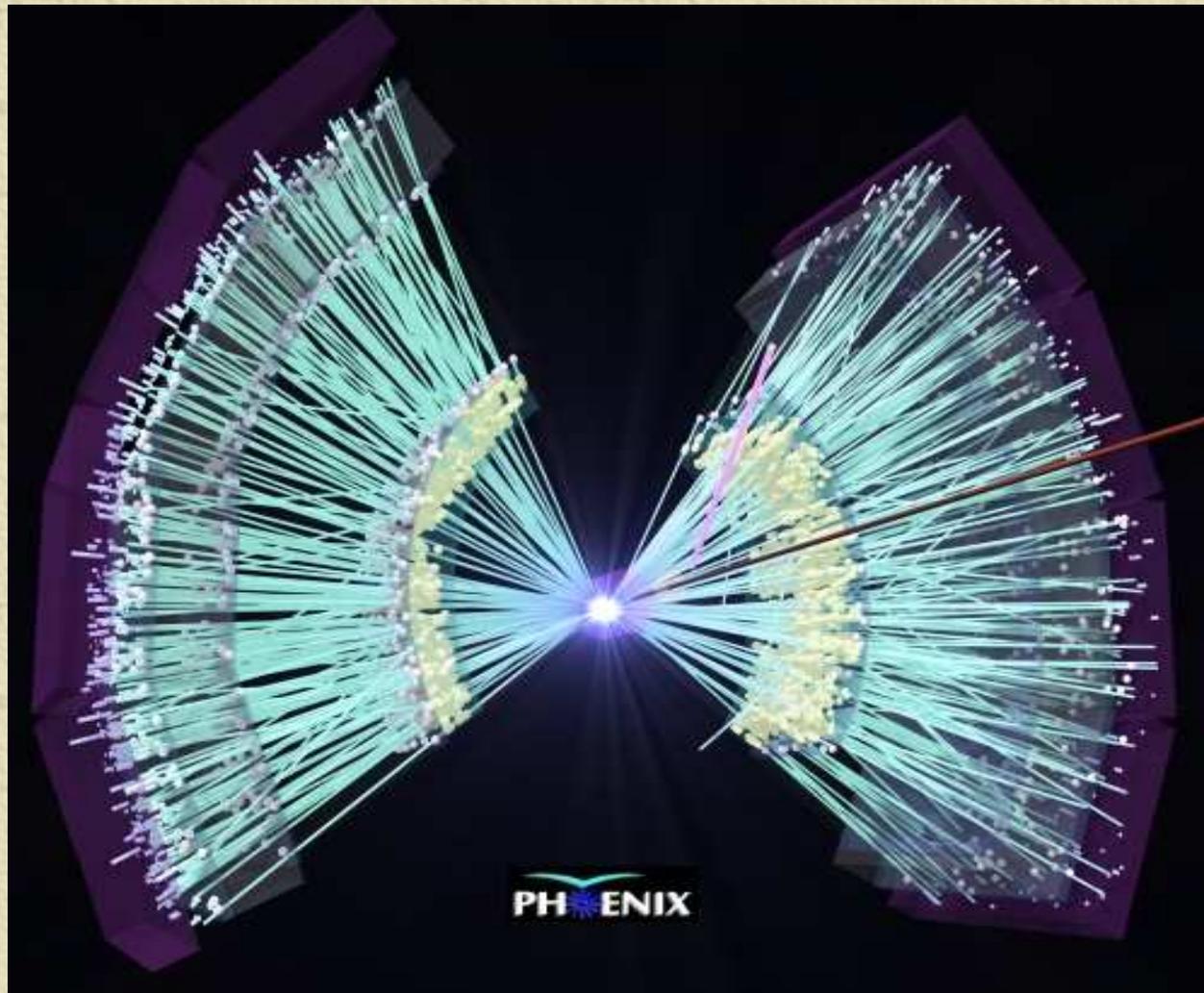


Event-by-Event $\langle P_T \rangle$ Fluctuations in PHENIX

Quark Matter 2002

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Searching for Critical Behavior

Analogy: Critical Opalescence (as observed in a CO₂ liquid-gas transition)



The image shows four glass tubes, each containing a liquid and a gas, illustrating critical opalescence. The tubes are labeled with temperature conditions relative to the critical temperature T_c :

- Leftmost tube: $T > T_c$ (clear liquid and gas)
- Second tube: $T \approx T_c$ (increasing opalescence)
- Third tube: $T \approx T_c$ (maximal opalescence, indicated by a blue arrow from the text above)
- Rightmost tube: $T < T_c$ (clear liquid and gas)

Each tube shows a central bulbous region where the liquid and gas meet, with varying degrees of cloudiness (opalescence) as the temperature approaches T_c .

- *S. Mrowczynski (see Phys. Lett. B314 (1993) 118.)*
Instability of the plasma could be present, initiated as random color fluctuations. For some events, the fluctuations of particle transverse quantities would be magnified.
- *M. Stephanov, et. al. (see hep-ph/9903292)* suggest that near a tri-critical point in the QCD phase diagram, the event-by-event fluctuations in p_T could increase significantly.

