

Electroweak Physics At An e-Ion Collider (EIC)

1. WEAK NC PARITY VIOLATION
AND NEW PHYSICS
 - i) APV vs Pol Electron Scattering
 - ii) QWEAK, Moller, DIS, eC...
2. Preliminary e-ion requirements
For Competitive A_{RL} Program
~100fb⁻¹ (K. Kumar et al.) 2009 Talk
Posted on the Web



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LDRD Proposal 2009

Electroweak Physics with an Electron-Ion Collider

Deshpande, Kumar, Marciano, Vogelsang

- DIS & Nuclear Structure Functions (γ, Z, W) (Beyond HERA)
- **$A_{RL}, \sin^2\theta_W(Q^2),$ Radiative Corrections, “New Physics”**
- Lepton Flavor Violation: eg $ep \rightarrow \tau X$
(inverse attobarn=1000fb⁻¹!)

What are the Machine and Detector Requirements?

Inclusion of Electroweak Radiative Corrections (Important?)

High Precision & Polarization($\pm 0.5\%$?, $\pm 0.25\%$?)

Nucleon vs Nuclear Asymmetries (EMC Effect, CSV?)

Proton Polarization (Spin Content-Other?)

Various Issues That Need Thorough Study

1) PV Weak Neutral Currents (Past, Present and Future)

- Ancient History: By 1975 the $SU(2)_L \times U(1)_Y$ Weinberg-Salam Model was nearly established. Predicted Weak Neutral Currents seen in neutrino scattering at CERN! But did the NC have the right coupling? $g_2/\cos\theta_W Z^\mu \bar{f} \gamma_\mu (T_{3f} - 2Q_f \sin^2\theta_W - T_{3f} \gamma_5) f$

A New Form of Parity Violation!

Non Maximal but Distinctive

γ -Z Interference \rightarrow Parity Violation Everywhere!

Atomic Parity Violation (APV)

- $Q_W(Z,N) = Z(1-4\sin^2\theta_W) - N$ Weak Charge
 $\theta_W = \text{Weak Mixing Angle}$

$$Q_W(p) = 1 - 4\sin^2\theta_W \sim 0.08$$

$$Q_W(^{209}\text{Bi}_{83}) = -43 - 332\sin^2\theta_W = -126$$

Bi Much Larger but Complicated Atomic Physics

Originally APV not seen in Bi \rightarrow SM Ruled Out?

(Later seen in Tl, Bi, Cs...)

1978 SLAC Polarized eD Asymmetry (Prescott, Hughes...)

e+D \rightarrow e+X γ -Z Interference

$$A_{RL} = \sigma_R - \sigma_L / \sigma_R + \sigma_L \propto 2 \times 10^{-4} Q^2 \text{GeV}^{-2} (1 - 2.5 \sin^2\theta_W) \sim 10^{-4} \text{Expected}$$

$$\text{Exp. Gave } A_{RL}^{\text{exp}} = 1.5 \times 10^{-4} \rightarrow \sin^2\theta_W = \underline{0.21(2)}$$

Confirmed $SU(2)_L \times U(1)_Y$ SM!

$\pm 10\%$ Determination of $\sin^2\theta_W$ Precision!

Seemed to agree with GUTS (SU(5), SO(10)...))

$\sin^2\theta_W^0 = 3/8$ at unification $\mu = m_X \sim 2 \times 10^{14} \text{ GeV}$

$$\sin^2\theta_W(m_Z)_{MS} = 3/8 [1 - 109\alpha/18\pi \ln(m_X/m_Z) + \dots]$$

$\approx 0.21!$ (Great Desert?)

