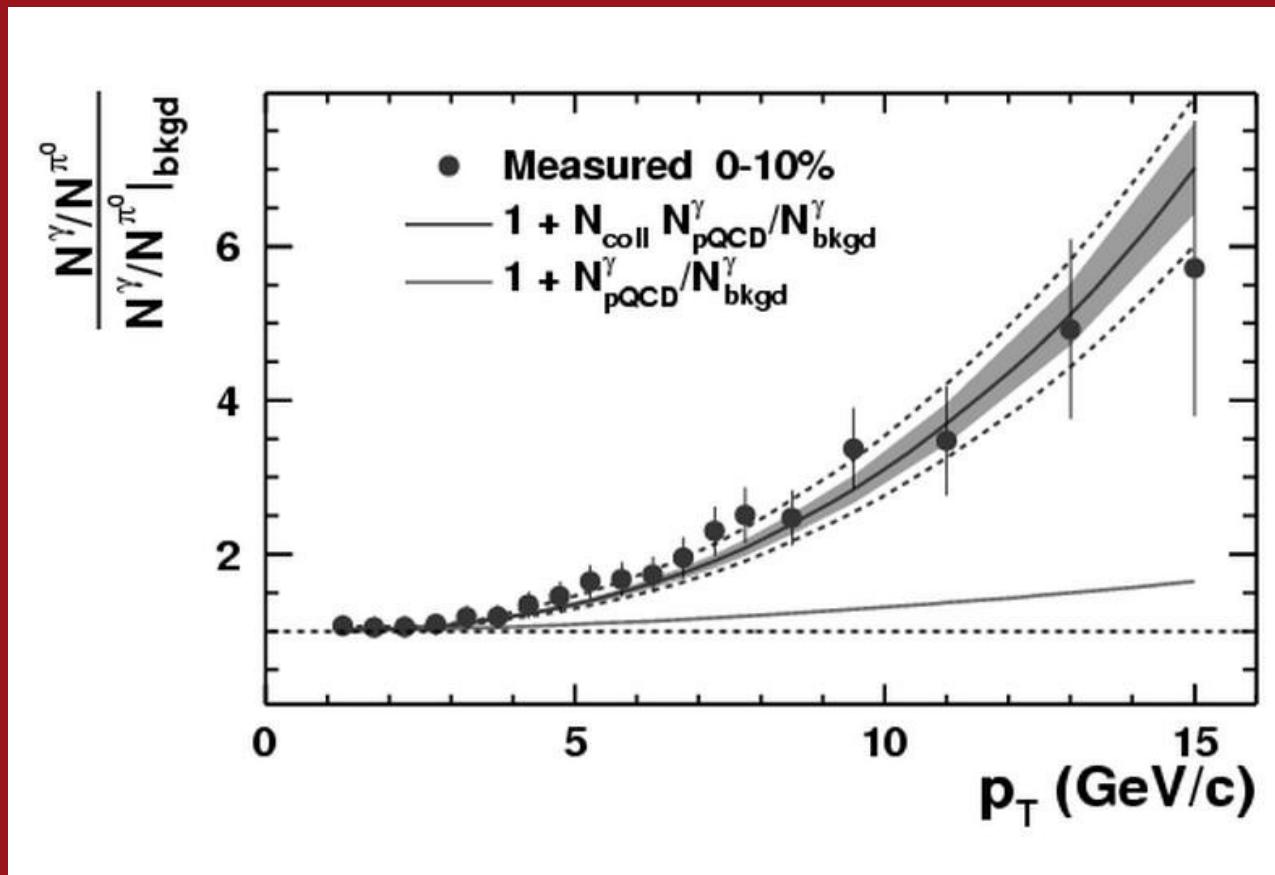


$\gamma_{\text{meas}}/\gamma_{\text{incl}}$





$\gamma_{\text{meas}}/\gamma_{\text{incl}}$



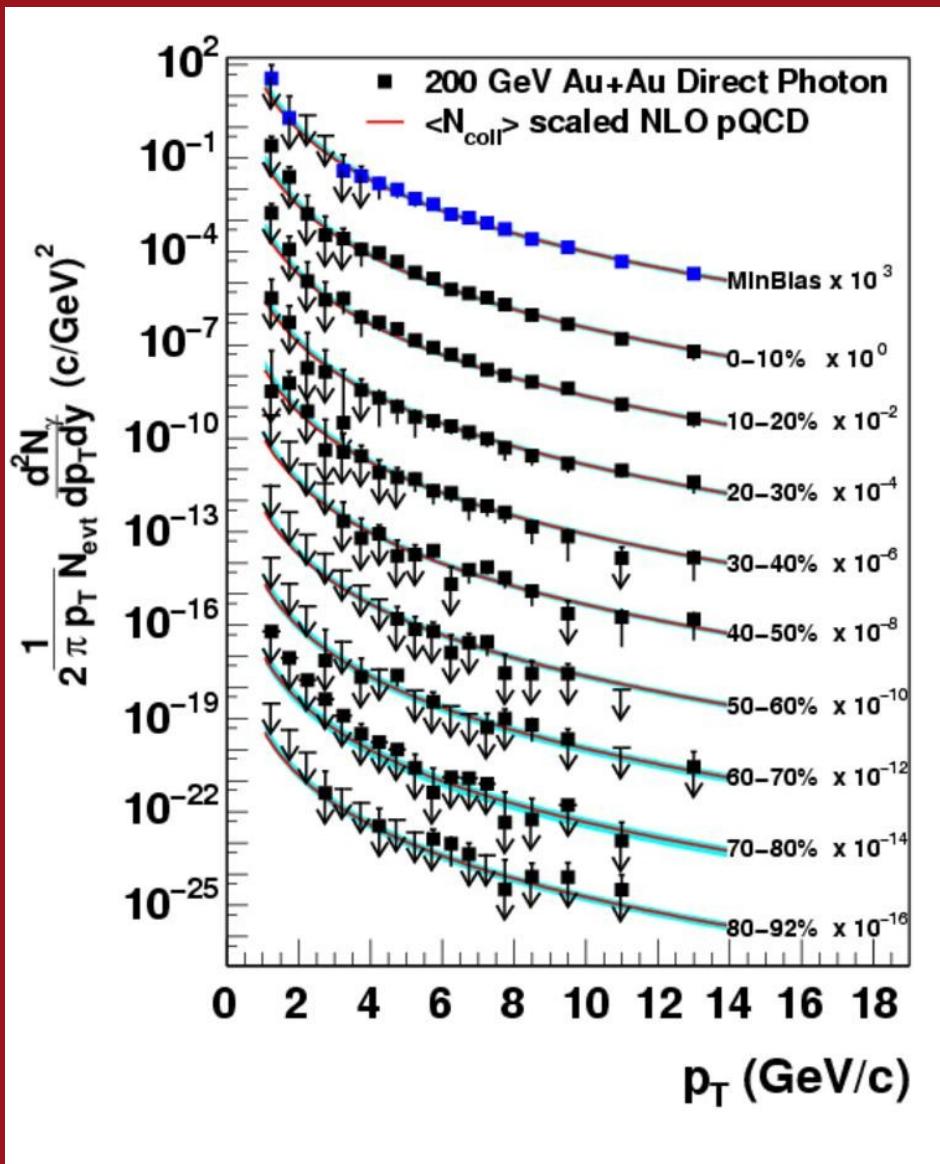


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- Extract direct photon signal
- Finally:
Subtract decay background from inclusive photon spectrum



Direct Photon Spectra



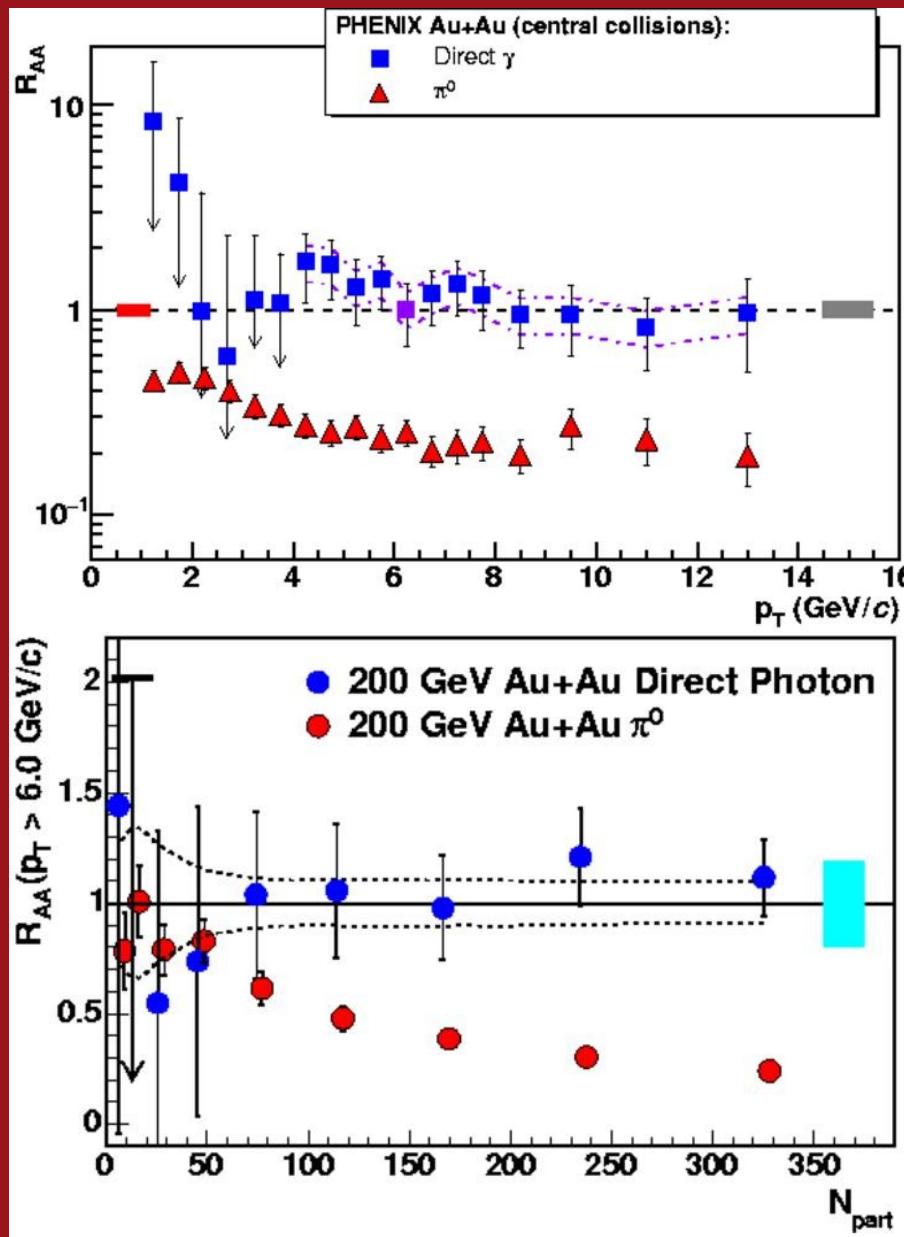
- Direct photon yield

$$\frac{d^2 N}{dp_T dy_{\text{direct}}} = \left(1 - \frac{\gamma_{\text{decay}}}{\gamma_{\text{meas}}} \right) \frac{d^2 N}{dp_T dy_{\text{incl}}}$$