Analysis Details

Data:

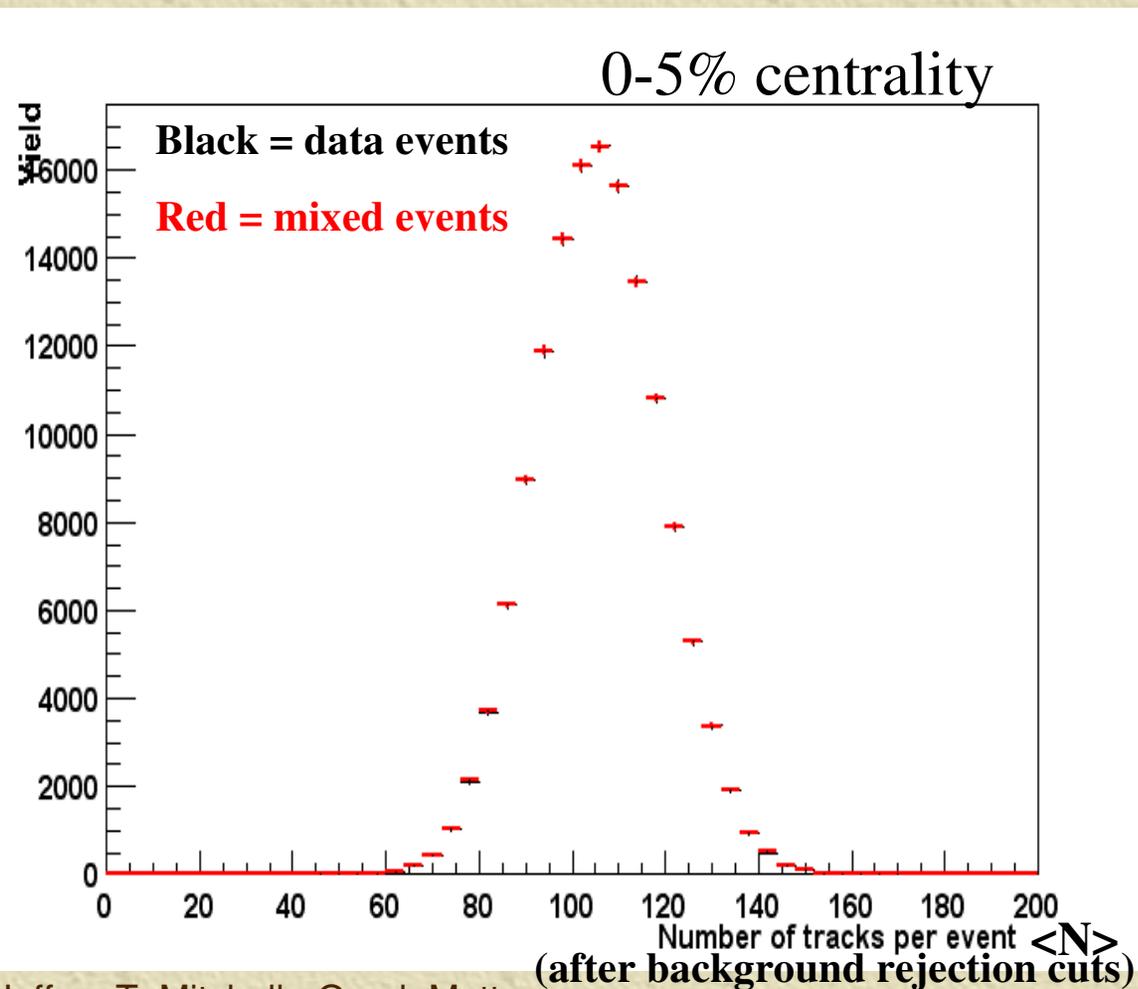
- The average p_T are determined on an event-by-event basis.
- Improvements over the $\sqrt{s_{NN}} = 130$ GeV analysis include:
 - *3x increase in azimuthal aperture. 2x event statistics.*
 - *Enhanced background rejection from the additional detectors.*

Mixed Events:

- Mixed events serve as the random baseline distributions.
- Mixed event distributions are built from reconstructed tracks in real data events from the same centrality/multiplicity and event vertex class.
- *No two tracks from the same real event are allowed in the same mixed event.*

Important Note: Matching mixed events to data events

Since the width of the $\langle p_T \rangle$ distribution depends on $\langle N \rangle$, it is important that there is an exact match of the mixed event $\langle N \rangle$ distribution to the data $\langle N \rangle$ distribution. The mixed events are constructed by sampling the data $\langle N \rangle$ distribution.



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Definition of Fluctuation Quantities

Define the magnitude of a fluctuation, ω :

$$\omega = \frac{\sqrt{\langle X^2 \rangle - \langle X \rangle^2}}{\langle X \rangle} \times 100\% = \frac{\sigma}{\mu} \times 100\%$$

Define the fractional fluctuation difference from random, F_{pT} :