But later, minimal SU(5) ruled out by proton decay

exps $\tau(p \rightarrow e^+ \pi^0) > 10^{33} \text{ yr} \rightarrow m_X > 5 \times 10^{15} \text{ GeV}$

SUSY GUT Unification $\rightarrow m_X \sim 10^{16} \text{ GeV}$ $\tau_p \sim 10^{35} \text{ yr}$

$$\sin^2\theta_W(m_Z)_{MS} = \underline{0.232 \text{ (Good Current Agreement!)}}$$

1980s - Age of EW Precision

$\sin^2\theta_W$ needed better than $\pm 1\%$ determination

Renormalization Prescription Required

EW Radiative Corrections Computed

Finite and Calculable: DIS $\nu_\mu N$, $\nu_\mu e$, APV (A. Sirlin & WJM)

$$m_Z, m_W, \Gamma_Z, A_{LR}, A_{FB}$$

Define Renormalized Weak Mixing Angle: $\sin^2\theta_W^R$

$\sin^2\theta_W^0 = 1 - (m_W^0/m_Z^0)^2 = (e^0/g^0)^2$ Natural Bare Relation

$$\sin^2\theta_W \equiv 1 - (m_W/m_Z)^2$$

On Shell Definition, Popular in 1980s

Induces large $\alpha(m_t/m_W)^2$ corrections

Now Largely Abandoned

$$\sin^2\theta_W(\mu)_{MS} \equiv e^2(\mu)_{MS}/g^2(\mu)_{MS}$$

Good for GUT running

No Large RC Induced

Theoretically Nice/ But Unphysical

$\sin^2\theta_W^{\text{lep}} = Z_{\mu\mu}$ coupling at the Z pole
very popular at LEP
 $= \sin^2\theta_W(m_Z)_{\text{MS}} + 0.00028$ (best feature)

$\sin^2\theta_W(Q^2) =$ Physical Running Angle
Continuous
Incorporates γZ mixing loops: quarks, leptons, W^\pm

Precision measurements at the Z Pole ($e^+e^- \rightarrow Z \rightarrow \bar{f}f$)

Best Determinations

$$\sin^2\theta_W(m_Z)_{\text{MS}} = 0.23070(26) \quad A_{\text{LR}} \quad (\text{SLAC})$$

$$\sin^2\theta_W(m_Z)_{\text{MS}} = 0.23193(29) \quad A_{\text{FB}}(b\bar{b}) \quad (\text{CERN})$$

(3 sigma difference!)

World Average: $\sin^2\theta_W(m_Z)_{\text{MS}} = \underline{0.23125(16)}$

IS IT CORRECT?

$$\alpha^{-1}=137.035999, G_{\mu}=1.16637 \times 10^{-5} \text{Gev}^{-2}, m_Z=91.1875 \text{Gev}$$

$$+ m_W=80.398(25) \text{Gev} \rightarrow \sin^2 \theta_W(m_Z) = \underline{0.23104(15)}$$

Implications: $114 \text{Gev} < m_{\text{Higgs}} < 150 \text{Gev}$.

New Physics Constraints From: $m_W, \sin^2 \theta_W, \alpha, \& G_{\mu}$

$S=N_D/6\pi$ (N_D =# of heavy new doublets, eg 4th generation $\rightarrow N_D=4$)

