Nucleon Structure and the Electron-Ion Collider

Lecture 1: Nucleon Structure and QCD

Christine A. Aidala University of Michigan

> GRK Retreat September 10, 2018

Theory of strong nuclear interactions: Quantum Chromodynamics

- Fundamental field theory in hand since the early 1970s—BUT...
- Quark and gluon degrees of freedom in the theory cannot be observed or manipulated directly in experiment!

Color *confinement*—quarks and gluons are confined to color-neutral bound states



CLAS, PRL 113, 152004 (2014) PRL Editor's Choice Oct. 2014

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How do we understand the visible matter in our universe in terms of the quark and gluon degrees of freedom of quantum chromodynamics?

How can studying QCD systems teach us more about fundamental aspects of QCD as a theory?





The proton as a "laboratory" for studying QCD

- Proton: simplest stable QCD bound state
- Different energy scales offer information on different aspects of proton internal structure











Halzen and Martin, "Quarks and Leptons", p. 201 Christine Aidala, GRK Retreat, Sep 2018











What have we learned in terms of this picture by now?

- Up and down quark "valence" distributions peaked ~1/3
- Lots of sea quarkantiquark pairs and even more gluons!







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Perturbative QCD

- Take advantage of running of strong coupling constant with energy (*asymptotic freedom*)—weak coupling at high energies (short distances)
- Perturbative expansion as in quantum electrodynamics (but many more diagrams due to gluon self-coupling!!)







Perturbative QCD

- Take advantage of running of strong coupling constant with energy (*asymptotic freedom*)—weak coupling at high energies (short distances)
- Perturbative expansion as in quantum electrodynamics (but many more diagrams due to gluon self-coupling!!)



Provides one rigorous way of relating the fundamental field theory to a variety of physical observables!



Factorization and universality in perturbative QCD

- Systematically *factorize* short- and long-distance physics
 - Observable physical QCD processes always involve at least one "long-distance" scale of ~10⁻¹⁵ m describing boundstate structure (confinement)!
- Long-distance (i.e. not perturbatively calculable) functions describing structure need to be *universal*
 - Physically meaningful descriptions
 - Portable across calculations for many processes

Constrain functions describing proton structure by measuring scattering cross sections in many colliding systems over wide kinematic range and performing *simultaneous fits to world data*



Factorization and universality in perturbative QCD

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Note: Nonperturbative lattice QCD techniques have made tremendous progress toward *ab initio* calculations of proton structure in last ~5 years!

Constrain functions describing proton structure by measuring scattering cross sections in many colliding systems over wide kinematic range and performing *simultaneous fits to world data*

PDFs and FFs in pQCD calculations of observables



High-energy processes have predictable rates given:

- Partonic hard scattering rates (calculable in pQCD)
- Parton distribution functions (experiment)
- Fragmentation functions (experiment)

Universal nonperturbative factors





pQCD in action at $\sqrt{s}=200$ GeV





Systematic uncertainty on calculation due to factorization, renormalization, and fragmentation scale dependence. All three scales taken as equal and varied from $p_T/2$ to $2p_T$. Cross section prediction varies by tens of percent here.





Complementary scattering systems

- Learn from p+p results in conjunction with information from simpler systems
 - Many subprocesses contribute to (e.g.) inclusive hadron production in p+p collisions—couldn't disentangle them with p+p data alone
 - (A few processes are simpler, e.g. Drell-Yan process of quark-antiquark annihilation to leptons)
- Most knowledge of PDFs from deep-inelastic leptonnucleon scattering (DIS)
- Most knowledge of fragmentation functions from e+eannihilation to qqbar





17



- Note that Drell-Yan, DIS, and e+e- are all *QED* processes involving hadrons
- Once you have reasonably constrained PDFs and/or FFs, can use p+p data to further refine those constraints
 - Hadronic collisions have been important in constraining *gluons*—interact at leading order. E.g. pion production results 2 slides ago have improved constraints on gluon → pion FFs
 - Hadronic collisions also open up opportunities to explore unique aspects of QCD...





What does the proton look like in terms of the quarks and gluons inside it?

- Position
- Momentum
- Spin
- Flavor
- Color

Vast majority of past four decades focused on *1-dimensional* momentum structure! Since 1990s starting to consider transverse components . . .





What does the proton look like in terms of the quarks and gluons inside it?