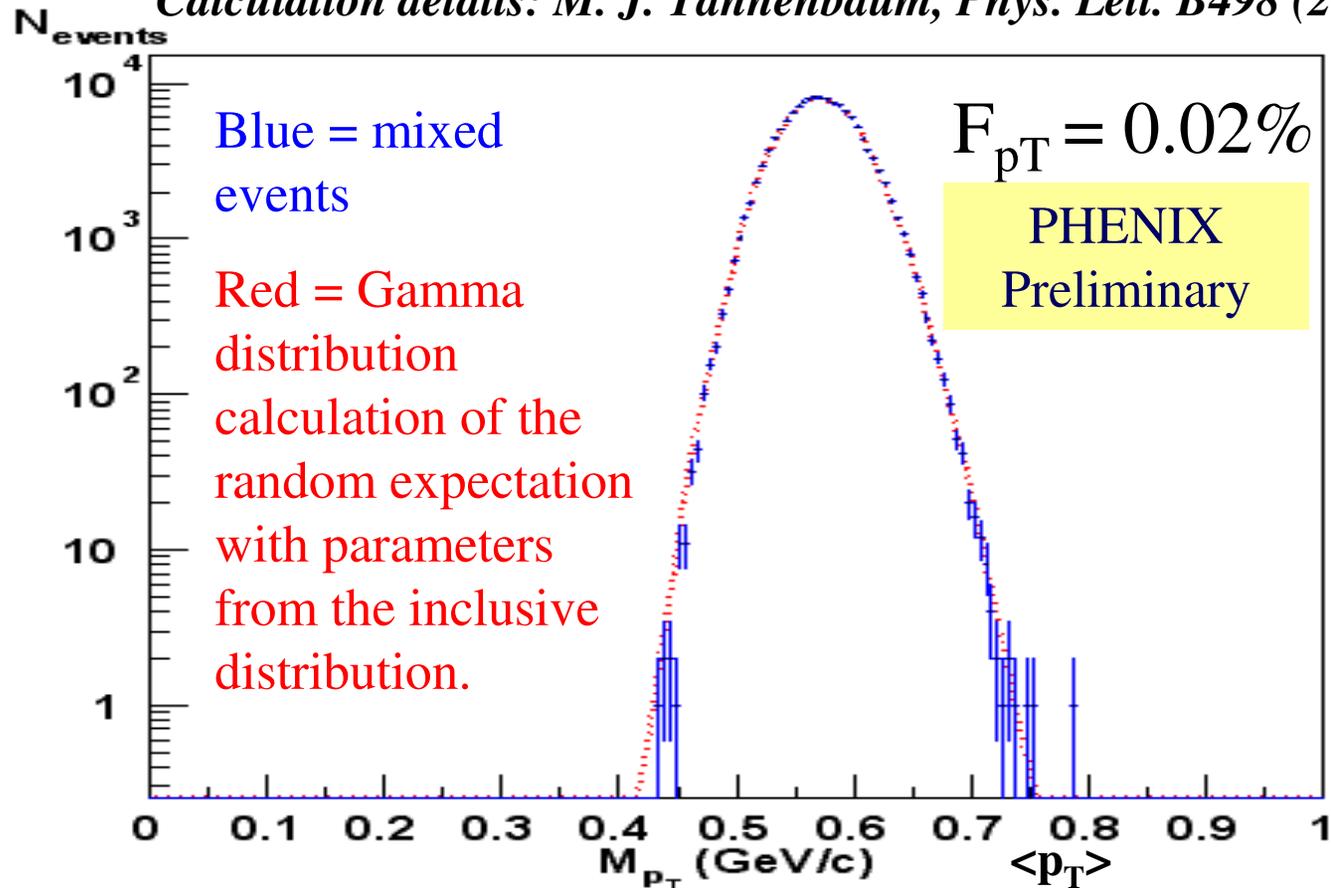
$$F_{pT} = \frac{\omega_{data} - \omega_{random}}{\omega_{random}}$$

Also commonly used is the variable, ϕ :

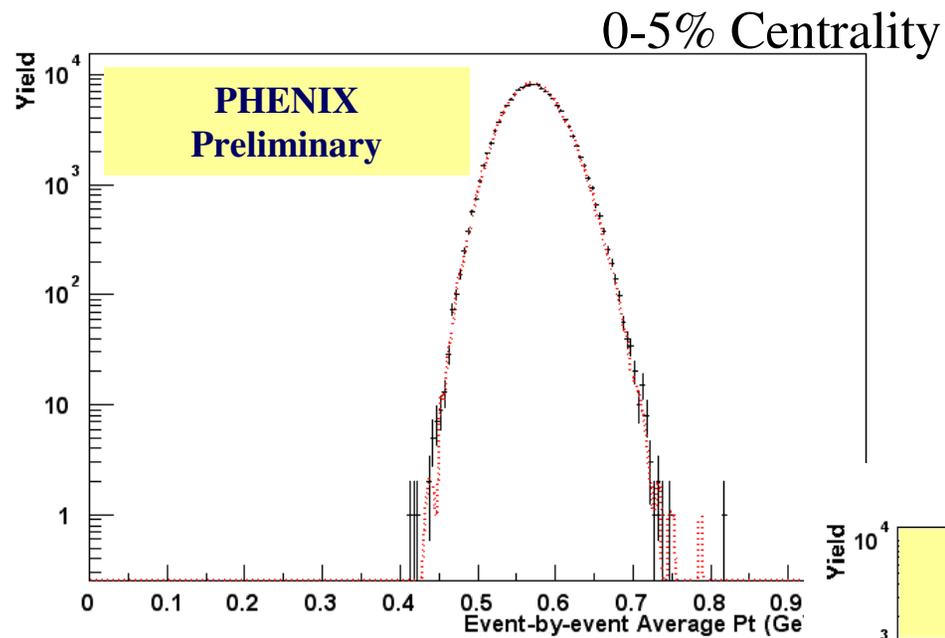
$$\phi = \sqrt{n} (\sigma_{data} - \sigma_{random}) = F_{pT} \sigma_{random} \sqrt{\langle N \rangle}$$

Mixed events as the random baseline distribution

Calculation details: M. J. Tannenbaum, *Phys. Lett. B*498 (2001) 29.