- Consistent with scaled p+p calculation



R_{AA} for direct γ vs. π^0



- R_{AA} for direct photons

- ✗ Comparison on linear scale

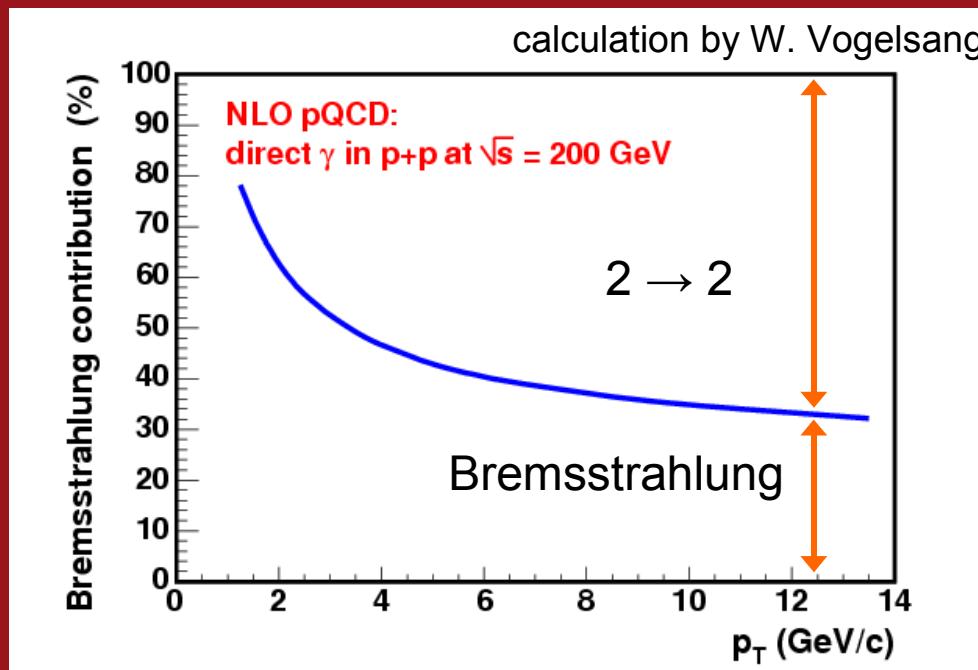
$$R_{AA} = \frac{d^2 N_{AA}/dydp_T}{T_{AA} d\sigma_{pp}/dydp_T}$$

- Direct photons are not suppressed

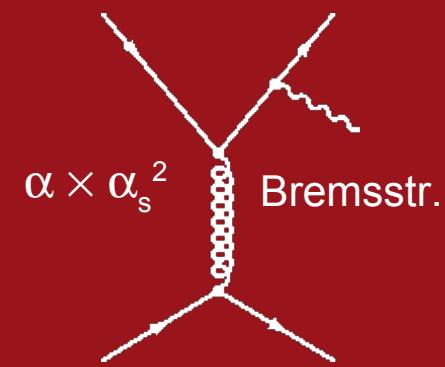
- ✗ Initial state **not** responsible for π^0 deficit
 - ✗ $\frac{d^2 \sigma}{dp_T dy} = \int \text{PDF} \times \text{pQCD} \times \text{FF}(E \rightarrow E')$



But...



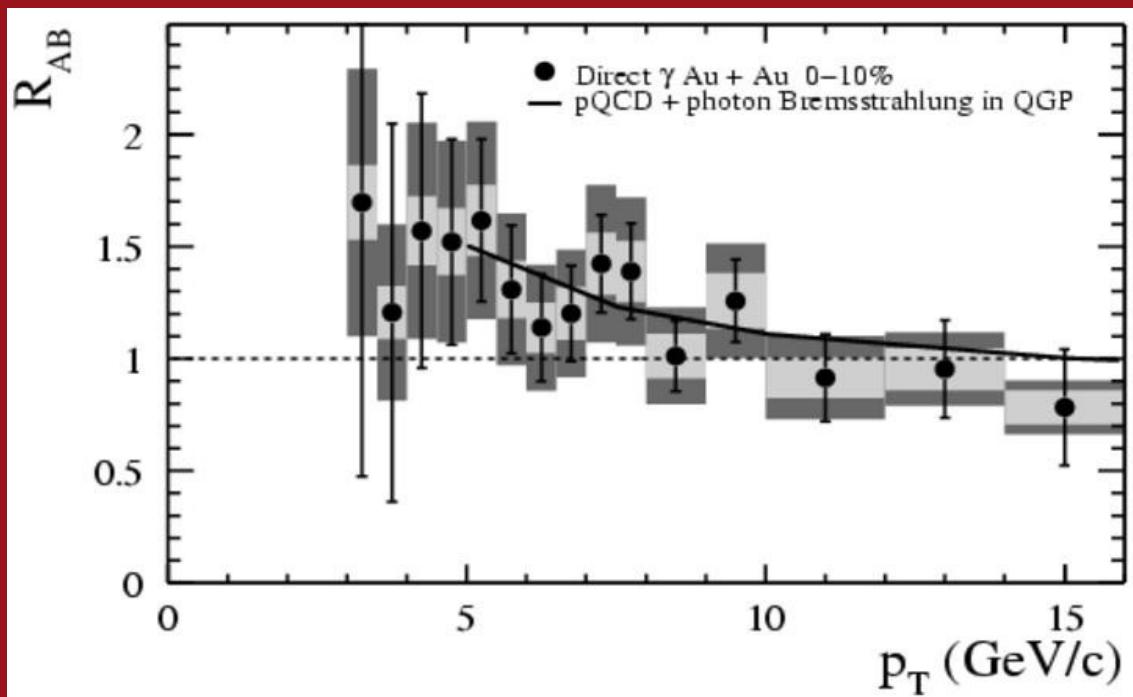
- ... Shouldn't we see some suppression:



- Consider also multiple scattering and gluon/photon formation time



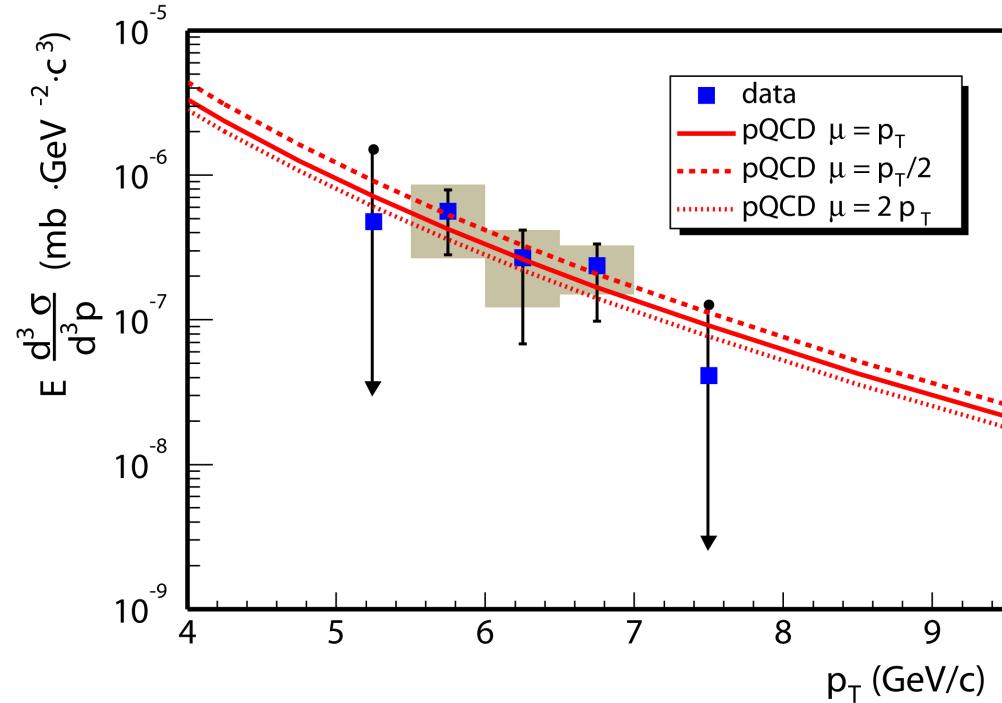
Bremsstrahlung of hard scattered Quarks



- Including multiple scattering and energy loss
 - Zakharov JETP Lett. 80 (2004)
- Only pQCD reference, need p+p
- d+Au for nuclear effects