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Polarized protons first studied in 1980s. How angular momentum of quarks and gluons add up still not well understood!





What does the proton look like in terms of the quarks and gluons inside it?

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• Color

Good measurements of flavor distributions in valence region. Flavor structure at lower momentum fractions still yielding surprises!





What does the proton look like in terms of the quarks and gluons inside it?

Theoretical and experimental concepts to describe and

access position only born in mid-1990s. Pioneering

measurements over past decade.

- Position
- Momentum
- Spin
- Flavor
- Color





What does the proton look like in terms of the quarks and gluons inside it?

- Position
- Momentum
- Spin
- Flavor

• Color

Accounted for theoretically from beginning of QCD, but more detailed, potentially observable effects of color flow have come to forefront in last few years . . .







0.5

x-Bjorken

0.7

0.2

0.1

Х



0.01

0.02

0.05









25

Quest for ΔG , gluon spin contribution to spin of proton

•



In mid-1990s predictions for the integrated gluon spin contribution to proton spin ranged from 0.7 - 2.3!

 Many models hypothesized large gluon spin contributions to screen the quark spin, but these would then require large orbital angular momentum in the opposite direction





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Proton Spin Mystery Gains a New Clue

Physicists long assumed a proton's spin came from its three constituent quarks. New measurements suggest particles called gluons make a significant contribution

By Clara Moskowitz | July 21, 2014

Protons have a constant spin that is an intrinsic particle property like mass or charge. Yet where this spin comes from is such a mystery it's dubbed the "proton spin crisis." Initially physicists thought a proton's spin was the sum of the spins of its three constituent quarks. But a 1987 experiment showed that quarks can account for only a small portion of a proton's spin, raising the question of where the rest arises. The quarks inside a proton are held together by gluons, so scientists suggested



Brookhaven National Laboratory

perhaps they contribute spin. That idea now has support from a pair of studies analyzing the results of proton collisions inside the Relativistic Heavy-Ion Collider (RHIC) at Brookhaven National Laboratory in Upton, N.Y.

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Synopsis: Gluons Chip in for Proton Spin

July 2, 2014

A new analysis of high-energy data shows that gluons may provide some of the proton's missing spin.



Brookhaven National Laboratory





First evidence for nonzero gluon polarization in proton

• Suite of RHIC measurements sensitive to gluon spin, using different final-state observables



- Jets STAR, PRD86, 032006; PRL 115, 092002
- Neutral pions PHENIX, PRD90, 012007



de Florian, Sassot, Stratmann, Vogelsang, PRL 113, 012001

15 $\Delta \chi^2$ 10 O^2 [GeV] 50 0.05 0.1 0.15 0.2 0.25 0.3 0.35 -0.1 -0.05 0 $\int dx \, \Delta g(x,Q^2)$ Christine Aidala, GRK Retreat, Sep 20

First evidence for nonzero gluon polarization in proton

Suite of RHIC
measurements sensitive
to gluon spin, using
different final-state
observables



But quark spin + (nonzero but small) gluon spin contributions still only add up to ~50% of proton spin → Orbital angular momentum important!



de Florian, Sassot, Stratmann, Vogelsang, PRL 113, 012001

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-0.1 -0.05 0 0.05 0.1 0.15 0.2 0.25 0.3 0.35 $\int_{0.05}^{0.2} dx \, \Delta g(x, Q^2)$

dan kan kan kan kan kan

Spin-momentum correlations: 1976 discovery in p+p collisions

Argonne \sqrt{s} =4.9 GeV



W.H. Dragoset et al., PRL36, 929 (1976)



Had to wait more than a decade for the birth of a new subfield in order to explore the possibilities . . .



 $x_F = 2p_{long} / \sqrt{}$



Transverse-momentum-dependent distributions and single-spin asymmetries



Fig. 1

1990: D.W. Sivers departs from traditional *collinear* factorization assumption in pQCD and proposes correlation between the *intrinsic transverse motion* of the quarks and gluons and the proton's spin

 $s \cdot (p_1 \times p_2)$

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Spin and momenta of quarks and/or bound states



32

Transverse-momentum-dependent distributions and single-spin asymmetries



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First quark distribution function describing a spin-momentum correlation in the proton



Fig. 1



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Spin and momenta of quarks and/or bound states



33

Transverse-momentum-dependent distributions and single-spin asymmetries



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First quark distribution function describing a spin-momentum correlation in the proton

New frontier! Quark dynamics inside QCD bound states, and in their formation process

 $s \cdot (p_1 \times p_2)$

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Spin and momenta of quarks and/or bound states



D.W. Sivers

PRD41, 83 (1990)

-0.2

-0.4

Spin-spin and spin-momentum correlations in QCD bound states





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Spin-spin and spin-momentum correlations in QCD bound states






Spin-spin and spin-momentum correlations in QCD bound states



Lots of evidence from deep-inelastic lepton-nucleon scattering experiments over past ~12 years that many of these correlations

are nonzero in nature!