$\langle P_T \rangle$ distributions

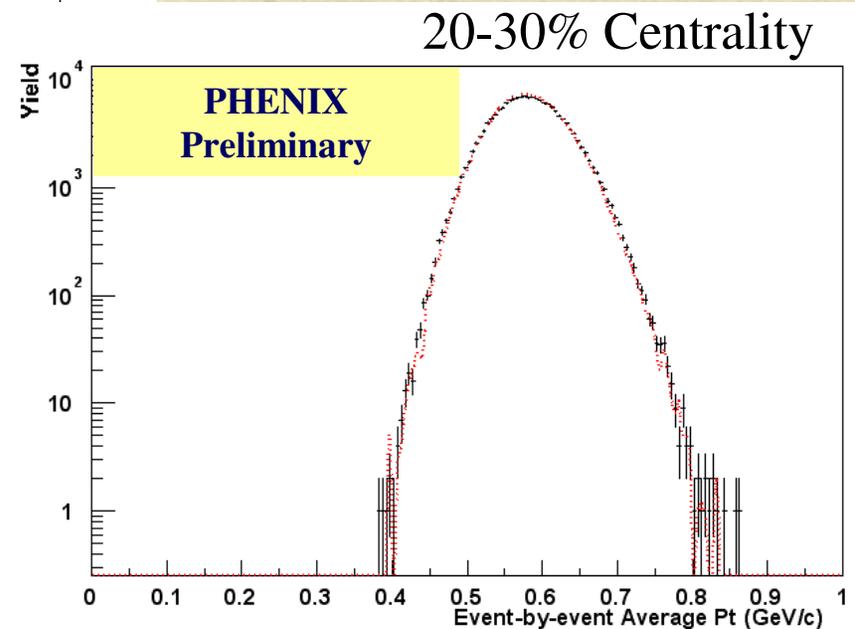


$$\sqrt{s_{NN}} = 200 \text{ GeV}$$

A small positive fluctuation is apparent.

