



# Light from Cascading Partons in Relativistic Heavy-Ion Collisions

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- Motivation
- The PCM: Fundamentals & Implementation
- Photon production in the PCM
- Medium Effects: Jet-Photon Conversion (FMS Photons)



# Part #1:

# Photon Production in the PCM

- *Light from cascading partons in relativistic heavy-ion collisions*  
- S.A. Bass, B. Mueller and D.K. Srivastava, Phys. Rev. Lett. **90** (2003) 082301
- *Intensity interferometry of direct photons in Au+Au collisions*  
- S.A. Bass, B. Mueller and D.K. Srivastava, Phys. Rev. Lett. **93** (2004) 162301
- *Dynamics of the LPM effect in Au+Au Collisions at 200 AGeV*  
- T. Renk, S.A. Bass and D.K. Srivastava, nucl-th/0505059



# Basic Principles of the PCM

**Goal:** provide a microscopic space-time description of relativistic heavy-ion collisions based on perturbative QCD

- degrees of freedom: quarks and gluons
- classical trajectories in phase space (with relativistic kinematics)
- initial state constructed from experimentally measured nucleon structure functions and elastic form factors
- an interaction takes place if at the time of closest approach  $d_{min}$  of two partons

$$d_{min} \leq \sqrt{\frac{\sigma_{tot}}{\pi}} \quad \text{with} \quad \sigma_{tot} = \sum_{p_3, p_4} \int \frac{d\sigma(\sqrt{\hat{s}}; p_1, p_2, p_3, p_4)}{d\hat{t}}$$

- system evolves through a sequence of binary (2→2) elastic and inelastic scatterings of partons and initial and final state radiations within a leading-logarithmic approximation (2→N)
- binary cross sections are calculated in leading order pQCD with either a momentum cut-off or Debye screening to regularize IR behavior
- guiding scales: initialization scale  $Q_0$ ,  $p_T$  cut-off  $p_0$  / Debye-mass  $\mu_D$



# Parton-Parton Scattering Cross-Sections

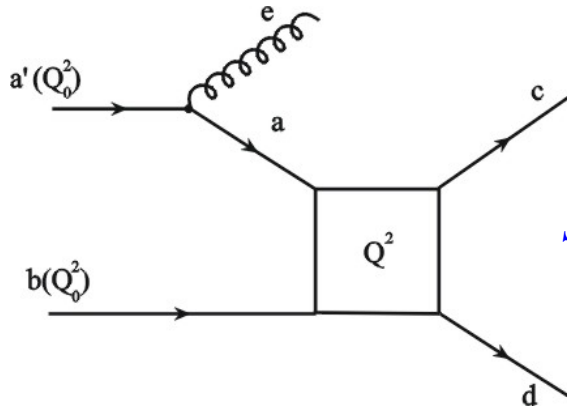
$g g \rightarrow g g$	$\frac{9}{2} \left( 3 - \frac{tu}{s^2} - \frac{su}{t^2} - \frac{st}{u^2} \right)$	$q q' \rightarrow q q'$	$\frac{4}{9} \frac{s^2 + u^2}{t^2}$
$q g \rightarrow q g$	$-\frac{4}{9} \left( \frac{s}{u} + \frac{u}{s} \right) + \frac{s^2 + u^2}{t^2}$	$q qbar \rightarrow q' qbar'$	$\frac{4}{9} \frac{t^2 + u^2}{s^2}$
$g g \rightarrow q qbar$	$\frac{1}{6} \left( \frac{t}{u} + \frac{u}{t} \right) - \frac{3}{8} \frac{t^2 + u^2}{s^2}$	$q g \rightarrow q \gamma$	$-\frac{e_q^2}{3} \left( \frac{u}{s} + \frac{s}{u} \right)$
$q q \rightarrow q q$	$\frac{4}{9} \left( \frac{s^2 + u^2}{t^2} + \frac{s^2 + t^2}{u^2} \right) - \frac{8}{27} \frac{s^2}{tu}$	$q qbar \rightarrow g \gamma$	$\frac{8}{9} e_q^2 \left( \frac{u}{t} + \frac{t}{u} \right)$
$q qbar \rightarrow q qbar$	$\frac{4}{9} \left( \frac{s^2 + u^2}{t^2} + \frac{u^2 + t^2}{s^2} \right) - \frac{8}{27} \frac{u^2}{st}$	$q qbar \rightarrow \gamma \gamma$	$\frac{2}{3} e_q^4 \left( \frac{u}{t} + \frac{t}{u} \right)$
$q qbar \rightarrow g g$	$\frac{32}{27} \left( \frac{t}{u} + \frac{u}{t} \right) - \frac{8}{3} \frac{t^2 + u^2}{s^2}$		

- a common factor of  $\pi \alpha_s^2(Q^2)/s^2$  etc.
- further decomposition according to color flow



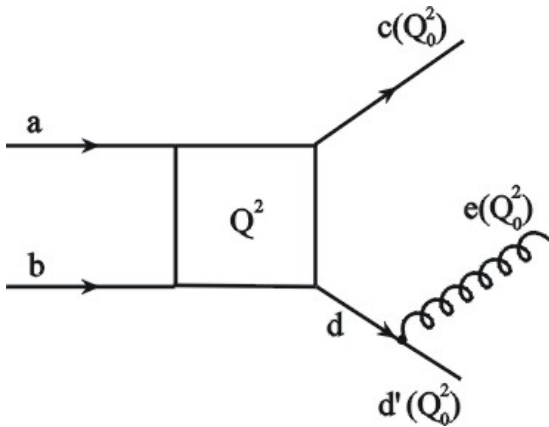
# Initial and final state radiation

Probability for a branching is given in terms of the Sudakov form factors:



**space-like branchings:**

$$S_a(x_a, t_{\max}, t) = \exp \left\{ - \int_t^{t_{\max}} dt' \frac{\alpha_s(t')}{2\pi} \sum_{a'} \int dz P_{a' \rightarrow ae}(z) \frac{x_{a'} f_{a'}(x_{a'}, t')}{x_a f_a(x_a, t')} \right\}$$