Spin-momentum correlations





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What about unpolarized TMD functions? Unpolarized TMD PDFs

- Can access via transverse-momentumdependent Drell-Yan, Z, and W boson production
 - Isolate initial state, i.e. access PDFs without FFs
 - Transverse momentum of the final-state Drell-Yan lepton pair, Z, or W for small (nonperturbative) transverse momentum values due to initial-state k_T of the interacting quark and antiquark
 - Larger final-state transverse momenta generated perturbatively via gluon radiation





Unpolarized quark TMD PDFs

- p_T of Z in this region due to k_T vectors of annihilating quark and antiquark
- Perturbatively generated tail out to hundreds of GeV





D'Alesio, Echevarria, Melis, Scimemi JHEP 1411 (2014) 098

Need nonperturbative input to describe Z production at low transverse momentum (here using Soft Collinear Effective Theory, which can be related to the TMD formalism) hristine Aidala, GRK Retreat, Sep 2018



Unpolarized gluon TMD PDFs



- Need more data, but same idea as for Drell-Yan and Z boson production
- k_T vectors of fusing gluons lead to nonperturbative p_T of J/Psi or Higgs; then long perturbative tail





Sea quarks and sea quark dynamics

• Proton-hydrogen and protondeuterium collisions

 $\frac{\sigma^{pd}(x_t)}{2\sigma_{pp}(x_t)} \approx \frac{1}{2} \left[1 + \frac{\bar{d}(x)}{\bar{u}(x)} \right]^*$ *simplest leading-order expression

- Expect anti-down/anti-up ratio of 1 if sea quarks only generated by gluon splitting
- Indicates additional mechanism to generate sea quarks—still not well understood
 - Recent review: Chang and Peng, Prog. Part. Nucl. Phys. 79, 95 (2014)



Fermilab E866 data: PRD64, 052002 (2001) CERN NA51 data: PLB332, 244 (1994)





Sea quarks—many hints of interesting behavior already!



Data from E537 (pbar+W): PRD38, 1377 (1988) E439: (p+W): AIP Conf. Proc. 45, 93 (1978)

- p+W: (Valence) quark from p, (sea) antiquark from W
- pbar+W: (Valence) quark from W, (valence) antiquark from pbar
- (Valence × sea) spectrum harder → Larger mean k_T for sea than valence quarks?
 - Agrees with chiral soliton model predictions (e.g. Schweitzer, Strikman, Weiss 2013)
 - Consistent with work by Bacchetta et al.





46

Sea quark spin-spin correlations (helicity distributions)

$\Delta q(x), \Delta \overline{q}(x)$



$$A_L^{W^+} \approx -\frac{\Delta u(x_1)\overline{d}(x_2) - \Delta \overline{d}(x_1)u(x_2)}{u(x_1)\overline{d}(x_2) - \overline{d}(x_1)u(x_2)}$$

$$A_L^{W^-} \approx -\frac{\Delta d(x_1)\overline{u}(x_2) - \Delta \overline{u}(x_1)d(x_2)}{d(x_1)\overline{u}(x_2) - \overline{u}(x_1)d(x_2)}$$

Parity violation of weak interaction + control over proton spin orientation gives access to *flavor*-spin structure of proton

 u_R









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48

World W cross section measurements







Large parity-violating single-helicity asymmetries



Improve constraints on light antiquark helicity distributions

$$A_{L} = \frac{1}{P} \frac{N^{+} / L^{+} - N^{-} / L^{-}}{N^{+} / L^{+} + N^{-} / L^{-}}$$



Flavor asymmetry in the sea helicity distributions

NNPDF, NPB 887.276 (2014)





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Transverse spin-spin correlation for sea quarks also nonzero and flavor-asymmetric?