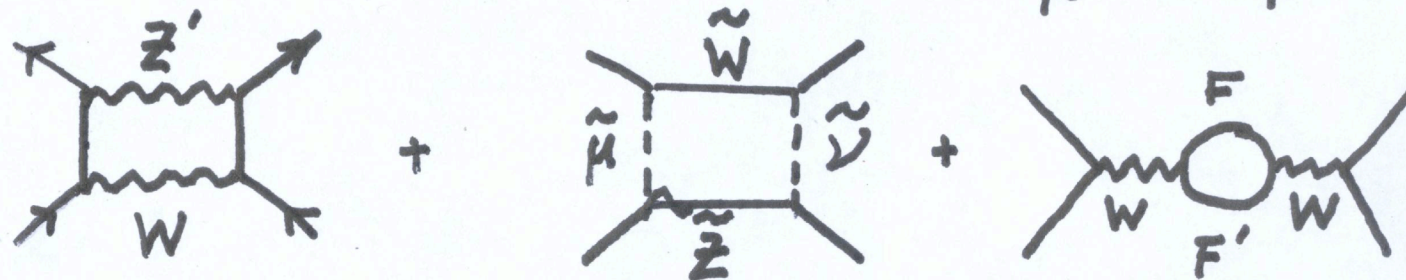
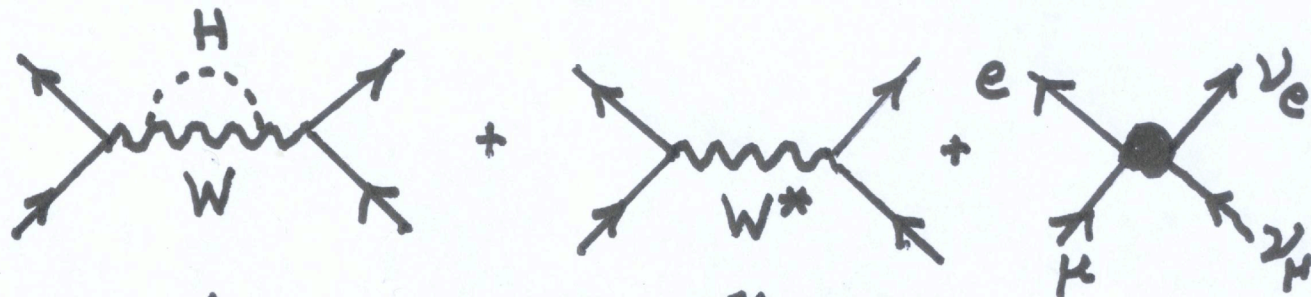
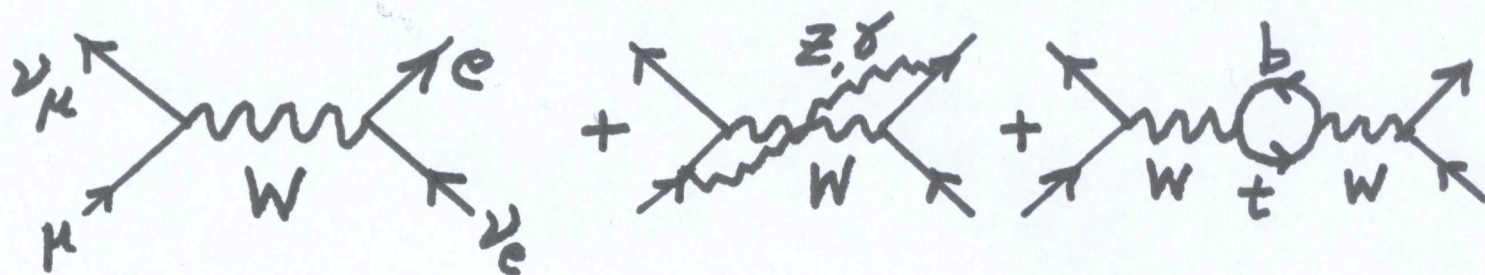
m_{W^*} = Kaluza-Klein Mass (Extra Dimensions)

$$G_{\mu} \rightarrow G_{\mu} (1 + 0.0085S + O(1)(m_W/m_{W^*})^2 + \dots)$$

	$\sin^2 \theta_W(m_Z)_{\overline{MS}}$	S	$N_D \& m_{W^*}$
<u>Average</u>	0.23125(16)	+0.11(11)	2(2), $m_{W^*} \geq 3 \text{TeV}$
A_{LR}	0.23070(26)	-0.18(15)	(SUSY)
$A_{FB}(b\bar{b})$	0.23193(29)	+0.46(17)	9(3)! Heavy Higgs, $m_{W^*} \sim 1-2 \text{TeV}$

Very Different Interpretations. We forgot to nail $\sin^2 \theta_W(m_Z)_{\overline{MS}}$!

Loop and Tree Level Corrections to Muon Decay



Z' Boson

SUSY

Technicolor

+ . . .

What about low energy measurements?

- DIS ν Scattering: $R_\nu \equiv \sigma(\nu_\mu N \rightarrow \nu_\mu X) / \sigma(\nu_\mu N \rightarrow \mu X)$ loops
 $\rightarrow m_t$ heavy, $\sin^2\theta_W(m_Z)_{MS} = 0.233 \rightarrow$ SUSY GUTS

NuTeV $\sin^2\theta_W(m_Z)_{MS} = 0.236(2)$ High?

Nuclear-Charge Symmetry Violation?

Atomic Parity Violation Strikes Back

1990 $Q_W(\text{Cs})^{\text{exp}} = -71.04(1.38)(0.88)$ C. Wieman et al.