Direct Photons Run02 p+p

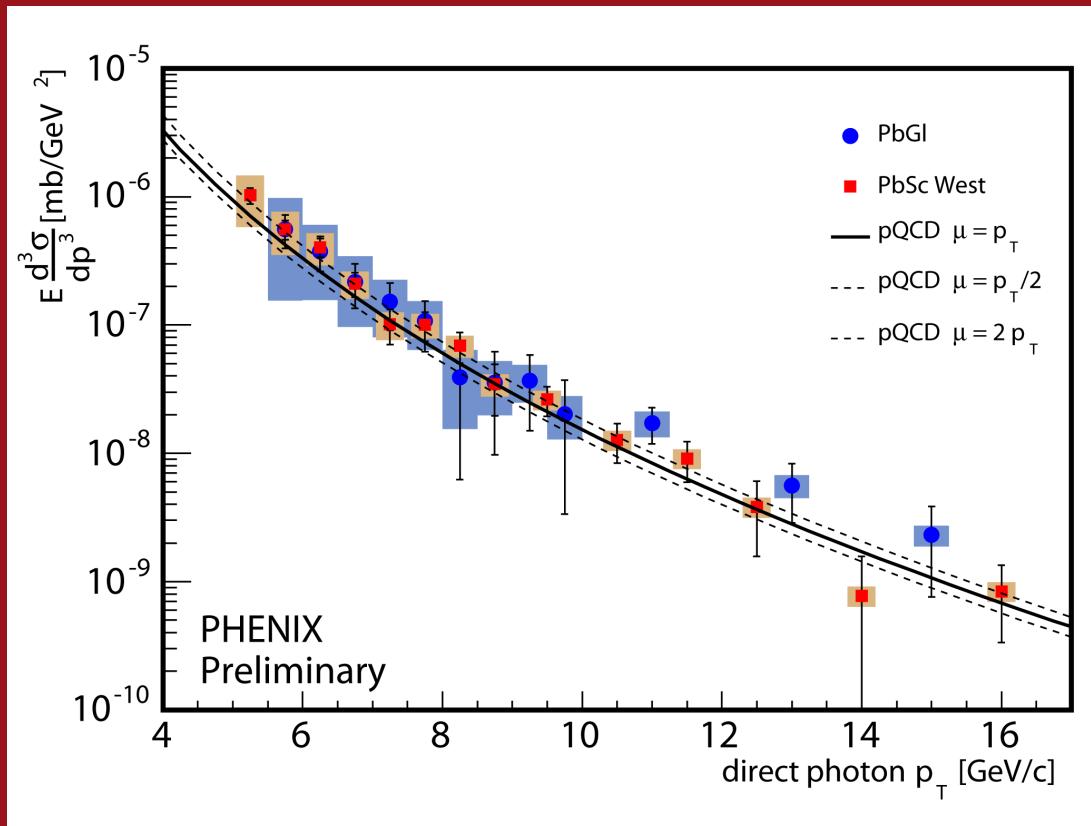


- **Cocktail subtraction with tagging**
 - × 900 M Events $\sim 41 \text{ nb}^{-1}$
- **Only three significant points**
- **Confirmation of pQCD**

Phys. Rev. D71, 071102 (2005)



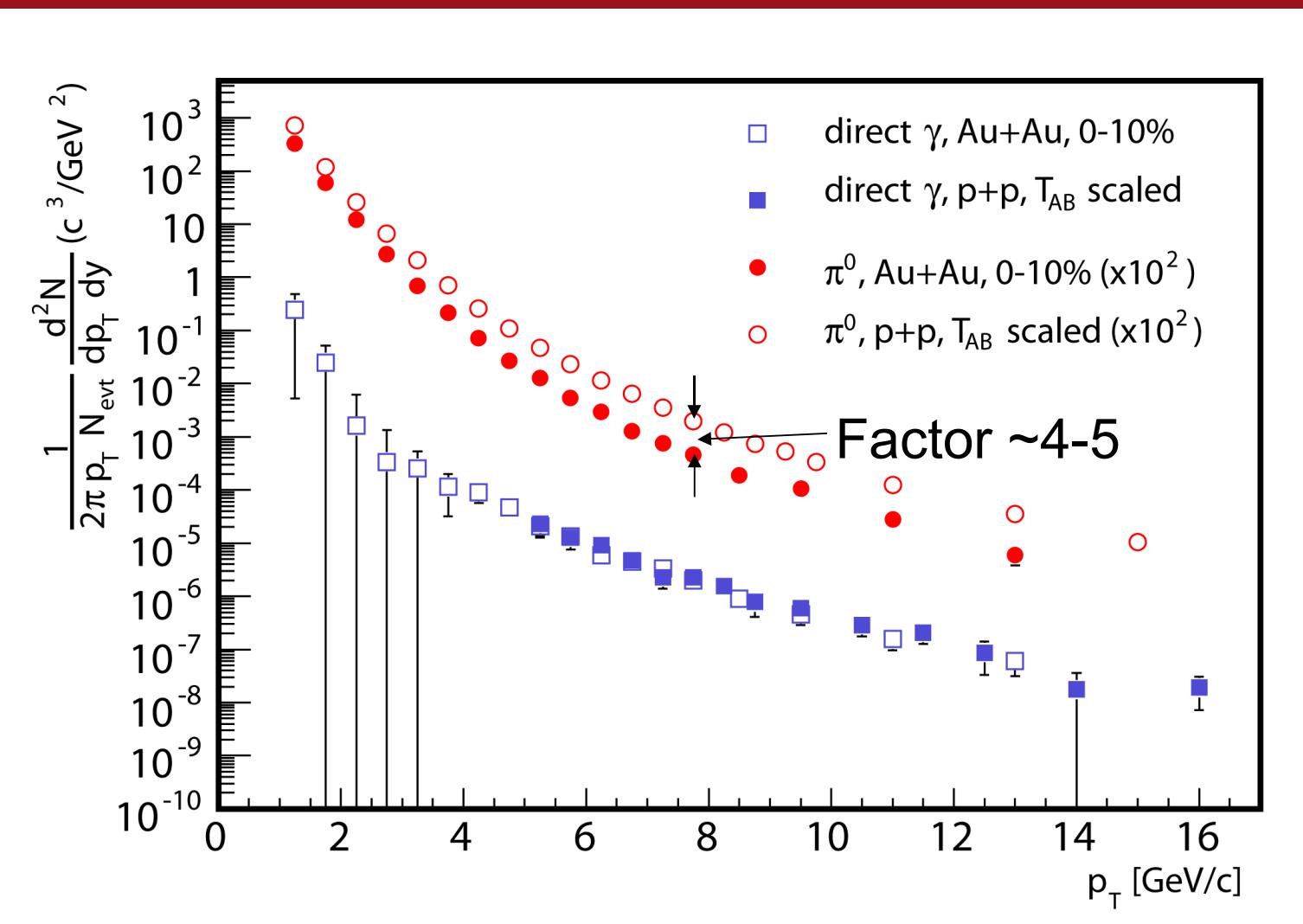
Direct Photons Run03 p+p



- **Cocktail subtraction**
 - × $10^* \text{Run02} \sim 0.35 \text{ pb}^{-1}$
- **Two independent analyses**
- **Very good agreement with pQCD**