Initial lattice calculation finds "transversity" for sea nonzero and flavor-asymmetric! Chen et al., arXiv:1603.06664

Also chiral quark soliton model Schweitzer et al., PRD64, 034043 (2001)

 $\delta \bar{q}(x) = -\delta q(-x)$

No constraining measurements yet





Spin-spin correlations (collinear or TMD): Helicity vs. transverse spin structure

- Transverse spin structure of the proton cannot be deduced from helicity structure
 - Spatial rotations and Lorentz boosts don't commute
 - Relationship between longitudinal and transverse structure provides information on the relativistic nature of partons in the proton
 - Even collinear transverse spin structure (transversity) should thus be linked to parton k_T





Spin-spin correlations in terms of helicity

Elastic proton-quark scattering

(related to inelastic scattering through optical theorem)

Three independent pdfs corresponding to following helicity states in scattering:



Helicity basis not "natural" for transversity

Corresponds to difference in probability of scattering off of transversely polarized quark within transversely polarized proton with quark spin parallel vs. antiparallel to proton's

Take linear combinations to form familiar collinear pdfs:

$$q \quad \longleftrightarrow \quad \left(\begin{array}{ccc} \frac{1}{2} & \frac{1}{2} & \rightarrow & \frac{1}{2} & \frac{1}{2} \end{array}\right) + \left(\begin{array}{ccc} \frac{1}{2} & -\frac{1}{2} & \rightarrow & \frac{1}{2} & -\frac{1}{2} \end{array}\right)$$
$$\Delta q \quad \longleftrightarrow \quad \left(\begin{array}{ccc} \frac{1}{2} & \frac{1}{2} & \rightarrow & \frac{1}{2} & \frac{1}{2} \end{array}\right) - \left(\begin{array}{ccc} \frac{1}{2} & -\frac{1}{2} & \rightarrow & \frac{1}{2} & -\frac{1}{2} \end{array}\right)$$
$$\delta q \quad \longleftrightarrow \quad \left(\begin{array}{ccc} \frac{1}{2} & -\frac{1}{2} & \rightarrow & -\frac{1}{2} & \frac{1}{2} \end{array}\right)$$



Helicity average (unpolarized pdf) Helicity difference (helicity pdf) Helicity flip (transversity pdf)



Semi-inclusive DIS "Sivers" spin-momentum correlations larger for K^+ than π^+





COMPASS, PLB744, 250 (2015)

Due to strangeness? K+: $u\bar{s}$ π +: $u\bar{d}$

NSF

Large K⁻ and antiproton transverse single-spin asymmetries in p+p at RHIC



We have a lot to learn about the nucleon sea!



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Need more data for sea quarks!

• And with more measurements to provide meaningful constraints, will need consistent treatment of sea quarks in theory/phenomenology



• Understanding the *dynamics* of sea quarks, which probe beyond static pictures of antiquarks in the nucleon, will be crucial to understanding how the nucleon sea is generated (and what in fact it is!)



Relationship between gluons and sea quarks

- What can be learned about gluons from sea quark distributions, and vice-versa, for
 - unpolarized, collinear PDFs?
 - helicity PDFs?
 - transversity PDFs and linearly polarized gluons?
 - TMD PDFs?
- Perturbative vs. nonperturbative interplay between sea quarks and gluons?
 - Do the nonperturbative mechanisms that must be generating the flavor asymmetry observed in the unpolarized, collinear sea affect gluon distributions at all?
 - In the low-x regime, is the relationship between gluons and sea quarks straightforward?





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 - Do the nonperturbative mechanisms that must be generating the flavor asymmetry observed in the unpolarized, collinear sea affect gluon distributions at all?
 - In the low-x regime, is the relationship between gluons and sea quarks straightforward?
- What role does Q² evolution play in the relationship?
 - Is this role exactly the same for DGLAP vs. CSS evolution, i.e. are collinear and TMD PDFs affected differently?
 - What about evolution of the transversity distributions?
- Recent work on gluons in nuclei that aren't associated with a single nucleon. Does this have implications for sea quarks not associated with a single nucleon?
 - Any relationship to pion exchange models? (See next lecture for more on nuclear PDFs)





Proton vs. neutron sea

- Isospin symmetry between proton and neutron ultimately an approximation
- Different masses
 - Well, okay, only a 0.1% difference here.
- What about different magnitudes of electromagnetic charges of valence quarks?
 Thinking in particular of a "dilute" picture of a nucleon, could this affect parton spin-momentum correlations or other dynamics?