Electroweak RC $\rightarrow Q_W(\text{Cs})^{\text{SM}} = \rho_{PV}(-23-220\kappa_{PV}(0)\sin^2\theta_W(m_Z)_{MS})$
= -73.19(3)

1999 $Q_W(\text{Cs})^{\text{exp}} = -72.06(28)(34)$ Better Atomic Th.

2008 $Q_W(\text{Cs})^{\text{exp}} = -72.69(28)(39) \rightarrow \sin^2\theta_W(m_Z)_{MS} = \underline{0.2290(22)}$

2009 $Q_W(\text{Cs})^{\text{exp}} = \underline{-73.16(28)(20)} \rightarrow \sin^2\theta_W(m_Z)_{MS} = \underline{0.2312(16)!}$

$\pm 0.5\%$ \rightarrow **Major Constraint On “New Physics”**

$Q_W(\text{Cs}) = Q_W(\text{Cs})^{\text{SM}}(1 + 0.011S - 0.9(m_Z/m_{Z_\chi})^2 + \dots)$

eg $S = 0.0 \pm 0.4$ $m_{Z_\chi} > 1.2 \text{ TeV}$, leptoquarks, ...

Radiative Corrections to APV

$$\rho_{PV} = 1 - \alpha/2\pi(1/s^2 + 4(1-4s^2)(\ln(m_Z/M)^2 + 3/2) + \dots) \approx \underline{0.99}$$

$$\kappa_{PV}(0) = 1 - \alpha/2\pi s^2((9-8s^2)/8s^2 + (9/4-4s^2)(1-4s^2)(\ln(m_Z/M)^2 + 3/2) - 2/3 \sum (T_{3f} Q_f - 2s^2 Q_f^2) \ln(m_Z/m_f)^2 + \dots) \approx \underline{1.003}$$

$$s^2 \equiv \sin^2 \theta_W(m_Z)_{MS} = 0.23125, \quad M = \text{Hadronic Mass Scale}$$

Radiative Corrections to APV small and insensitive to hadronic unc.

Same Corrections Apply to elastic eN scattering as $Q^2 \rightarrow 0$, $E_e \ll m_N$

E158 at SLAC Pol ee→ee Moller)

$E_e \approx 50 \text{ GeV}$ on fixed target, $Q^2 = 0.02 \text{ GeV}^2$

$$A_{LR}(ee) = -131(14)(10) \times 10^{-9} \propto (1 - 4\sin^2\theta_W)$$

EW Radiative Corrections ~-50%! (Czarnecki & WJM)