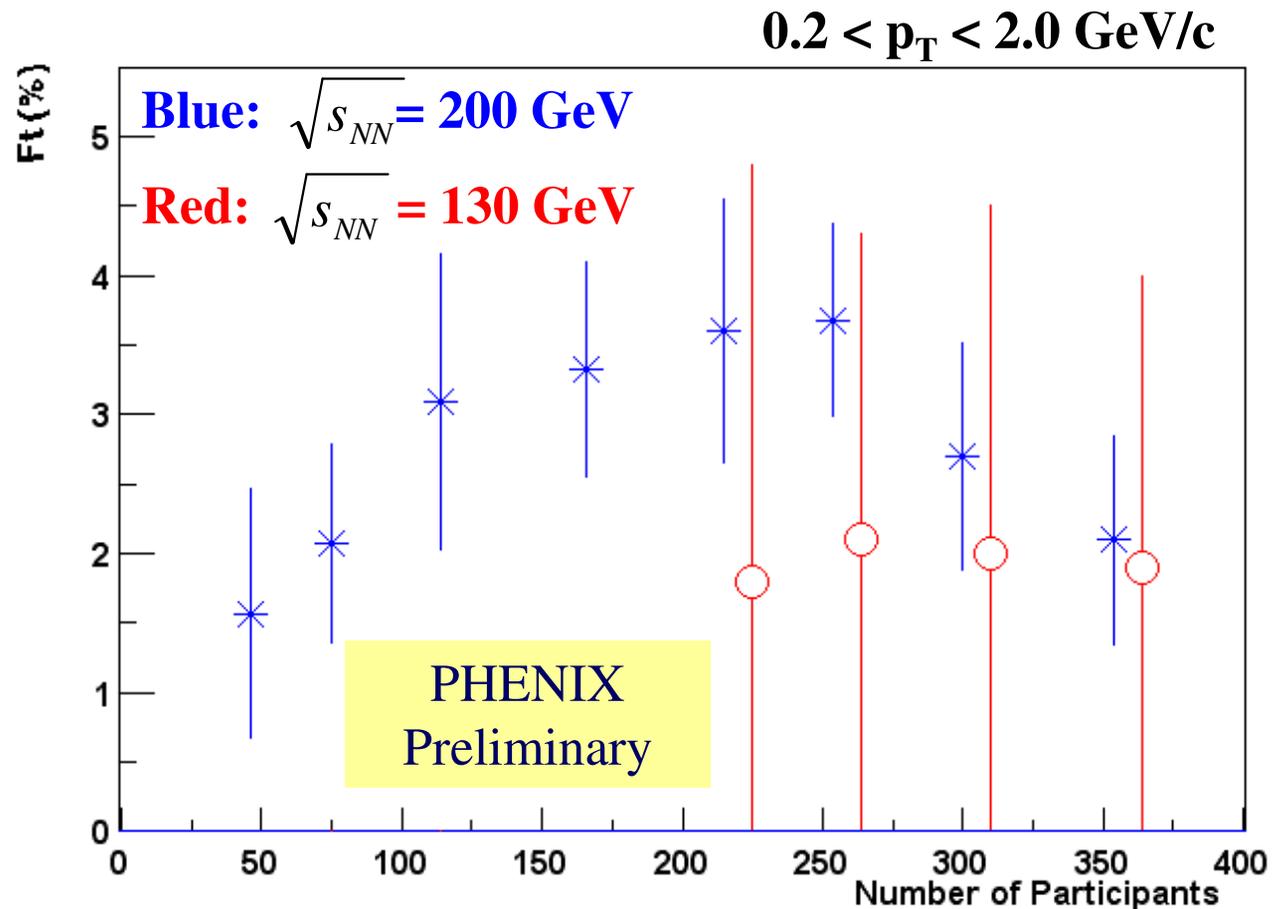
Black = data events

Red = mixed events



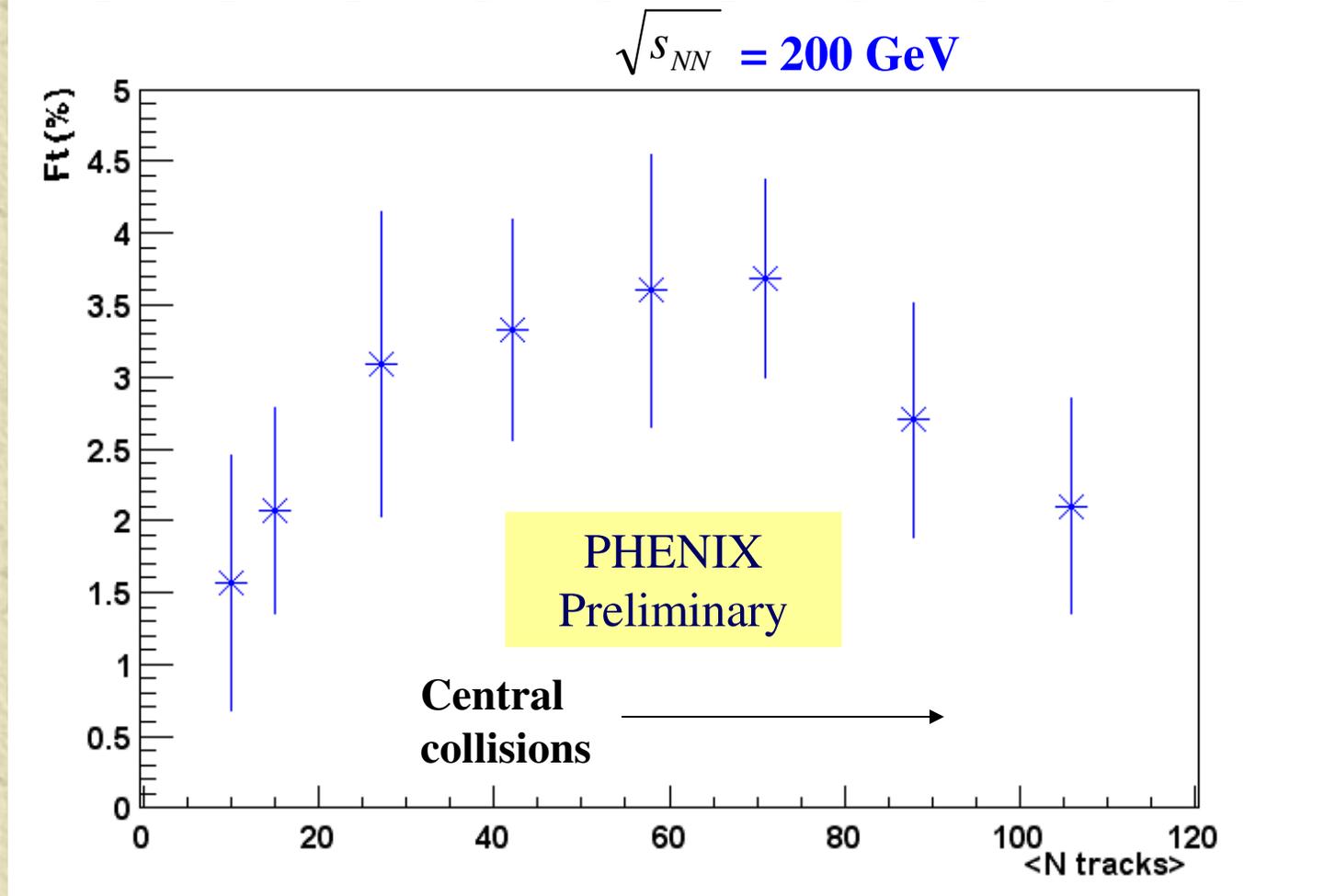
F_{pT} as a function of centrality

The fluctuation magnitude follows a decreasing trend for peripheral collisions.