Baryon vs. meson sea

- Would naively expect dynamics of valence quarks in baryons vs. mesons to be different. Also dynamics of sea quarks?
 - Three-(anti)quark system vs. quark-antiquark pair
 - Baryons as fermions vs. mesons as bosons—different spins
- Is strangeness suppressed in the sea of the phi meson through Pauli blocking? Charm suppressed in the sea of the J/Psi? Does it even make sense to think of these resonances as having a "sea"?
- Do different binding energies e.g of different heavy quarkonium states lead to different dynamics in the sea, or of the valence quarks?





61

What do we really mean by "valence" and "sea" anyway??

- At any given instant, the proton has a net up content of 2 and net down content of 1, which determines the +1 charge.
- It also determines the total spin somehow . . .





What do we really mean by "valence" and "sea" anyway??

- At any given instant, the proton has a net up content of 2 and net down content of 1, which determines the +1 charge.
- It also determines the total spin somehow . . .
- We talk about "the valence quarks" being at large x, but e.g. Drell-Yan experiments have already measured (sea) antiquarks up to 0.35. Is it meaningful to think also of sea *quarks* at these high x values, i.e. up or down sea quarks rather than antiup or antidown?
 - If we measure an up or down quark at x~0.35, we call it "valence."
 - So what do hints of different dynamics for sea quarks than "valence" quarks mean? Should what we call "valence" vs. "sea" be associated with different processes/behavior within the proton?







Back to those huge spin-momentum correlations in proton-proton collisions...



Back to those huge spin-momentum correlations in proton-proton collisions...



Much larger spin-momentum correlations, and strikingly similar effects across energies!







Single-spin asymmetries in transversely polarized proton-proton collisions





Effects persist to kinematic regimes where perturbative QCD techniques clearly apply







proton-proton → pion + X: Challenging to interpret

• Always huge effects!

 But in p+p → pion +X don't have enough information to separate initial-state (proton structure) from final-state (pion formation) effects

• Need to think more carefully . . .





Different symmetry properties for different spin-momentum correlations

• Some transverse-momentum-dependent parton distribution functions odd under a parity- and time-reversal (PT) transformation







Different symmetry properties for different spin-momentum correlations

- Some transverse-momentum-dependent parton distribution functions odd under a parity- and time-reversal (PT) transformation
- In 1993, after original 1990 paper by D.W. Sivers, J.C. Collins claimed such functions must vanish





Different symmetry properties for different spin-momentum correlations

- Some transverse-momentum-dependent parton distribution functions odd under a parity- and time-reversal (PT) transformation
- In 1993, after original 1990 paper by D.W. Sivers, J.C. Collins claimed such functions must vanish
- Only realized in 2002 by Brodsky, Hwang, and Schmidt that could be nonvanishing if *phase interference effects due to color interactions* present





Modified universality of PT-odd correlations: Color in action!

Deep-inelastic lepton-nucleon scattering: Final-state color exchange Quark-antiquark annihilation to leptons: Initial-state color exchange



Opposite sign for PT-odd transverse-momentum-dependent distributions measured in these two processes: *process-dependent*! (Collins 2002)



Figures by J.D. Osborn

71

Modified universality: Initial experimental hints



First measurements by STAR at RHIC and COMPASS at CERN suggestive of predicted sign change in color-annihilation processes compared to quark knock-out by an electron. More statistics forthcoming . . .




Modified universality requires full QCD: Gauge-invariant quantum field theory

We have ignored here the subtleties needed to make this a gauge invariant definition: an appropriate path ordered exponential of the gluon field is needed [18].



Brodsky, Hwang, Schmidt, PL B530 (2002) 99 - Collins, PL B536 (2002) 43

An earlier proof that the Sivers asymmetry vanishes because of time-reversal invariance is invalidated by the path-ordered exponential of the gluon field in the operator definition of parton densities. Instead, the time-reversal argument shows that the Sivers asymmetry is reversed in sign in hadron-induced hard processes (e.g., Drell-Yan), thereby violating naive universality of parton densities. Previous phenomenology with time-reversal-odd parton densities is therefore validated.

$$[f_{1T}^{q\perp}]_{\text{SIDIS}} = -[f_{1T}^{q\perp}]_{\text{DY}}$$

From 1993 claim by J.C. Collins that such processes must vanish

Slide from M. Anselmino, Transversity 2014





Physical consequences of a gauge-invariant quantum theory: Aharonov-Bohm (1959)

Wikipedia:

"The Aharonov–Bohm effect is important conceptually because it bears on three issues apparent in the recasting of (Maxwell's) classical electromagnetic theory as a gauge theory, which before the advent of quantum mechanics could be argued to be a mathematical reformulation with no physical consequences. The Aharonov–Bohm thought experiments and their experimental realization imply that the issues were not just philosophical.