**time-like branchings:**

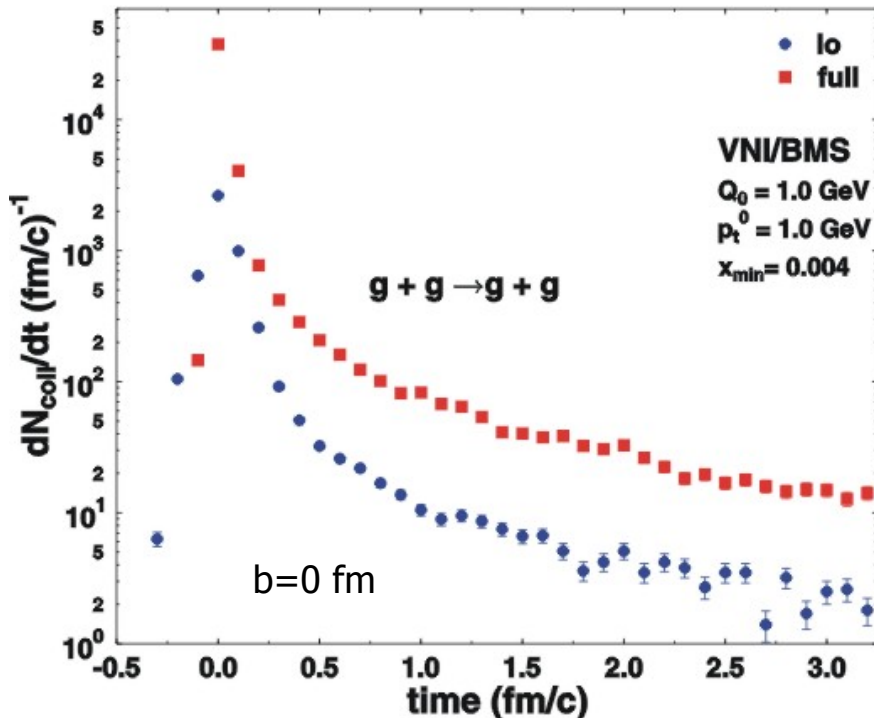
$$T_d(x_d, t_{\max}, t) = \exp \left\{ - \int_t^{t_{\max}} dt' \frac{\alpha_s(t')}{2\pi} \sum_{a'} \int dz P_{d \rightarrow d'e}(z) \right\}$$

- Altarelli-Parisi splitting functions included:  
 $P_{q \rightarrow qg}$ ,  $P_{g \rightarrow gg}$ ,  $P_{g \rightarrow qqbar}$  &  $P_{q \rightarrow q\gamma}$



# Collision Rates & Numbers

Au+Au;  $E_{\text{CM}}=200$  AGeV



# of collisions	lo	full
q + q	70.6	274
q + qbar	1.3	38.52
q + g	428.3	2422.6
g + g	514.4	4025.6

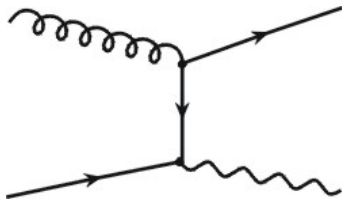
- lifetime of interacting phase:  $\sim 3$  fm/c
- partonic multiplication due to the initial & final state radiation increases the collision rate by a factor of 4-10
- are time-scales and collision rates sufficient for thermalization?



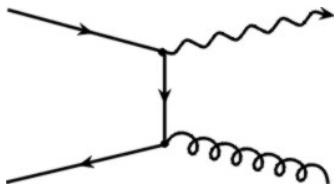
# Photon Production in the PCM

relevant processes:

• Compton:  $q g \rightarrow q \gamma$



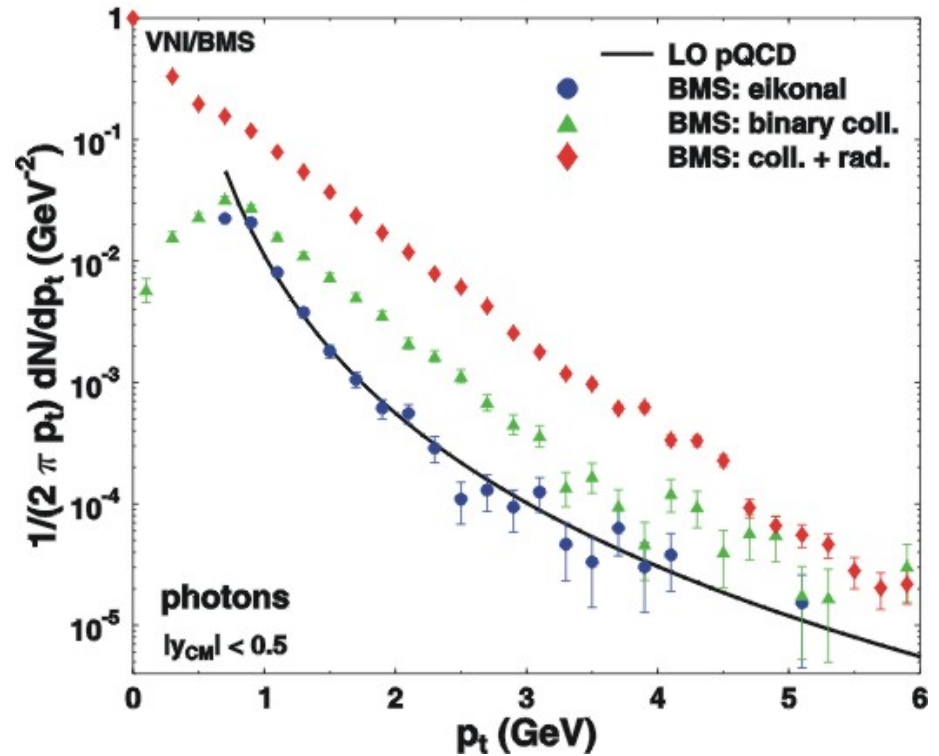
• annihilation:  $q qbar \rightarrow g \gamma$