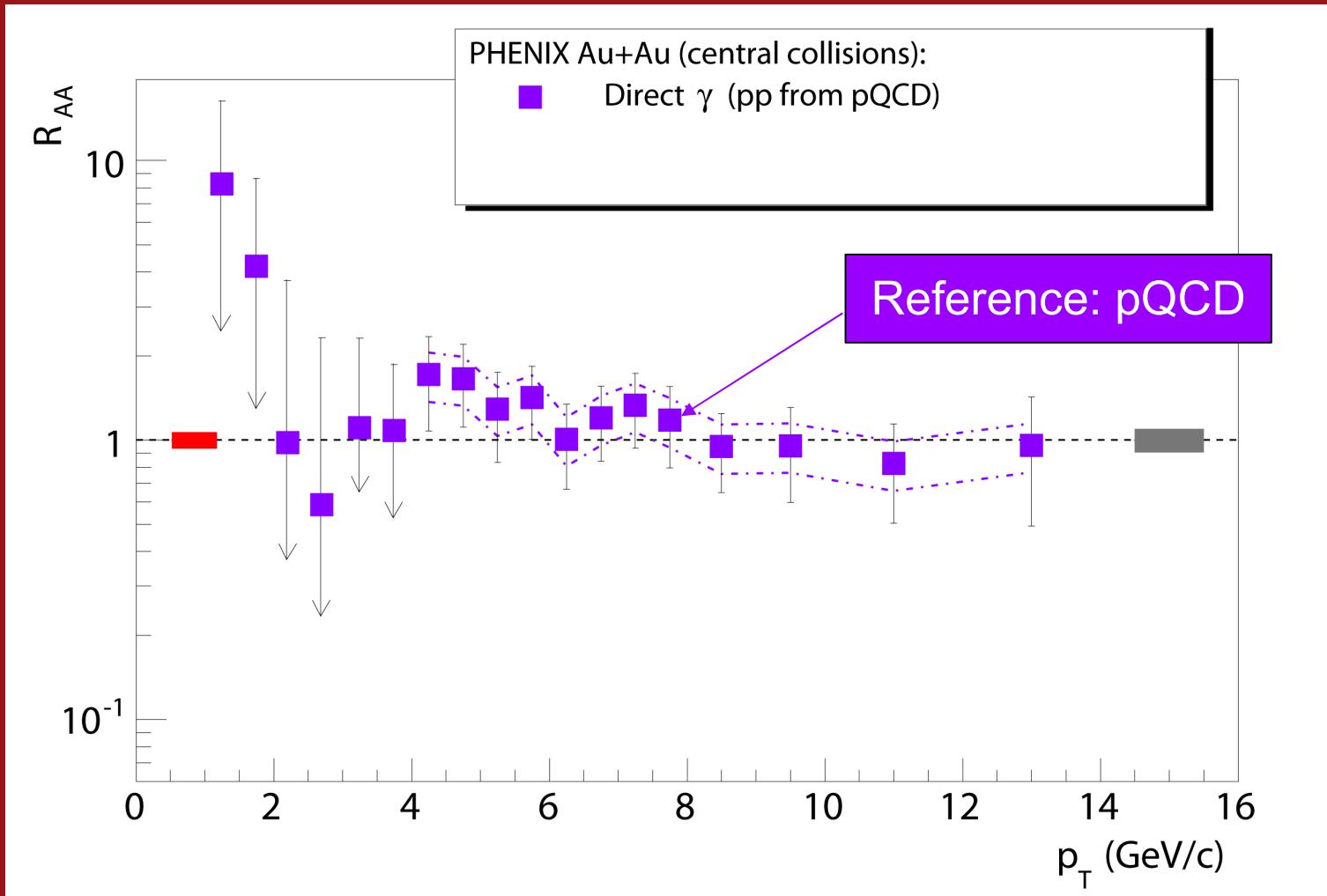
Spectra in p+p vs. Au+Au



T_{AB} -scaling works perfect also with measured direct γ

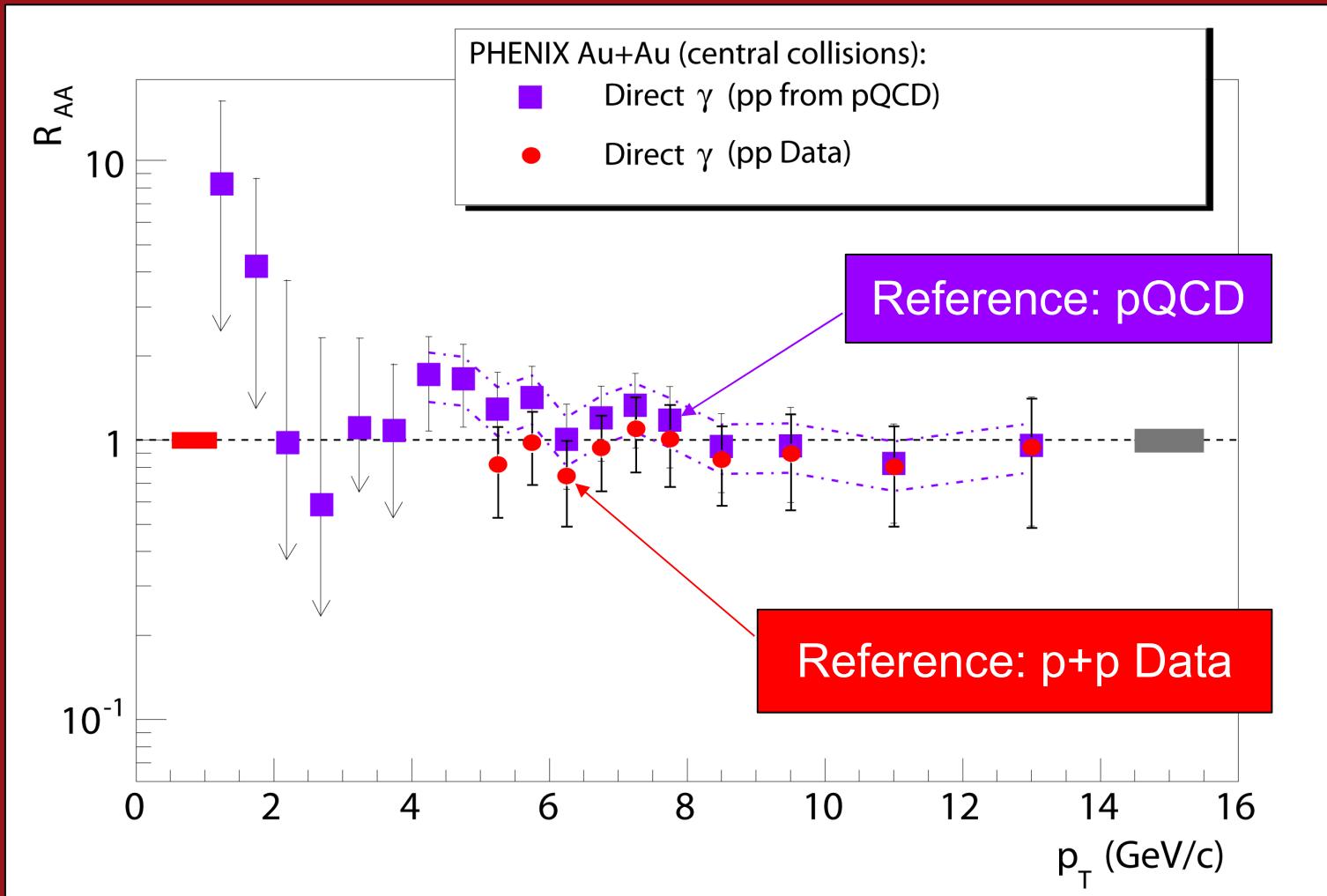


Direct Photon R_{AA}



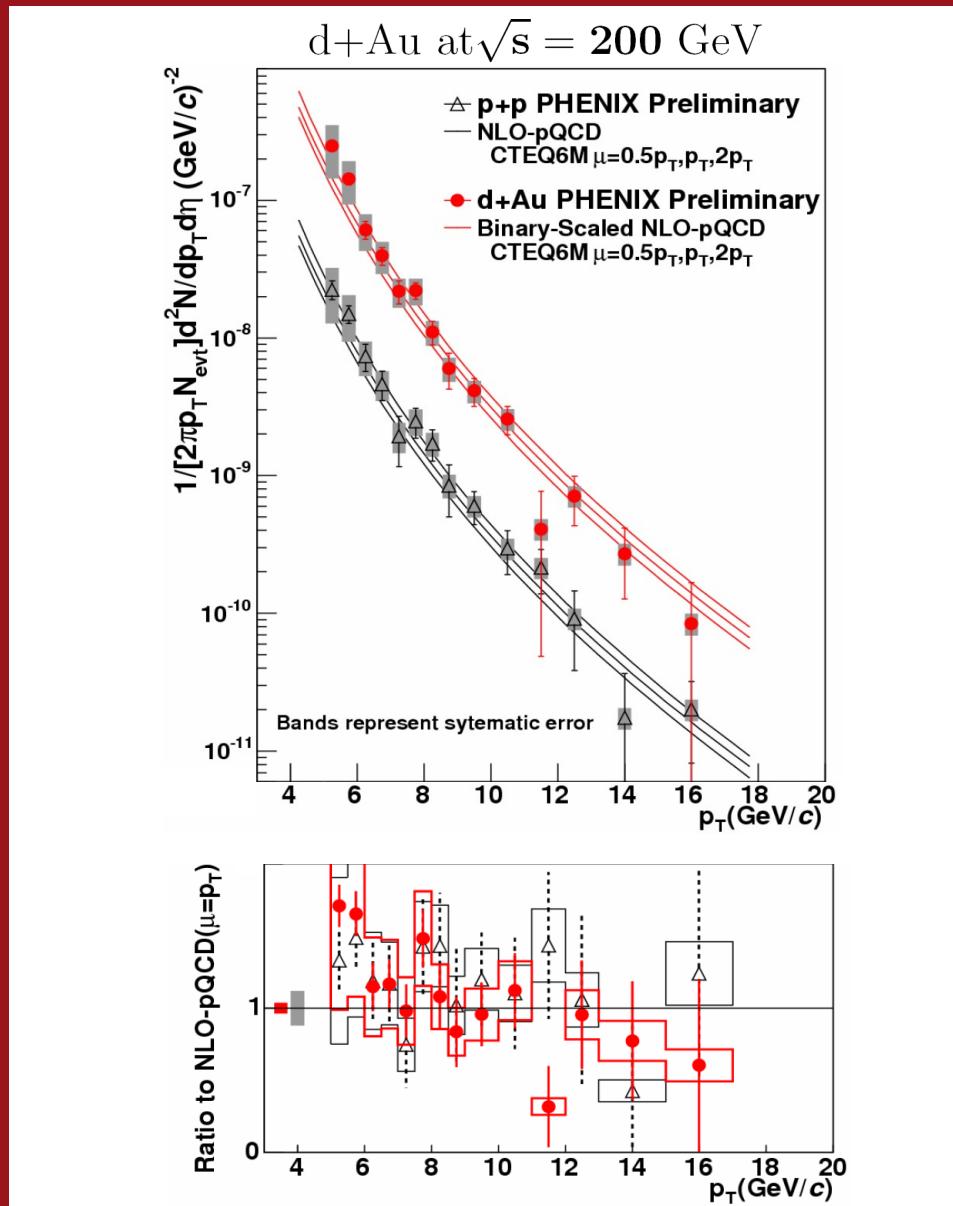


Direct Photon R_{AA}

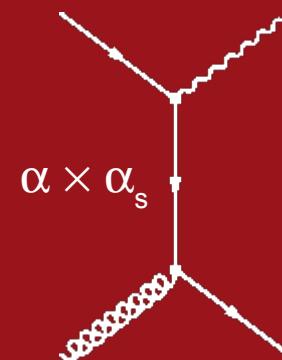




Nuclear Effects in d+Au?



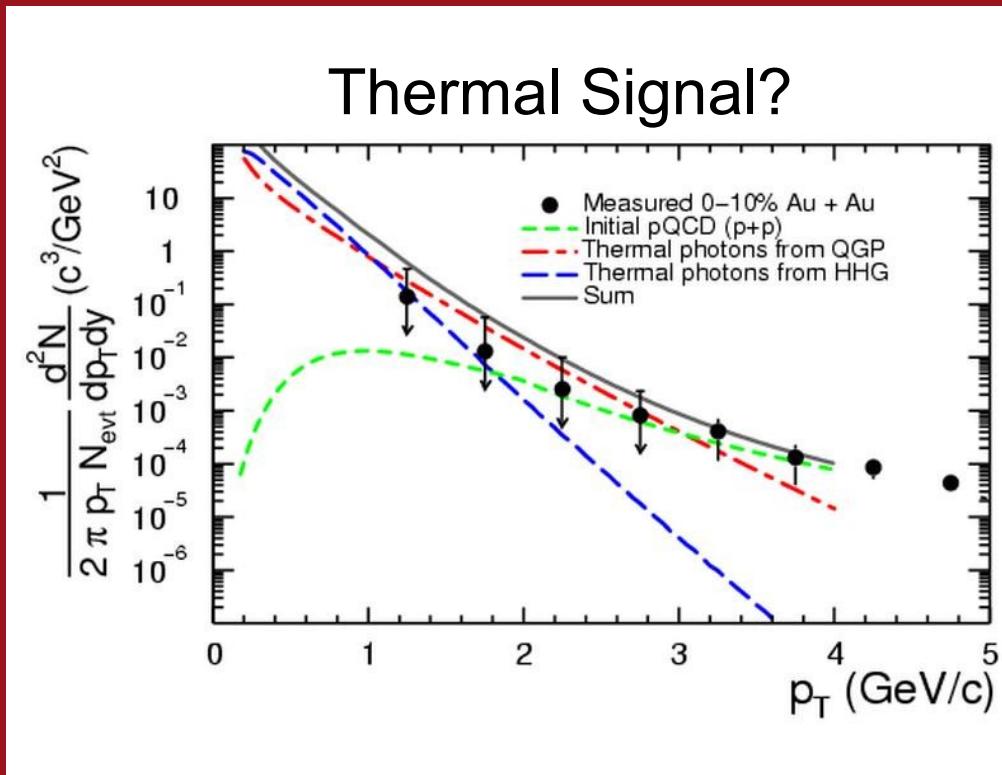
- Directly sensitiv to gluon PDF (CGC?)