The three issues are:

- whether potentials are "physical" or just a convenient tool for calculating force fields;
- whether action principles are fundamental;
- the principle of locality."





Physical consequences of a gauge-invariant quantum theory: Aharonov-Bohm (1959)

Physics Today, September 2009 : The Aharonov–Bohm effects: Variations on a subtle theme, by Herman Batelaan and Akira Tonomura.

"Aharonov stresses that the arguments that led to the prediction of the various electromagnetic AB effects apply equally well to any other gauge-invariant quantum theory. In the standard model of particle physics, the strong and weak nuclear interactions are also described by gauge-invariant theories. So one may expect that particle-physics experimenters will be looking for new AB effects in new domains."





Physical consequences of a gauge-invariant quantum theory: Aharonov-Bohm effect in QCD!!

Deep-inelastic lepton-nucleon scattering: Final-state color exchange



Quark-antiquark annihilation to leptons: Initial-state color exchange



See e.g. Pijlman, hep-ph/0604226 or Sivers, arXiv:1109.2521





Physical consequences of a gauge-invariant quantum theory: Aharonov-Bohm effect in QCD!!

Deep-inelastic lepton-nucleon scattering: Final-state color exchange **Quark-antiquark annihilation to leptons: Initial-state color exchange**



QCD Aharonov-Bohm effect: Color entanglement

- 2010: T.C. Rogers and P. Mulders predict *color entanglement* in processes involving proton-proton production of QCD bound states if quark transverse momentum taken into account
- Quarks become correlated *across* the two colliding protons
- Consequence of QCD specifically as a *non-Abelian* gauge theory!



$$p + p \rightarrow h_1 + h_2 + X$$

Color flow can't be described as flow in the two gluons separately. Requires presence of both.





QCD Aharonov-Bohm effect: Color entanglement

- 2010: T.C. Rogers and P. Mulders predict *color entanglement* in processes involving proton-proton production of QCD bound states if quark transverse momentum taken into account
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$$p + p \rightarrow h_1 + h_2 + X$$

Color flow can't be described as flow in the two gluons separately. Requires presence of both.

Huge transverse spin asymmetries in p+p a color entanglement effect??



Searching for evidence of color entanglement at RHIC

- Need observable sensitive to a nonperturbative momentum scale
 - Nearly back-to-back particle production
- Need 2 initial QCD bound states
 - color exchange between a scattering quark and remnant of other proton
- And at least 1 final QCD bound state
 - exchange between scattered quark and either remnant

→ In p+p collisions, measure out-ofplane momentum component in nearly back-to-back photon-hadron and hadron-hadron production







Out-of-plane momentum component distributions



- Gaussian near 0 nonperturbative transverse momentum
- Power-law at large
 p_{out}—kicks from hard
 (perturbative) gluon
 radiation
- Different colors → different bins in hard interaction scale



PRD95, 072002 (2017)

Curves are fits to Gaussian and Kaplan functions, not calculations!





Look at evolution of nonperturbative transverse momentum widths with hard scale (Q^2)

- Proof of factorization (i.e. no entanglement) for processes sensitive to nonperturbative transverse momentum directly predicts that nonperturbative transverse momentum widths *increase* as a function of the hard scattering energy scale
 - Increased phase space for gluon radiation





Look at evolution of nonperturbative transverse momentum widths with hard scale (Q^2)

- Proof of factorization (i.e. no entanglement) for processes sensitive to nonperturbative transverse momentum directly predicts that nonperturbative transverse momentum widths *increase* as a function of the hard scattering energy scale
 - Increased phase space for gluon radiation
- Confirmed experimentally in deep-inelastic lepton-nucleon scattering (left) and quark-antiquark annihilation to leptons (right)



Evolution of nonperturbative momentum widths in processes where entanglement predicted

- No clear qualitative difference observed. Will need *quantitative* calculations from theorists to draw a conclusion.
 - Perform calculations assuming factorization holds, and look for discrepancies with measurement.
 - Currently no idea how to perform calculations for partons entangled across colliding protons!