• bremsstrahlung:  $q^* \rightarrow q \gamma$



Au+Au;  $E_{CM}=200$  AGeV

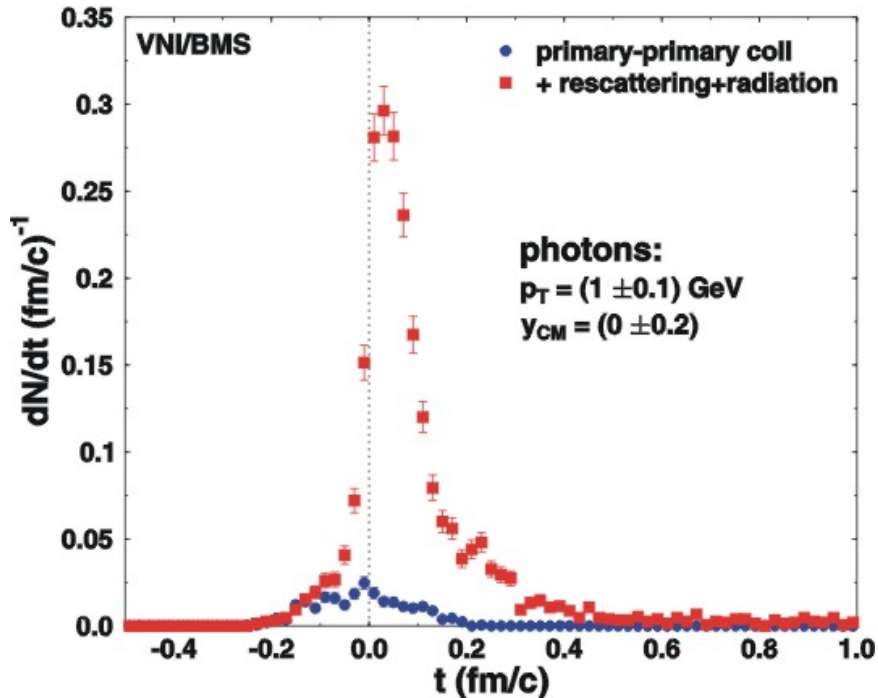


➤ photon yield very sensitive to parton-parton rescattering



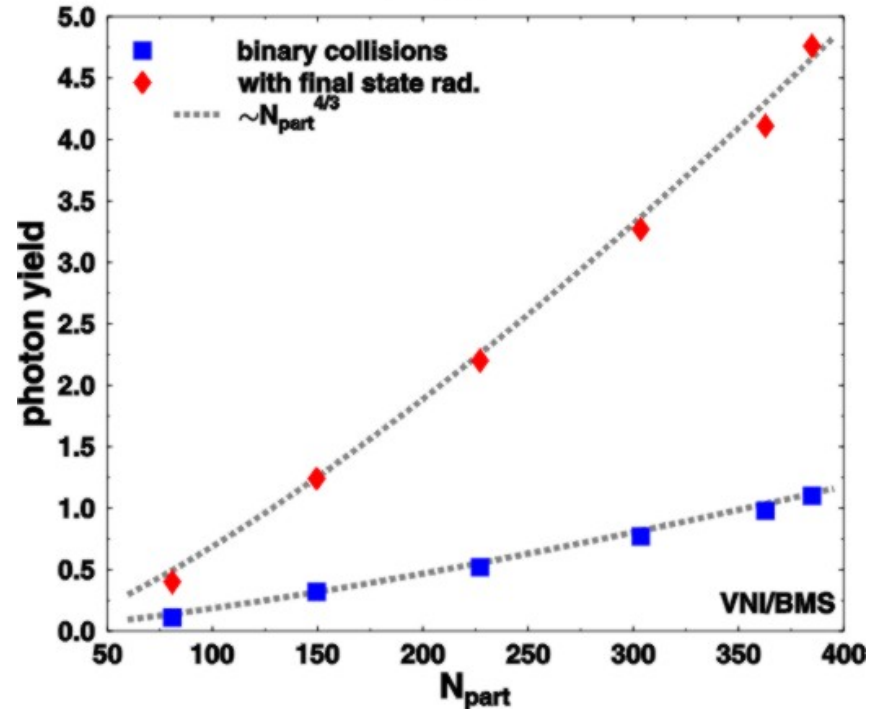
# What can we learn from photons?

Au+Au @ 200 AGeV



- primary-primary collision contribution to yield is  $< 10\%$
- emission duration of pre-equilibrium phase:  $\sim 0.5 \text{ fm}/c$

Au+Au;  $E_{\text{CM}}=200 \text{ AGeV}$

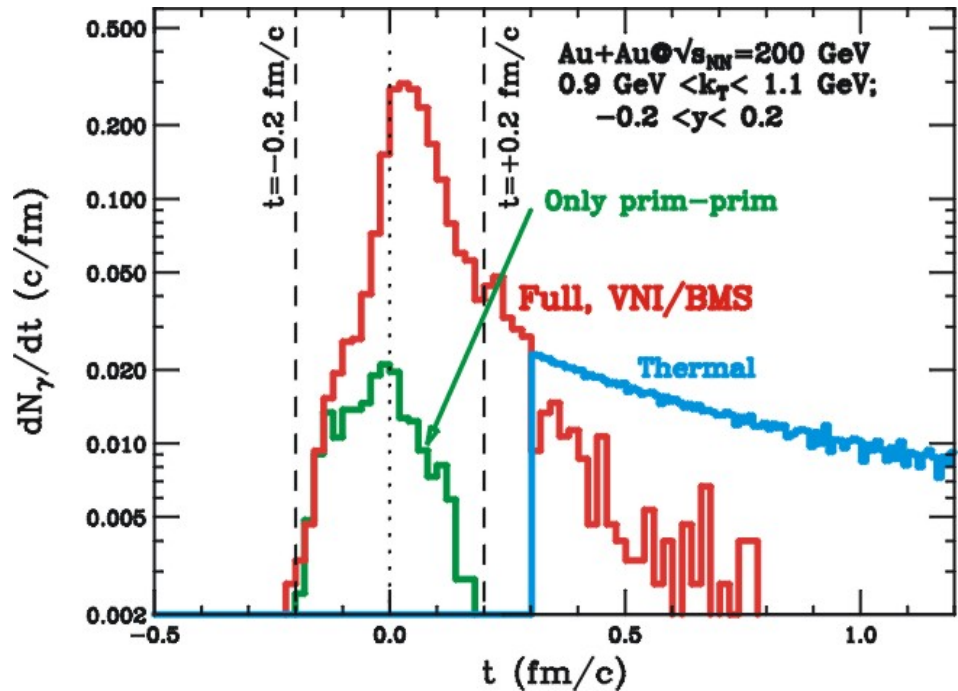


- photon yield directly proportional to the # of hard collisions
- photon yield scales with  $N_{\text{part}}^{4/3}$





# Photons: pre-equilibrium vs. thermal



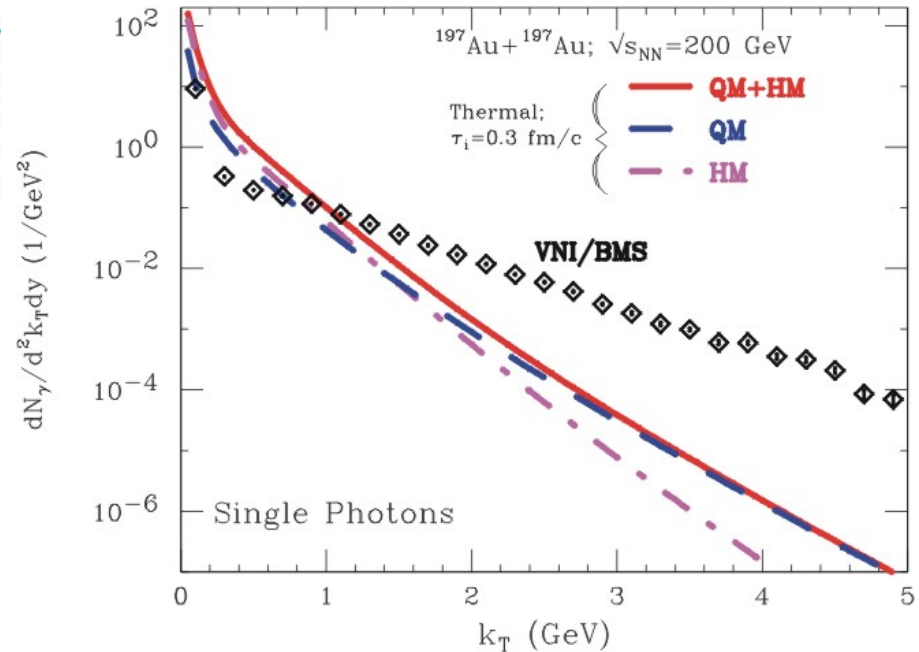
- short emission time in the PCM, 90% of photons before 0.3 fm/c

- hydrodynamic calculation with  $\tau_0=0.3 \text{ fm/c}$  allows for a smooth continuation of emission rate