- No effect at high p_T
- Similar to high $p_T \pi^0$



What we missed in this talk?



- **Many interesting effects at lower p_T**
- **Need refined methods**
 - ✗ Conversions (internal and external)
 - ✗ HBT correlation strength
 - ✗ Reaction plane dependence
- **See S. Bathe's talk**

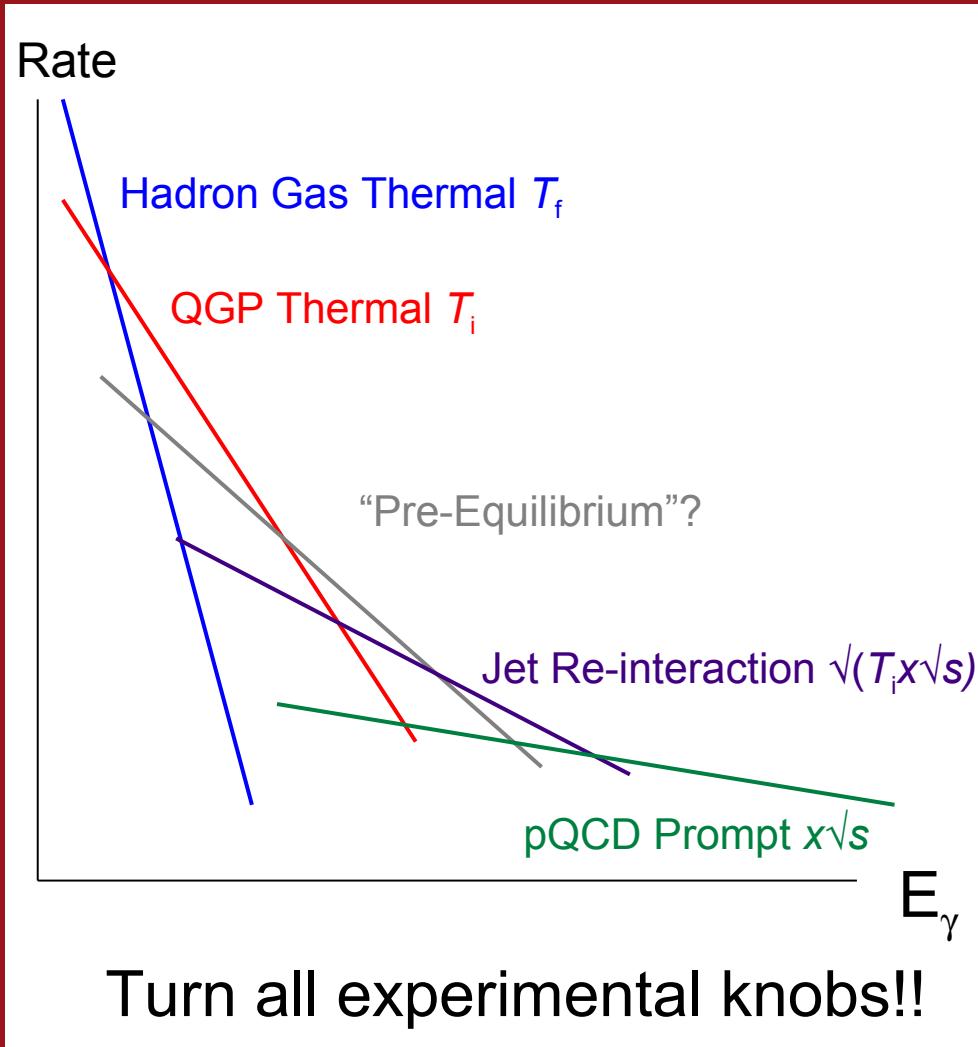


Summary

- **No suppression of direct photons at high p_T in central Au+Au reactions at PHENIX/RHIC**
 - ✗ Direct control for hard scattering and strong energy loss of partons
- **First measurement of direct photons in p+p nearly 30 years ago, in HIC only 6 years (WA98)**
 - ✗ At the moment only the very high p_T part (a.k.a the scaled p+p part) is theoretically under control/understood!!
 - ✗ Again 30 years needed?



30 years needed? No!



- A wealth of data available and analyzed right now!
 - ✗ with new methods
 - ✗ Au+Au (x10 Run02)
 - ✗ p+p (x100 Run03)
 - ✗ Cu+Cu
 - ✗ 22 GeV, 62 GeV, 200 GeV
 - ✗ ...
- And will be coming with
 - ✗ LHC
 - ✗ RHIC upgrades



Westfälische
Wilhelms-Universität
Münster

Thanks



Isolation Cut in PHENIX

- **What fraction of direct photons is isolated?**

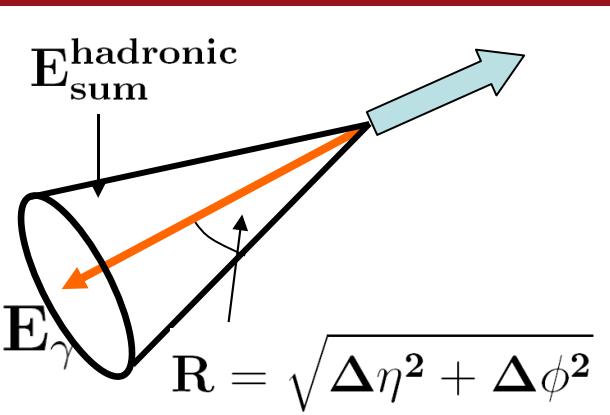
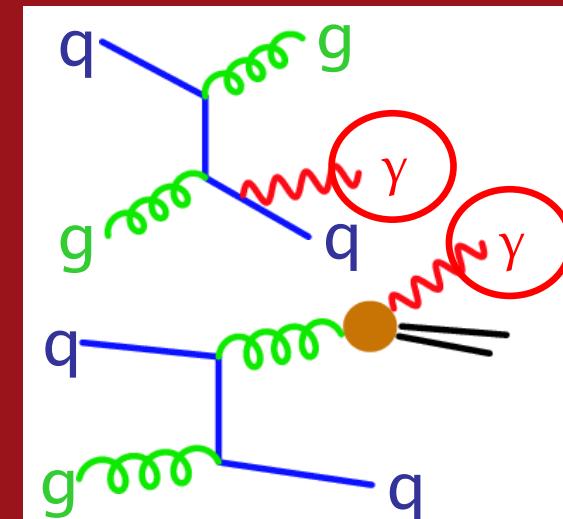
$$E_{\gamma}^{\text{hadronic}}(R < 0.5 \text{ rad}) < 0.1 \times E_{\gamma}$$

- ✗ Isolation cut should remove Bremsstrahlung

- **Difficult to estimate efficiency of isolation cut:**

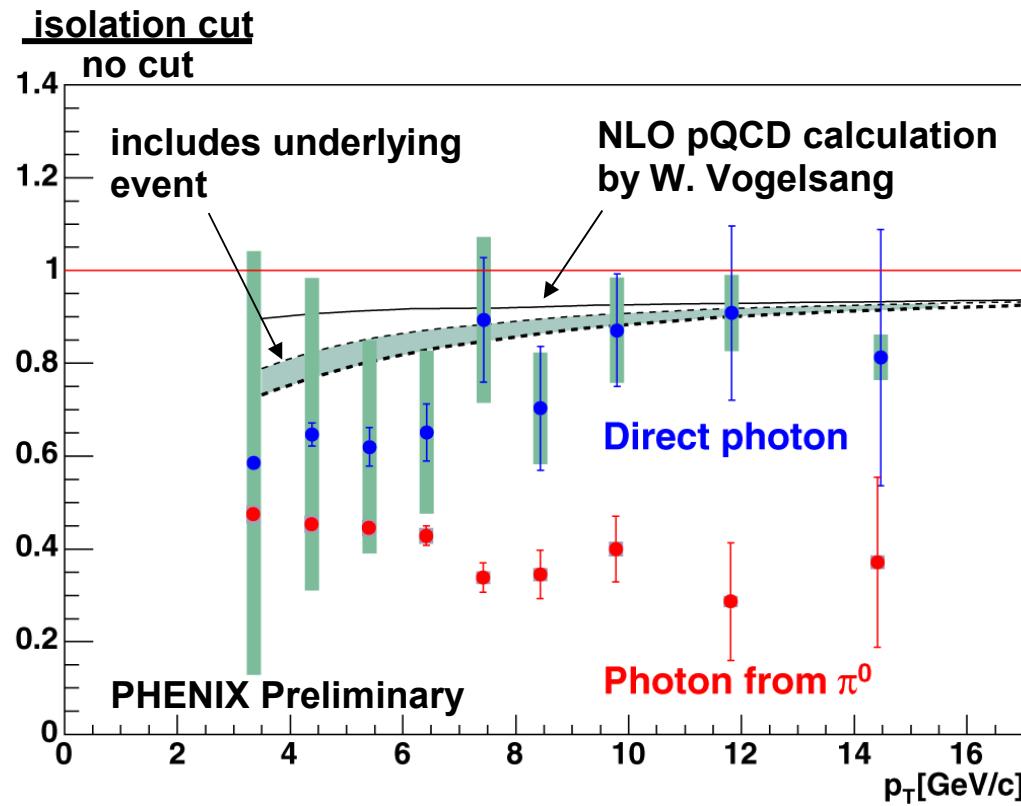
- Underlying event (soft physics)
- Limited acceptance