Stay tuned! Discussions of other potential observables ongoing . . .





84

A cyclical process



Synthesis



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Summary

- The proton as the simplest stable QCD bound state serves as a "laboratory" to study the behavior of quarks and gluons confined in color-neutral states
 - But should keep in mind that what we learn about the internal structure and dynamics of the proton won't represent all QCD bound states
 - E.g. spin-1/2 fermion vs. pseudoscalar vs. vector bosons—partitioning of angular momentum must be different
 - Isospin mapping from proton to neutron not exact
- Puzzles remain
 - How exactly is the proton spin generated from its constituents, and how should we think about orbital angular momentum in confined systems more generally?
 - What generates the 40% asymmetries in spin-momentum correlations in $p+p \rightarrow hadrons$?





Summary

- And there is much still to be learned
 - How can we relate partonic pictures of hadrons in the highenergy limit to internal dynamics at lower energies, where a partonic picture shouldn't apply?
 - p+p → h+X transverse single-spin asymmetries show remarkably similar behavior across a huge range of energies
 - What are the nonperturbative dynamics governing sea quarks?
 - What are the spatial distributions of quarks and gluons around the charge center of the proton? (See next lecture)
 - How is the behavior or quarks and gluons modified in a nucleus compared to a nucleon? (See next lecture)
 - Is there a universal state of hadronic matter when considering the smallest parton momentum fractions, i.e. gluon saturation? (See next lecture)



Summary

- Gradually shifting to think about QCD systems in new ways, focusing on topics/ideas/concepts that have long been familiar to the world of condensed matter and atomic, molecular, and optical physics
 - All sorts of correlations within systems
 - Quantum mechanical phase interference effects
 - Quantum entangled systems

• These new ways of thinking will help deepen our understanding of QCD as a non-Abelian quantum gauge theory











Advancing into the era of quantitative QCD: Theory has been forging ahead

• In perturbative QCD, since 1990s starting to consider detailed internal *dynamics* that parts with traditional parton model ways of looking at hadrons—and perform <u>phenomenological calculations</u> using these new ideas/tools!

E.g.:

- Various *resummation* techniques
- Non-linear evolution at small momentum fractions
- Spin-spin and spin-momentum correlations in QCD bound states
- Spatial distributions of partons in QCD bound states
- Nonperturbative methods:
 - Lattice QCD less and less limited by computing resources—since 2010 starting to perform calculations at the physical pion mass (after 36 years!). Plus recent new ideas on how to calculate previously intractable quantities.
 - AdS/CFT "gauge-string duality" an exciting recent development as first fundamentally new handle to try to tackle QCD in decades!



Effective field theories

- QCD exhibits different behavior at different scales—effective field theories are useful approximations within these different regimes
 - Color Glass Condensate high energies, high densities
 - Soft-Collinear Effective Theory new insights into performing complicated perturbative calculations very quickly
 - Chiral Effective Theory, Heavy Quark Effective Theory, Non-Relativistic QCD, . . .
 - Many effective theories for nonperturbative QCD chiral symmetry breaking, . . .





Parton distribution functions in perturbative QCD calculations of observables



High-energy processes have predictable rates given:

- Partonic hard scattering rates (calculable in pQCD)
- Parton distribution functions (experiment or lattice)
- Fragmentation functions (experiment or lattice)



Universal nonperturbative factors

Transverse Momentum Dependent Nonperturbative Functions Transverse Momentum

Dependent Quark PDFs:



- Also TMD PDFs for gluons, except they can't be transversely polarized
- Corresponding TMD
 Fragmentation
 Functions
- Collins-Soper-Sterman evolution equations



Forward transverse single-spin asymmetries for neutral pions







TSSA at Higher Energies



(STAR Collaboration) *Phys. Rev. Lett.* **101**, 222001 (2008)

Yuxi Pan for the STAR Collaboration International Journal of Modern Physics: Conference Series **40**, 1660037 (2016)







Partonic process contributions for direct photon production



Quark-gluon Compton scattering still dominates at NLO -PLB140, 87 (1984)

PHENIX Collab., arXiv:1609.04769, Submitted to PRD. Calculation by T. Kaufmann







Two-particle correlation distributions show expected jet-like structure



PRD95, 072002 (2017)



Christine Aidala, GRK Retreat, Sep 2018



Links to "color coherence" at Tevatron and LHC?