Measured to $\pm 12\%$ $\rightarrow \sin^2\theta_W$ to $\pm 0.6\%$

$\rightarrow \sin^2\theta_W(m_Z)_{MS} = 0.2329(13)$ slightly high

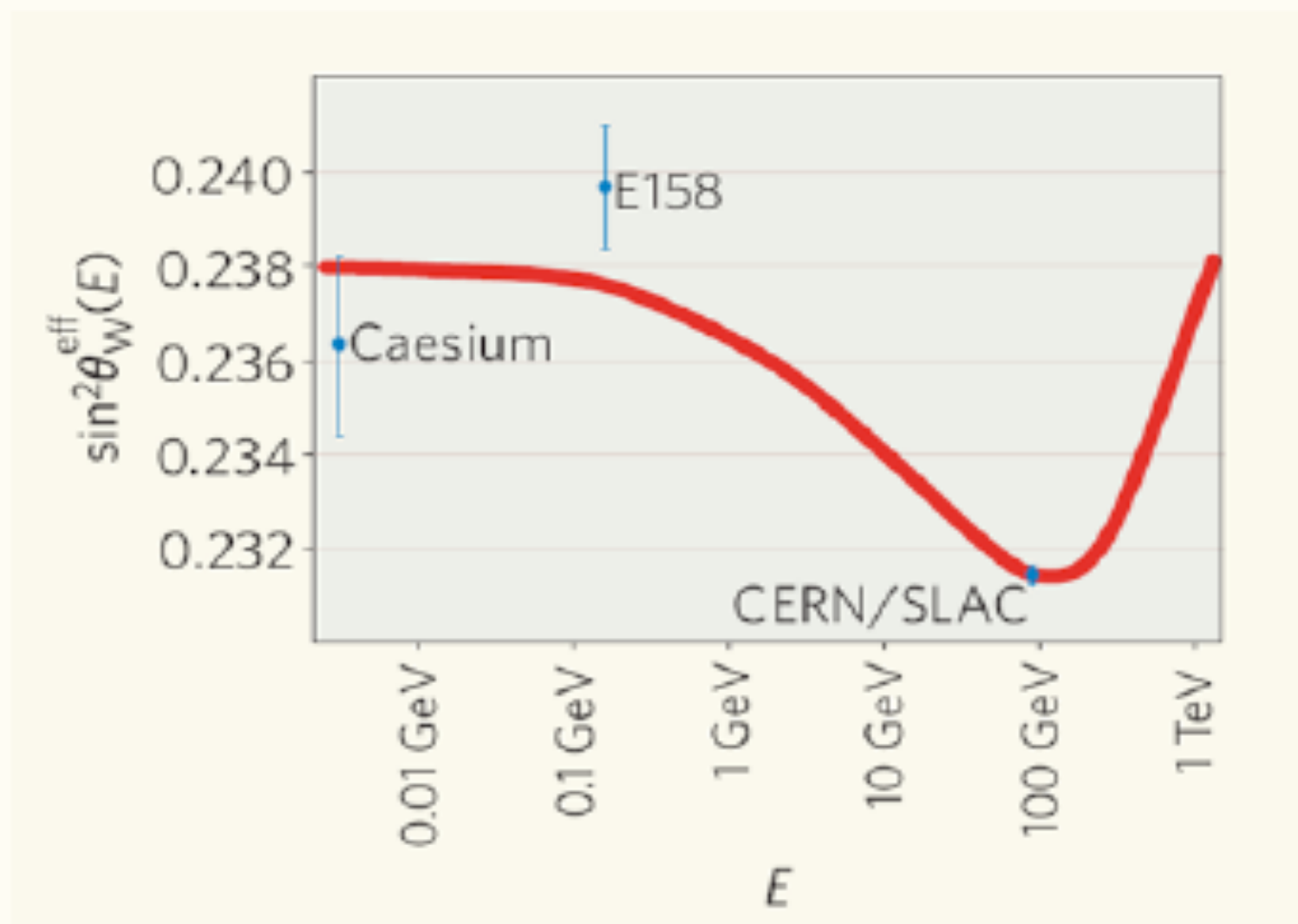
Best Low Q^2 Determination of $\sin^2\theta_W$

Together APV(Cs) & E158 $\rightarrow \sin^2\theta_W(Q^2)$ running

$$A_{LR}(ee)^{\text{exp}} = A_{LR}(ee)^{\text{SM}} (1 + 0.13T - 0.20S + 7(m_Z/m_{Z\chi})^2 \dots)$$

Constrains “New Physics” eq $m_{Z\chi} > 0.6 \text{ TeV}$, H^- , S , Anapole Moment, ...

Running $\sin^2\theta$



Goals of Future Experiments

- High Precision: $\Delta \sin^2 \theta_W \sim 0.00025$ or better
- Low Q^2 Sensitivity to “New Physics”
 $m_{Z'} > 1\text{TeV}$, $|S| < 0.1-0.2$, SUSY Loops, Extra Dim.,
Compositeness.....

Other A_{LR} Experiments

Strange Quark Content Program: Bates, JLAB, MAMI

Proton strange charge radius and magnetic moment consistent with 0. Axial Vector effects and RC cloud strangeness.

PREX Experiment: Neutron distribution

Preparing the way for future experiments, pushing technology and instrumentation, polarization

Future Efforts

QWEAK exp at JLAB being prepared

Will measure forward $A_{LR}(ep \rightarrow ep) \propto (1 - 4\sin^2\theta_W) = Q_W(p)$

$E = 1.1 \text{ GeV}$, $Q^2 \approx 0.03 \text{ GeV}^2$, $\text{Pol} = 0.80 \pm 1\% \rightarrow A_{RL}(ep) \approx 3 \times 10^{-7}$

small A_{RL} requires long running

Goal $\Delta \sin^2\theta_W(m_Z)_{MS} = 0.0008$ via $\pm 4\%$ measurement of A_{LR}

Will be best low energy measurement of $\sin^2\theta_W$

$A_{LR}(ep)^{\text{exp}} = A_{LR}(ep)^{\text{SM}}(1 + 4(m_Z/m_{Z\chi})^2 + \dots)$

eg $m_{Z\chi} \sim 0.9 \text{ TeV}$ Sensitivity (Not as good as APV)

- **The Gorchtein - Horowitz Problem (PRL)**

γZ box diagrams: $O(2\alpha E_e/\pi m_p) \approx 6\%$ of $Q_W(p)$!