- pre-equilibrium contributions are easier identified at large  $p_t$ :

- window of opportunity above  $p_t=2 \text{ GeV}$

- at 1 GeV, need to take thermal contributions into account





# HBT Interferometry: formalism

- Correlation between two photons with momenta  $k_1$  and  $k_2$  is given by:

$$C(\vec{q}, \vec{K}) = 1 + \frac{1}{2} \frac{\left| \int d^4x S(x, \vec{K}) e^{ixq} \right|^2}{\int d^4x S(x, \vec{k}_1) \int d^4x S(x, \vec{k}_2)} \quad \text{with } \vec{q} = \vec{k}_1 - \vec{k}_2 \text{ and } \vec{K} = (\vec{k}_1 + \vec{k}_2) / 2$$

with  $S(x, k)$  the photon source function for a chaotic source

- use Wigner function scheme (Hansa code by Sollfrank & Heinz)
  - emission vertices of a semiclassical transport are not valid Wigner fnct.
  - need to smear out emission vertices  $x_i$  by  $\hbar/p_i$
- results are given in terms of outward, sideward & longitudinal correlators

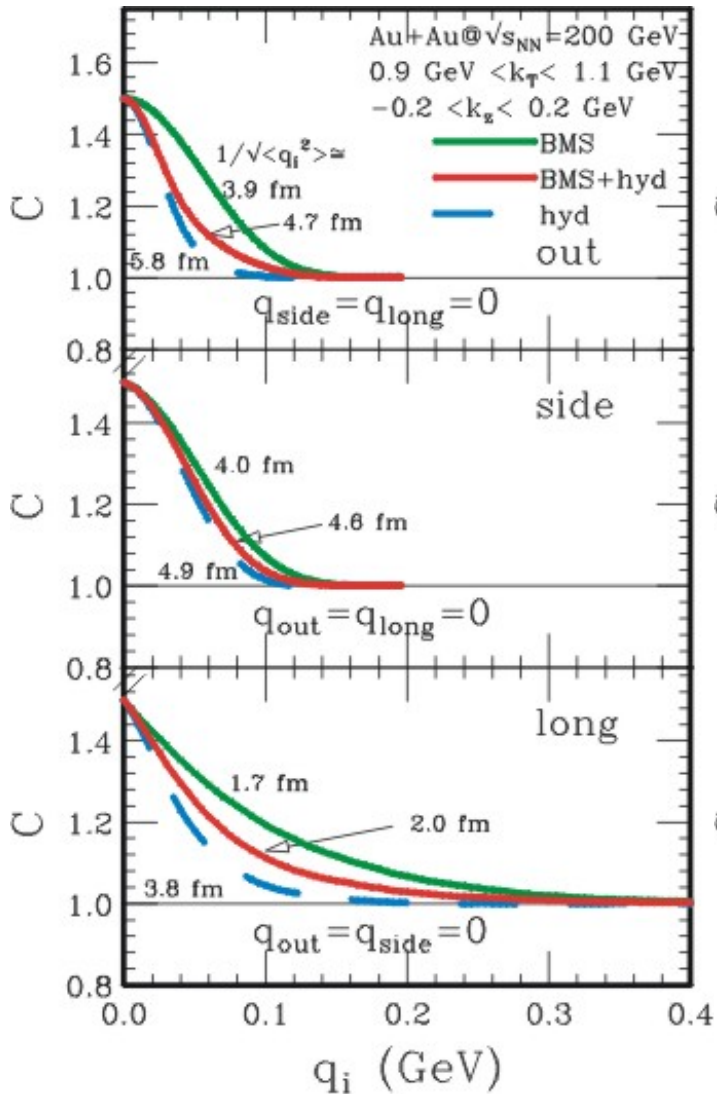
$$q_{long} = |k_{1z} - k_{2z}| = |k_{1T} \sinh y_1 - k_{2T} \sinh y_2|$$

$$q_{out} = \vec{q}_T \cdot \vec{K}_T / K_T$$

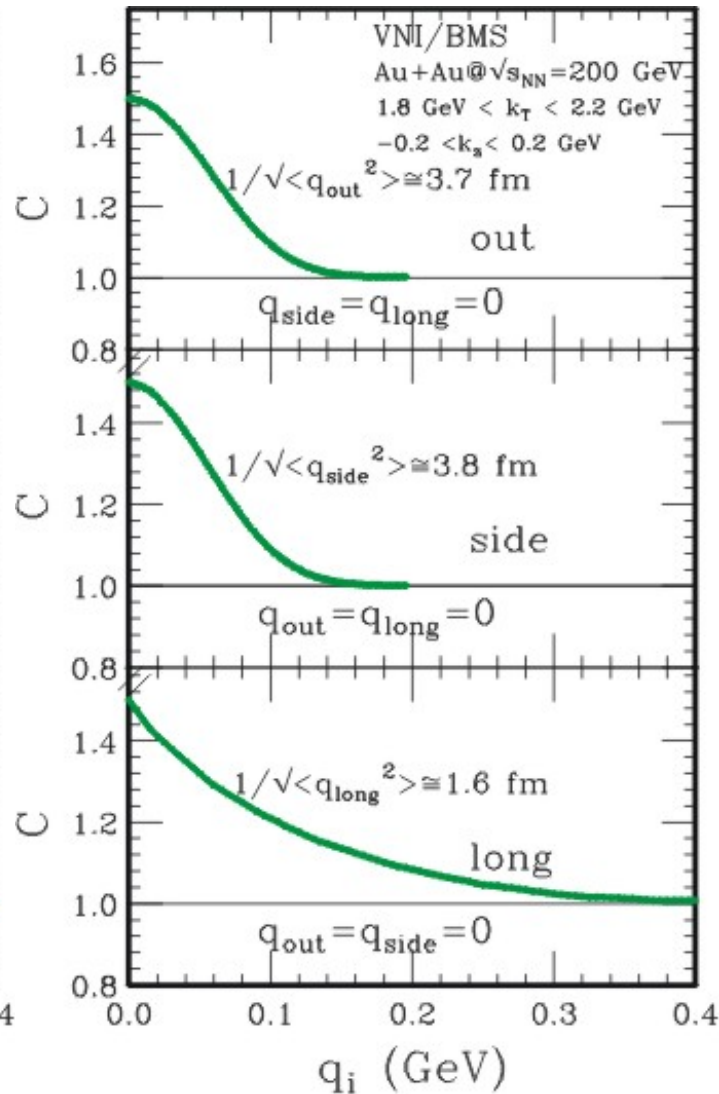
$$q_{side} = \left| \vec{q}_T - q_{out} \vec{K}_T / K_T \right|$$



# Photons: HBT Interferometry



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•  $p_t = 2 \text{ GeV}$ : pre-thermal photons dominate, small radii