- D0, CDF, CMS have all published evidence for "color coherence effects"
 - CMS: EPJ C74, 2901 (2014)
 - CDF: PRD50, 5562 (1994)
 - D0: PLB414, 419 (1997)
- Few citations—relatively little-known work thus far. Need to get different communities talking to explore detailed color effects more in upcoming years!







TSSAs in $p^{\uparrow} + p$

Large TSSA in $p^{\uparrow} + p \rightarrow h + X$

- Uncovered the need for a TMD framework
- Not sensitive to soft scale $k_T \rightarrow$ Only one (hard) scale available: p_T





Multiparton correlations in hadronization

- Traditional fragmentation functions describe probability of single parton to hadronize into particular hadron, as function of momentum fraction (z) of parton carried by the final hadron
- Can have matrix elements describing *multiparton correlations in hadronization*
 - Interference between a (quark+gluon) hadronizing and only a quark
 - Similarly, interference between (gluon+gluon) and only a single gluon
 - Kanazawa+Koike, 2000





Summary of spin-momentum correlation results

- Clear empirical evidence for nonzero
 - Sivers TMD pdf correlation between proton transverse spin and quark transverse momentum
 - SIDIS
 - Collins TMD FF correlation between quark transverse spin and transverse momentum of produced hadron
 - e+e-, SIDIS
 - Boer-Mulders TMD pdf correlation between quark transverse spin and quark transverse momentum
 - Drell-Yan, SIDIS
- Hints from SIDIS measurements (in backup) of nonzero
 - Worm gear TMD pdf correlation between proton transverse spin, quark longitudinal spin, quark transverse momentum
 - Pretzelosity TMD pdf correlation between proton transverse spin, perpendicular quark transverse spin, quark transverse momentum
- Also clear evidence for nonzero helicity and transversity collinear pdfs from SIDIS and p+p, collinear dihadron interference FF from e+e-, SIDIS, p+p



High-energy QCD: Thinking in terms of individual partons

- PDFs are *single-parton* functions in *single* nucleons
 - Or in nuclei, but typically still think of partons in individual nucleons within nucleus

• Can we go beyond this single-parton picture while staying in the hard (short-distance) limit of perturbative QCD?





An alternative approach to describing the large single-spin asymmetries: Higher-twist multiparton correlations

- Extend our ideas about (single-parton) pdfs to correlation functions that can't be associated with a single parton
- Non-perturbative structure → matrix elements involving the quantum mechanical *interference* between scattering off of a (quark+gluon) and scattering off of a single quark (of the same flavor and at the same x)
 - Can also have interference between (gluon+gluon) and single gluon
 - No explicit dependence on partonic transverse momentum
 - Efremov+Teryaev 1981, 84; Qiu+Sterman 1991, 98





Beware: Two common usages of the term "twist"

- Formal definition of twist: "mass dimension minus spin" of the operator in a matrix element within the Operator Product Expansion
 - "Leading twist" is twist-2
 - Twist-n *matrix element* carries a factor of 1/Q⁽ⁿ⁻²⁾
- But *observables* with measurable contributions from terms suppressed by a factor of $1/Q^{(n-2)}$ often referred to as sensitive to "twist-n" contributions
 - Never measure a matrix element, only matrix elements squared!
 - To get 1/Q term describing an *observable*, need interference term in the square modulus:
 - A = order 1 + order 1/Q + order $1/Q^2$ + ...
 - $|A|^2 = |order 1|^2 + |order 1/Q|^2 + (order 1)(order 1/Q)^* + (order 1)^*(order 1/Q) + \dots$
 - So twist-3 term in matrix element times twist-2 term gives 1/Q
 - Square modulus of *twist-3* term gives $1/Q^2$, sometimes referred to as "twist-4"



Transverse single-spin asymmetries provide <u>new</u> information on hadron structure

- <u>Leading</u> contribution to transverse single-spin asymmetries comes from *either*:
 - Convolution of two twist-2 *transverse-momentumdependent* parton distribution functions and/or fragmentation functions, or . . .
 - Convolution of one twist-2 collinear pdf or fragmentation function and one twist-3 (collinear) *multiparton correlation* matrix element