Bremsstrahlung





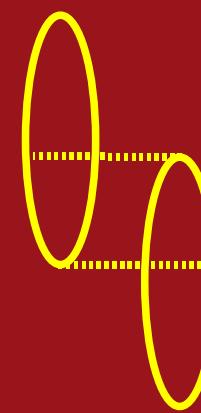
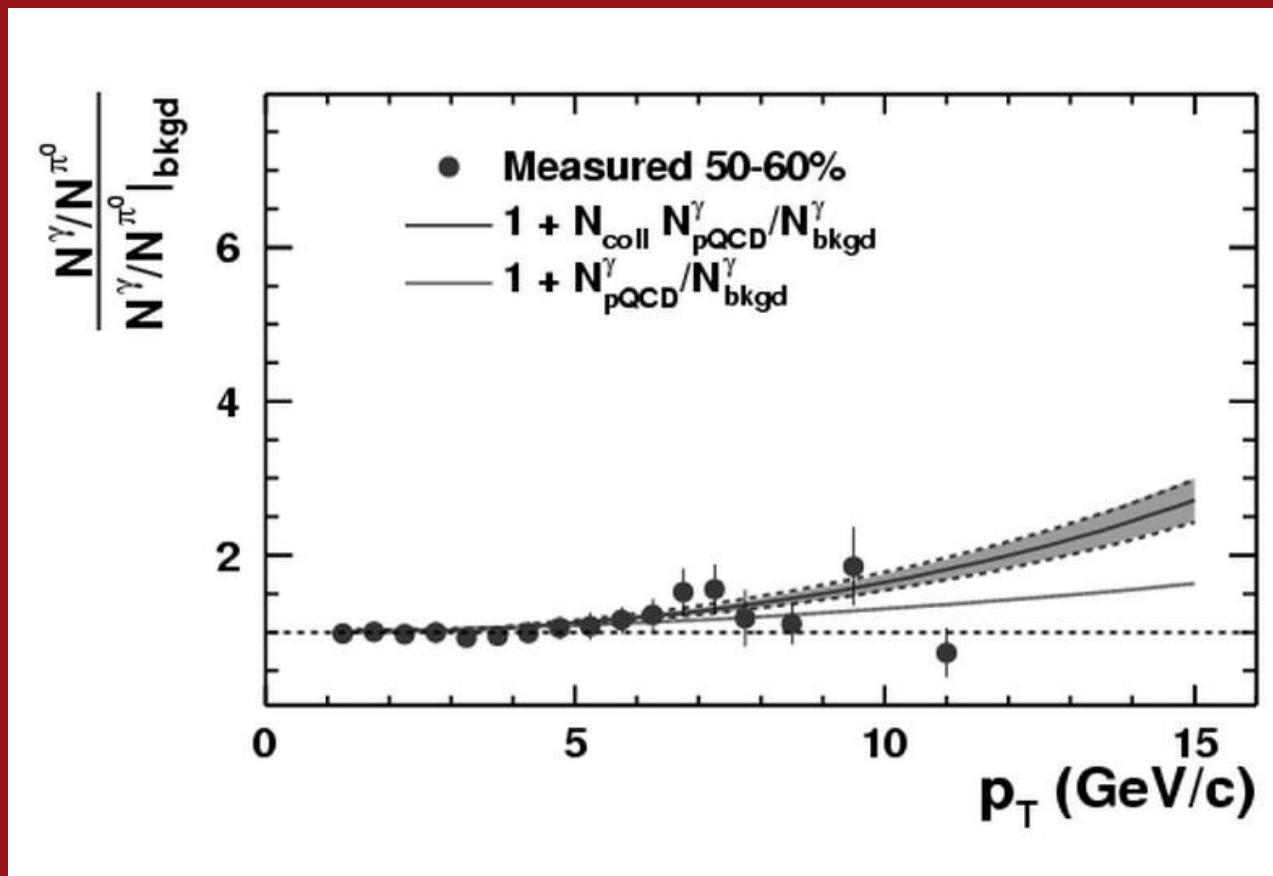
Results



- Isolation cut affects photons from π^0
- Large uncertainties
 - ✗ Bigger effect on direct γ at lower p_T ? (expected)
 - ✗ Better agreement when including underlying event?
- RHIC Run06 p+p
 - ✗ Integrated lumi $\sim 45 \text{ pb}^{-1}$
 - ✗ Factor 100!!

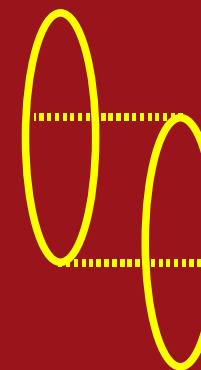
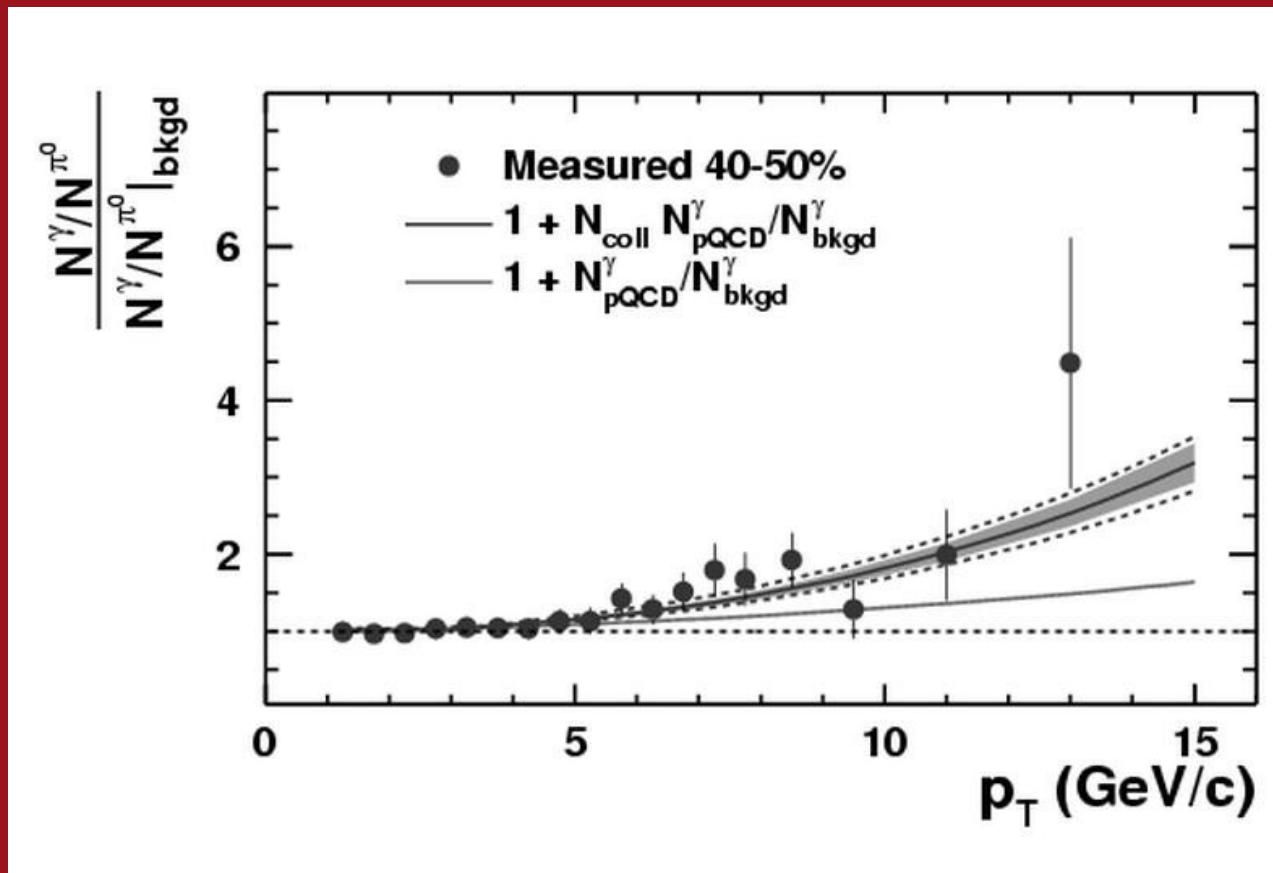