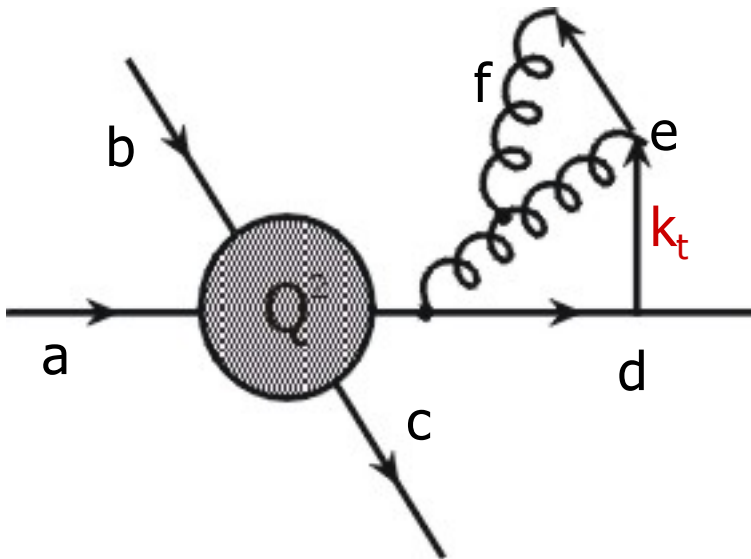
•  $p_t = 1 \text{ GeV}$ : superposition of pre- & thermal photons: increase in radii

Light from Cascading Partons #11



# Landau-Pomeranchuk-Migdal Suppression

- the LPM effect accounts for the suppression of radiation due to coherence effects in multiple scattering



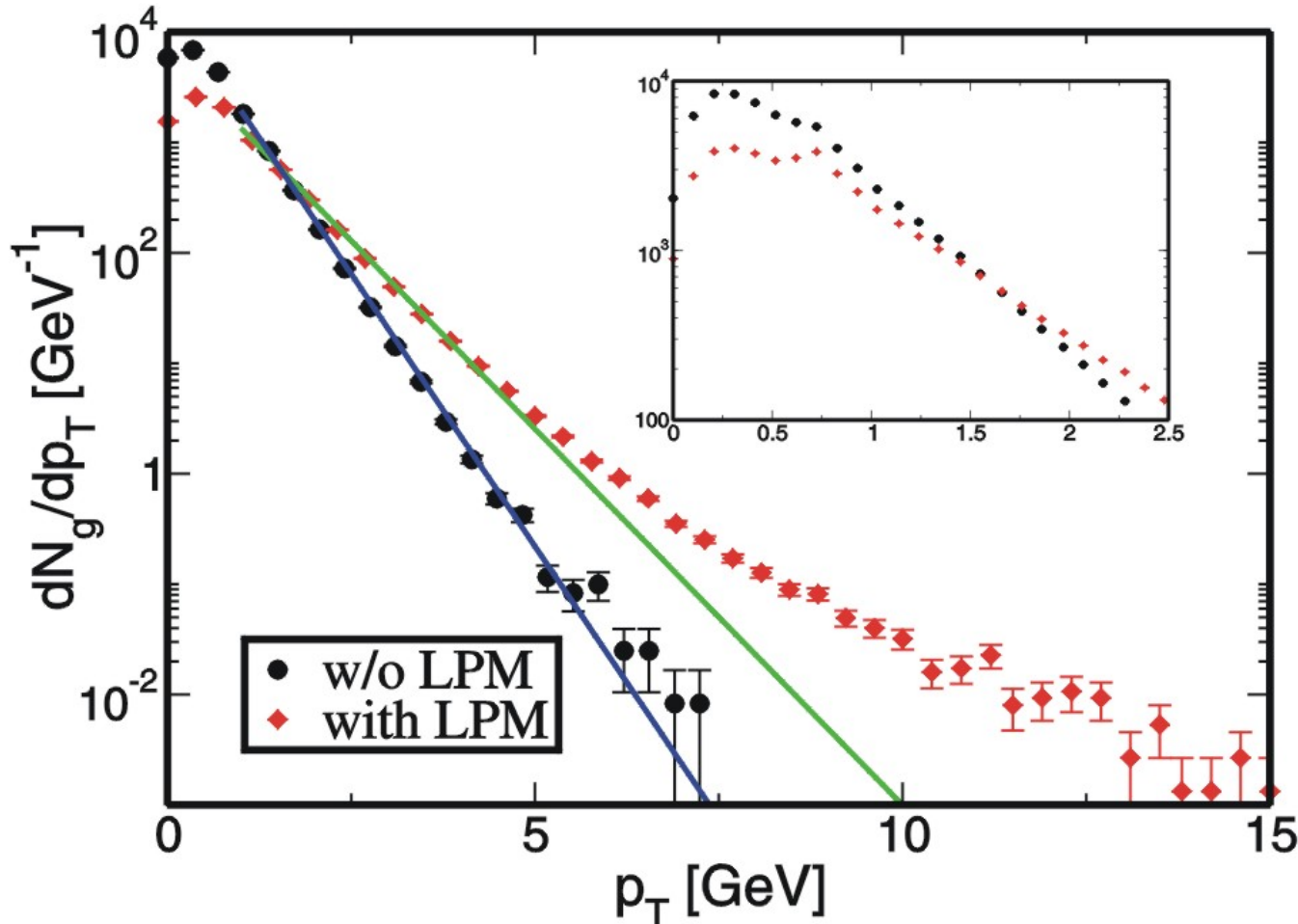
- the radiated parton  $e$  is assigned a formation time:

$$\tau_{\text{form}} = \frac{z(1-z)E_a}{(1-z)q_d^2 + zq_e^2 + k_t^2} \approx \frac{E_a}{q_a^2}$$

- if the radiating parton  $d$  suffers a collision before  $\tau_{\text{form}}$  has elapsed, then the radiation of parton  $e$  and its daughters does not take place
- likewise for parton  $f$  with respect to  $e$  ...