RC Estimate needs to be checked

Proposed Qweak Theory Uncertainty $< 2\%$?

JLAB Flagship Experiment (has some theory issue)

Longer Future Efforts: Polarized **Moller** at JLAB
After 12GeV Upgrade

$$A_{LR}(ee \rightarrow ee) \text{ to } \pm 2.5\%$$

$$\Delta \sin^2 \theta_W (m_Z)_{MS} = \pm 0.00025!$$

Comparable to Z pole studies!

$$A_{LR}(ee)^{\text{exp}} = A_{LR}(ee)^{\text{SM}} (1 + 7(m_Z/m_{Z\chi})^2 + \dots)$$

Explores $m_{Z\chi} \rightarrow 1.5\text{TeV}$ Better than APV, $S \sim 0.1$ etc.

Future JLAB Flagship Experiment (difficult!)

[Can any \(Mainz\) Pol. Electron exp. compete with QWEAK/Moller?
\(MESA Low Energy\(0.15GeV\), High Current Energy Recovery Linac](#)

Consider $A_{LR}(eC^{12} \rightarrow eC^{12})_{\text{elastic}} \ 0^+ \rightarrow 0^+$ transition measures $Q_W(C)$

Only Vector Hadronic Current Contributes, CVC!

Not Affected By Strong Interactions at $Q^2=0$ Theoretically Clean!

Proposed MESA Goal Redo QWEAK
(Elastic ep scattering)

- Low Energy 0.15GeV (Theory Cleaner)
- Small Asymmetry (Long Running)
- Polarization (Better than $\pm 1\%$)

BATES EXP $A_{RL}(eC)$ (1978-1990)

- P. Souder et al. PRL65, 694(1990) (Pioneering Effort)

$E_e=0.25\text{GeV}$ Very Modest Effort by today's standards

$P_e=0.37\pm 0.02$ $A_{RL}(eC)^{\text{exp}}=0.60\pm 0.14\pm 0.02\times 10^{-6}$

$Q^2=0.02\text{GeV}^2$ $A_{RL}(eC)^{\text{SM}}=G_\mu Q^2 \rho_{PV} \kappa_{PV} \sin^2\theta_W (m_Z)_{\text{MS}} / \sqrt{2} \pi \alpha$

$I=30\text{-}60\mu\text{A}$ Directly Measures $\sin^2\theta_W (m_Z)_{\text{MS}}=0.20\pm 0.05$

$T=150\text{hrs}$

Current $\pm 25\%$ can be improved to $\pm 1\%$ or better!

$P_e=0.80$, $I=160\mu\text{A}$, $T=1500\text{hrs}$, $20\times$ Acceptance $\rightarrow \pm 0.5\%$!

Essentially Equivalent to APV(Cs) but no Atomic Theory

For Many Types of New Physics $2\times$ Better than QWEAK

But no real theory(RC) uncertainty.

Main Issue: Polarization $\pm 0.5\%$, $\pm 0.3\%$, $\pm 0.2\%$?

Comparison of $Q_W(p)$, $Q_W(Cs)$ & $Q_W(C)$

- $$H_{PV} = G_\mu / \sqrt{2} [(C_{1u} \bar{u} \gamma^\nu u + C_{1d} \bar{d} \gamma^\nu d) \bar{e} \gamma_\nu \gamma_5 e + (C_{2u} \bar{u} \gamma^\nu \gamma_5 u + C_{2d} \bar{d} \gamma^\nu \gamma_5 d) \bar{e} \gamma_\nu e + \dots]$$

$$Q_W(p) = 2(2C_{1u} + C_{1d})$$

$$Q_W(Cs) = 2(188C_{1u} + 211C_{1d})$$

$$Q_W(C) = 2(18C_{1u} + 18C_{1d})$$

$Q_W(C)$ & $Q_W(Cs)$ similar (mainly isoscalar), but measurement of all three \rightarrow over determined.