$\gamma_{\text{meas}}/\gamma_{\text{incl}}$



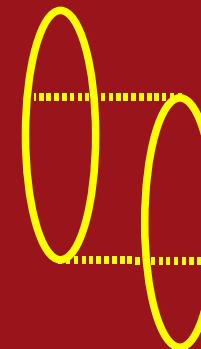
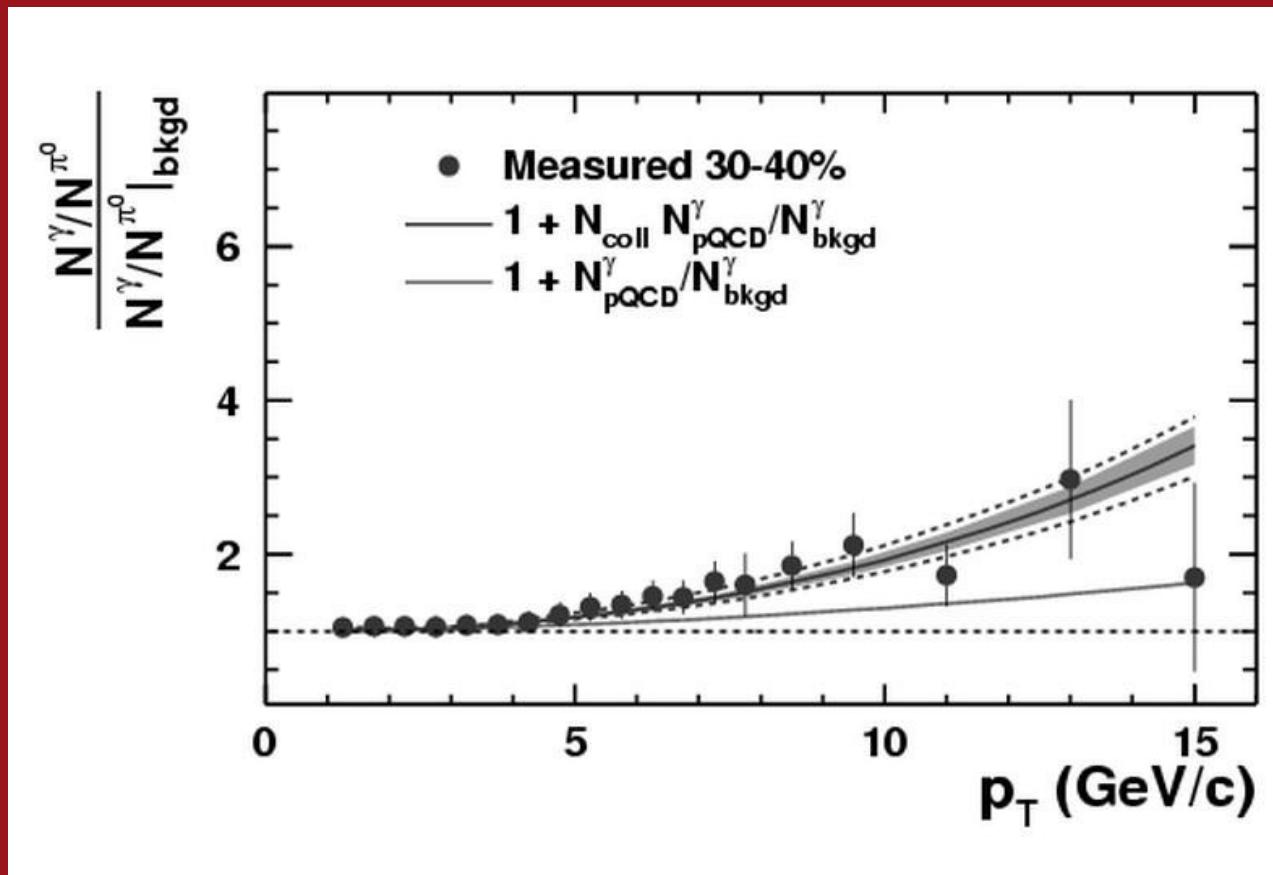


$\gamma_{\text{meas}}/\gamma_{\text{incl}}$



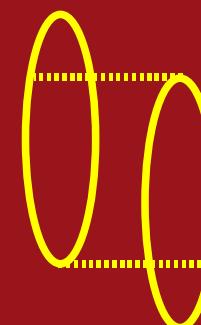
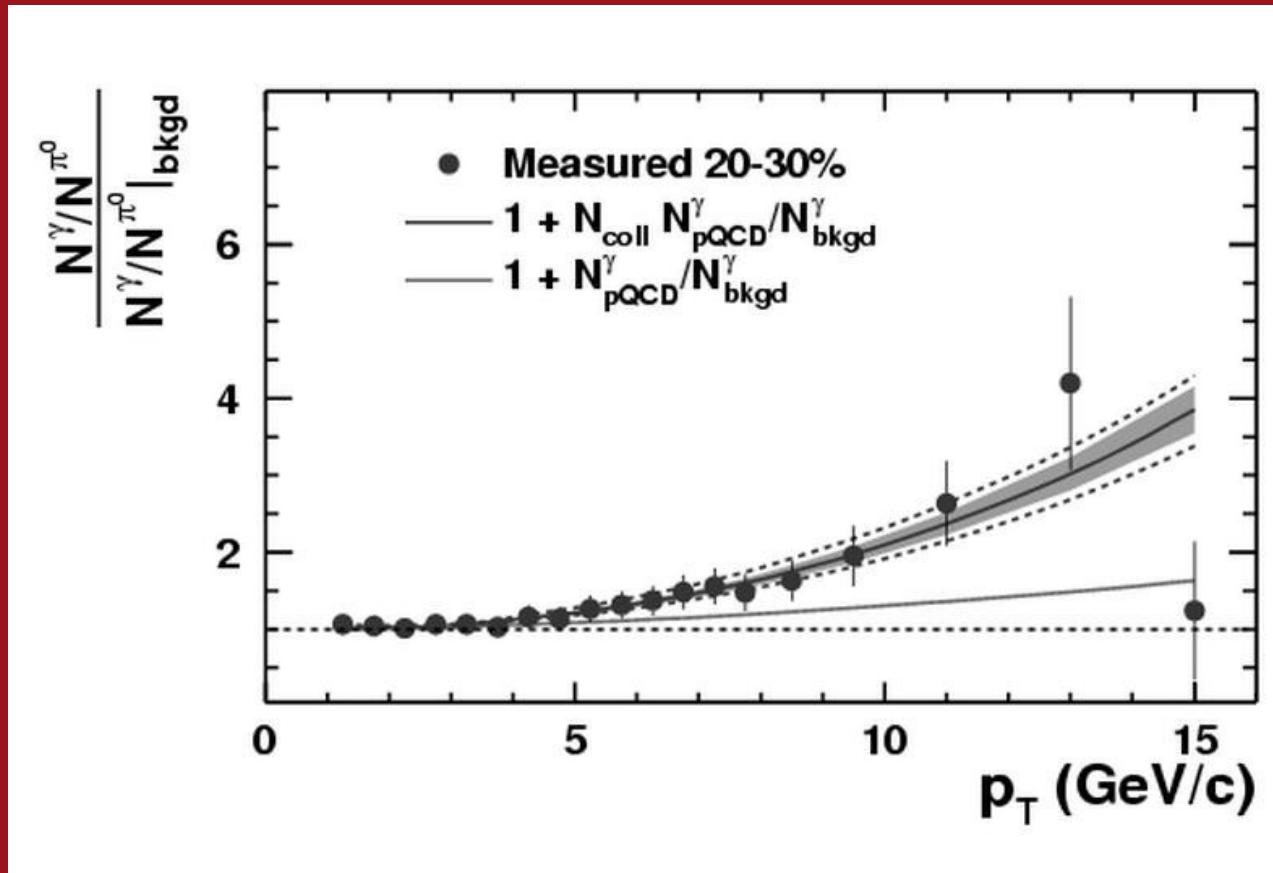