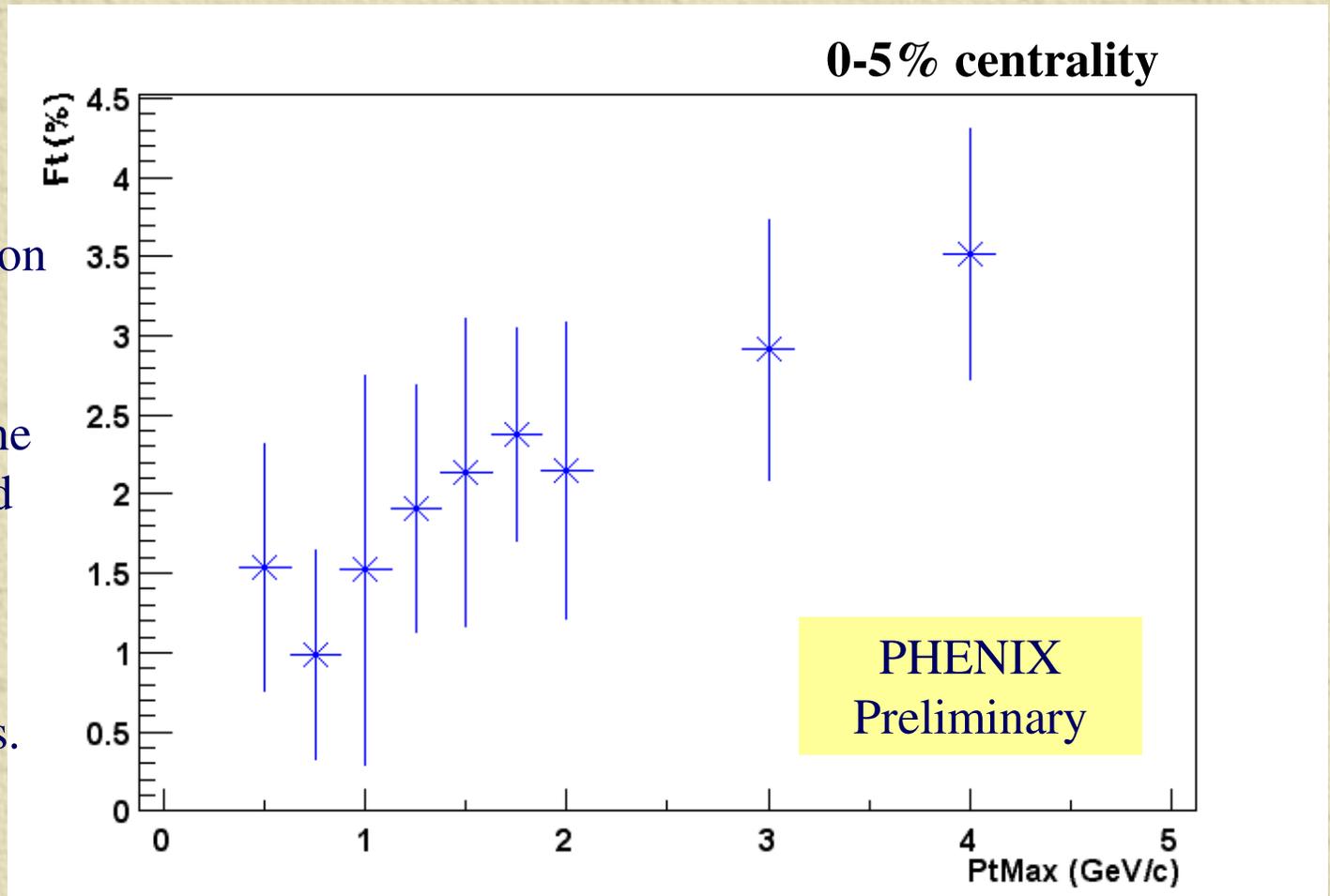
Using the same centrality binning as in the previous figure.

F_{pT} vs. $\langle N_{\text{tracks}} \rangle$



F_T vs. P_T range ($0.2 < p_T < p_{T, \max}$)

The fluctuation magnitude tends to increase as the p_T range used to calculate $\langle p_T \rangle$ is extended to higher values.



Sensitivity: Modeling a Fluctuation

Goal: Produce a fluctuation that does not change the mean or variance of the final inclusive distribution.

- The final inclusive distribution (fixed by observation) can be expressed as a Gamma distribution:

$$\frac{dN}{dp_T} = \Gamma(p_T, p, b)$$

where $T = 1/b$ is the *inverse slope parameter* of the distribution.

- Consider an event sample with two classes of events.

Define $q = N_{\text{events, class 1}} / N_{\text{events, total}}$

- The distribution for the two component fluctuating sample can be taken as:

$$f(p_T) = q \times \Gamma(p_T, b1, p1) + (q - 1) \times \Gamma(p_T, b2, p2)$$

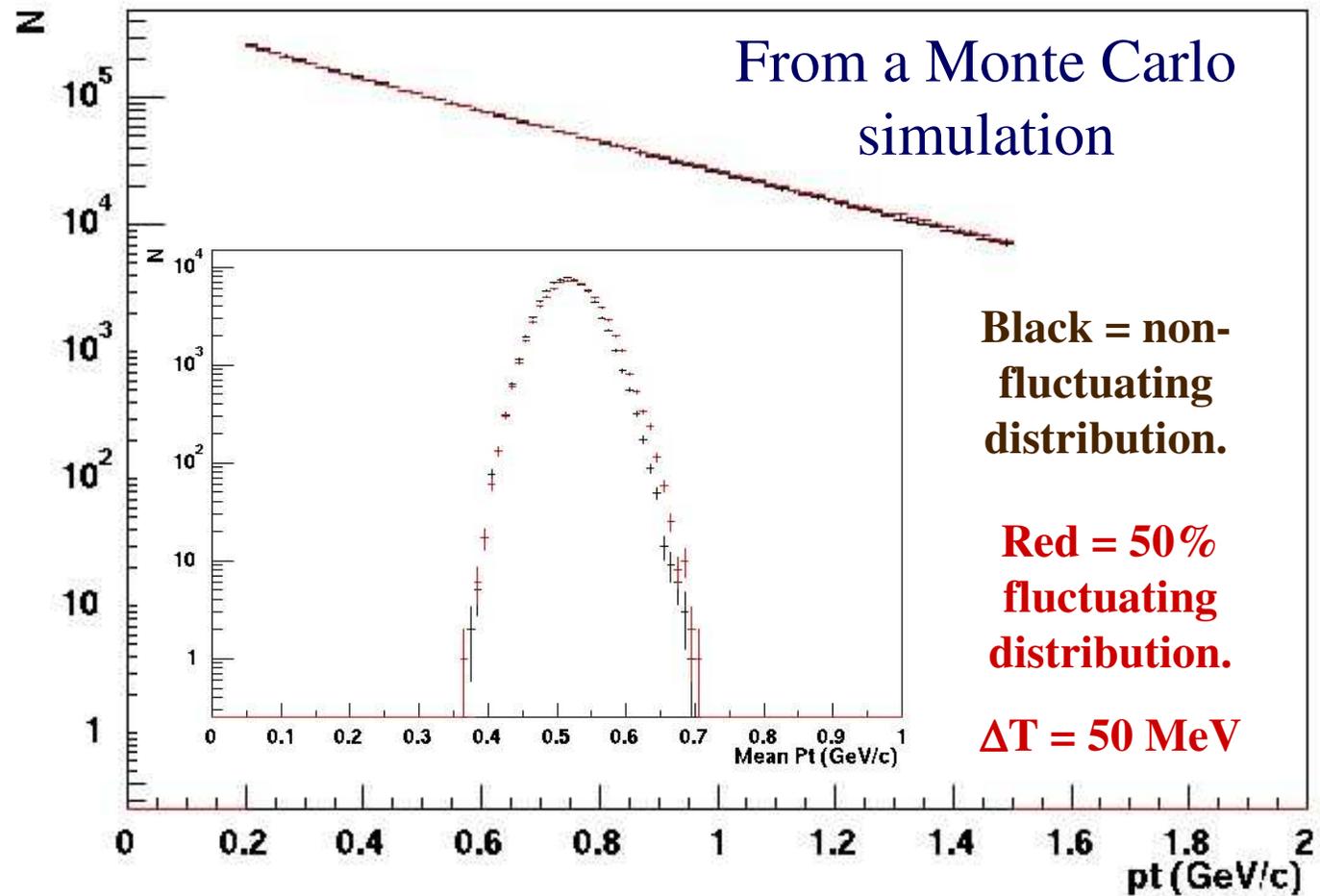
Fluctuation Models

Goal: Produce a fluctuation that does not change the mean or variance of the final inclusive distribution.

- We consider two models of this type:
 - Fluctuation Model A: *The inclusive distributions of the two event classes have the same mean, but different variance.*
 - Fluctuation Model B: *The inclusive distributions of the two event classes have the same variance, but different means.*
- After applying the constraints for each model, two event classes are defined with differing inverse slope parameters.

$$\text{Define } \Delta T = T_{\text{class 1}} - T_{\text{class 2}} > 0$$

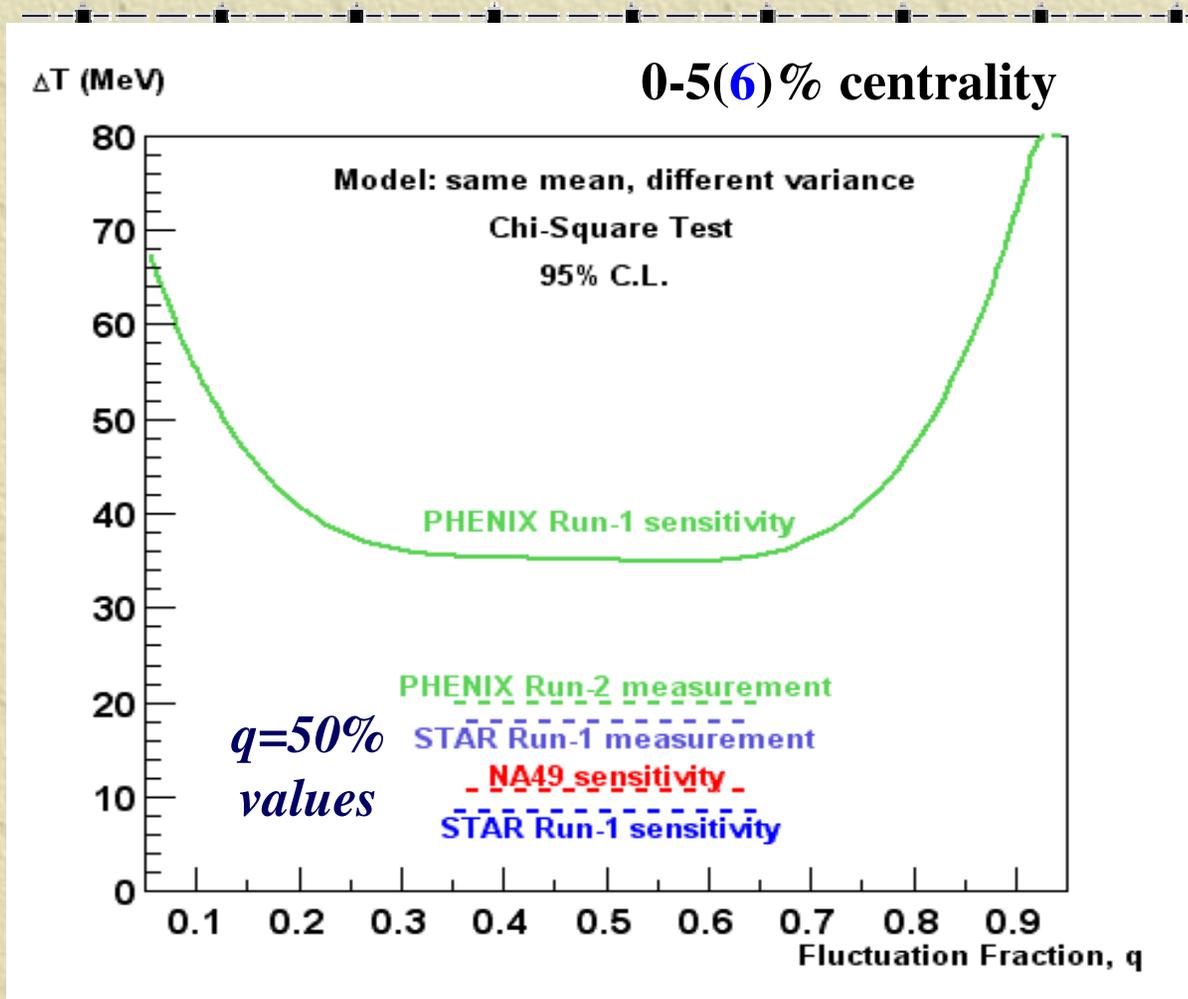
“Different Mean, Same Variance” Model Demonstration