A $\pm 0.25\%$ determination of $A_{RL}(eC)$ would probe:
 $m_{Z\chi} \sim 1.8\text{TeV}$ (About the same as 12GeV MOLLER)
S ~ 0.15 (Independent of T)

About a factor of 1- 4 better than QWEAK for:

SUSY Loops, Leptoquarks

Similar Sensitivity for Electron Anapole Moment

Can Be Combined with APV(Cs) & QWEAK

Worth A More Careful Study

Do Both QWEAK and $A_{RL}(eC)$ at MESA

Comparable to APV $\rightarrow C_{1u}$ & C_{1d}

What About C_{2u} and C_{2d} ?

- Renormalized at low Q^2 by Strong Interactions

Measure in Deep-Inelastic Scattering (DIS), eD & ep

$$A_{RL}(eD \rightarrow eX) \propto 2 \times 10^{-4} \text{GeV}^{-2} Q^2 [(C_{1u} - C_{1d}/2) + f(y)(C_{2u} - C_{2d}/2)]$$

Standard Model: $C_{1u} = (1 - 8\sin^2\theta_W)/3 \approx 0.20$

$$C_{1d} = -(1 - 4/\sin^2\theta_W)/3 \approx -0.32$$

$$C_{2u} = (1 - 4\sin^2\theta_W)/2 \approx 0.04$$

$$C_{2d} = -(1 - 4\sin^2\theta_W)/2 \approx -0.04$$

C_{2q} sensitive to RC & “New Physics” eg Z_χ (SO(10))

Measure A_{RL} to $\pm 1/2\%$?

Measure C_{2q} to $\pm 1-2\%$? Theory (loops)?

JLAB 6 GeV DIS $eD \rightarrow eX$ On the books

JLAB 12 GeV DIS eD Proposed (Likely)

Goals: Measure C_{2q} s, “New Physics”, Charge Sym. Violation ...

Effective Luminosity (Fixed Target) $10^{38} \text{cm}^{-2} \text{sec}^{-1}$!

What can ep and ed at e-Ion contribute?

Asymmetry $F.O, M, \sim A^2 N$, $A \propto Q^2$, $N \propto 1/Q^2$ (acceptance?)

High Q^2 Better (but Collider Luminosity?)

K. Kumar Talk $\rightarrow 100 \text{fb}^{-1}$ Needed

Program can be started with lower luminosity

Do DIS ep, eD, eN at factor of 10 lower

Single and Double Polarization Asymmetries

Polarized e: $A_{RL}^e = (\sigma_{RR} + \sigma_{RL} - \sigma_{LL} - \sigma_{LR}) / (\sigma_{RR} + \sigma_{RL} + \sigma_{LL} + \sigma_{LR}) \propto P_e$

Polarized p: $A_{RL}^p = (\sigma_{RR} + \sigma_{LR} - \sigma_{RL} - \sigma_{LL}) / (\sigma_{RR} + \sigma_{LR} + \sigma_{RL} + \sigma_{LL}) \propto P_p$

Polarized e&p $A_{RLL}^{ep} = (\sigma_{RR} - \sigma_{LL}) / (\sigma_{RR} + \sigma_{LL}) \propto P_{\text{eff}}$

$P_{\text{eff}} = (P_e - P_p) / (1 - P_e P_p)$ opposite signs

like relativistic velocities addition ≤ 1

eg $P_e = 0.8 \pm 0.008$, $P_p = -0.6 \pm 0.06 \rightarrow P_{\text{eff}} = \underline{0.95 \pm 0.01}$

small uncertainty

How to best utilize P_{eff} ?

LDRD A_{RL} GOALS

Examine Machine and Detector Requirements For $\pm 1\%$

Include EW Radiative Corrections to DIS

Is 100fb^{-1} Sufficient?

Utility of Proton Polarization?

Stage 1 e-Ion aim for $\pm 4\%$

Study Nuclear Effects (EMC, CSV)

Important Secondary e-Ion Goal? Improves Proposal?