$\gamma_{\text{meas}}/\gamma_{\text{incl}}$



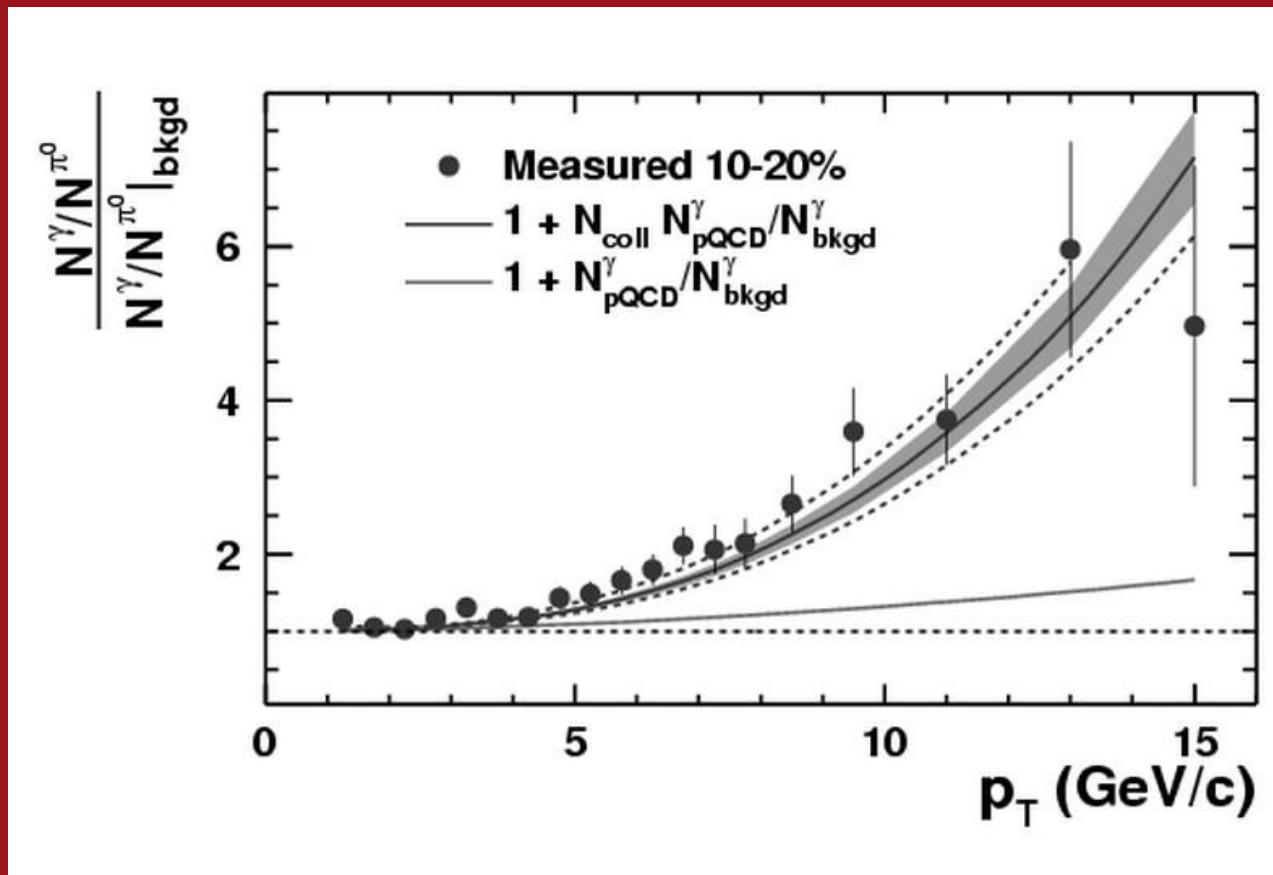


$\gamma_{\text{meas}}/\gamma_{\text{incl}}$



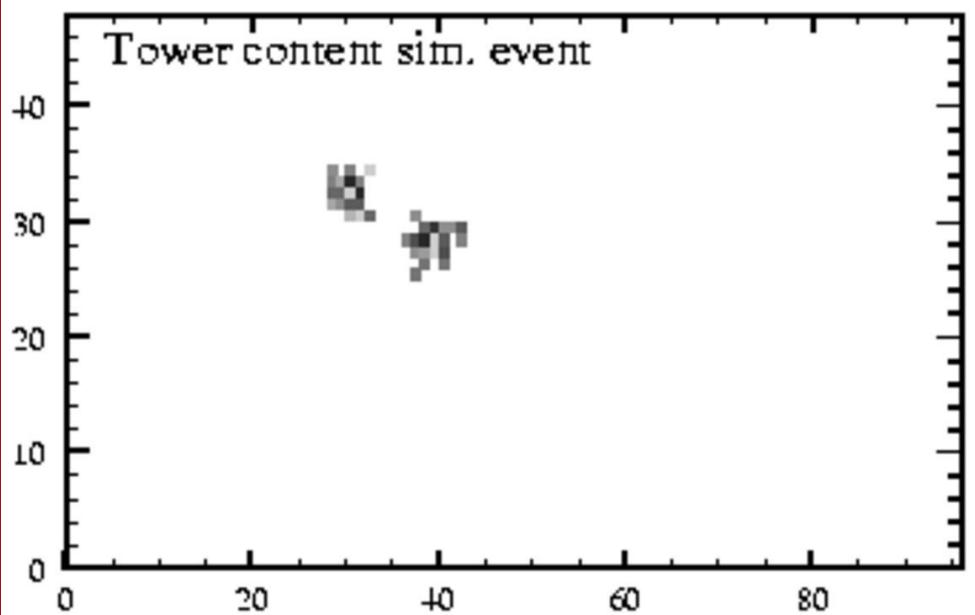
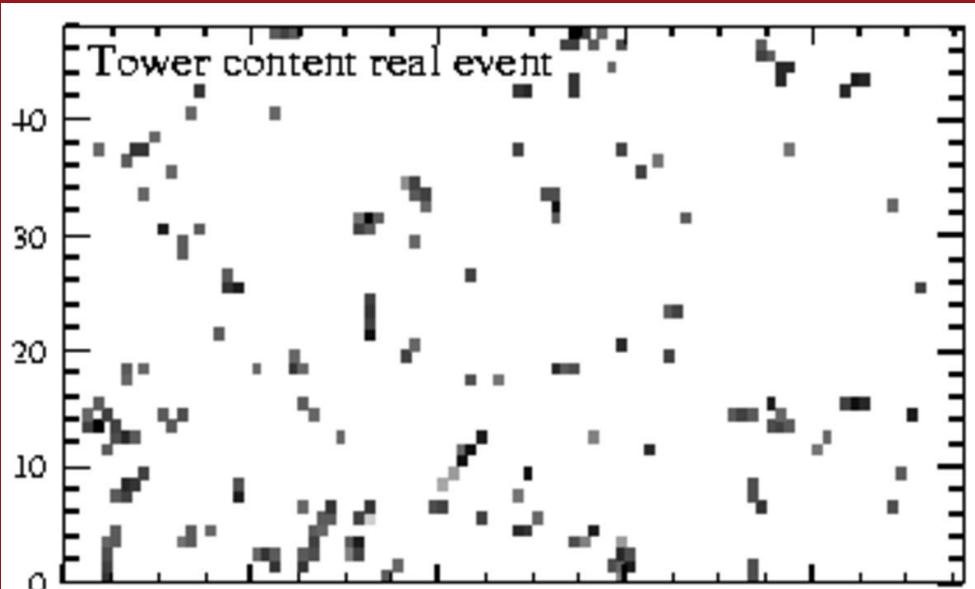


$\gamma_{\text{meas}}/\gamma_{\text{incl}}$





Efficiency via Embedding

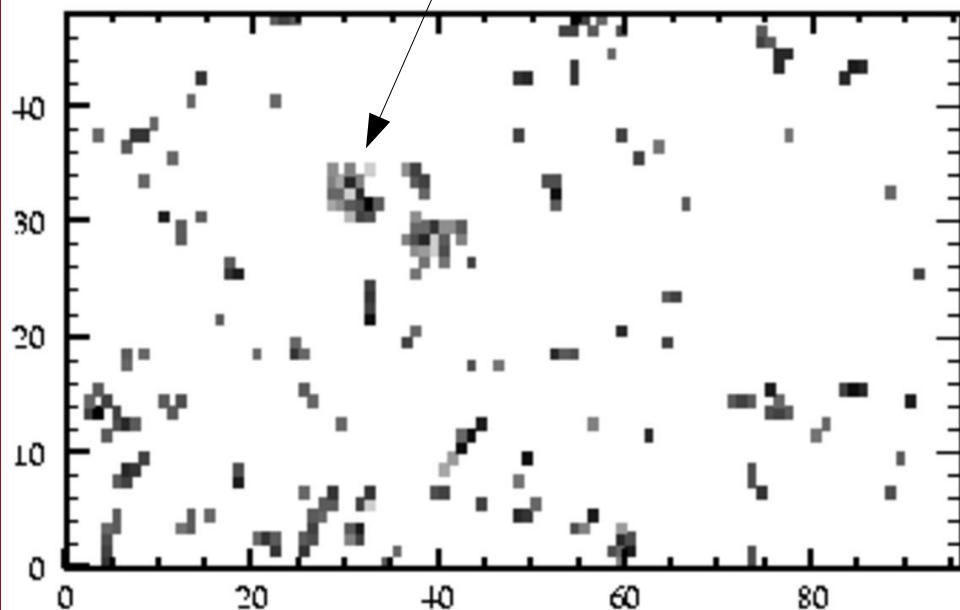


- **Embedding of simulated particles into REAL events**
- **Most realistic conditions**
 - ✗ Exact event topology
 - ✗ Crucial for high multiplicity (cluster overlap)
 - ✗ Exactly the same cuts/code for real and merged events
- **Done for π^0, γ and neutrons**



Efficiency via Embedding

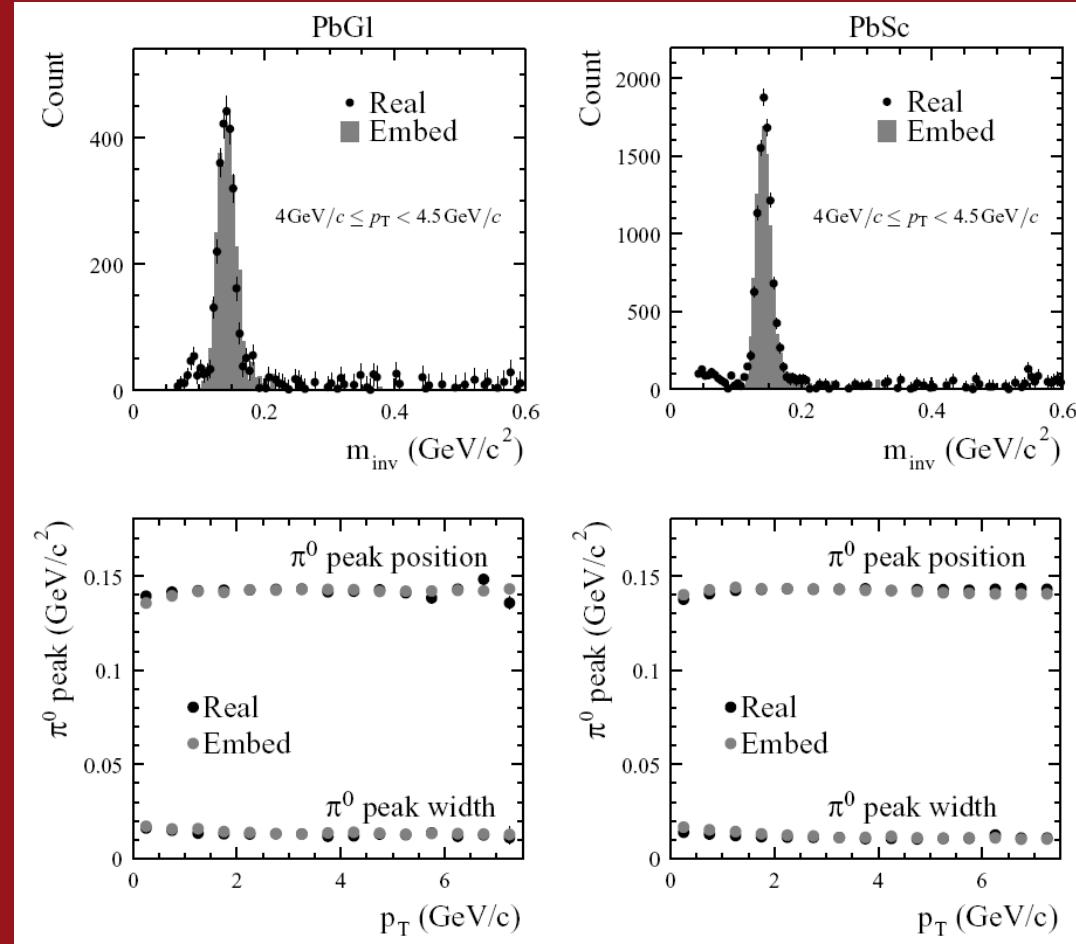
Embedded photon
modified by overlap



- **Embedding of simulated particles into REAL events**
- **Most realistic conditions**
 - ✗ Exact event topology
 - ✗ Crucial for high multiplicity (cluster overlap)
 - ✗ Exactly the same cuts/code for real and merged events
- **Done for π^0, γ and neutrons**
 - ✗ Single photon efficiency:
 - Including module cuts
 - ~95% (PbSc)
 - ~80% (PbGl)



An Important Cross Check



- Efficiency simulation reproduces π^0 peak positions and widths over the entire p_T range