Estimated Experimental Sensitivities: Model A

$$\text{Run-1: } \sqrt{s_{NN}} = 130 \text{ GeV}$$

$$\text{Run-2: } \sqrt{s_{NN}} = 200 \text{ GeV}$$

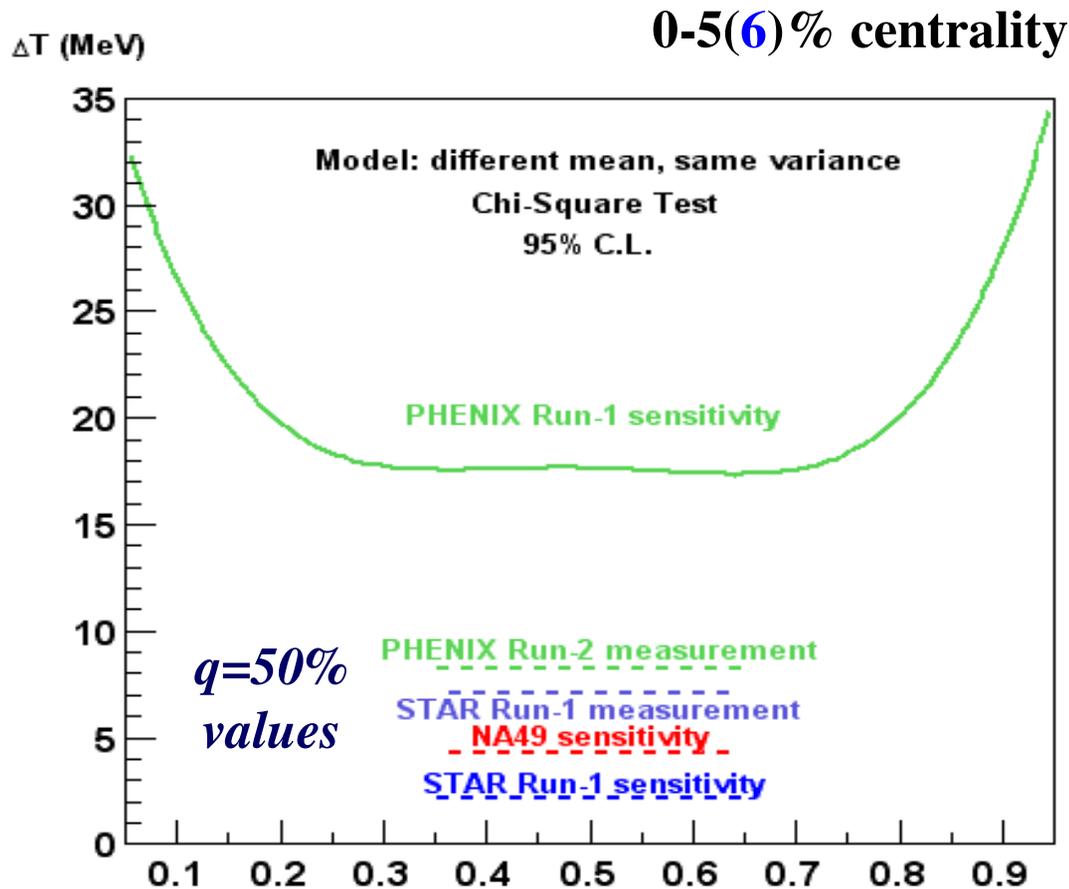


Estimated by comparing the experimental data to Monte Carlo simulation results that reproduce the $\langle N \rangle$ and inclusive p_T distributions.

Estimated Experimental Sensitivities: Model B

$$\text{Run-1: } \sqrt{s_{NN}} = 130 \text{ GeV}$$

$$\text{Run-2: } \sqrt{s_{NN}} = 200 \text{ GeV}$$



Estimated by comparing the experimental data to Monte Carlo simulation results that reproduce the $\langle N \rangle$ and inclusive p_T distributions.

Summary and Conclusions

- ✦ With the increased PHENIX azimuthal aperture and improved background rejection, a positive non-random fluctuation in event-by-event average p_T is now observed. The fluctuations tend to decrease for peripheral collisions.
- ✦ The magnitude of the fluctuation tends to increase slightly with increasing p_T range. Possible causes for this trend await further investigation.
- ✦ The contribution of elliptic flow into the PHENIX azimuthal acceptance is estimated (via Monte Carlo simulation using PHENIX preliminary p_T -dependent v_2 measurements wrt to the reaction plane) to be on the order of -0.3% for mid-central collisions, thus not accounting for the observed signal.
- ✦ The magnitude of the fluctuations within a pair of dual-event-class models processed through the PHENIX acceptance are estimated to be on the order of $\Delta T = 10\text{-}20$ MeV.