# LPM: Reaction Dynamics



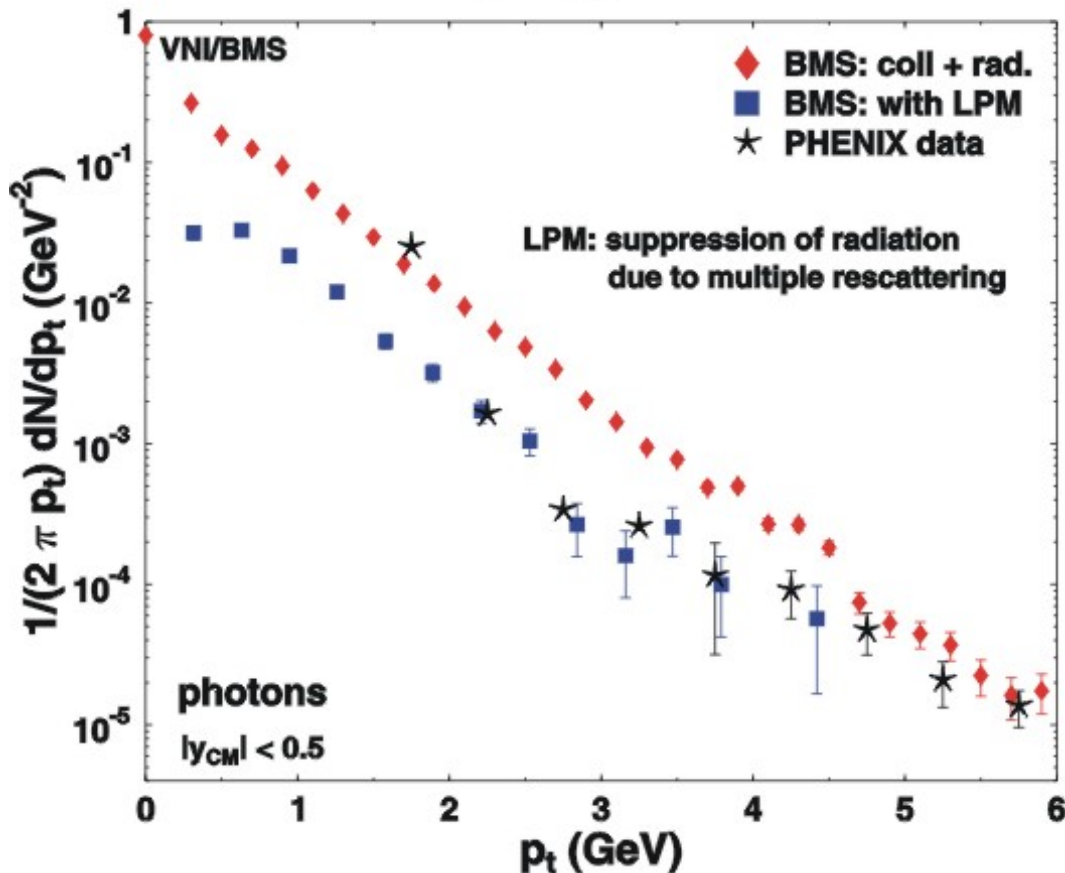
gluon  $p_t$  distribution

- high  $p_t$ : harder slope, enhanced particle production
- low  $p_t$ : suppression of particle production



# Photon Production: LPM & comparison to data

Au+Au;  $E_{\text{CM}}=200$  AGeV



PCM without LPM:

- overprediction of photon yield

PCM with LPM:

- photon yield for  $p_t < 6$  GeV strongly reduced
- strong  $p_t$  dependence of LPM suppression
- good agreement with data



Part #2:

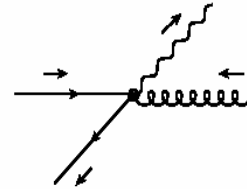
# Photons via Jet-Plasma Interactions

R.J. Fries, B. Mueller & D.K. Srivastava, PRL **90**, 132301 (2003)



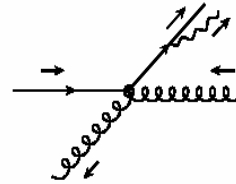
# Photon sources

- Hard direct photons



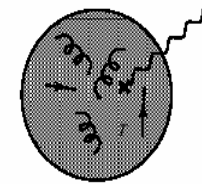
pQCD calculation including shadowing

- EM bremsstrahlung

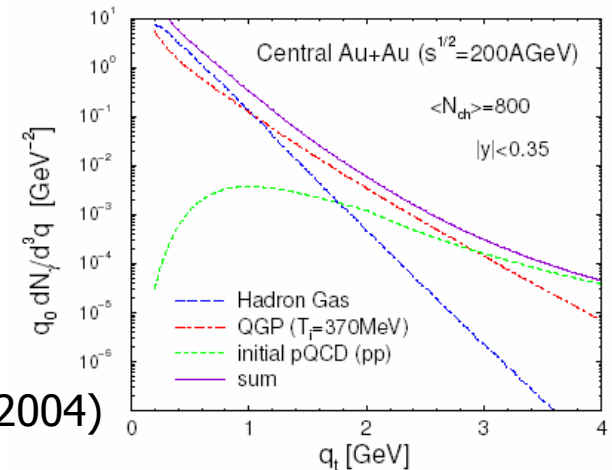
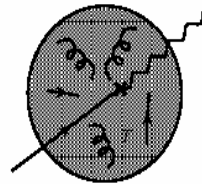


pQCD calculation including shadowing

- Thermal photons from hot medium



- Jet-photon conversion



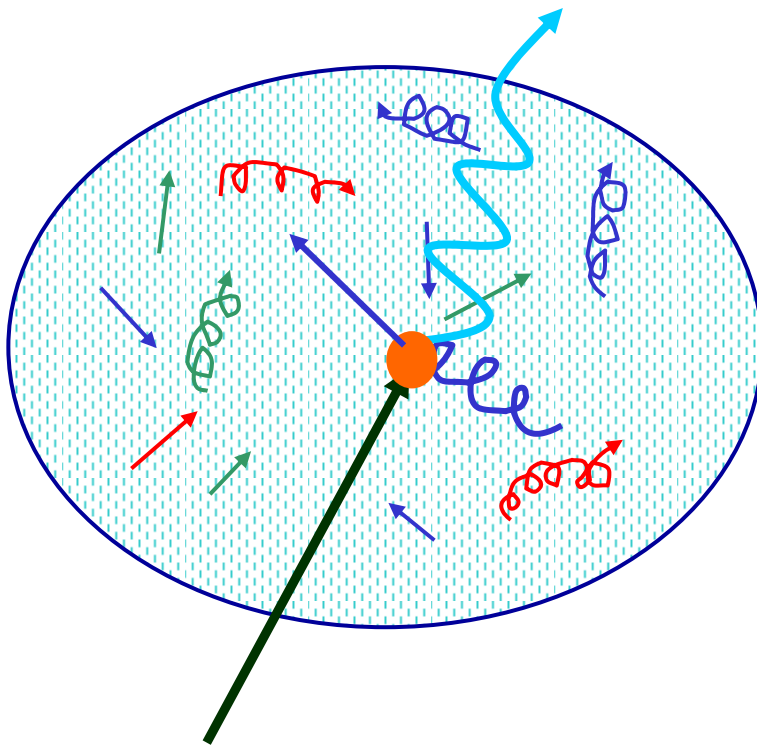
Turbide, Gale & Rapp, PRC 69 014903 (2004)





# Jet-Plasma interactions

plasma mediates a jet-photon conversion:



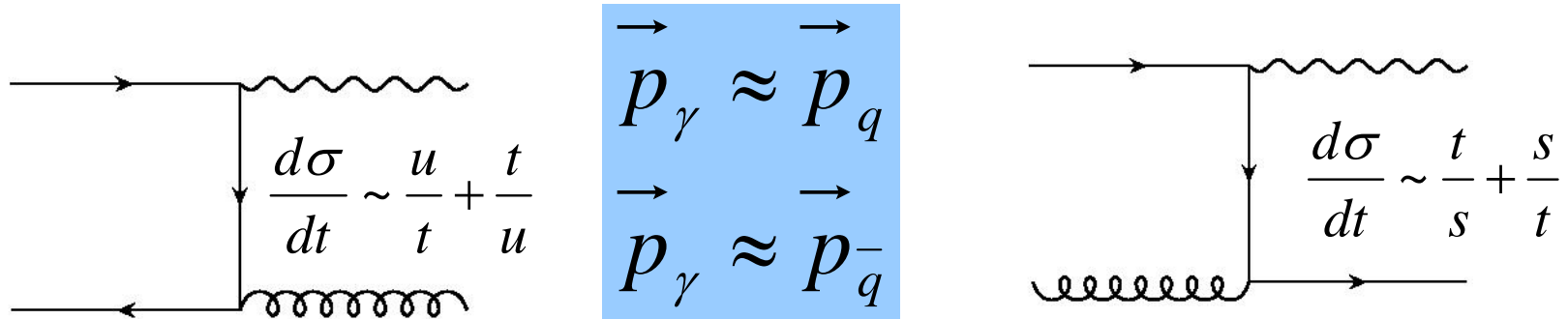
jet passing through the medium:

- large energy loss: jet quenching
- electromagnetic radiation (real and virtual photons) from jet-medium interactions
- suppressed by  $\alpha_{EM}$ ; negligible as a source of additional jet quenching
- can escape without rescattering
  - use as probe of energy loss?
- visible among other sources of electromagnetic signals?



# QGP-Induced EM Radiation

- annihilation and compton processes peak in forward and backward directions:



- one parton from hard scattering, one parton from the thermal medium; cutoff  $p_{\gamma, \min} > 1 \text{ GeV}/c$ .
- photon carries momentum of the hard parton
- Jet-Photon Conversion



# Jet-Photon Conversion: Rates

- annihilation and compton rates:

$$E_\gamma \frac{dN^{(A)}}{d^4x d^3p_\gamma} = \frac{16E_\gamma}{2(2\pi)^6} \sum_{q=1}^{N_f} f_q(p_\gamma) \\ \times \int d^3p f_{\bar{q}}(p)[1 + f_q(p)] \sigma^{(A)}(s) \frac{\sqrt{s(s-4m^2)}}{2E_\gamma E} + (q \leftrightarrow \bar{q})$$

$$E_\gamma \frac{dN^{(C)}}{d^4x d^3p_\gamma} = \frac{16E_\gamma}{2(2\pi)^6} \sum_{q=1}^{N_f} f_q(p_\gamma) \\ \times \int d^3p f_q(p)[1 - f_{\bar{q}}(p)] \sigma^{(C)}(s) \frac{s-m^2}{2E_\gamma E} + (q \leftrightarrow \bar{q})$$

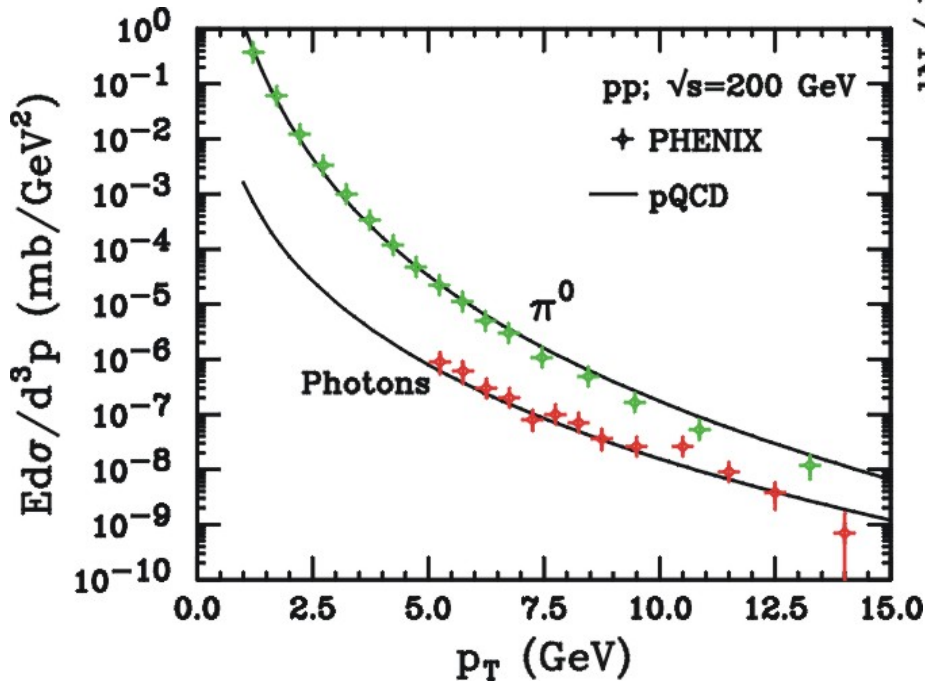
- thermal medium:

$$E_\gamma \frac{dN_\gamma}{d^3p_\gamma} = \frac{\alpha\alpha_s}{8\pi^2} \int d^4x \frac{2}{3} [f_q(p_\gamma) + f_{\bar{q}}(p_\gamma)] T^2 \left( \ln \frac{4E_\gamma T}{m^2} + C \right)$$

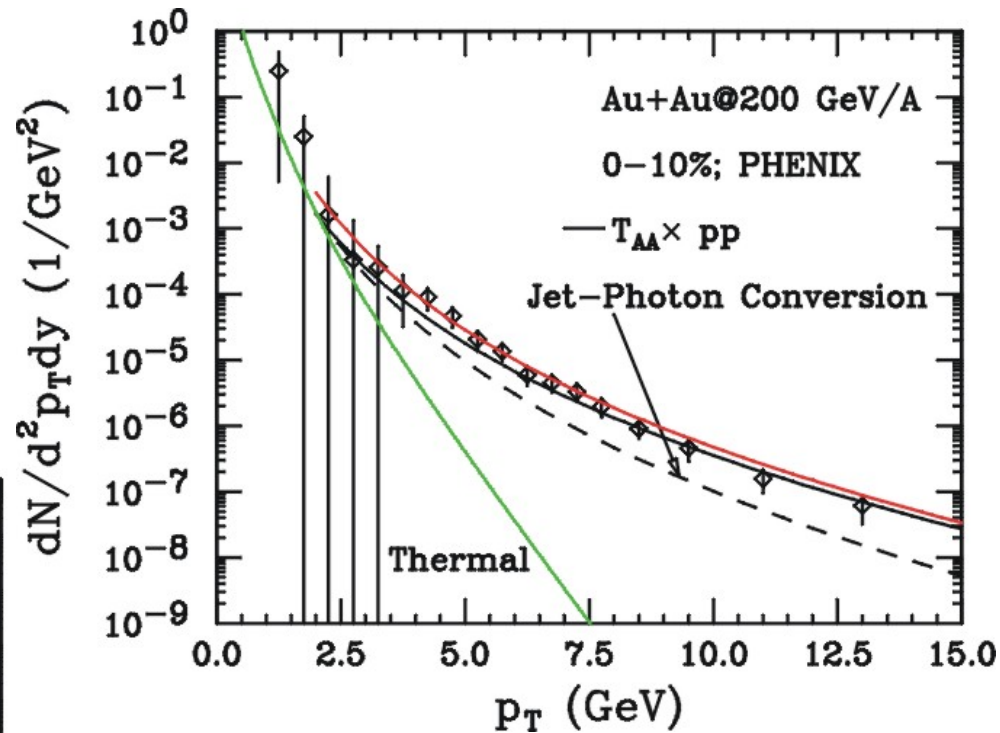


# FMS Results: Comparison to Data

calibrate pQCD calculation of direct and Bremsstrahlung photons via p+p data:



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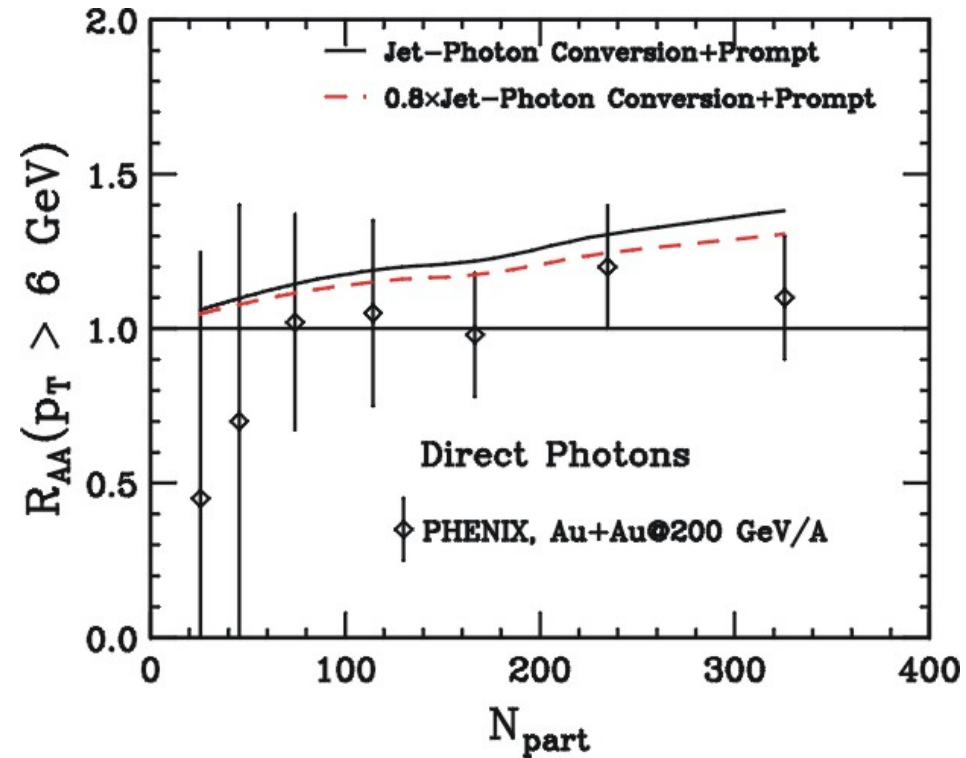
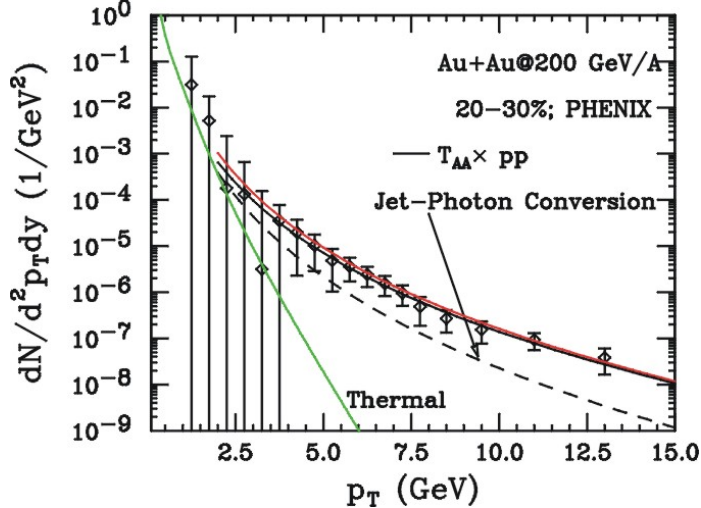
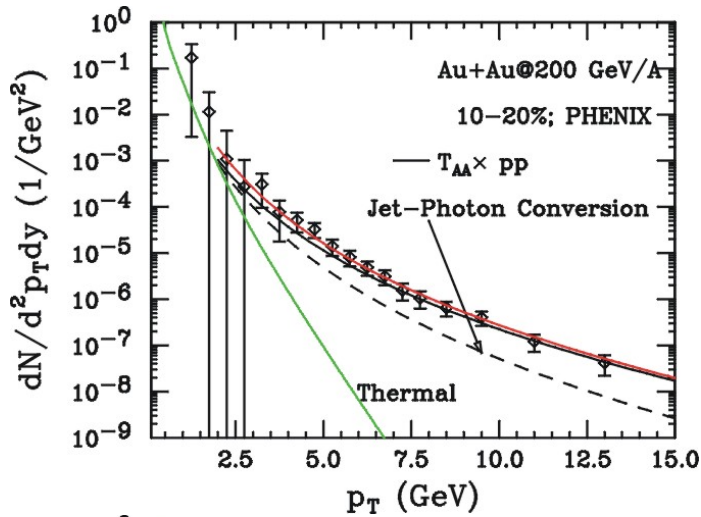
➤ for  $p_t < 6$  GeV, FMS photons give significant contribution to photon spectrum: 50% @ 4 GeV

(Fries, Mueller & Srivastava, ms in preparation)

Light from Cascading Partons #20



# FMS: Centrality Dependence and Jet-Quenching



- centrality dependence well described
- effect of energy-loss on jets before conversion  $\sim 20\%$   
(Turbide, Gale, Jeon & Moore: hep-ph/0502248)



# Application: Monitoring Jet Quenching

full jet reconstruction not possible at RHIC:

- ✓ Measure suppression of single inclusive hadron spectra (compare to p+p baseline)
- ❖ better: photon-tagged jets (Wang & Sarcevic)
  - $q+g \rightarrow q+\gamma$ : recoil photon knows the initial energy of the jet
  - measure energy loss of quark as a function of quark energy  $E$
- ❖ photons from jet-photon conversion provide a third, independent measurement. (FMS)
  - better handle on the  $L$  dependence of energy loss
  - jet-photon conversion is background for photon tagged jets



# Summary

## Photon Production in the PCM:

- Photon yield very sensitive to parton rescattering
- LPM effect needed for proper description of reaction dynamics
- HBT experimentally challenging, but feasible with high statistics data sets
- calculable in the framework of PCM and hydro
- short emission duration in pre-equilibrium phase: small radii at high  $p_t$
- larger source at later times due to emission of thermal photons

## Photon Production via Jet-Medium Interactions:

- jet-photon conversion may contribute up to 50% @ 4 GeV to photon yield
- results compatible with PHENIX data (centrality dependence,  $R_{AA}$ )
- analogous process for virtual photons: contribution to dilepton production